

**THE MECHANICAL  
ENGINEER'S  
POCKET-BOOK OF  
TABLES,  
FORMULAE, ...**

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THE  
**MECHANICAL ENGINEER**  
**POCKET-BOOK**

**Tables, Formulæ, Rules, and Data**

*A HANDY BOOK OF REFERENCE FOR  
DAILY USE IN ENGINEERING PRACTICE*

BY

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"RAILWAY MACHINERY;" "TRAMWAYS;" "THE STEAM ENGINE;"

"A MANUAL OF RULES, TABLES, AND DATA," ETC.

**Second Edition, Revised and Enlarged.**

NEW YORK

**D. VAN NOSTRAND COMPANY**

23 MURRAY, AND 27 WARREN STREET

1893

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## PREFACE.

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MANY works of the POCKET-BOOK class have already been published for the use of professional men ; but not one of those with which I am acquainted has been compiled expressly with a view to the requirements of the Mechanical Engineer.

This POCKET-BOOK has accordingly been prepared for the purpose of shortening the calculations and other intricate mental operations which are amongst the daily recurring needs of mechanical men. To meet such needs, there will be found in the following pages about 350 Tables of results of calculations, relating to the principal branches of mechanical practice, which have either been compiled anew, or drawn from various sources. There are, in addition, about 500 Formulæ and Rules, with Data of general utility, classified for ready reference. By their aid, many a weary search in larger and more ambitious books may be dispensed with, and the labour of calculation greatly abridged, or even entirely avoided.

I do not lay especial claim in these pages to origi-

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nality, for much of the matter of the book is necessarily common property. I have, nevertheless, contributed many original tables, formulæ, and data, herein published for the first time. And with regard to all matter in the work, I have spared no pains, on the one hand, to select such questions as the mechanical engineer would probably most desire to find elucidated ; and on the other, to draw my material from the best and most trustworthy sources.

Besides the usual indispensable mathematical tables, and rules for measurement of surfaces and solids, full tables of English weights and measures, with French metric equivalents, are given ; tables of French metric weights and measures, with equivalent English values, are also given.

Many useful tables are given of the weights and strength of bars, sheets, beams, joists, girders, tubes, pipes, bolts and nuts, cylinders, nails, chains, and other manufactured pieces. For the strength of materials, a variety of experimental evidence is given, with many new formulæ and tables. Heat and its applications have been fully considered in various aspects. The best proportions of steam engines, simple and compound, are discussed ; together with pumping engines, water power, and compressed-air power.

I am indebted to Mr. H. R. Kempe, A.M.I.C.E., for his assistance in the preparation of the section on Electrical Engineering ; and in various sections acknowledgment will be found duly made of my indebtedness to other authorities.

I am in hopes that the variety of matter here pre-

sented will meet all reasonable requirements of practical men in such a work, and enable them to dispense very largely with exterior aid.

At the same time, I shall be glad to avail myself of the hints or suggestions of mechanical men using the book, with a view to improve and to perfect its contents ; and I shall receive with pleasure communications which may be made to me from any quarter with that object.

D. K. CLARK.

LONDON, *November*, 1831.

## NOTE TO SECOND EDITION.

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IN preparing the second edition of this POCKET-BOOK for the press, I have taken advantage of the opportunity to import various new matters into the text, and, at the same time, to revise or alter the text where it has been found necessary.

I may again remind my readers that I am open to hints or suggestions with a view to improve or perfect the contents of this book ; and that I shall receive them with pleasure.

D. K. CLARK.

LONDON, *January*, 1893.

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# THE MECHANICAL ENGINEER'S POCKET-BOOK.

## MATHEMATICAL TABLES.

### Introduction to the Tables.

**TABLE 1.**—*Circumferences and Areas of Circles, Squares, Cubes, Square Roots, and Cube Roots of Numbers, from 1 to 1000.*

THE powers and roots of numbers may be calculated by means of logarithms; but this table will considerably economise calculation.

The columns of squares and cubes may be utilised inversely, for finding in the first column the roots of numbers contained in those columns.

The columns of square roots and cube roots, also, may be utilised for finding, in the first column, the squares and cubes of numbers containing decimals in those columns.

Further, the squares in the fourth column are the fourth powers of the square roots in the sixth column.

Again, any number in the first column may be conceived to consist of an integer and decimals, when the corresponding square or cube, with a decimal point suitably placed, will be the square or the cube of the assumed number. For example, suppose that the number 186 represents 18·6, or 1·86, or ·186, the square will contain two, or four, or six places of decimals respectively; and the cube will contain three, or six, or nine places of decimals respectively. Thus,—

Number.	Square.	Cube.
186	34,596	6,434,856
18·6	345·96	6,434·856
1·86	3·4596	6·434856
·186	·034596	·006434856



The number of places of decimals is fixed in each instance according to the common rule of twice the number of decimal places in the original number for a square, and three times the number in the original for a cube.

TABLE 2.—*Diameter, Circumference, and Area of Circles, advancing by Vulgar Fractions, from  $\frac{1}{16}$  to 120.*

The diameters specifically represent lengths, in inches and parts of inches. But they may represent values in any other units, as feet or yards.

TABLE 3.—*Reciprocals of Numbers, from 1 to 1000.*

The reciprocal of a number is the quotient obtained by dividing 1 by the given number.

The product of any number with its reciprocal is equal to 1. Hence a ready means of checking the accuracy of any reciprocal, which when multiplied by its number should give a quotient of 1.

The reciprocal of a vulgar fraction is equal to the quotient of the denominator by the numerator. Thus the reciprocal of  $\frac{1}{2}$  is equal to  $\left(\frac{2}{1} =\right) 2$ . Or, the vulgar fraction may be reduced to a decimal form, and the decimal value divided into 1. Thus  $\frac{1}{2} = .5$ , and  $1 \div .5 = 2$ .

TABLE 4.—*Logarithms of Numbers, from 1 to 10,000.*

Logarithms are designed to abbreviate calculations involving multiplication and division of numbers, by the substitution of calculations by addition and subtraction respectively. Logarithms consist of integers and decimals, and they are given in Table 4 for numbers ranging from 1 to 10,000. The integers or indices, as they are called, are, except in the small preliminary tablet, omitted in the table, for the sake of brevity, but chiefly for the sake of clearness and simplicity. The decimal values of the logarithms are given to six places. The integer or index of each logarithm is less by 1 than the number of places in the integer of the number; and if the number contain only decimals, the index is equal to the number of cyphers next the decimal point, plus 1. The index in this case is negative, and is so distinguished by the sign minus, —, written over it. The adjustment of the integer of a logarithm to the composition of the given number is exemplified in the following series, in which the same number is repeated several

times, having the decimal point shifted regularly by one digit towards the left :—

5314	.	.	.	.	3·725422
531·4	.	.	.	.	2·725422
53·14	.	.	.	.	1·725422
5·314	.	.	.	.	0·725422
·5314	.	.	.	.	$\bar{1}$ ·725422
·05314	.	.	.	.	$\bar{2}$ ·725422
·005314	.	.	.	.	$\bar{3}$ ·725422

*To find the logarithm of a number.* If the number contain only one or two digits, look for it in the columns marked N in the preliminary tablet, and find the logarithm next to it, or, look for the number in the body of the table, with one, or two, cyphers following it ; and the decimal part of the logarithm stands next to the number, in the column headed 0. For example, the decimal part of the logarithm of 5, ·698970, is in the column next to 500, in page 63 of the table ; corresponding to the single digit in the integer, the integral figure of the logarithm is 0, and the complete logarithm is 0·698970. For 50, the logarithm is 1·698970 ; and for 500, the logarithm is 2·698970 ; but for ·5, the logarithm is  $\bar{1}$ ·698970.

In short, if the given number consist of one, two, or three digits, the decimal part of its logarithm is found in the column headed 0. If the number consist of four digits, look for the first, second, and third in the column N, and the fourth in the row of headings or footings at the top or the bottom of the table ; and the logarithmic decimal is found opposite the number in the marginal column, and below or above the fourth. If the number consist of five or more digits, the logarithm for the first to the fourth digits being found as above, multiply the corresponding difference in the last column, D, by the remaining digits, and divide by 10 if there be only one digit more, by 100 if there be ten more, and so on. Add the quotient to the logarithm already obtained, to give the logarithm required. For example, to find the logarithm of 62·355. The decimal part of the logarithm of 6235 is ·794836, and the corresponding difference ( $70 \times 5 \div 10 =$ ) 35, is to be added, thus—

$$\begin{array}{r} 0\cdot794836 \\ 35 \\ \hline \end{array}$$

0·794871 the completed logarithm.

Conversely, the number for a given logarithm is found by searching for the decimal part of the logarithm. If it be found exactly or within a few units of the right-hand digit,

note the first, second, and third digits of the required number in the column N, and the fourth digit at the top or the bottom, above or below the decimal; and place the decimal point. If the logarithm differ materially from the nearest in the table, find the number for the next less logarithm in the table, to give the first, second, third, and fourth digits. To find the fifth and, if necessary, the sixth digit, subtract the tabulated logarithm from the given logarithm, add two cyphers, and divide by the difference found in column D in a line with the logarithm. Annex the quotient to the four digits already found, and place the decimal point. For example, to find the number represented by the logarithm 0·497151. The nearest less logarithm in the table is 0·497068, for the number 3141. Subtracting this logarithm from that, thus—

$$0\cdot497151$$

$$0\cdot497068$$

---


$$83$$

add two cyphers to the difference, making 8300, and divide by 138, the difference in column D. Then  $8300 \div 138 = 60$ , and annexing 60 to 3141, the number is 314160. Placing the decimal point, the completed number is 3·14160, or 3·1416.

*To multiply two or more numbers together*, add together their logarithms. The sum is the logarithm of the product. To divide one number by another, subtract the logarithm of this from the logarithm of that; the number corresponding to the difference is the quotient.

*To find any power of a given number*, multiply the logarithm of the number by the exponent of the power. The product is the logarithm of the power.

*To find any root of a given number*, divide the logarithm of the number by the index of the root.

*To find the reciprocal of a given number*, subtract the decimal part of the logarithm of the number from 0·000000; add 1 to the index of the logarithm and change the sign of the index. For example, to find the reciprocal of 350 :—

$$\begin{array}{r} 0\cdot000000 \\ \log. 350 \quad . \quad . \quad 2\cdot544068 \end{array}$$

---


$$3\cdot455932 = \log. \cdot002857.$$

Conversely, to find the reciprocal of the decimal ·002857:—

$$\begin{array}{r} 0\cdot000000 \\ \log. \cdot002857 \quad . \quad 3\cdot455932 \end{array}$$

---


$$2\cdot544068 = \log. 350.$$

These two calculations afford examples of negative indices. In the first, the logarithm of 350 has the index 2, or + 2, the sign of which is changed for subtraction, making - 2. In deducting the digit 5, the first decimal, from 0, 1 is carried to it from the previous subtraction, making 6, which deducted from 10 leaves 4. Carrying 1, - 2 and - 1 make - 3, which is the index of the remainder,  $\bar{3} \cdot 455932$ , the logarithm of  $\cdot 002857$ .

In the second calculation above, in deducting the first decimal, 4 augmented by 1 carried, or 5, from 10, there remains 5, the first decimal in the remainder; and 1 is carried to the index place. But, first, the sign of the index is changed, and the index becomes + 3; and from this the carried 1 is deducted, leaving + 2 the index of the remaining logarithm of 350.

*To add together two negative indices*, they are simply added and the negative sign placed over the sum, thus  $\bar{3} + \bar{2} = \bar{5}$ . In the addition together of a positive index and a negative index, their difference is the sum, bearing the sign of the greater additive; thus  $3 + \bar{2} = 1$ ; or  $2 + \bar{3} = \bar{1}$ . For example:—

$$\log. 3442 = 3 \cdot 536811$$

$$\log. \cdot 02801 = \bar{2} \cdot 447313$$

---


$$\log. 96 \cdot 41 = 1 \cdot 984124$$

*To subtract a negative index*, change the sign and add. Thus, to subtract  $\bar{2}$  from  $\bar{3}$ , there is  $\bar{3} + 2 = \bar{1}$ ; but this may be done simply thus  $\bar{3} - \bar{2} = \bar{1}$ . Again,  $\bar{3}$  from  $2 = 3 + 2 = 5$ . To subtract a positive index from a negative index, change the positive sign to negative and add; thus, 3 from  $\bar{5} = \bar{3} + \bar{5} = \bar{8}$ .

*To find a root of a given number*. Divide the logarithm of the number by the exponent of the root: the quotient is the logarithm of the root. If the index be negative, and is divisible without a remainder, the quotient of the index is negative. If it be not so divisible, add to it so much in the negative as will make it divisible, and divide it, to give the index, which is negative; prefix an equal quantity to the decimal part of the logarithm, and divide separately. The two quotients together make the logarithm of the root. For example, to find the square root of 1849:—

$$\log. 1849 = 3 \cdot 266937$$

$$\text{divided by } 2 = 1 \cdot 633469 = \log. 43.$$

To find the fourth root of  $\cdot 00578$  :—

$$\begin{aligned} \log. \cdot 00578 &= \bar{3} \cdot 761928 \\ \text{divide by 4, say } \bar{4} &+ 1 \cdot 761928 \\ \text{giving } \bar{1} \cdot 440482 &= \log. \cdot 2757. \end{aligned}$$

It is, in ordinary practice, for the most part, unnecessary to note the indices of logarithms, as the numbers are mostly sufficiently indicated without the indices. Besides, in many cases, rough approximations suffice, particularly where numbers are expressed wholly or partly in decimals.

TABLE 5.—*Hyperbolic Logarithms of Numbers from 1.01 to 20.*

The table of hyperbolic logarithms is useful chiefly in calculations of the work of steam by expansion. The numbers range from 1.01 to 20. Hyperbolic, or Neperian, logarithms, are calculated by multiplying the common logarithms of numbers, as given in Table 4, by the constant multiplier 2.302585.

TABLE 6.—*Sines and Cosines of Angles from  $0^\circ$  to  $90^\circ$ .*

The tabulated values are the proportional values when the length of the radius of the circle is taken as 1. When the actual length of the radius is given, the actual length of any sine or cosine is found by multiplying the tabular value by the length of the radius.

The table is arranged so that each value signifies the sine of an angle and the cosine of its complement for  $90$  degrees. The values are given for angles advancing by half a degree. The values for intermediate angles, sufficiently near exactness for most purposes, can be found by interpolation in simple proportion. By an inverse operation, the angle may be found for any given sine or cosine not given in the table.

TABLE 7.—*Tangents and Cotangents of Angles from  $0^\circ$  to  $90^\circ$ .*

The values are, like those of the sines and cosines, proportional values, the radius being taken as 1. The actual values of the tangents and cotangents are calculated by multiplying the actual length of the radius by the corresponding tabular value of the tangent or the cotangent.

Each tabular value is that of the tangent of an angle, and also that of the cotangent of the complementary angle. The values are given for angles advancing by half a degree; and values for intermediate angles may be found by interpolation. Inversely, the angle may be found for any given tangent or cotangent not found in the table.

TABLE 8.—*Lengths of Circular Arcs, from 1° to 180°.*

The lengths of circular arcs of which the magnitudes in degrees are given, are stated in proportion to the length of the radius, taken as 1. The actual length of the arc is found by multiplying the actual length of the radius by the tabular length corresponding to the number of degrees in the arc.

TABLE 9.—*Lengths of Circular Arcs, up to a Semicircle, when the Chord is given.*

In this table, the length of the arc is given proportionally to the length of the chord, which is taken as 1. The heights of the arcs in the table are the quotients arising by dividing the actual heights by the actual lengths of the chords, and are the ratios of the heights to the chords.

To use the table, therefore, divide the height of the arc by the length of the chord; find the quotient in the columns of heights in the table, and multiply the corresponding tabular length of the arc by the actual length of the chord. The product is the length of the arc.

TABLE 10.—*Areas of Circular Segments.*

The tabular areas of circular segments are in proportional superficial measure, corresponding to the length of the diameter, which is taken as 1. The tabular heights of the segments are the quotients of the heights divided by the diameters; the relative areas are given in the columns of areas.

To use the table, divide the actual height by the actual diameter, find the quotient in the columns of heights; and multiply the corresponding tabular area by the square of the actual length of the diameter. The product is the actual area.

TABLE 11.—*Lengths of Semi-Elliptic Arcs up to a Semi-Circle.*

This table has been calculated by means of Mr. Trautwine's formula. In the columns of heights are the ratios of the rise to the span or chord of an elliptic arc. To use the table, divide the given rise by the chord, and find the quotient in the columns of heights. Next to this quotient, in the adjoining column, is a multiplier, which when multiplied by the actual length of the span, gives the length of the arc.

TABLE 1.—NUMBERS (FROM 1 TO 1,000), OR DIAMETERS OF CIRCLES, CIRCUMFERENCES, AREAS, SQUARES, CUBES, SQUARE ROOTS, AND CUBE ROOTS.\*

No. or Di. m.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
1	3.1416	0.7854	1	1	1.000	1.000
2	6.2832	3.1416	4	8	1.414	1.259
3	9.4248	7.0686	9	27	1.732	1.442
4	12.57	12.57	16	64	2.000	1.587
5	15.71	19.63	25	125	2.236	1.709
6	18.85	28.27	36	216	2.449	1.817
7	21.99	38.48	49	343	2.645	1.912
8	25.13	50.27	64	512	2.828	2.000
9	28.27	63.62	81	729	3.000	2.080
10	31.42	78.54	100	1,000	3.162	2.154
11	34.56	95.03	121	1,331	3.316	2.223
12	37.70	113.10	144	1,728	3.464	2.289
13	40.84	132.73	169	2,197	3.605	2.351
14	43.98	153.94	196	2,744	3.741	2.410
15	47.12	176.71	225	3,375	3.872	2.466
16	50.26	201.06	256	4,096	4.000	2.519
17	53.41	226.98	289	4,913	4.123	2.571
18	56.55	254.47	324	5,832	4.242	2.620
19	59.69	283.53	361	6,859	4.358	2.668
20	62.83	314.16	400	8,000	4.472	2.714
21	65.97	346.36	441	9,261	4.582	2.758
22	69.11	380.13	484	10,648	4.690	2.802
23	72.26	415.48	529	12,167	4.795	2.843
24	75.40	452.39	576	13,824	4.898	2.884
25	78.54	490.87	625	15,625	5.000	2.924
26	81.68	530.93	676	17,576	5.099	2.962
27	84.82	572.56	729	19,683	5.196	3.000
28	87.96	615.75	784	21,952	5.291	3.036
29	91.11	660.52	841	24,389	5.385	3.072
30	94.25	706.86	900	27,000	5.477	3.107
31	97.39	754.77	961	29,791	5.567	3.141
32	100.53	804.25	1,024	32,768	5.656	3.174
33	103.67	855.30	1,089	35,937	5.744	3.207
34	106.81	907.92	1,156	39,304	5.830	3.239
35	109.96	962.11	1,225	42,875	5.916	3.271
36	113.10	1017.88	1,296	46,656	6.000	3.301
37	116.24	1075.21	1,369	50,653	6.082	3.332
38	119.38	1134.11	1,444	54,872	6.164	3.361
39	122.52	1194.59	1,521	59,319	6.244	3.391

\* See Introduction, *ante*, p. 1.

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
40	125.66	1256.64	1,600	64,000	6.326	3.419
41	128.80	1320.25	1,681	68,921	6.403	3.448
42	131.95	1385.44	1,764	74,088	6.480	3.476
43	135.09	1452.20	1,849	79,507	6.557	3.503
44	138.23	1520.53	1,936	85,184	6.633	3.530
45	141.37	1590.43	2,025	91,125	6.708	3.556
46	144.51	1661.90	2,116	97,336	6.782	3.583
47	147.65	1734.94	2,209	103,823	6.855	3.608
48	150.80	1809.56	2,304	110,592	6.928	3.634
49	153.94	1885.74	2,401	117,649	7.000	3.659
50	157.08	1963.50	2,500	125,000	7.071	3.684
51	160.22	2042.82	2,601	132,651	7.141	3.708
52	163.36	2123.72	2,704	140,608	7.211	3.732
53	166.50	2205.18	2,809	148,877	7.280	3.756
54	169.65	2290.22	2,916	157,464	7.348	3.779
55	172.79	2375.83	3,025	166,375	7.416	3.802
56	175.93	2463.01	3,136	175,616	7.483	3.825
57	179.07	2551.76	3,249	185,193	7.549	3.848
58	182.21	2642.08	3,364	195,112	7.615	3.870
59	185.35	2733.97	3,481	205,379	7.681	3.892
60	188.50	2827.43	3,600	216,000	7.745	3.914
61	191.64	2922.47	3,721	226,981	7.810	3.936
62	194.78	3019.07	3,844	238,328	7.874	3.957
63	197.92	3117.25	3,969	250,047	7.937	3.979
64	201.06	3216.99	4,096	262,144	8.000	4.000
65	204.20	3318.31	4,225	274,625	8.062	4.020
66	207.34	3421.19	4,356	287,496	8.124	4.041
67	210.49	3525.65	4,489	300,763	8.185	4.061
68	213.63	3631.68	4,624	314,432	8.246	4.081
69	216.77	3739.28	4,761	328,509	8.306	4.101
70	219.91	3848.45	4,900	343,000	8.366	4.121
71	223.05	3959.19	5,041	357,911	8.426	4.140
72	226.19	4071.50	5,184	373,248	8.485	4.160
73	229.34	4185.39	5,329	389,017	8.544	4.179
74	232.48	4300.84	5,476	405,224	8.602	4.198
75	235.62	4417.86	5,625	421,875	8.660	4.217
76	238.76	4536.46	5,776	438,976	8.717	4.235
77	241.90	4656.63	5,929	456,533	8.774	4.254
78	245.04	4778.36	6,084	474,552	8.831	4.272
79	248.19	4901.67	6,241	493,039	8.888	4.290
80	251.33	5026.55	6,400	512,000	8.944	4.308
81	254.47	5153.00	6,561	531,441	9.000	4.326



No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
82	257·61	5281·02	6,724	551,368	9·055	4·344
83	260·75	5410·61	6,889	571,787	9·110	4·362
84	263·89	5541·77	7,056	592,704	9·165	4·379
85	267·03	5674·50	7,225	614,125	9·219	4·396
86	270·18	5808·80	7,396	636,056	9·273	4·414
87	273·32	5944·68	7,569	658,503	9·327	4·431
88	276·46	6082·12	7,744	681,472	9·380	4·447
89	279·60	6221·14	7,921	704,969	9·433	4·461
90	282·74	6361·73	8,100	729,000	9·486	4·481
91	285·88	6503·88	8,281	753,571	9·539	4·497
92	289·03	6647·61	8,464	778,688	9·591	4·514
93	292·17	6792·91	8,649	804,357	9·643	4·530
94	295·31	6939·78	8,836	830,584	9·695	4·546
95	298·45	7088·22	9,025	857,375	9·746	4·562
96	301·59	7238·23	9,216	884,736	9·797	4·578
97	304·73	7389·81	9,409	912,673	9·848	4·594
98	307·88	7542·96	9,604	941,192	9·899	4·610
99	311·02	7697·69	9,801	970,299	9·949	4·626
100	314·16	7853·98	10,000	1,000,000	10·000	4·641
101	317·30	8011·85	10,201	1,030,301	10·049	4·657
102	320·41	8171·28	10,404	1,061,208	10·099	4·672
103	323·58	8332·29	10,609	1,092,727	10·148	4·687
104	326·73	8494·87	10,816	1,124,864	10·198	4·702
105	329·87	8659·01	11,025	1,157,625	10·246	4·717
106	333·01	8824·73	11,236	1,191,016	10·295	4·732
107	336·15	8992·02	11,449	1,225,043	10·344	4·747
108	339·29	9160·88	11,664	1,259,712	10·392	4·762
109	342·43	9331·32	11,881	1,295,029	10·440	4·776
110	345·57	9503·32	12,100	1,331,000	10·488	4·791
111	348·72	9676·89	12,321	1,367,631	10·535	4·805
112	351·86	9852·03	12,544	1,404,928	10·583	4·820
113	355·00	10028·75	12,769	1,442,897	10·630	4·834
114	358·14	10207·03	12,996	1,481,544	10·677	4·848
115	361·28	10386·89	13,225	1,520,875	10·723	4·862
116	364·42	10568·32	13,456	1,560,896	10·770	4·876
117	367·57	10751·32	13,689	1,601,613	10·816	4·890
118	370·71	10935·88	13,924	1,643,032	10·862	4·904
119	373·85	11122·02	14,161	1,685,159	10·908	4·918
120	376·99	11309·73	14,400	1,728,000	10·954	4·932
121	380·13	11499·01	14,641	1,771,561	11·000	4·946
122	383·27	11689·87	14,884	1,815,848	11·045	4·959
123	386·42	11882·29	15,129	1,860,867	11·090	4·973

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
124	389.56	12076.28	15,376	1,906,624	11.135	4.986
125	392.70	12271.85	15,625	1,953,125	11.180	5.000
126	395.84	12468.98	15,876	2,000,376	11.224	5.013
127	398.98	12667.69	16,129	2,048,383	11.269	5.026
128	402.12	12867.96	16,384	2,097,152	11.313	5.039
129	405.26	13069.81	16,641	2,146,689	11.357	5.052
130	408.41	13273.23	16,900	2,197,000	11.401	5.065
131	411.55	13478.22	17,161	2,248,091	11.445	5.078
132	414.69	13684.78	17,424	2,299,968	11.489	5.091
133	417.83	13892.91	17,689	2,352,637	11.532	5.104
134	420.97	14102.61	17,956	2,406,104	11.575	5.117
135	424.11	14313.88	18,225	2,460,375	11.618	5.129
136	427.26	14526.72	18,496	2,515,456	11.661	5.142
137	430.40	14741.14	18,769	2,571,353	11.704	5.155
138	433.54	14957.12	19,044	2,620,872	11.747	5.167
139	436.68	15174.68	19,321	2,685,619	11.789	5.180
140	439.82	15393.80	19,600	2,744,000	11.832	5.192
141	442.96	15614.50	19,881	2,803,221	11.874	5.204
142	446.11	15836.77	20,164	2,863,288	11.916	5.217
143	449.25	16060.61	20,449	2,924,207	11.958	5.229
144	452.39	16286.02	20,736	2,985,984	12.000	5.241
145	455.53	16513.00	21,025	3,048,625	12.041	5.253
146	458.67	16741.55	21,316	3,112,136	12.083	5.265
147	461.81	16971.67	21,609	3,176,523	12.124	5.277
148	464.96	17203.36	21,904	3,241,792	12.165	5.289
149	468.10	17436.62	22,201	3,307,949	12.206	5.301
150	471.24	17671.46	22,500	3,375,000	12.247	5.313
151	474.38	17907.86	22,801	3,442,951	12.288	5.325
152	477.52	18145.84	23,104	3,511,808	12.328	5.336
153	480.66	18385.39	23,409	3,581,577	12.369	5.348
154	483.80	18626.50	23,716	3,652,264	12.409	5.360
155	486.95	18869.19	24,025	3,723,875	12.449	5.371
156	490.09	19113.45	24,336	3,796,416	12.489	5.383
157	493.23	19359.28	24,649	3,869,893	12.529	5.394
158	496.37	19606.68	24,964	3,944,312	12.569	5.406
159	499.51	19855.65	25,281	4,019,679	12.609	5.417
160	502.65	20106.19	25,600	4,096,000	12.649	5.428
161	505.80	20358.34	25,921	4,173,281	12.688	5.440
162	508.94	20611.99	26,244	4,251,528	12.727	5.451
163	512.08	20867.24	26,569	4,330,747	12.767	5.462
164	515.22	21124.07	26,896	4,410,944	12.806	5.473
165	518.36	21382.46	27,225	4,492,125	12.845	5.484

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
166	521.50	21642.43	27,556	4,574,296	12.844	5.495
167	524.65	21903.97	27,889	4,657,463	12.922	5.506
168	527.79	22167.08	28,224	4,741,632	12.961	5.517
169	530.93	22431.76	28,561	4,826,809	13.000	5.528
170	534.07	22698.01	28,900	4,913,000	13.038	5.539
171	537.21	22965.83	29,241	5,000,211	13.076	5.550
172	540.35	23235.22	29,584	5,088,448	13.114	5.561
173	543.50	23506.18	29,929	5,177,717	13.152	5.572
174	546.64	23778.71	30,276	5,268,024	13.190	5.582
175	549.78	24052.82	30,625	5,359,375	13.228	5.593
176	552.92	24328.49	30,976	5,451,776	13.266	5.604
177	556.06	24605.79	31,329	5,545,233	13.304	5.614
178	559.20	24884.56	31,684	5,639,752	13.341	5.625
179	562.34	25164.94	32,041	5,735,339	13.379	5.635
180	565.49	25446.90	32,400	5,832,000	13.416	5.646
181	568.63	25730.43	32,761	5,929,741	13.453	5.656
182	571.77	26015.53	33,124	6,028,568	13.490	5.667
183	574.91	26302.20	33,489	6,128,487	13.527	5.677
184	578.05	26590.44	33,856	6,229,504	13.564	5.687
185	581.19	26880.25	34,225	6,331,625	13.601	5.698
186	584.34	27171.63	34,596	6,434,856	13.638	5.708
187	587.48	27464.59	34,969	6,539,203	13.674	5.718
188	590.62	27759.11	35,344	6,644,672	13.711	5.728
189	593.76	28055.21	35,721	6,751,269	13.747	5.738
190	596.90	28352.87	36,100	6,859,000	13.784	5.748
191	600.04	28652.11	36,481	6,967,871	13.820	5.758
192	603.19	28952.92	36,864	7,077,888	13.856	5.768
193	606.33	29255.30	37,249	7,189,057	13.892	5.778
194	609.47	29559.26	37,636	7,301,384	13.928	5.788
195	612.61	29864.77	38,025	7,414,875	13.964	5.798
196	615.75	30171.86	38,416	7,529,536	14.000	5.808
197	618.89	30480.52	38,809	7,645,373	14.035	5.818
198	622.03	30790.75	39,204	7,762,392	14.071	5.828
199	625.18	31102.55	39,601	7,880,599	14.106	5.838
200	628.32	31415.93	40,000	8,000,000	14.142	5.848
201	631.46	31730.87	40,401	8,120,601	14.177	5.857
202	634.60	32047.39	40,804	8,242,408	14.212	5.867
203	637.74	32365.47	41,209	8,365,427	14.247	5.877
204	640.88	32685.13	41,616	8,489,664	14.282	5.886
205	644.03	33006.36	42,025	8,615,125	14.317	5.896
206	647.17	33329.16	42,436	8,741,816	14.352	5.905
207	650.31	33653.53	42,849	8,869,743	14.387	5.915

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
208	653.45	33979.47	13,264	8,998,912	14.422	5.924
209	656.59	34306.98	43,681	9,123,329	14.456	5.934
210	659.73	34636.06	44,100	9,261,000	14.491	5.943
211	662.88	34966.71	44,521	9,393,931	14.525	5.953
212	666.02	35298.94	44,944	9,528,128	14.560	5.962
213	669.16	35632.73	45,369	9,663,597	14.594	5.972
214	672.30	35968.09	45,796	9,800,344	14.628	5.981
215	675.44	36305.03	46,225	9,938,375	14.662	5.990
216	678.58	36643.61	46,656	10,077,696	14.696	6.000
217	681.73	36983.61	47,089	10,218,313	14.730	6.009
218	684.87	37325.26	47,524	10,360,232	14.764	6.018
219	688.01	37668.48	47,961	10,503,459	14.798	6.027
220	691.15	38013.27	48,400	10,648,000	14.832	6.036
221	694.29	38359.63	48,841	10,793,861	14.866	6.045
222	697.43	38707.56	49,284	10,941,048	14.899	6.055
223	700.57	39057.07	49,729	11,089,567	14.933	6.064
224	703.72	39408.14	50,176	11,239,424	14.966	6.073
225	706.86	39760.78	50,625	11,390,625	15.000	6.082
226	710.00	40115.00	51,076	11,543,176	15.033	6.091
227	713.14	40470.78	51,529	11,697,083	15.066	6.100
228	716.28	40828.14	51,984	11,852,352	15.099	6.109
229	719.42	41187.07	52,441	12,008,989	15.132	6.118
230	722.57	41547.56	52,900	12,167,000	15.165	6.126
231	725.71	41909.63	53,361	12,326,391	15.198	6.135
232	728.85	42273.27	53,824	12,487,168	15.231	6.144
233	731.99	42638.48	54,289	12,649,337	15.264	6.153
234	735.13	43005.26	54,756	12,812,901	15.297	6.162
235	738.27	43373.61	55,225	12,977,875	15.329	6.171
236	741.42	43743.54	55,696	13,144,256	15.362	6.179
237	744.56	44115.03	56,169	13,312,053	15.394	6.188
238	747.70	44488.09	56,644	13,481,272	15.427	6.197
239	750.84	44862.73	57,121	13,651,919	15.459	6.205
240	753.98	45238.93	57,600	13,824,000	15.491	6.214
241	757.12	45616.71	58,081	13,997,521	15.524	6.223
242	760.26	45996.06	58,564	14,172,488	15.556	6.231
243	763.41	46376.98	59,049	14,348,907	15.588	6.240
244	766.55	46759.47	59,536	14,526,784	15.620	6.248
245	769.69	47143.52	60,025	14,706,125	15.652	6.257
246	772.83	47529.16	60,516	14,886,936	15.684	6.265
247	775.97	47916.36	61,009	15,069,223	15.716	6.274
248	779.11	48305.13	61,504	15,252,992	15.748	6.282
249	782.26	48695.47	62,001	15,438,249	15.779	6.291

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
250	785.40	49087.39	62,500	15,625,000	15.811	6.299
251	788.54	49480.87	63,001	15,813,251	15.842	6.307
252	791.68	49875.92	63,504	16,003,008	15.874	6.316
253	794.82	50272.55	64,009	16,194,277	15.905	6.324
254	797.96	50670.75	64,516	16,387,064	15.937	6.333
255	801.11	51070.52	65,025	16,581,375	15.968	6.341
256	804.25	51471.86	65,536	16,777,216	16.000	6.349
257	807.39	51874.76	66,049	16,974,593	16.031	6.357
258	810.53	52279.24	66,564	17,173,512	16.062	6.366
259	813.67	52685.29	67,081	17,373,979	16.093	6.374
260	816.81	53092.96	67,600	17,576,000	16.124	6.382
261	819.96	53502.11	68,121	17,779,581	16.155	6.390
262	823.10	53912.87	68,644	17,984,728	16.186	6.398
263	826.24	54325.21	69,169	18,191,447	16.217	6.406
264	829.38	54739.11	69,696	18,399,744	16.248	6.415
265	832.52	55154.59	70,225	18,609,625	16.278	6.423
266	835.66	55571.63	70,756	18,821,096	16.309	6.431
267	838.80	55990.25	71,289	19,034,163	16.340	6.439
268	841.95	56410.44	71,824	19,248,832	16.370	6.447
269	845.09	56832.20	72,361	19,465,109	16.401	6.455
270	848.23	57255.53	72,900	19,683,000	16.431	6.463
271	851.37	57680.43	73,441	19,902,511	16.462	6.471
272	854.51	58106.90	73,984	20,123,648	16.492	6.479
273	857.65	58534.94	74,529	20,346,417	16.522	6.487
274	860.80	58964.55	75,076	20,570,824	16.552	6.495
275	863.94	59395.74	75,625	20,796,875	16.583	6.502
276	867.08	59828.49	76,176	21,024,576	16.613	6.510
277	870.22	60262.82	76,729	21,253,933	16.643	6.518
278	873.36	60698.72	77,284	21,484,952	16.673	6.526
279	876.50	61136.18	77,841	21,717,639	16.703	6.534
280	879.65	61575.22	78,400	21,952,000	16.733	6.542
281	882.79	62015.82	78,961	22,188,041	16.763	6.549
282	885.93	62458.00	79,524	22,425,768	16.792	6.557
283	889.07	62901.75	80,089	22,665,187	16.822	6.565
284	892.21	63347.07	80,656	22,906,304	16.852	6.573
285	895.35	63793.97	81,225	23,149,125	16.881	6.580
286	898.49	64242.43	81,796	23,393,656	16.911	6.588
287	901.64	64692.46	82,369	23,639,903	16.941	6.596
288	904.78	65144.07	82,944	23,887,872	16.970	6.603
289	907.92	65597.24	83,521	24,137,569	17.000	6.611
290	911.06	66051.99	84,100	24,389,000	17.029	6.619
291	914.20	66508.30	84,681	24,642,171	17.059	6.627

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
292	917.34	66966.19	85,264	24,897,088	17.088	6.634
293	920.49	67425.65	85,849	25,153,757	17.117	6.642
294	923.63	67886.68	86,436	25,412,184	17.146	6.649
295	926.77	68349.28	87,025	25,672,375	17.176	6.657
296	929.91	68813.45	87,616	25,934,336	17.205	6.664
297	933.05	69279.19	88,209	26,198,073	17.234	6.672
298	936.19	69746.50	88,804	26,463,592	17.263	6.679
299	939.34	70215.38	89,401	26,730,899	17.292	6.687
300	942.48	70685.83	90,000	27,000,000	17.320	6.694
301	945.62	71157.86	90,601	27,270,901	17.349	6.702
302	948.76	71631.45	91,204	27,543,608	17.378	6.709
303	951.90	72106.62	91,809	27,818,127	17.407	6.717
304	955.04	72583.36	92,416	28,094,464	17.436	6.724
305	958.19	73061.66	93,025	28,372,625	17.464	6.731
306	961.33	73541.54	93,636	28,652,616	17.493	6.739
307	964.47	74022.99	94,249	28,934,443	17.521	6.746
308	967.61	74506.01	94,864	29,218,112	17.549	6.753
309	970.75	74990.60	95,481	29,503,629	17.578	6.761
310	973.89	75476.76	96,100	29,791,000	17.607	6.768
311	977.03	75964.50	96,721	30,080,231	17.635	6.775
312	980.18	76453.80	97,344	30,371,328	17.663	6.782
313	983.32	76944.67	97,969	30,664,297	17.692	6.789
314	986.46	77437.12	98,596	30,959,144	17.720	6.797
315	989.60	77931.13	99,225	31,255,875	17.748	6.804
316	992.74	78426.72	99,856	31,554,496	17.776	6.811
317	995.88	78923.88	100,489	31,855,013	17.804	6.818
318	999.03	79422.60	101,124	32,157,432	17.832	6.826
319	1002.17	79922.90	101,761	32,461,759	17.860	6.833
320	1005.31	80424.77	102,400	32,768,000	17.888	6.839
321	1008.45	80928.21	103,041	33,076,161	17.916	6.847
322	1011.59	81433.22	103,684	33,386,248	17.944	6.854
323	1014.73	81939.80	104,329	33,698,267	17.972	6.861
324	1017.88	82447.96	104,976	34,012,224	18.000	6.868
325	1021.02	82957.68	105,625	34,328,125	18.028	6.875
326	1024.16	83468.98	106,276	34,645,976	18.055	6.882
327	1027.30	83981.84	106,929	34,965,783	18.083	6.889
328	1030.44	84496.28	107,584	35,287,552	18.111	6.896
329	1033.58	85012.28	108,241	35,611,289	18.138	6.903
330	1036.73	85529.86	108,900	35,937,000	18.166	6.910
331	1039.87	86049.01	109,561	36,264,691	18.193	6.917
332	1043.01	86569.73	110,224	36,594,368	18.221	6.924
333	1046.15	87092.02	110,889	36,926,037	18.248	6.931

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
334	1049.29	87615.88	111,556	37,259,704	18.276	6.938
335	1052.43	88141.31	112,225	37,595,375	18.303	6.945
336	1055.57	88668.31	112,896	37,933,056	18.330	6.952
337	1058.72	89196.88	113,569	38,272,753	18.357	6.959
338	1061.86	89727.03	114,244	38,614,472	18.385	6.965
339	1065.00	90258.74	114,921	38,958,219	18.412	6.973
340	1068.14	90792.03	115,600	39,304,000	18.439	6.979
341	1071.28	91326.88	116,281	39,651,821	18.466	6.986
342	1074.42	91863.31	116,964	40,001,688	18.493	6.993
343	1077.57	92401.31	117,649	40,353,607	18.520	7.000
344	1080.71	92940.88	118,336	40,707,584	18.547	7.007
345	1083.85	93482.02	119,025	41,063,625	18.574	7.014
346	1086.99	94024.73	119,716	41,421,736	18.601	7.020
347	1090.13	94569.01	120,409	41,781,923	18.628	7.027
348	1093.27	95114.86	121,104	42,144,192	18.655	7.034
349	1096.42	95662.28	121,801	42,508,549	18.681	7.040
350	1099.56	96211.28	122,500	42,875,000	18.708	7.047
351	1102.70	96761.84	123,201	43,243,551	18.735	7.054
352	1105.84	97314.76	123,904	43,614,208	18.762	7.061
353	1108.98	97867.68	124,609	43,986,977	18.788	7.067
354	1112.12	98422.96	125,316	44,361,864	18.815	7.074
355	1115.26	98979.80	126,025	44,738,875	18.842	7.081
356	1118.41	99538.22	126,736	45,118,016	18.868	7.087
357	1121.55	100098.21	127,449	45,499,293	18.894	7.094
358	1124.69	100659.27	128,164	45,882,712	18.921	7.101
359	1127.83	101222.90	128,881	46,268,279	18.947	7.107
360	1130.97	101787.60	129,600	46,656,000	18.974	7.114
361	1134.11	102353.87	130,321	47,045,881	19.000	7.120
362	1137.26	102921.72	131,044	47,437,928	19.026	7.127
363	1140.40	103491.13	131,769	47,832,147	19.052	7.133
364	1143.54	104062.12	132,496	48,228,544	19.079	7.140
365	1146.68	104634.67	133,225	48,627,125	19.105	7.146
366	1149.82	105208.80	133,956	49,027,896	19.131	7.153
367	1152.96	105784.49	134,689	49,430,863	19.157	7.159
368	1156.11	106361.76	135,424	49,836,032	19.183	7.166
369	1159.25	106940.60	136,161	50,243,409	19.209	7.172
370	1162.39	107521.01	136,900	50,653,000	19.235	7.179
371	1165.53	108102.99	137,641	51,064,811	19.261	7.185
372	1168.67	108686.54	138,384	51,478,848	19.287	7.192
373	1171.81	109271.66	139,129	51,895,117	19.313	7.198
374	1174.96	109858.35	139,876	52,313,624	19.339	7.205
375	1178.10	110446.62	140,625	52,734,375	19.365	7.211

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
376	1181.24	111036.45	141,376	53,157,376	19.391	7.218
377	1184.38	111627.86	142,129	53,582,633	19.416	7.224
378	1187.52	112220.83	142,884	54,010,152	19.442	7.230
379	1190.66	112815.38	143,641	54,439,939	19.468	7.237
380	1193.80	113411.49	144,400	54,872,000	19.493	7.243
381	1196.95	114009.18	145,161	55,306,341	19.519	7.249
382	1200.09	114608.44	145,924	55,742,968	19.545	7.256
383	1203.23	115209.27	146,689	56,181,887	19.570	7.262
384	1206.37	115811.67	147,456	56,623,104	19.596	7.268
385	1209.51	116415.64	148,225	57,066,625	19.621	7.275
386	1212.65	117021.18	148,996	57,512,456	19.647	7.281
387	1215.80	117628.30	149,769	57,960,603	19.672	7.287
388	1218.94	118236.98	150,544	58,411,072	19.698	7.294
389	1222.08	118847.24	151,321	58,863,869	19.723	7.299
390	1225.22	119459.06	152,100	59,319,000	19.748	7.306
391	1228.36	120072.46	152,881	59,776,471	19.774	7.312
392	1231.50	120687.42	153,664	60,236,288	19.799	7.319
393	1234.65	121303.96	154,449	60,698,457	19.824	7.325
394	1237.79	121922.07	155,236	61,162,984	19.849	7.331
395	1240.93	122541.75	156,025	61,629,875	19.875	7.337
396	1244.07	123163.00	156,816	62,099,136	19.899	7.343
397	1247.21	123785.82	157,609	62,570,773	19.925	7.349
398	1250.35	124410.21	158,404	63,044,792	19.949	7.356
399	1253.49	125036.17	159,201	63,521,199	19.975	7.362
400	1256.61	125663.71	160,000	64,000,000	20.000	7.368
401	1259.78	126292.81	160,801	64,481,201	20.025	7.374
402	1262.92	126923.48	161,604	64,964,808	20.049	7.380
403	1266.06	127553.73	162,409	65,450,827	20.075	7.386
404	1269.20	128189.55	163,216	65,939,264	20.099	7.392
405	1272.34	128824.93	164,025	66,430,125	20.125	7.399
406	1275.49	129461.89	164,836	66,923,416	20.149	7.405
407	1278.63	130100.42	165,649	67,419,143	20.174	7.411
408	1281.77	130740.52	166,464	67,911,312	20.199	7.417
409	1284.91	131382.19	167,281	68,417,929	20.224	7.422
410	1288.05	132025.43	168,100	68,921,000	20.248	7.429
411	1291.19	132670.24	168,921	69,426,531	20.273	7.434
412	1294.34	133316.63	169,744	69,934,528	20.298	7.441
413	1297.48	133964.58	170,569	70,444,997	20.322	7.447
414	1300.62	134614.10	171,396	70,957,944	20.347	7.453
415	1303.76	135265.20	172,225	71,473,375	20.371	7.459
416	1306.90	135917.86	173,056	71,991,296	20.396	7.465
417	1310.04	136572.10	173,889	72,511,713	20.421	7.471



No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
418	1313.19	137227.91	174,724	73,034,632	20.445	7.477
419	1316.33	137885.29	175,561	73,560,059	20.469	7.483
420	1319.47	138544.24	176,400	74,088,000	20.494	7.489
421	1322.61	139204.70	177,241	74,618,461	20.518	7.495
422	1325.75	139866.85	178,084	75,151,448	20.543	7.501
423	1328.89	140530.51	178,929	75,686,967	20.567	7.507
424	1332.03	141195.74	179,776	76,225,024	20.591	7.513
425	1335.18	141862.54	180,625	76,765,625	20.615	7.518
426	1338.32	142530.92	181,476	77,308,776	20.639	7.524
427	1341.46	143200.86	182,329	77,854,483	20.664	7.530
428	1344.60	143872.38	183,184	78,402,752	20.688	7.536
429	1347.74	144545.46	184,041	78,953,589	20.712	7.542
430	1550.88	145220.12	184,900	79,507,000	20.736	7.548
431	1354.03	145896.35	185,761	80,062,991	20.760	7.554
432	1357.17	146574.15	186,624	80,621,568	20.785	7.559
433	1360.31	147253.52	187,489	81,182,737	20.809	7.565
434	1363.45	147934.46	188,356	81,746,504	20.833	7.571
435	1366.59	148616.97	189,225	82,312,875	20.857	7.577
436	1369.73	149301.05	190,096	82,881,856	20.881	7.583
437	1372.88	149986.70	190,969	83,453,453	20.904	7.588
438	1376.02	150673.93	191,844	84,027,672	20.928	7.594
439	1379.16	151362.72	192,721	84,604,519	20.952	7.600
440	1382.30	152053.08	193,600	85,184,000	20.976	7.606
441	1385.44	152745.02	194,481	85,766,121	21.000	7.612
442	1388.58	153438.53	195,364	86,350,388	21.024	7.617
443	1391.73	154133.60	196,249	86,938,307	21.047	7.623
444	1394.87	154830.25	197,136	87,528,384	21.071	7.629
445	1398.01	155528.47	198,025	88,121,125	21.095	7.635
446	1401.15	156228.26	198,916	88,716,536	21.119	7.640
447	1404.29	156929.62	199,809	89,314,623	21.142	7.646
448	1407.43	157632.55	200,704	89,915,392	21.166	7.652
449	1410.57	158337.06	201,601	90,518,849	21.189	7.657
450	1413.72	159043.13	202,500	91,125,000	21.213	7.663
451	1416.86	159750.77	203,401	91,733,851	21.237	7.669
452	1420.00	160459.99	204,304	92,345,408	21.260	7.674
453	1423.14	161170.77	205,209	92,959,677	21.284	7.680
454	1426.28	161883.13	206,106	93,576,664	21.307	7.686
455	1429.42	162597.06	207,025	94,196,375	21.331	7.691
456	1432.57	163312.55	207,936	94,818,816	21.354	7.697
457	1435.71	164029.62	208,849	95,443,993	21.377	7.703
458	1438.85	164748.26	209,764	96,071,912	21.401	7.708
459	1441.99	165468.47	210,681	96,702,579	21.424	7.714

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
460	1445.13	166190.25	211,600	97,336,000	21.447	7.719
461	1448.27	166913.60	212,521	97,972,181	21.471	7.725
462	1451.42	167638.53	213,444	98,611,128	21.494	7.731
463	1454.56	168365.02	214,369	99,252,847	21.517	7.736
464	1457.70	169093.08	215,296	99,897,345	21.541	7.742
465	1460.84	169822.72	216,225	100,544,625	21.564	7.747
466	1463.98	170553.92	217,156	101,194,696	21.587	7.753
467	1467.12	171286.70	218,089	101,847,563	21.610	7.758
468	1470.26	172021.05	219,024	102,503,232	21.633	7.764
469	1473.41	172756.97	219,961	103,161,709	21.656	7.769
470	1476.55	173494.45	220,900	103,823,000	21.679	7.775
471	1479.69	174233.51	221,841	104,487,111	21.702	7.780
472	1482.83	174974.14	222,784	105,154,048	21.725	7.786
473	1485.97	175716.35	223,729	105,823,817	21.749	7.791
474	1489.11	176460.12	224,676	106,496,424	21.771	7.797
475	1492.26	177205.46	225,625	107,171,875	21.794	7.802
476	1495.40	177952.37	226,576	107,850,176	21.817	7.808
477	1498.54	178700.86	227,529	108,531,333	21.840	7.813
478	1501.68	179450.91	228,484	109,215,352	21.863	7.819
479	1504.82	180202.54	229,441	109,902,239	21.886	7.824
480	1507.96	180955.74	230,400	110,592,000	21.909	7.830
481	1511.11	181710.50	231,361	111,284,641	21.932	7.835
482	1514.25	182466.84	232,324	111,980,168	21.954	7.840
483	1517.39	183224.75	233,289	112,678,587	21.977	7.846
484	1520.53	183984.23	234,256	113,379,904	22.000	7.851
485	1523.67	184745.28	235,225	114,084,125	22.023	7.857
486	1526.81	185507.90	236,196	114,791,256	22.045	7.862
487	1529.96	186272.10	237,169	115,501,303	22.069	7.868
488	1533.10	187037.86	238,144	116,214,272	22.091	7.873
489	1536.24	187805.19	239,121	116,936,169	22.113	7.878
490	1539.38	188574.10	240,100	117,649,000	22.136	7.884
491	1542.52	189344.57	241,081	118,370,771	22.158	7.889
492	1545.66	190116.62	242,064	119,095,488	22.181	7.894
493	1548.80	190890.24	243,049	119,823,157	22.204	7.899
494	1551.95	191665.43	244,036	120,553,784	22.226	7.905
495	1555.09	192442.19	245,025	121,287,375	22.248	7.910
496	1558.23	193220.51	246,016	122,023,936	22.271	7.915
497	1561.37	194000.42	247,009	122,763,473	22.293	7.921
498	1564.51	194781.89	248,004	123,505,992	22.316	7.926
499	1567.65	195564.93	249,001	124,251,499	22.338	7.932
500	1570.80	196349.54	250,000	125,000,000	22.361	7.937
501	1573.94	197135.72	251,001	125,751,501	22.383	7.942

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
502	1577.08	197923.48	252,004	126,506,008	22.405	7.947
503	1580.22	198712.80	253,009	127,263,527	22.428	7.953
504	1583.36	199503.70	254,016	128,024,864	22.449	7.958
505	1586.50	200296.17	255,025	128,787,625	22.472	7.963
506	1589.65	201090.20	256,036	129,554,216	22.494	7.969
507	1592.79	201885.81	257,049	130,323,843	22.517	7.974
508	1595.93	202682.99	258,064	131,096,512	22.539	7.979
509	1599.07	203481.74	259,081	131,872,229	22.561	7.984
510	1602.21	204282.06	260,100	132,651,000	22.583	7.989
511	1605.35	205083.95	261,121	133,432,831	22.605	7.995
512	1608.49	205887.42	262,144	134,217,728	22.627	8.000
513	1611.64	206692.45	263,169	135,005,697	22.649	8.005
514	1614.78	207499.05	264,196	135,796,744	22.671	8.010
515	1617.92	208307.23	265,225	136,590,875	22.694	8.016
516	1621.06	209116.97	266,256	137,388,096	22.716	8.021
517	1624.20	209928.29	267,289	138,188,413	22.738	8.026
518	1627.34	210741.18	268,324	138,991,832	22.759	8.031
519	1630.49	211555.63	269,361	139,798,359	22.782	8.036
520	1633.63	212371.66	270,400	140,608,000	22.803	8.041
521	1636.77	213189.26	271,441	141,420,761	22.825	8.047
522	1639.91	214008.43	272,484	142,236,648	22.847	8.052
523	1643.05	214829.17	273,529	143,055,667	22.869	8.057
524	1646.19	215651.49	274,576	143,877,824	22.891	8.062
525	1649.34	216475.37	275,625	144,703,125	22.913	8.067
526	1652.48	217300.82	276,676	145,531,576	22.935	8.072
527	1655.62	218127.85	277,729	146,363,183	22.956	8.077
528	1658.76	218956.44	278,784	147,197,952	22.978	8.082
529	1661.90	219786.61	279,841	148,035,889	23.000	8.087
530	1665.04	220618.32	280,900	148,877,000	23.022	8.093
531	1668.19	221451.65	281,961	149,721,291	23.043	8.098
532	1671.33	222286.53	283,024	150,568,768	23.065	8.103
533	1674.47	223122.98	284,089	151,419,437	23.087	8.108
534	1677.61	223961.00	285,156	152,273,304	23.108	8.113
535	1680.75	224800.59	286,225	153,130,375	23.130	8.118
536	1683.89	225641.75	287,296	153,990,656	23.152	8.123
537	1687.04	226484.48	288,369	154,854,153	23.173	8.128
538	1690.18	227328.77	289,444	155,720,872	23.195	8.133
539	1693.32	228174.66	290,521	156,590,819	23.216	8.138
540	1696.46	229022.10	291,600	157,464,000	23.238	8.143
541	1699.60	229871.12	292,681	158,340,421	23.259	8.148
542	1702.74	230721.71	293,764	159,220,088	23.281	8.153
543	1705.88	231573.86	294,849	160,103,007	23.302	8.158

No. or Diam.	Circum- ference	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
544	1709.03	232427.59	295,936	160,989,184	23.324	8.163
545	1712.17	233282.89	297,025	161,878,625	23.345	8.168
546	1715.31	234139.76	298,116	162,771,336	23.367	8.173
547	1718.45	234998.20	299,209	163,667,323	23.388	8.178
548	1721.59	235858.21	300,304	164,566,592	23.409	8.183
549	1724.73	236719.79	301,401	165,469,149	23.431	8.188
550	1727.88	237582.94	302,500	166,375,000	23.452	8.193
551	1731.02	238447.67	303,601	167,284,151	23.473	8.198
552	1734.16	239313.96	304,704	168,196,608	23.495	8.203
553	1737.30	240181.83	305,809	169,112,377	23.516	8.208
554	1740.44	241051.26	306,916	170,031,464	23.537	8.213
555	1743.58	241922.27	308,025	170,953,875	23.558	8.218
556	1746.73	242794.85	309,136	171,879,616	23.579	8.223
557	1749.87	243668.99	310,249	172,808,693	23.601	8.228
558	1753.00	244544.61	311,364	173,741,112	23.622	8.233
559	1756.15	245422.00	312,481	174,676,879	23.643	8.238
560	1759.29	246300.86	313,600	175,616,000	23.664	8.242
561	1762.43	247181.30	314,721	176,558,481	23.685	8.247
562	1765.57	248062.30	315,844	177,504,328	23.706	8.252
563	1768.72	248946.87	316,969	178,453,547	23.728	8.257
564	1771.86	249832.01	318,096	179,406,144	23.749	8.262
565	1775.00	250718.73	319,225	180,362,125	23.769	8.267
566	1778.14	251607.01	320,356	181,321,496	23.791	8.272
567	1781.28	252496.87	321,489	182,284,263	23.812	8.277
568	1784.42	253388.30	322,624	183,250,432	23.833	8.282
569	1787.57	254281.30	323,761	184,220,009	23.854	8.286
570	1790.71	255175.86	324,900	185,193,000	23.875	8.291
571	1793.85	256072.00	326,041	186,169,411	23.896	8.296
572	1796.99	256969.71	327,184	187,149,248	23.916	8.301
573	1800.13	257868.99	328,329	188,132,517	23.937	8.306
574	1803.27	258769.85	329,476	189,119,224	23.958	8.311
575	1806.42	259672.27	330,625	190,109,375	23.979	8.315
576	1809.56	260576.26	331,776	191,102,976	24.000	8.320
577	1812.70	261481.83	332,929	192,100,033	24.021	8.325
578	1815.84	262388.96	334,084	193,100,552	24.042	8.330
579	1818.98	263297.67	335,241	194,104,539	24.062	8.335
580	1822.12	264207.94	336,400	195,112,000	24.083	8.339
581	1825.26	265119.79	337,561	196,122,941	24.104	8.344
582	1828.41	266033.21	338,724	197,137,368	24.125	8.349
583	1831.55	266948.20	339,889	198,155,287	24.145	8.354
584	1834.69	267864.76	341,056	199,176,704	24.166	8.359
585	1837.83	268782.80	342,225	200,201,625	24.187	8.363

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
586	1840.97	269702.59	343,396	201,230,056	24.207	8.368
587	1844.11	270623.86	344,569	202,262,003	24.228	8.373
588	1847.26	271546.70	345,744	203,297,472	24.249	8.378
589	1850.40	272471.12	346,921	204,336,469	24.269	8.382
590	1853.54	273397.10	348,100	205,379,000	24.289	8.387
591	1856.68	274324.66	349,281	206,425,071	24.310	8.392
592	1859.82	275253.78	350,464	207,474,688	24.331	8.397
593	1862.96	276184.48	351,649	208,527,857	24.351	8.401
594	1866.11	277116.75	352,836	209,584,584	24.372	8.406
595	1869.25	278050.59	354,025	210,644,875	24.393	8.411
596	1872.39	278985.99	355,216	211,708,736	24.413	8.415
597	1875.53	279922.97	356,409	212,776,173	24.433	8.420
598	1878.67	280861.53	357,604	213,847,192	24.454	8.425
599	1881.81	281801.65	358,801	214,921,799	24.474	8.429
600	1884.96	282743.34	360,000	216,000,000	24.495	8.434
601	1888.10	283686.60	361,201	217,081,801	24.515	8.439
602	1891.24	284631.44	362,404	218,167,208	24.536	8.444
603	1894.38	285577.84	363,609	219,256,227	24.556	8.448
604	1897.52	286525.82	364,816	220,348,864	24.576	8.453
605	1900.66	287475.36	366,025	221,445,125	24.597	8.458
606	1903.80	288426.48	367,236	222,545,016	24.617	8.462
607	1906.95	289379.17	368,449	223,648,543	24.637	8.467
608	1910.09	290333.43	369,664	224,755,712	24.658	8.472
609	1913.23	291289.26	370,881	225,866,529	24.678	8.476
610	1916.37	292246.66	372,100	226,981,000	24.698	8.481
611	1919.51	293205.63	373,321	228,099,131	24.718	8.485
612	1922.65	294166.17	374,544	229,220,928	24.739	8.490
613	1925.80	295128.28	375,769	230,346,397	24.758	8.495
614	1928.94	296091.97	376,996	231,475,544	24.779	8.499
615	1932.08	297057.22	378,225	232,608,375	24.799	8.504
616	1935.22	298024.05	379,456	233,744,896	24.819	8.509
617	1938.36	298992.44	380,689	234,885,113	24.839	8.513
618	1941.50	299962.41	381,924	236,029,032	24.859	8.518
619	1944.65	300933.95	383,161	237,176,659	24.879	8.522
620	1947.79	301907.05	384,400	238,628,000	24.899	8.527
621	1950.93	302881.73	385,641	239,483,061	24.919	8.532
622	1954.07	303857.98	386,884	240,641,848	24.939	8.536
623	1957.21	304835.80	388,129	241,804,367	24.959	8.541
624	1960.35	305815.20	389,376	242,970,624	24.980	8.545
625	1963.50	306796.16	390,625	244,140,625	25.000	8.549
626	1966.64	307778.69	391,876	245,314,376	25.019	8.554
627	1969.78	308762.79	393,129	246,491,883	25.040	8.559

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
628	1972.92	309748.47	394,384	247,673,152	25.059	8.563
629	1976.06	310735.71	395,641	248,858,189	25.079	8.568
630	1979.20	311724.53	396,900	250,047,000	25.099	8.573
631	1982.34	312714.92	398,161	251,239,591	25.119	8.577
632	1985.49	313706.88	399,424	252,435,968	25.139	8.582
633	1988.63	314700.40	400,689	253,636,137	25.159	8.586
634	1991.77	315695.50	401,956	254,840,104	25.179	8.591
635	1994.91	316692.17	403,225	256,047,875	25.199	8.595
636	1998.05	317690.42	404,496	257,259,456	25.219	8.599
637	2001.19	318690.23	405,769	258,474,853	25.239	8.604
638	2004.34	319691.61	407,044	259,694,072	25.259	8.609
639	2007.48	320694.56	408,321	260,917,119	25.278	8.613
640	2010.62	321699.09	409,600	262,144,000	25.298	8.618
641	2013.76	322705.18	410,881	263,374,721	25.318	8.622
642	2016.90	323712.85	412,164	264,609,288	25.338	8.627
643	2020.04	324722.09	413,449	265,847,707	25.357	8.631
644	2023.19	325732.89	414,736	267,089,984	25.377	8.636
645	2026.33	326745.27	416,025	268,836,125	25.397	8.640
646	2029.47	327759.22	417,316	269,586,136	25.416	8.644
647	2032.61	328774.74	418,609	270,840,023	25.436	8.649
648	2035.75	329791.83	419,904	272,097,792	25.456	8.653
649	2038.89	330810.49	421,201	273,359,449	25.475	8.658
650	2042.04	331830.72	422,500	274,625,000	25.495	8.662
651	2045.18	332852.53	423,801	275,894,451	25.515	8.667
652	2048.32	333875.90	425,104	277,167,808	25.534	8.671
653	2051.46	334900.85	426,409	278,445,077	25.554	8.676
654	2054.60	335927.36	427,716	279,726,264	25.573	8.680
655	2057.74	336955.45	429,025	281,011,375	25.593	8.684
656	2060.88	337985.10	430,336	282,800,416	25.612	8.689
657	2064.03	339016.33	431,649	283,593,393	25.632	8.693
658	2067.17	340049.13	432,964	284,890,312	25.651	8.698
659	2070.31	341083.50	434,281	286,191,179	25.671	8.702
660	2073.45	342119.44	435,600	287,496,000	25.690	8.706
661	2076.59	343156.95	436,921	288,804,781	25.710	8.711
662	2079.73	344196.03	438,244	290,117,528	25.720	8.715
663	2082.88	345236.69	439,569	291,434,247	25.749	8.719
664	2086.02	346278.91	440,896	292,754,944	25.768	8.724
665	2089.16	347322.70	442,225	294,079,625	25.787	8.728
666	2092.30	348368.07	443,556	295,408,296	25.807	8.733
667	2095.44	349415.00	444,889	296,740,963	25.826	8.737
668	2098.58	350463.51	446,224	298,077,632	25.846	8.742
669	2101.73	351513.59	447,561	299,418,309	25.865	8.746

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
670	2104.87	352565.24	448,900	300,763,000	25.884	8.750
671	2108.01	353618.43	450,241	302,111,711	25.904	8.753
672	2111.15	354673.24	451,584	303,464,448	25.923	8.759
673	2114.29	355729.60	452,929	304,821,217	25.942	8.763
674	2117.43	356787.54	454,276	306,182,024	25.961	8.768
675	2120.58	357847.04	455,625	307,546,875	25.981	8.772
676	2123.72	358908.11	456,976	308,915,776	26.000	8.776
677	2126.86	359970.75	458,329	310,288,733	26.019	8.781
678	2130.00	361034.97	459,684	311,665,752	26.038	8.785
679	2133.14	362100.75	461,041	313,046,839	26.058	8.789
680	2136.28	363168.11	462,400	314,432,000	26.077	8.794
681	2139.42	364237.04	463,761	315,821,241	26.096	8.798
682	2142.57	365307.54	465,124	317,214,568	26.115	8.802
683	2145.71	366379.60	466,489	318,611,987	26.134	8.807
684	2148.85	367453.24	467,856	320,013,504	26.153	8.811
685	2151.99	368528.45	469,225	321,419,125	26.172	8.815
686	2155.13	369605.23	470,596	322,828,856	26.192	8.819
687	2158.27	370683.59	471,969	324,242,703	26.211	8.824
688	2161.42	371763.51	473,344	325,660,672	26.229	8.828
689	2164.56	372845.00	474,721	327,082,769	26.249	8.832
690	2167.70	373928.07	476,100	328,509,000	26.268	8.836
691	2170.84	375012.70	477,481	329,939,371	26.287	8.841
692	2173.98	376098.91	478,864	331,373,888	26.306	8.845
693	2177.12	377186.68	480,249	332,812,557	26.325	8.849
694	2180.27	378276.03	481,636	334,255,384	26.344	8.853
695	2183.41	379366.95	483,025	335,702,375	26.363	8.858
696	2186.55	380459.44	484,416	337,153,536	26.382	8.862
697	2189.69	381553.50	485,809	338,608,873	26.401	8.866
698	2192.83	382649.43	487,204	340,068,392	26.419	8.870
699	2195.97	383746.33	488,601	341,532,099	26.439	8.875
700	2199.12	384845.10	490,000	343,000,000	26.457	8.879
701	2202.26	385945.44	491,401	344,472,101	26.476	8.883
702	2205.40	387047.36	492,804	345,948,088	26.495	8.887
703	2208.54	388150.84	494,209	347,428,927	26.514	8.892
704	2211.68	389255.90	495,616	348,913,664	26.533	8.896
705	2214.82	390362.52	497,025	350,402,625	26.552	8.900
706	2217.96	391470.32	498,436	351,895,816	26.571	8.904
707	2221.11	392580.49	499,849	353,393,243	26.589	8.908
708	2224.25	393691.83	501,264	354,894,912	26.608	8.913
709	2227.39	394804.74	502,681	356,400,829	26.627	8.917
710	2230.53	395919.21	504,100	357,911,000	26.644	8.921
711	2233.67	397035.27	505,521	359,425,431	26.664	8.925



No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
712	2236·81	398152·89	506,944	360,944,128	26·683	8·929
713	2239·96	399272·08	508,369	362,467,097	26·702	8·934
714	2243·10	400392·84	509,796	363,994,344	26·721	8·938
715	2246·24	401515·18	511,225	365,525,875	26·739	8·942
716	2249·38	402639·08	512,656	367,061,696	26·758	8·946
717	2252·52	403764·56	514,089	368,601,813	26·777	8·950
718	2255·66	404891·60	515,524	370,146,232	26·795	8·954
719	2258·81	406020·22	516,961	371,694,959	26·814	8·959
720	2261·95	407150·41	518,400	373,248,000	26·833	8·963
721	2265·09	408282·17	519,841	374,805,361	26·851	8·967
722	2268·23	409415·50	521,284	376,367,048	26·870	8·971
723	2271·37	410550·40	522,729	377,933,067	26·889	8·975
724	2274·51	411686·87	524,176	379,503,424	26·907	8·979
725	2277·66	412824·91	525,625	381,078,125	26·926	8·983
726	2280·80	413964·52	527,076	382,657,176	26·944	8·988
727	2283·94	415105·71	528,529	384,240,583	26·963	8·992
728	2287·08	416248·46	529,984	385,828,352	26·991	8·996
729	2290·22	417392·79	531,441	387,420,489	27·000	9·000
730	2293·36	418538·68	532,900	389,017,000	27·018	9·004
731	2296·50	419686·15	534,361	390,617,891	27·037	9·008
732	2299·65	420835·19	535,824	392,223,168	27·055	9·012
733	2302·79	421985·79	537,289	393,832,837	27·074	9·016
734	2305·93	423137·97	538,756	395,446,904	27·092	9·020
735	2309·07	424291·72	540,225	397,065,375	27·111	9·023
736	2312·21	425447·04	541,696	398,688,256	27·129	9·029
737	2315·35	426603·93	543,169	400,315,553	27·148	9·033
738	2318·50	427762·40	544,644	401,947,272	27·166	9·037
739	2321·64	428922·43	546,121	403,583,419	27·184	9·041
740	2324·78	430084·03	547,600	405,224,000	27·203	9·045
741	2327·92	431247·21	549,081	406,869,021	27·221	9·049
742	2331·06	432411·95	550,564	408,518,488	27·239	9·053
743	2334·20	433578·27	552,049	410,172,407	27·258	9·057
744	2337·35	434746·16	553,536	411,830,784	27·276	9·061
745	2340·49	435915·62	555,025	413,493,625	27·295	9·065
746	2343·63	437086·64	556,516	415,160,936	27·313	9·069
747	2346·77	438259·24	558,009	416,832,723	27·331	9·073
748	2349·91	439433·41	559,504	418,508,992	27·349	9·077
749	2353·05	440609·17	561,001	420,189,749	27·368	9·081
750	2356·20	441786·47	562,500	421,875,000	27·386	9·086
751	2359·34	442965·35	564,001	423,564,751	27·404	9·089
752	2362·48	444145·80	565,504	424,525,900	27·423	9·094
753	2365·62	445327·83	567,009	426,957,777	27·441	9·098

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
754	2368.76	446511.42	568,516	428,661,064	27.459	9.102
755	2371.90	447696.59	570,025	430,368,875	27.477	9.106
756	2375.04	448883.32	571,536	432,081,216	27.495	9.109
757	2378.19	450071.63	573,049	433,798,093	27.514	9.114
758	2381.33	451261.51	574,564	435,519,512	27.532	9.118
759	2384.47	452452.96	576,081	437,245,479	27.549	8.122
760	2387.61	453645.98	577,600	438,976,000	27.568	9.126
761	2390.75	454840.57	579,121	440,711,081	27.586	9.129
762	2393.89	456036.73	580,644	442,450,728	27.604	9.134
763	2397.04	457234.46	582,169	444,194,947	27.622	9.138
764	2400.18	458433.77	583,696	445,943,744	27.640	9.142
765	2403.32	459634.64	585,225	447,697,125	27.659	9.146
766	2406.46	460837.08	586,756	449,455,096	27.677	9.149
767	2409.60	462041.10	588,289	451,217,663	27.695	9.154
768	2412.74	463246.69	589,824	452,984,832	27.713	9.158
769	2415.89	464453.84	591,361	454,756,609	27.731	9.162
770	2419.03	465662.57	592,900	456,533,000	27.749	9.166
771	2422.17	466872.87	594,441	458,314,011	27.767	9.169
772	2425.31	468084.74	595,984	460,099,648	27.785	9.173
773	2428.45	469298.18	597,529	461,889,917	27.803	9.177
774	2431.59	470513.19	599,076	463,684,824	27.821	9.181
775	2434.73	471729.77	600,625	465,484,375	27.839	9.185
776	2437.88	472947.92	602,176	467,288,576	27.857	9.189
777	2441.02	474167.65	603,729	469,097,433	27.875	9.193
778	2444.16	475388.94	605,284	470,910,952	27.893	9.197
779	2447.30	476611.81	606,841	472,729,139	27.910	9.201
780	2450.44	477836.24	608,400	474,552,000	27.928	9.205
781	2453.58	479062.25	609,961	476,379,541	27.946	9.209
782	2456.73	480289.83	611,524	478,211,768	27.964	9.213
783	2459.87	481518.97	613,089	480,048,687	27.982	9.217
784	2463.01	482749.69	614,656	481,890,304	28.000	9.221
785	2466.15	483981.98	616,225	483,736,025	28.017	9.225
786	2469.29	485215.84	617,796	485,587,656	28.036	9.229
787	2472.43	486451.28	619,369	487,443,403	28.053	9.233
788	2475.58	487688.28	620,944	489,303,872	28.071	9.237
789	2478.72	488926.85	622,521	491,169,069	28.089	9.240
790	2481.86	490166.99	624,100	493,039,000	28.107	9.244
791	2485.00	491408.71	625,681	494,913,671	28.125	9.248
792	2488.14	492651.99	627,264	496,793,088	28.142	9.252
793	2491.28	493896.85	628,849	498,677,257	28.160	9.256
794	2494.43	495143.28	630,436	500,566,184	28.178	9.260
795	2497.57	496391.27	632,025	502,459,875	28.196	9.264

No. or Diam	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
796	2500.71	497640.84	633,616	504,358,336	28.213	9.268
797	2503.85	498891.98	635,209	506,261,573	28.231	9.271
798	2506.99	500144.69	636,804	508,169,592	28.249	9.275
799	2510.13	501398.97	638,401	510,082,399	28.266	9.279
800	2513.27	502654.82	640,000	512,000,000	28.284	9.283
801	2516.42	503912.25	641,601	513,922,401	28.302	9.287
802	2519.56	505171.24	643,204	515,849,608	28.319	9.291
803	2522.70	506431.80	644,809	517,781,627	28.337	9.295
804	2525.84	507693.94	646,416	519,718,464	28.355	9.299
805	2528.98	508957.65	648,025	521,660,125	28.372	9.302
806	2532.12	510222.92	649,636	523,606,616	28.390	9.306
807	2535.27	511489.77	651,249	525,557,943	28.408	9.310
808	2538.41	512758.19	652,864	527,514,112	28.425	9.314
809	2541.55	514028.19	654,481	529,474,129	28.443	9.318
810	2544.69	515299.74	656,100	531,441,000	28.460	9.321
811	2547.83	516572.86	657,721	533,411,731	28.478	9.325
812	2550.97	517847.57	659,344	535,387,328	28.496	9.329
813	2554.12	519123.84	660,969	537,366,797	28.513	9.333
814	2557.26	520401.68	662,596	539,353,144	28.531	9.337
815	2560.40	521681.10	664,225	541,343,375	28.548	9.341
816	2563.54	522962.08	665,856	543,338,496	28.566	9.345
817	2566.68	524244.63	667,489	545,338,513	28.583	9.348
818	2569.82	525528.76	669,124	547,343,432	28.601	9.352
819	2572.96	526814.46	670,761	549,353,259	28.618	9.356
820	2576.11	528101.73	672,400	551,368,000	28.636	9.360
821	2579.25	529390.56	674,041	553,387,661	28.653	9.364
822	2582.39	530680.97	675,684	555,412,248	28.670	9.367
823	2585.53	531972.95	677,329	557,441,767	28.688	9.371
824	2588.67	533266.50	678,976	559,476,224	28.705	9.375
825	2591.81	534561.63	680,625	561,515,625	28.723	9.379
826	2594.96	535858.32	682,276	563,559,976	28.740	9.383
827	2598.10	537156.58	683,929	565,609,283	28.758	9.386
828	2601.24	538456.41	685,584	567,663,552	28.775	9.390
829	2604.38	539757.82	687,241	569,722,789	28.792	9.394
830	2607.52	541060.79	688,900	571,787,000	28.810	9.398
831	2610.66	542365.34	690,561	573,856,191	28.827	9.401
832	2613.81	543671.46	692,224	575,930,368	28.844	9.405
833	2616.95	544979.15	693,889	578,009,537	28.862	9.409
834	2620.09	546288.40	695,556	580,093,704	28.879	9.413
835	2623.23	547599.23	697,225	582,182,875	28.896	9.417
836	2626.37	548911.63	698,896	584,277,056	28.914	9.420
837	2629.51	550225.61	700,569	586,376,253	28.931	9.424

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
838	2632.64	551541.15	702,244	588,480,472	28.948	9.428
839	2635.80	552858.26	703,921	590,589,719	28.965	9.432
840	2638.94	554176.94	705,600	592,704,000	28.983	9.435
841	2642.08	555497.20	707,281	594,823,321	29.000	9.439
842	2645.22	556819.02	708,964	596,947,688	29.017	9.443
843	2648.36	558142.42	710,649	599,077,107	29.034	9.447
844	2651.50	559467.39	712,336	601,211,584	29.052	9.450
845	2654.65	560793.92	714,025	603,351,125	29.069	9.454
846	2657.79	562122.03	715,716	605,495,736	29.086	9.458
847	2660.93	563451.71	717,409	607,645,423	29.103	9.461
848	2664.07	564782.96	719,104	609,800,192	29.120	9.465
849	2667.21	566115.78	720,801	611,960,049	29.138	9.469
850	2670.35	567450.17	722,500	614,125,000	29.155	9.473
851	2673.50	568786.14	724,201	616,295,051	29.172	9.476
852	2676.64	570123.67	725,904	618,470,208	29.189	9.480
853	2679.78	571462.77	727,609	620,650,477	29.206	9.483
854	2682.92	572803.45	729,316	622,835,864	29.223	9.487
855	2686.06	574145.69	731,025	625,026,375	29.240	9.491
856	2689.20	575489.51	732,736	627,222,016	29.257	9.495
857	2692.35	576834.90	734,449	629,422,793	29.274	9.499
858	2695.49	578181.85	736,164	631,628,712	29.292	9.502
859	2698.63	579530.38	737,881	633,839,779	29.309	9.506
860	2701.77	580880.48	739,600	636,056,000	29.326	9.509
861	2704.91	582232.15	741,321	638,277,381	29.343	9.513
862	2708.05	583585.39	743,044	640,503,928	29.360	9.517
863	2711.19	584940.21	744,769	642,735,647	29.377	9.520
864	2714.34	586296.59	746,496	644,972,544	29.394	9.524
865	2717.45	587654.54	748,225	647,214,625	29.411	9.528
866	2720.62	589014.07	749,956	649,461,896	29.428	9.532
867	2723.76	590375.16	751,689	651,714,363	29.445	9.535
868	2726.90	591737.83	753,424	653,972,032	29.462	9.539
869	2730.04	593102.06	755,161	656,234,909	29.479	9.543
870	2733.19	594467.87	756,900	658,503,000	29.496	9.546
871	2736.33	595835.25	758,641	660,776,311	29.513	9.550
872	2739.47	597204.20	760,384	663,054,848	29.529	9.554
873	2742.61	598574.72	762,129	665,338,617	29.546	9.557
874	2745.75	599946.81	763,876	667,627,624	29.563	9.561
875	2748.89	601320.47	765,625	669,921,875	29.580	9.565
876	2752.04	602695.70	767,376	672,221,376	29.597	9.568
877	2755.18	604072.50	769,129	674,526,133	29.614	9.572
878	2758.32	605450.88	770,884	676,836,152	29.631	9.575
879	2761.46	606830.82	772,641	679,151,439	29.648	9.579

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
880	2764.60	608212.34	774,400	681,472,000	29.665	9.583
881	2767.74	609595.42	776,161	683,797,841	29.682	9.586
882	2770.89	610980.08	777,924	686,128,968	29.698	9.590
883	2774.03	612366.31	779,689	688,465,387	29.715	9.594
884	2777.17	613754.11	781,456	690,807,104	29.732	9.597
885	2780.31	615143.48	783,225	693,154,125	29.749	9.601
886	2783.45	616534.42	784,996	695,506,456	29.766	9.604
887	2786.59	617926.93	786,769	697,864,103	29.782	9.608
888	2789.73	619321.01	788,544	700,227,072	29.799	9.612
889	2792.88	620716.66	790,321	702,595,369	29.816	9.615
890	2796.02	622113.89	792,100	704,969,000	29.833	9.619
891	2799.16	623512.68	793,881	707,347,971	29.850	9.623
892	2802.30	624913.04	795,664	709,732,288	29.866	9.626
893	2805.44	626314.98	797,449	712,121,957	29.883	9.630
894	2808.58	627718.49	799,236	714,516,984	29.900	9.633
895	2811.73	629128.56	801,025	716,917,375	29.916	9.637
896	2814.87	630530.21	802,816	719,323,136	29.933	9.640
897	2818.01	631938.43	804,609	721,734,273	29.950	9.644
898	2821.15	633348.22	806,404	724,150,792	29.967	9.648
899	2824.29	634759.58	808,201	726,572,699	29.983	9.651
900	2827.43	636172.51	810,000	729,000,000	30.000	9.655
901	2830.58	637587.01	811,804	731,432,701	30.017	9.658
902	2833.72	639003.09	813,604	733,870,808	30.033	9.662
903	2836.86	640420.73	815,409	736,314,327	30.050	9.666
904	2840.00	641839.95	817,216	738,763,264	30.066	9.669
905	2843.14	643260.73	819,025	741,217,625	30.083	9.673
906	2846.28	644683.09	820,836	743,677,416	30.100	9.676
907	2849.43	646107.01	822,649	746,142,643	30.116	9.680
908	2852.57	647532.51	824,464	748,613,312	30.133	9.683
909	2855.71	648959.58	826,281	751,089,429	30.150	9.687
910	2858.85	650388.21	828,100	753,571,000	30.163	9.690
911	2861.99	651818.43	829,921	756,058,031	30.183	9.694
912	2865.13	653250.21	831,744	758,550,528	30.199	9.698
913	2868.27	654683.56	833,569	761,048,497	30.216	9.701
914	2871.42	656118.48	835,396	763,551,944	30.232	9.705
215	2874.56	657554.98	837,225	766,060,875	30.249	9.708
916	2877.70	658993.04	839,056	768,575,296	30.265	9.712
917	2880.84	660432.68	840,889	771,095,213	30.282	9.715
918	2883.98	661873.88	842,724	773,620,632	30.298	9.718
919	2887.12	663316.66	844,561	776,151,559	30.315	9.722
920	2890.27	664761.01	846,400	778,688,000	30.331	9.726
921	2893.41	666206.92	848,241	781,229,961	30.348	9.729

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
922	2896·55	667654·41	850,084	783,777,448	30·364	9·733
923	2899·69	669103·47	851,929	786,330,467	30·381	9·736
924	2902·83	670554·10	853,776	788,889,024	30·397	9·740
925	2905·97	672006·30	855,625	791,453,125	30·414	9·743
926	2909·12	673460·08	857,476	794,022,776	30·430	9·747
927	2912·26	674915·42	859,329	796,597,983	30·447	9·750
928	2915·40	676372·33	861,184	799,178,752	30·463	9·754
929	2918·54	677830·82	863,041	801,765,089	30·479	9·757
930	2921·68	679290·87	864,900	804,357,000	30·496	9·761
931	2924·82	680752·50	866,761	806,954,491	30·512	9·764
932	2927·96	682215·69	868,624	809,557,568	30·529	9·768
933	2931·11	683680·46	870,489	812,166,237	30·545	9·771
934	2934·25	685146·80	872,356	814,780,504	30·561	9·775
935	2937·39	686614·71	874,225	817,400,375	30·578	9·778
936	2940·53	688084·19	876,096	820,025,856	30·594	9·783
937	2943·67	689555·24	877,969	822,656,953	30·610	9·785
938	2946·81	691027·86	879,844	825,293,672	30·627	9·789
939	2949·96	692502·05	881,721	827,936,019	30·643	9·792
940	2953·10	693977·82	883,600	830,584,000	30·659	9·796
941	2956·24	695455·15	885,481	833,237,621	30·676	9·799
942	2959·38	696934·06	887,364	835,896,888	30·692	9·803
943	2962·52	698414·53	889,249	838,561,807	30·708	9·806
944	2965·66	699896·58	891,136	841,232,384	30·724	9·810
945	2968·81	701380·28	893,025	843,908,625	30·741	9·813
946	2971·95	702865·38	894,916	846,590,536	30·757	9·817
947	2975·09	704352·14	896,809	849,278,123	30·773	9·820
948	2978·23	705840·47	898,704	851,971,392	30·790	9·823
949	2981·37	707330·37	900,601	854,670,349	30·806	9·827
950	2984·51	708821·84	902,500	857,375,000	30·822	9·830
951	2987·66	710314·88	904,401	860,085,351	30·838	9·834
952	2990·80	711809·58	906,304	862,801,408	30·854	9·837
953	2993·94	713305·68	908,209	865,523,177	30·871	9·841
954	2997·08	714803·48	910,116	868,250,664	30·887	9·844
955	3000·22	716302·76	912,025	870,983,875	30·903	9·848
956	3003·36	717803·66	913,936	873,722,816	30·919	9·851
957	3006·50	719306·12	915,849	876,467,493	30·935	9·854
958	3009·65	720810·16	917,764	879,217,912	30·951	9·858
959	3012·79	722315·77	919,681	881,974,079	30·968	9·861
960	3015·93	723822·95	921,600	884,736,000	30·984	9·865
961	3019·07	725331·70	923,521	887,503,681	31·000	9·868
962	3022·21	726842·02	925,444	890,277,128	31·016	9·872
963	3025·35	728353·91	927,369	893,056,347	31·032	9·875

No. or Diam.	Circum- ference.	Circular Area.	Square.	Cube.	Square Root.	Cube Root.
964	3028.50	729867.37	929,296	895,841,344	31.048	9.878
965	3031.64	731382.40	931,225	898,632,125	31.064	9.881
966	3034.78	732899.01	933,156	901,428,696	31.080	9.885
967	3037.92	734417.18	935,089	904,231,063	31.097	9.889
968	3041.06	735936.93	937,024	907,039,232	31.113	9.892
969	3044.20	737458.25	938,961	909,853,209	31.129	9.895
970	3047.35	738981.13	940,900	912,673,000	31.145	9.899
971	3050.49	740505.59	942,841	915,498,611	31.161	9.902
972	3053.63	742031.62	944,784	918,330,048	31.177	9.905
973	3056.77	743559.22	946,729	921,167,317	31.193	9.909
974	3059.91	745088.39	948,676	924,010,424	31.209	9.912
975	3063.05	746619.13	950,625	926,859,375	31.225	9.916
976	3066.19	748151.44	952,576	929,714,176	31.241	9.919
977	3069.34	749685.32	954,529	932,574,833	31.257	9.923
978	3072.48	751220.78	956,484	935,441,352	31.273	9.926
979	3075.62	752757.80	958,441	938,313,739	31.289	9.929
980	3078.76	754296.40	960,400	941,192,000	31.305	9.933
981	3081.90	755836.56	962,361	944,076,141	31.321	9.936
982	3085.04	757378.30	964,324	946,966,168	31.337	9.940
983	3088.19	758921.61	966,289	949,862,087	31.353	9.943
984	3091.33	760466.18	968,256	952,763,904	31.369	9.946
985	3094.47	762012.93	970,225	955,671,625	31.385	9.950
986	3097.61	763560.95	972,196	958,585,256	31.401	9.953
987	3100.75	765110.54	974,169	961,504,803	31.416	9.956
988	3103.89	766661.71	976,144	964,430,272	31.432	9.960
989	3107.04	768214.44	978,121	967,361,669	31.448	9.963
990	3110.18	769768.74	980,100	970,299,000	31.464	9.966
991	3113.32	771324.61	982,081	973,242,271	31.480	9.970
992	3116.46	772882.06	984,064	976,191,488	31.496	9.973
993	3119.60	774441.07	986,049	979,146,657	31.512	9.977
994	3122.74	776001.66	988,036	982,107,784	31.528	9.980
995	3125.89	777563.82	990,025	985,074,875	31.544	9.983
996	3129.03	779127.54	992,016	988,047,936	31.559	9.987
997	3132.17	780692.84	994,009	991,026,973	31.575	9.990
998	3135.31	782259.71	996,004	994,011,992	31.591	9.993
999	3138.45	783828.15	998,001	997,002,999	31.607	9.997
1000	3141.60	785398.16	1,000,000	1,000,000,000	31.623	10.000



TABLE 2.—CIRCLES : DIAMETER (FROM  $\frac{1}{16}$  TO 120),  
CIRCUMFERENCE, AND AREA.\*

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
$\frac{1}{16}$	·1963	·00307	$2\frac{9}{16}$	8·0503	5·1573
$\frac{1}{8}$	·3927	·01227	$2\frac{7}{8}$	8·2467	5·4119
$\frac{3}{16}$	·5890	·02761	$2\frac{11}{16}$	8·4430	5·6723
$\frac{1}{4}$	·7854	·04909	$2\frac{3}{4}$	8·6394	5·9395
$\frac{5}{16}$	·9817	·07670	$2\frac{13}{16}$	8·8357	6·2126
$\frac{3}{8}$	1·1781	·1104	$2\frac{7}{8}$	9·0321	6·4918
$\frac{7}{16}$	1·3744	·1503	$2\frac{15}{16}$	9·2284	6·7772
$\frac{1}{2}$	1·5708	·1963	3	9·4248	7·0686
$\frac{9}{16}$	1·7771	·2485	$3\frac{1}{16}$	9·6211	7·3662
$\frac{5}{8}$	1·9635	·3068	$3\frac{1}{8}$	9·8175	7·6699
$\frac{11}{16}$	2·1598	·3712	$3\frac{3}{16}$	10·014	7·9798
$\frac{3}{4}$	2·3562	·4417	$3\frac{1}{4}$	10·210	8·2957
$\frac{13}{16}$	2·5525	·5185	$3\frac{5}{16}$	10·406	8·6180
$\frac{7}{8}$	2·7489	·6013	$3\frac{3}{8}$	10·602	8·9462
$\frac{15}{16}$	2·9452	·6903	$3\frac{7}{16}$	10·799	9·2807
1	3·1416	·7854	$3\frac{1}{2}$	10·995	9·6211
$1\frac{1}{16}$	3·3379	·8866	$3\frac{9}{16}$	11·191	9·9680
$1\frac{1}{8}$	3·5343	·9940	$3\frac{5}{8}$	11·388	10·320
$1\frac{3}{16}$	3·7306	1·1075	$3\frac{11}{16}$	11·584	10·679
$1\frac{1}{4}$	3·9270	1·2271	$3\frac{3}{4}$	11·781	11·044
$1\frac{5}{16}$	4·1233	1·3530	$3\frac{13}{16}$	11·977	11·416
$1\frac{3}{8}$	4·3197	1·4848	$3\frac{7}{8}$	12·173	11·793
$1\frac{7}{16}$	4·5160	1·6229	$3\frac{15}{16}$	12·369	12·177
$1\frac{1}{2}$	4·7124	1·7671	4	12·566	12·566
$1\frac{9}{16}$	4·9087	1·9175	$4\frac{1}{16}$	12·762	12·962
$1\frac{5}{8}$	5·1051	2·0739	$4\frac{1}{8}$	12·959	13·364
$1\frac{11}{16}$	5·3014	2·2365	$4\frac{3}{16}$	13·155	13·772
$1\frac{3}{4}$	5·4978	2·4052	$4\frac{1}{4}$	13·351	14·186
$1\frac{13}{16}$	5·6941	2·5800	$4\frac{5}{16}$	13·547	14·606
$1\frac{7}{8}$	5·8905	2·7611	$4\frac{3}{8}$	13·744	15·033
$1\frac{15}{16}$	6·0868	2·9483	$4\frac{7}{16}$	13·940	15·465
2	6·2832	3·1416	$4\frac{1}{2}$	14·137	15·904
$2\frac{1}{16}$	6·4795	3·3380	$4\frac{9}{16}$	14·333	16·349
$2\frac{1}{8}$	6·6759	3·5465	$4\frac{5}{8}$	14·529	16·800
$2\frac{3}{16}$	6·8722	3·7584	$4\frac{11}{16}$	14·725	17·257
$2\frac{1}{4}$	7·0686	3·9760	$4\frac{3}{4}$	14·922	17·720
$2\frac{5}{16}$	7·2649	4·2000	$4\frac{13}{16}$	15·119	18·190
$2\frac{3}{8}$	7·4613	4·4302	$4\frac{7}{8}$	15·315	18·665
$2\frac{7}{16}$	7·6576	4·7066	$4\frac{15}{16}$	15·511	19·147
$2\frac{1}{2}$	7·8540	4·9087	5	15·708	19·635

\* See Introduction, *ante*, p. 2.

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
5 $\frac{1}{16}$	15·904	20·129	9 $\frac{3}{8}$	29·452	69·029
5 $\frac{1}{8}$	16·100	20·629	9 $\frac{1}{2}$	29·845	70·882
5 $\frac{3}{16}$	16·296	21·135	9 $\frac{5}{16}$	30·237	72·759
5 $\frac{1}{4}$	16·493	21·647	9 $\frac{3}{4}$	30·630	74·662
5 $\frac{5}{16}$	16·689	22·166	9 $\frac{7}{8}$	31·023	76·588
5 $\frac{3}{8}$	16·886	22·690	10	31·416	78·540
5 $\frac{7}{16}$	17·082	23·221	10 $\frac{1}{16}$	31·808	80·515
5 $\frac{1}{2}$	17·278	23·758	10 $\frac{1}{8}$	32·201	82·516
5 $\frac{9}{16}$	17·474	24·301	10 $\frac{3}{16}$	32·594	84·540
5 $\frac{5}{8}$	17·671	24·850	10 $\frac{1}{2}$	32·986	86·590
5 $\frac{11}{16}$	17·867	25·406	10 $\frac{5}{8}$	33·379	88·664
5 $\frac{3}{4}$	18·064	25·967	10 $\frac{3}{4}$	33·772	90·762
5 $\frac{13}{16}$	18·261	26·535	10 $\frac{7}{8}$	34·164	92·885
5 $\frac{7}{8}$	18·457	27·108	11	34·558	95·033
5 $\frac{15}{16}$	18·653	27·688	11 $\frac{1}{16}$	34·950	97·205
6	18·849	28·274	11 $\frac{1}{8}$	35·343	99·402
6 $\frac{1}{16}$	19·242	29·464	11 $\frac{1}{4}$	35·735	101·623
6 $\frac{1}{8}$	19·635	30·679	11 $\frac{3}{8}$	36·128	103·869
6 $\frac{3}{16}$	20·027	31·919	11 $\frac{1}{2}$	36·521	106·139
6 $\frac{1}{2}$	20·420	33·183	11 $\frac{5}{8}$	36·913	108·434
6 $\frac{5}{16}$	20·813	34·471	11 $\frac{3}{4}$	37·306	110·753
6 $\frac{3}{8}$	21·205	35·784	11 $\frac{7}{8}$	37·699	113·097
6 $\frac{7}{16}$	21·598	37·122	12	38·091	115·466
7	21·991	38·484	12 $\frac{1}{16}$	38·484	117·859
7 $\frac{1}{16}$	22·383	39·871	12 $\frac{1}{8}$	38·877	120·276
7 $\frac{1}{8}$	22·776	41·282	12 $\frac{1}{4}$	39·270	122·718
7 $\frac{3}{16}$	23·169	42·718	12 $\frac{3}{8}$	39·662	125·184
7 $\frac{1}{2}$	23·562	44·178	12 $\frac{1}{2}$	40·055	127·676
7 $\frac{5}{16}$	23·954	45·663	12 $\frac{5}{8}$	40·448	130·192
7 $\frac{3}{8}$	24·347	47·173	12 $\frac{3}{4}$	40·840	132·732
7 $\frac{7}{16}$	24·740	48·707	13	41·233	135·297
8	25·132	50·265	13 $\frac{1}{16}$	41·626	137·886
8 $\frac{1}{16}$	25·515	51·848	13 $\frac{1}{8}$	42·018	140·500
8 $\frac{1}{8}$	25·918	53·456	13 $\frac{1}{4}$	42·411	143·139
8 $\frac{3}{16}$	26·310	55·088	13 $\frac{3}{8}$	42·804	145·802
8 $\frac{1}{2}$	26·703	56·745	13 $\frac{1}{2}$	43·197	148·489
8 $\frac{5}{16}$	27·096	58·426	13 $\frac{5}{8}$	43·589	151·201
8 $\frac{3}{8}$	27·489	60·132	13 $\frac{3}{4}$	43·982	153·938
8 $\frac{7}{16}$	27·881	61·862	14	44·375	156·699
9	28·274	63·617	14 $\frac{1}{16}$	44·767	159·485
9 $\frac{1}{16}$	28·667	65·396	14 $\frac{1}{8}$	45·160	162·295
9 $\frac{1}{8}$	29·059	67·200	14 $\frac{1}{4}$	45·553	165·130

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
14 $\frac{5}{8}$	45.945	167.989	19 $\frac{7}{8}$	62.439	310.245
14 $\frac{1}{2}$	46.338	170.873	20	62.832	314.160
14 $\frac{1}{4}$	46.731	173.782	20 $\frac{1}{8}$	63.224	318.099
15	47.124	176.715	20 $\frac{1}{4}$	63.617	322.063
15 $\frac{1}{8}$	47.516	179.672	20 $\frac{1}{2}$	64.010	326.051
15 $\frac{1}{4}$	47.909	182.654	20 $\frac{3}{8}$	64.402	330.064
15 $\frac{3}{8}$	48.302	185.661	20 $\frac{1}{2}$	64.795	334.101
15 $\frac{1}{2}$	48.694	188.692	20 $\frac{5}{8}$	65.188	338.163
15 $\frac{3}{4}$	49.087	191.748	20 $\frac{3}{4}$	65.580	342.250
15 $\frac{7}{8}$	49.480	194.828	21	65.973	346.361
16	49.872	197.933	21 $\frac{1}{8}$	66.366	350.497
16 $\frac{1}{8}$	50.265	201.062	21 $\frac{1}{4}$	66.759	354.657
16 $\frac{1}{4}$	50.658	204.216	21 $\frac{3}{8}$	67.151	358.841
16 $\frac{3}{8}$	51.051	207.394	21 $\frac{1}{2}$	67.544	363.051
16 $\frac{1}{2}$	51.443	210.597	21 $\frac{3}{4}$	67.937	367.284
16 $\frac{3}{4}$	51.836	213.825	21 $\frac{7}{8}$	68.329	371.543
16 $\frac{7}{8}$	52.229	217.077	22	68.722	375.826
17	52.621	220.353	22 $\frac{1}{8}$	69.115	380.133
17 $\frac{1}{8}$	53.014	223.654	22 $\frac{1}{4}$	69.507	384.465
17 $\frac{1}{4}$	53.407	226.980	22 $\frac{1}{2}$	69.900	388.822
17 $\frac{3}{8}$	53.799	230.330	22 $\frac{3}{8}$	70.293	393.203
17 $\frac{1}{2}$	54.192	233.705	22 $\frac{1}{2}$	70.686	397.608
17 $\frac{3}{4}$	54.585	237.104	22 $\frac{5}{8}$	71.078	402.038
17 $\frac{7}{8}$	54.978	240.528	22 $\frac{3}{4}$	71.471	406.493
18	55.370	243.977	22 $\frac{7}{8}$	71.864	410.972
18 $\frac{1}{8}$	55.763	247.450	23	72.256	415.476
18 $\frac{1}{4}$	56.156	250.947	23 $\frac{1}{8}$	72.649	420.004
18 $\frac{3}{8}$	56.548	254.469	23 $\frac{1}{4}$	73.042	424.557
18 $\frac{1}{2}$	56.941	258.016	23 $\frac{3}{8}$	73.434	429.135
18 $\frac{3}{4}$	57.334	261.587	23 $\frac{1}{2}$	73.827	433.731
18 $\frac{7}{8}$	57.726	265.182	23 $\frac{5}{8}$	74.220	438.363
19	58.119	268.803	23 $\frac{3}{4}$	74.613	443.014
19 $\frac{1}{8}$	58.512	272.447	23 $\frac{7}{8}$	75.005	447.699
19 $\frac{1}{4}$	58.905	276.117	24	75.398	452.390
19 $\frac{3}{8}$	59.297	279.811	24 $\frac{1}{8}$	75.791	457.115
19 $\frac{1}{2}$	59.690	283.529	24 $\frac{1}{4}$	76.183	461.864
19 $\frac{3}{4}$	60.083	287.272	24 $\frac{3}{8}$	76.576	466.638
19 $\frac{7}{8}$	60.475	291.039	24 $\frac{1}{2}$	76.969	471.436
20	60.868	294.831	24 $\frac{3}{4}$	77.361	476.259
20 $\frac{1}{8}$	61.261	298.648	24 $\frac{5}{8}$	77.754	481.106
20 $\frac{1}{4}$	61.653	302.489	24 $\frac{3}{4}$	78.147	485.978
20 $\frac{3}{8}$	62.046	306.355	25	78.540	490.875

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
25 $\frac{1}{8}$	78.932	495.796	30 $\frac{3}{8}$	95.426	724.641
25 $\frac{1}{4}$	79.325	500.741	30 $\frac{1}{2}$	95.818	730.618
25 $\frac{3}{8}$	79.718	505.711	30 $\frac{5}{8}$	96.211	736.619
25 $\frac{1}{2}$	80.110	510.706	30 $\frac{7}{8}$	96.604	742.644
25 $\frac{5}{8}$	80.503	515.725	30 $\frac{9}{8}$	96.996	748.694
25 $\frac{3}{4}$	80.896	520.769	31	97.389	754.769
25 $\frac{7}{8}$	81.288	525.837	31 $\frac{1}{8}$	97.782	760.868
26	81.681	530.930	31 $\frac{1}{4}$	98.175	766.992
26 $\frac{1}{8}$	82.074	536.047	31 $\frac{3}{8}$	98.567	773.140
26 $\frac{1}{4}$	82.467	541.189	31 $\frac{5}{8}$	98.968	779.313
26 $\frac{3}{8}$	82.859	546.356	31 $\frac{7}{8}$	99.353	785.510
26 $\frac{1}{2}$	83.252	551.547	31 $\frac{9}{8}$	99.745	791.732
26 $\frac{5}{8}$	83.645	556.762	31 $\frac{7}{4}$	100.138	797.978
26 $\frac{3}{4}$	84.037	562.002	32	100.531	804.249
26 $\frac{7}{8}$	84.430	567.267	32 $\frac{1}{8}$	100.924	810.545
27	84.823	572.556	32 $\frac{1}{4}$	101.316	816.865
27 $\frac{1}{8}$	85.215	577.870	32 $\frac{3}{8}$	101.709	823.209
27 $\frac{1}{4}$	85.608	583.208	32 $\frac{5}{8}$	102.102	829.578
27 $\frac{3}{8}$	86.001	588.571	32 $\frac{7}{8}$	102.494	835.972
27 $\frac{1}{2}$	86.394	593.958	32 $\frac{9}{8}$	102.887	842.390
27 $\frac{5}{8}$	86.786	599.370	32 $\frac{7}{4}$	103.280	848.833
27 $\frac{3}{4}$	87.179	604.807	33	103.672	855.30
27 $\frac{7}{8}$	87.572	610.268	33 $\frac{1}{8}$	104.055	861.79
28	87.964	615.753	33 $\frac{1}{4}$	104.458	868.30
28 $\frac{1}{8}$	88.357	621.263	33 $\frac{3}{8}$	104.850	874.84
28 $\frac{1}{4}$	88.750	626.798	33 $\frac{5}{8}$	105.243	881.41
28 $\frac{3}{8}$	89.142	632.357	33 $\frac{7}{8}$	105.636	888.00
28 $\frac{1}{2}$	89.535	637.941	33 $\frac{9}{8}$	106.029	894.61
28 $\frac{5}{8}$	89.928	643.594	33 $\frac{7}{4}$	106.421	901.25
28 $\frac{3}{4}$	90.321	649.182	34	106.814	907.92
28 $\frac{7}{8}$	90.713	654.839	34 $\frac{1}{8}$	107.207	914.61
29	91.106	660.521	34 $\frac{1}{4}$	107.599	921.32
29 $\frac{1}{8}$	91.499	666.227	34 $\frac{3}{8}$	107.992	928.06
29 $\frac{1}{4}$	91.891	671.958	34 $\frac{5}{8}$	108.385	934.82
29 $\frac{3}{8}$	92.284	677.714	34 $\frac{7}{8}$	108.777	941.60
29 $\frac{1}{2}$	92.677	683.494	34 $\frac{9}{8}$	109.170	948.41
29 $\frac{5}{8}$	93.069	689.298	34 $\frac{7}{4}$	109.563	955.25
29 $\frac{3}{4}$	93.462	695.128	35	109.956	962.11
29 $\frac{7}{8}$	93.855	700.981	35 $\frac{1}{8}$	110.348	968.99
30	94.248	706.860	35 $\frac{1}{4}$	110.741	975.90
30 $\frac{1}{8}$	94.640	712.762	35 $\frac{3}{8}$	111.134	982.84
30 $\frac{1}{4}$	95.033	718.690	35 $\frac{5}{8}$	111.526	989.80

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
35 $\frac{3}{8}$	111·919	996·78	40 $\frac{7}{8}$	128·412	1312·21
35 $\frac{1}{2}$	112·312	1003·78	41	128·805	1320·25
35 $\frac{5}{8}$	112·704	1010·82	41 $\frac{1}{8}$	129·198	1328·32
36	113·097	1017·88	41 $\frac{1}{4}$	129·591	1336·40
36 $\frac{1}{8}$	113·490	1024·95	41 $\frac{3}{8}$	129·983	1344·51
36 $\frac{1}{4}$	113·883	1032·06	41 $\frac{1}{2}$	130·376	1352·65
36 $\frac{3}{8}$	114·275	1039·19	41 $\frac{5}{8}$	130·769	1360·81
36 $\frac{1}{2}$	114·668	1046·35	41 $\frac{3}{4}$	131·161	1369·00
36 $\frac{5}{8}$	115·061	1053·52	41 $\frac{7}{8}$	131·554	1377·21
36 $\frac{3}{4}$	115·453	1060·73	42	131·947	1385·44
36 $\frac{7}{8}$	115·846	1067·95	42 $\frac{1}{8}$	132·339	1393·70
37	116·239	1075·21	42 $\frac{1}{4}$	132·732	1401·98
37 $\frac{1}{8}$	116·631	1082·48	42 $\frac{3}{8}$	133·125	1410·29
37 $\frac{1}{4}$	117·024	1089·79	42 $\frac{1}{2}$	133·518	1418·62
37 $\frac{3}{8}$	117·417	1097·11	42 $\frac{5}{8}$	133·910	1426·98
37 $\frac{1}{2}$	117·810	1104·46	42 $\frac{3}{4}$	134·303	1435·36
37 $\frac{5}{8}$	118·202	1111·84	42 $\frac{7}{8}$	134·696	1443·77
37 $\frac{3}{4}$	118·595	1119·24	43	135·088	1452·20
37 $\frac{7}{8}$	118·988	1126·66	43 $\frac{1}{8}$	135·481	1460·65
38	119·380	1134·11	43 $\frac{1}{4}$	135·874	1469·13
38 $\frac{1}{8}$	119·773	1141·59	43 $\frac{3}{8}$	136·266	1477·63
38 $\frac{1}{4}$	120·166	1149·08	43 $\frac{1}{2}$	136·659	1486·17
38 $\frac{3}{8}$	120·558	1156·61	43 $\frac{5}{8}$	137·052	1494·72
38 $\frac{1}{2}$	120·951	1164·15	43 $\frac{3}{4}$	137·445	1503·30
38 $\frac{5}{8}$	121·344	1171·73	43 $\frac{7}{8}$	137·837	1511·90
38 $\frac{3}{4}$	121·737	1179·32	44	138·230	1520·53
38 $\frac{7}{8}$	122·129	1186·94	44 $\frac{1}{8}$	138·623	1529·18
39	122·522	1194·59	44 $\frac{1}{4}$	139·015	1537·86
39 $\frac{1}{8}$	122·915	1202·26	44 $\frac{3}{8}$	139·408	1546·55
39 $\frac{1}{4}$	123·307	1209·95	44 $\frac{1}{2}$	139·801	1555·28
39 $\frac{3}{8}$	123·700	1217·67	44 $\frac{5}{8}$	140·193	1564·03
39 $\frac{1}{2}$	124·093	1225·42	44 $\frac{3}{4}$	140·586	1572·81
39 $\frac{5}{8}$	124·485	1233·18	44 $\frac{7}{8}$	140·979	1581·61
39 $\frac{3}{4}$	124·878	1240·98	45	141·372	1590·43
39 $\frac{7}{8}$	125·271	1248·79	45 $\frac{1}{8}$	141·764	1599·28
40	125·664	1256·64	45 $\frac{1}{4}$	142·157	1608·15
40 $\frac{1}{8}$	126·056	1264·50	45 $\frac{3}{8}$	142·550	1617·04
40 $\frac{1}{4}$	126·449	1272·39	45 $\frac{1}{2}$	142·942	1625·97
40 $\frac{3}{8}$	126·842	1280·31	45 $\frac{5}{8}$	143·335	1634·92
40 $\frac{1}{2}$	127·234	1288·25	45 $\frac{3}{4}$	143·728	1643·89
40 $\frac{5}{8}$	127·627	1296·21	45 $\frac{7}{8}$	144·120	1652·88
40 $\frac{3}{4}$	128·020	1304·20	46	144·513	1661·90

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
46 $\frac{1}{2}$	144·906	1670·95	52 $\frac{1}{2}$	165·719	2185·42
46 $\frac{1}{4}$	145·299	1680·01	53	166·504	2206·18
46 $\frac{3}{4}$	145·691	1689·10	53 $\frac{1}{4}$	167·290	2227·05
46 $\frac{1}{2}$	146·084	1698·23	53 $\frac{1}{2}$	168·075	2248·01
46 $\frac{3}{4}$	146·477	1707·37	53 $\frac{3}{4}$	168·861	2269·06
46 $\frac{5}{8}$	146·869	1716·54	54	169·646	2290·22
46 $\frac{7}{8}$	147·262	1725·73	54 $\frac{1}{4}$	170·431	2311·48
47	147·655	1734·94	54 $\frac{1}{2}$	171·217	2332·83
47 $\frac{1}{4}$	148·047	1744·18	54 $\frac{3}{4}$	172·002	2354·28
47 $\frac{1}{2}$	148·440	1753·45	55	172·788	2375·83
47 $\frac{3}{4}$	148·833	1762·73	55 $\frac{1}{4}$	173·573	2397·48
47 $\frac{5}{8}$	149·226	1772·05	55 $\frac{1}{2}$	174·358	2419·22
47 $\frac{7}{8}$	149·618	1781·39	55 $\frac{3}{4}$	175·144	2441·07
47 $\frac{5}{4}$	150·011	1790·76	56	175·929	2463·01
47 $\frac{3}{2}$	150·404	1800·14	56 $\frac{1}{4}$	176·715	2485·05
48	150·796	1809·56	56 $\frac{1}{2}$	177·500	2507·19
48 $\frac{1}{4}$	151·189	1818·99	56 $\frac{3}{4}$	178·285	2529·42
48 $\frac{1}{2}$	151·582	1828·46	57	179·071	2551·76
48 $\frac{3}{4}$	151·974	1837·93	57 $\frac{1}{4}$	179·856	2574·19
48 $\frac{5}{8}$	152·367	1847·45	57 $\frac{1}{2}$	180·642	2596·72
48 $\frac{7}{8}$	152·760	1856·99	57 $\frac{3}{4}$	181·427	2619·35
48 $\frac{5}{4}$	153·153	1866·55	58	182·212	2642·08
48 $\frac{3}{2}$	153·545	1876·13	58 $\frac{1}{4}$	182·998	2664·91
49	153·938	1885·74	58 $\frac{1}{2}$	183·783	2687·83
49 $\frac{1}{4}$	154·331	1895·37	58 $\frac{3}{4}$	184·569	2710·85
49 $\frac{1}{2}$	154·723	1905·03	59	185·354	2733·97
49 $\frac{3}{4}$	155·116	1914·70	59 $\frac{1}{4}$	186·139	2757·19
49 $\frac{5}{8}$	155·509	1924·42	59 $\frac{1}{2}$	186·925	2780·51
49 $\frac{7}{8}$	155·901	1934·15	59 $\frac{3}{4}$	187·710	2803·92
49 $\frac{5}{4}$	156·294	1943·91	60	188·496	2827·43
49 $\frac{3}{2}$	156·687	1953·69	60 $\frac{1}{4}$	189·281	2851·05
50	157·080	1963·50	60 $\frac{1}{2}$	190·066	2874·76
50 $\frac{1}{4}$	157·865	1983·18	60 $\frac{3}{4}$	190·852	2898·56
50 $\frac{1}{2}$	158·650	2002·96	61	191·637	2922·47
50 $\frac{3}{4}$	159·436	2022·84	61 $\frac{1}{4}$	192·423	2946·47
51	160·221	2042·82	61 $\frac{1}{2}$	193·208	2970·57
51 $\frac{1}{4}$	161·007	2062·90	61 $\frac{3}{4}$	193·993	2994·77
51 $\frac{1}{2}$	161·792	2083·07	62	194·779	3019·07
51 $\frac{3}{4}$	162·577	2103·35	62 $\frac{1}{4}$	195·564	3043·47
52	163·363	2123·72	62 $\frac{1}{2}$	196·350	3067·96
52 $\frac{1}{4}$	164·148	2144·19	62 $\frac{3}{4}$	197·135	3092·56
52 $\frac{1}{2}$	164·934	2164·75	63	197·920	3117·25

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
63 $\frac{1}{4}$	198.706	3142.04	73 $\frac{3}{4}$	231.693	4271.83
63 $\frac{1}{2}$	199.491	3166.92	74	232.478	4300.84
63 $\frac{3}{4}$	200.277	3191.91	74 $\frac{1}{4}$	233.263	4329.95
64	201.062	3216.99	74 $\frac{1}{2}$	234.049	4359.16
64 $\frac{1}{4}$	201.847	3242.17	74 $\frac{3}{4}$	234.834	4388.47
64 $\frac{1}{2}$	202.633	3267.46	75	235.620	4417.86
64 $\frac{3}{4}$	203.418	3292.83	75 $\frac{1}{4}$	236.405	4447.37
65	204.204	3318.31	75 $\frac{1}{2}$	237.190	4476.97
65 $\frac{1}{4}$	204.989	3343.88	75 $\frac{3}{4}$	237.976	4506.67
65 $\frac{1}{2}$	205.774	3369.56	76	238.761	4536.46
65 $\frac{3}{4}$	206.560	3395.33	76 $\frac{1}{4}$	239.547	4566.36
66	207.345	3421.19	76 $\frac{1}{2}$	240.332	4596.35
66 $\frac{1}{4}$	208.131	3447.16	76 $\frac{3}{4}$	241.117	4626.44
66 $\frac{1}{2}$	208.916	3473.23	77	241.903	4656.63
66 $\frac{3}{4}$	209.701	3499.39	77 $\frac{1}{4}$	242.688	4686.92
67	210.487	3525.66	77 $\frac{1}{2}$	243.474	4717.30
67 $\frac{1}{4}$	211.272	3552.01	77 $\frac{3}{4}$	244.259	4747.79
67 $\frac{1}{2}$	212.058	3578.47	78	245.044	4778.36
67 $\frac{3}{4}$	212.843	3605.03	78 $\frac{1}{4}$	245.830	4809.05
68	213.628	3631.68	78 $\frac{1}{2}$	246.615	4839.83
68 $\frac{1}{4}$	214.414	3658.44	78 $\frac{3}{4}$	247.401	4870.70
68 $\frac{1}{2}$	215.199	3685.29	79	248.186	4901.68
68 $\frac{3}{4}$	215.985	3712.24	79 $\frac{1}{4}$	248.971	4932.75
69	216.770	3739.28	79 $\frac{1}{2}$	249.757	4963.92
69 $\frac{1}{4}$	217.555	3766.43	79 $\frac{3}{4}$	250.542	4995.19
69 $\frac{1}{2}$	218.341	3793.67	80	251.328	5026.55
69 $\frac{3}{4}$	219.126	3821.02	80 $\frac{1}{4}$	252.113	5058.00
70	219.912	3848.45	80 $\frac{1}{2}$	252.898	5089.58
70 $\frac{1}{4}$	220.697	3875.99	80 $\frac{3}{4}$	253.683	5121.22
70 $\frac{1}{2}$	221.482	3903.63	81	254.469	5153.00
70 $\frac{3}{4}$	222.268	3931.36	81 $\frac{1}{4}$	255.254	5184.84
71	223.053	3959.19	81 $\frac{1}{2}$	256.040	5216.82
71 $\frac{1}{4}$	223.839	3987.13	81 $\frac{3}{4}$	256.825	5248.84
71 $\frac{1}{2}$	224.624	4015.16	82	257.611	5281.02
71 $\frac{3}{4}$	225.409	4043.28	82 $\frac{1}{4}$	258.396	5313.28
72	226.195	4071.50	82 $\frac{1}{2}$	259.182	5345.62
72 $\frac{1}{4}$	226.980	4099.83	82 $\frac{3}{4}$	259.967	5378.04
72 $\frac{1}{2}$	227.766	4128.25	83	260.752	5410.61
72 $\frac{3}{4}$	228.551	4156.77	83 $\frac{1}{4}$	261.537	5443.24
73	229.336	4185.39	83 $\frac{1}{2}$	262.323	5476.00
73	230.122	4214.11	83 $\frac{3}{4}$	263.108	5508.84
73	230.907	4242.92	84	263.894	5541.77



Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
84 $\frac{1}{4}$	264·679	5574·80	94 $\frac{3}{4}$	297·666	7050·92
84 $\frac{1}{2}$	265·465	5607·95	95	298·452	7088·22
84 $\frac{3}{4}$	266·250	5641·16	95 $\frac{1}{4}$	299·237	7125·56
85	267·035	5674·51	95 $\frac{1}{2}$	300·022	7163·04
85 $\frac{1}{4}$	267·821	5707·92	95 $\frac{3}{4}$	300·807	7200·56
85 $\frac{1}{2}$	268·606	5741·47	96	301·593	7238·23
85 $\frac{3}{4}$	269·392	5775·09	96 $\frac{1}{4}$	302·378	7275·96
86	270·177	5808·80	96 $\frac{1}{2}$	302·164	7313·84
86 $\frac{1}{4}$	270·962	5842·60	96 $\frac{3}{4}$	303·948	7351·72
86 $\frac{1}{2}$	271·748	5876·55	97	304·734	7389·81
86 $\frac{3}{4}$	272·533	5910·52	97 $\frac{1}{4}$	305·520	7427·96
87	273·319	5944·68	97 $\frac{1}{2}$	306·306	7474·20
87 $\frac{1}{4}$	274·104	5978·88	97 $\frac{3}{4}$	307·090	7504·52
87 $\frac{1}{2}$	274·890	6013·21	98	307·876	7542·96
87 $\frac{3}{4}$	275·675	6047·60	98 $\frac{1}{4}$	308·662	7581·48
88	276·460	6082·12	98 $\frac{1}{2}$	309·446	7620·12
88 $\frac{1}{4}$	277·245	6116·72	98 $\frac{3}{4}$	310·232	7658·80
88 $\frac{1}{2}$	278·031	6151·44	99	311·018	7697·69
88 $\frac{3}{4}$	278·816	6186·20	99 $\frac{1}{4}$	311·802	7736·60
89	279·602	6221·14	99 $\frac{1}{2}$	312·588	7775·64
89 $\frac{1}{4}$	280·387	6256·12	99 $\frac{3}{4}$	313·374	7814·76
89 $\frac{1}{2}$	281·173	6291·25	100	314·159	7853·98
89 $\frac{3}{4}$	281·958	6326·44	100 $\frac{1}{2}$	315·730	7938·72
90	282·744	6361·73	101	317·301	8011·85
90 $\frac{1}{4}$	283·529	6399·12	101 $\frac{1}{2}$	318·872	8091·36
90 $\frac{1}{2}$	284·314	6432·62	102	320·442	8171·28
90 $\frac{3}{4}$	285·099	6468·16	102 $\frac{1}{2}$	322·014	8251·60
91	285·885	6503·88	103	323·584	8332·29
91 $\frac{1}{4}$	286·670	6539·68	103 $\frac{1}{2}$	325·154	8413·40
91 $\frac{1}{2}$	287·456	6573·56	104	326·726	8494·87
91 $\frac{3}{4}$	288·242	6611·52	104 $\frac{1}{2}$	328·296	8576·76
92	289·027	6647·61	105	329·867	8659·01
92 $\frac{1}{4}$	289·812	6683·80	105 $\frac{1}{2}$	331·438	8741·68
92 $\frac{1}{2}$	290·598	6720·07	106	333·009	8824·73
92 $\frac{3}{4}$	291·383	6756·40	106 $\frac{1}{2}$	334·580	8908·20
93	292·168	6792·91	107	336·150	8992·02
93 $\frac{1}{4}$	292·953	6829·48	107 $\frac{1}{2}$	337·722	9076·24
93 $\frac{1}{2}$	293·739	6866·16	108	339·292	9160·88
93 $\frac{3}{4}$	294·524	6882·92	108 $\frac{1}{2}$	340·862	9245·92
94	295·310	6939·78	109	342·434	9331·32
94 $\frac{1}{4}$	296·095	6976·72	109 $\frac{1}{2}$	344·004	9417·12
94 $\frac{1}{2}$	296·881	7013·81	110	345·575	9503·32

Dia- meter.	Circum- ference.	Area.	Dia- meter.	Circum- ference.	Area.
110½	347·146	9589·92	115½	362·854	10477·40
111	348·717	9676·89	116	364·425	10568·32
111½	350·288	9764·28	116½	365·996	10659·64
112	351·858	9852·03	117	367·566	10751·32
112½	353·430	9940·20	117½	369·138	10843·40
113	355·000	10028·75	118	370·708	10935·88
113½	356·570	10117·68	118½	372·278	11028·76
114	358·142	10207·03	119	373·849	11122·02
114½	359·712	10296·76	119½	375·420	11215·68
115	361·283	10386·89	120	376·991	11309·73

TABLE 3.—RECIPROCAL OF NUMBERS, FROM 1 TO 1,000.\*

No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.
1	1·000000	25	·040000	49	·020408	73	·013699
2	·500000	26	·038462	50	·020000	74	·013514
3	·333333	27	·037037	51	·019608	75	·013333
4	·250000	28	·035714	52	·019231	76	·013158
5	·200000	29	·034483	53	·018868	77	·012987
6	·166667	30	·033333	54	·018519	78	·012821
7	·142857	31	·032258	55	·018182	79	·012658
8	·125000	32	·031250	56	·017857	80	·012500
9	·111111	33	·030303	57	·017544	81	·012346
10	·100000	34	·029412	58	·017241	82	·012195
11	·090909	35	·028571	59	·016949	83	·012048
12	·083333	36	·027778	60	·016667	84	·011905
13	·076923	37	·027027	61	·016393	85	·011765
14	·071429	38	·026316	62	·016129	86	·011628
15	·066667	39	·025641	63	·015873	87	·011494
16	·062500	40	·025000	64	·015625	88	·011364
17	·058824	41	·024390	65	·015385	89	·011236
18	·055556	42	·023810	66	·015152	90	·011111
19	·052632	43	·023256	67	·014925	91	·010989
20	·050000	44	·022727	68	·014706	92	·010870
21	·047619	45	·022222	69	·014493	93	·010753
22	·045455	46	·021739	70	·014286	94	·010638
23	·043478	47	·021277	71	·014085	95	·010526
24	·041667	48	·020833	72	·013889	96	·010417

\* See Introduction, *ante*, p. 2.

No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.
97	·010309	139	·007194	181	·005525	223	·004484
98	·010204	140	·007143	182	·005495	224	·004464
99	·010101	141	·007092	183	·005464	225	·004444
100	·010000	142	·007042	184	·005435	226	·004425
101	·009901	143	·006993	185	·005405	227	·004405
102	·009804	144	·006944	186	·005376	228	·004386
103	·009709	145	·006897	187	·005348	229	·004367
104	·009615	146	·006849	188	·005319	230	·004348
105	·009524	147	·006803	189	·005291	231	·004329
106	·009434	148	·006757	190	·005263	232	·004310
107	·009346	149	·006711	191	·005236	233	·004292
108	·009259	150	·006667	192	·005208	234	·004274
109	·009174	151	·006623	193	·005181	235	·004255
110	·009091	152	·006579	194	·005155	236	·004237
111	·009009	153	·006536	195	·005128	237	·004219
112	·008929	154	·006494	196	·005102	238	·004202
113	·008850	155	·006452	197	·005076	239	·004184
114	·008772	156	·006410	198	·005051	240	·004167
115	·008696	157	·006369	199	·005025	241	·004149
116	·008621	158	·006329	200	·005000	242	·004132
117	·008547	159	·006289	201	·004975	243	·004115
118	·008475	160	·006250	202	·004950	244	·004098
119	·008403	161	·006211	203	·004926	245	·004082
120	·008333	162	·006173	204	·004902	246	·004065
121	·008264	163	·006135	205	·004878	247	·004049
122	·008197	164	·006098	206	·004854	248	·004032
123	·008130	165	·006061	207	·004831	249	·004016
124	·008065	166	·006024	208	·004808	250	·004000
125	·008000	167	·005988	209	·004785	251	·003984
126	·007937	168	·005952	210	·004762	252	·003968
127	·007874	169	·005917	211	·004739	253	·003953
128	·007813	170	·005882	212	·004717	254	·003937
129	·007752	171	·005848	213	·004695	255	·003922
130	·007692	172	·005814	214	·004673	256	·003906
131	·007634	173	·005780	215	·004651	257	·003891
132	·007576	174	·005747	216	·004630	258	·003876
133	·007519	175	·005714	217	·004608	259	·003861
134	·007463	176	·005682	218	·004587	260	·003846
135	·007407	177	·005650	219	·004566	261	·003831
136	·007353	178	·005618	220	·004545	262	·003817
137	·007299	179	·005587	221	·004525	263	·003802
138	·007246	180	·005556	222	·004505	264	·003788

No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.
265	·003774	307	·003257	349	·002865	391	·002558
266	·003759	308	·003247	350	·002857	392	·002551
267	·003745	309	·003236	351	·002849	393	·002545
268	·003731	310	·003226	352	·002841	394	·002538
269	·003717	311	·003215	353	·002833	395	·002532
270	·003704	312	·003205	354	·002825	396	·002525
271	·003690	313	·003195	355	·002817	397	·002519
272	·003676	314	·003185	356	·002809	398	·002513
273	·003663	315	·003175	357	·002801	399	·002506
274	·003650	316	·003165	358	·002793	400	·002500
275	·003636	317	·003155	359	·002786	401	·002494
276	·003623	318	·003145	360	·002778	402	·002488
277	·003610	319	·003135	361	·002770	403	·002481
278	·003597	320	·003125	362	·002762	404	·002475
279	·003584	321	·003115	363	·002755	405	·002469
280	·003571	322	·003106	364	·002747	406	·002463
281	·003559	323	·003096	365	·002740	407	·002457
282	·003546	324	·003086	366	·002732	408	·002451
283	·003534	325	·003077	367	·002725	409	·002445
284	·003522	326	·003067	368	·002717	410	·002439
285	·003509	327	·003058	369	·002710	411	·002433
286	·003497	328	·003049	370	·002703	412	·002427
287	·003484	329	·003040	371	·002695	413	·002421
288	·003472	330	·003030	372	·002688	414	·002415
289	·003460	331	·003021	373	·002681	415	·002410
290	·003448	332	·003012	374	·002674	416	·002407
291	·003436	333	·003003	375	·002667	417	·002398
292	·003425	334	·002994	376	·002660	418	·002392
293	·003413	335	·002985	377	·002653	419	·002387
294	·003401	336	·002976	378	·002646	420	·002381
295	·003390	337	·002967	379	·002639	421	·002375
296	·003378	338	·002959	380	·002632	422	·002370
297	·003367	339	·002950	381	·002625	423	·002364
298	·003356	340	·002941	382	·002618	424	·002358
299	·003344	341	·002933	383	·002611	425	·002353
300	·003333	342	·002924	384	·002604	426	·002347
301	·003322	343	·002915	385	·002597	427	·002342
302	·003311	344	·002907	386	·002591	428	·002336
303	·003301	345	·002899	387	·002584	429	·002331
304	·003289	346	·002890	388	·002577	430	·002326
305	·003279	347	·002882	389	·002571	431	·002320
306	·003268	348	·002874	390	·002564	432	·002315

No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.
433	·002309	475	·002105	517	·001934	559	·001789
434	·002304	476	·002101	518	·001931	560	·001786
435	·002299	477	·002096	519	·001927	561	·001783
436	·002294	478	·002092	520	·001923	562	·001779
437	·002288	479	·002088	521	·001919	563	·001776
438	·002283	480	·002083	522	·001916	564	·001773
439	·002278	481	·002079	523	·001912	565	·001770
440	·002273	482	·002075	524	·001908	566	·001767
441	·002268	483	·002070	525	·001905	567	·001764
442	·002262	484	·002066	526	·001901	568	·001761
443	·002257	485	·002062	527	·001898	569	·001757
444	·002252	486	·002058	528	·001894	570	·001754
445	·002247	487	·002053	529	·001890	571	·001751
446	·002242	488	·002049	530	·001887	572	·001748
447	·002237	489	·002045	531	·001883	573	·001745
448	·002232	490	·002041	532	·001880	574	·001742
449	·002227	491	·002037	533	·001876	575	·001739
450	·002222	492	·002033	534	·001873	576	·001736
451	·002217	493	·002028	535	·001869	577	·001733
452	·002212	494	·002024	536	·001866	578	·001730
453	·002208	495	·002020	537	·001862	579	·001727
454	·002203	496	·002016	538	·001859	580	·001724
455	·002198	497	·002012	539	·001855	581	·001721
456	·002193	498	·002008	540	·001852	582	·001718
457	·002188	499	·002004	541	·001848	583	·001715
458	·002183	500	·002000	542	·001845	584	·001712
459	·002179	501	·001996	543	·001842	585	·001709
460	·002174	502	·001992	544	·001838	586	·001706
461	·002169	503	·001988	545	·001835	587	·001704
462	·002165	504	·001984	546	·001832	588	·001701
463	·002160	505	·001980	547	·001828	589	·001698
464	·002155	506	·001976	548	·001825	590	·001695
465	·002151	507	·001972	549	·001821	591	·001692
466	·002146	508	·001969	550	·001818	592	·001689
467	·002141	509	·001965	551	·001815	593	·001686
468	·002137	510	·001961	552	·001812	594	·001684
469	·002132	511	·001957	553	·001808	595	·001681
470	·002128	512	·001953	554	·001805	596	·001678
471	·002123	513	·001949	555	·001802	597	·001675
472	·002119	514	·001946	556	·001799	598	·001672
473	·002114	515	·001942	557	·001795	599	·001669
474	·002110	516	·001938	558	·001792	600	·001667

No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.
601	·001664	643	·001555	685	·001460	727	·001376
602	·001661	644	·001553	686	·001458	728	·001374
603	·001658	645	·001550	687	·001456	729	·001372
604	·001656	646	·001548	688	·001453	730	·001370
605	·001653	647	·001546	689	·001451	731	·001368
606	·001650	648	·001543	690	·001449	732	·001366
607	·001647	649	·001541	691	·001447	733	·001364
608	·001645	650	·001538	692	·001445	734	·001362
609	·001642	651	·001536	693	·001443	735	·001361
610	·001639	652	·001534	694	·001441	736	·001359
611	·001637	653	·001531	695	·001439	737	·001357
612	·001634	654	·001529	696	·001437	738	·001355
613	·001631	655	·001527	697	·001435	739	·001353
614	·001629	656	·001524	698	·001433	740	·001351
615	·001626	657	·001522	699	·001431	741	·001350
616	·001623	658	·001520	700	·001429	742	·001348
617	·001621	659	·001517	701	·001427	743	·001346
618	·001618	660	·001515	702	·001425	744	·001344
619	·001616	661	·001513	703	·001422	745	·001342
620	·001613	662	·001511	704	·001420	746	·001340
621	·001610	663	·001508	705	·001418	747	·001339
622	·001608	664	·001506	706	·001416	748	·001337
623	·001605	665	·001504	707	·001414	749	·001335
624	·001603	666	·001502	708	·001412	750	·001333
625	·001600	667	·001499	709	·001410	751	·001332
626	·001597	668	·001497	710	·001408	752	·001330
627	·001595	669	·001495	711	·001406	753	·001328
628	·001592	670	·001493	712	·001404	754	·001326
629	·001590	671	·001490	713	·001403	755	·001325
630	·001587	672	·001488	714	·001401	756	·001323
631	·001585	673	·001486	715	·001399	757	·001321
632	·001582	674	·001484	716	·001397	758	·001319
633	·001580	675	·001481	717	·001395	759	·001318
634	·001577	676	·001479	718	·001393	760	·001316
635	·001575	677	·001477	719	·001391	761	·001314
636	·001572	678	·001475	720	·001389	762	·001312
637	·001570	679	·001473	721	·001387	763	·001311
638	·001567	680	·001471	722	·001385	764	·001309
639	·001565	681	·001468	723	·001383	765	·001307
640	·001563	682	·001466	724	·001381	766	·001305
641	·001560	683	·001464	725	·001379	767	·001304
642	·001558	684	·001462	726	·001377	768	·001302

No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.
769	·001300	811	·001233	853	·001172	895	·001118
770	·001299	812	·001232	854	·001171	896	·001116
771	·001297	813	·001230	855	·001170	897	·001115
772	·001295	814	·001229	856	·001168	898	·001114
773	·001294	815	·001227	857	·001167	899	·001112
774	·001292	816	·001225	858	·001166	900	·001111
775	·001290	817	·001224	859	·001164	901	·001110
776	·001289	818	·001222	860	·001163	902	·001109
777	·001287	819	·001221	861	·001161	903	·001107
778	·001285	820	·001220	862	·001160	904	·001106
779	·001284	821	·001218	863	·001159	905	·001105
780	·001282	822	·001217	864	·001157	906	·001104
781	·001280	823	·001215	865	·001156	907	·001103
782	·001279	824	·001214	866	·001155	908	·001101
783	·001277	825	·001212	867	·001153	909	·001100
784	·001276	826	·001211	868	·001152	910	·001099
785	·001274	827	·001209	869	·001151	911	·001098
786	·001272	828	·001208	870	·001149	912	·001096
787	·001271	829	·001206	871	·001148	913	·001095
788	·001269	830	·001205	872	·001147	914	·001094
789	·001267	831	·001203	873	·001145	915	·001093
790	·001266	832	·001202	874	·001144	916	·001092
791	·001264	833	·001200	875	·001143	917	·001091
792	·001263	834	·001199	876	·001142	918	·001089
793	·001261	835	·001198	877	·001140	919	·001088
794	·001259	836	·001196	878	·001139	920	·001087
795	·001258	837	·001195	879	·001138	921	·001086
796	·001256	838	·001193	880	·001136	922	·001085
797	·001255	839	·001192	881	·001135	923	·001083
798	·001253	840	·001190	882	·001134	924	·001082
799	·001251	841	·001189	883	·001133	925	·001081
800	·001250	842	·001188	884	·001131	926	·001080
801	·001248	843	·001186	885	·001130	927	·001079
802	·001247	844	·001185	886	·001129	928	·001078
803	·001245	845	·001183	887	·001127	929	·001076
804	·001244	846	·001182	888	·001126	930	·001075
805	·001242	847	·001181	889	·001125	931	·001074
806	·001241	848	·001179	890	·001124	932	·001073
807	·001239	849	·001178	891	·001122	933	·001072
808	·001238	850	·001176	892	·001121	934	·001071
809	·001236	851	·001175	893	·001120	935	·001070
810	·001235	852	·001174	894	·001119	936	·001068

No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.	No.	Reci- procal.
937	·001067	953	·001049	969	·001032	985	·001015
938	·001066	954	·001048	970	·001031	986	·001014
939	·001065	955	·001047	971	·001030	987	·001013
940	·001064	956	·001046	972	·001029	988	·001012
941	·001063	957	·001045	973	·001028	989	·001011
942	·001062	958	·001044	974	·001027	990	·001010
943	·001060	959	·001043	975	·001026	991	·001009
944	·001059	960	·001042	976	·001025	992	·001008
945	·001058	961	·001041	977	·001024	993	·001007
946	·001057	962	·001040	978	·001022	994	·001006
947	·001056	963	·001038	979	·001021	995	·001005
948	·001055	964	·001037	980	·001020	996	·001004
949	·001054	965	·001036	981	·001019	997	·001003
950	·001053	966	·001035	982	·001018	998	·001002
951	·001052	967	·001034	983	·001017	999	·001001
952	·001050	968	·001033	984	·001016	1000	·001000

TABLE 3A.—RHUMBS, OR POINTS OF THE COMPASS.

Points.	Angles.	NORTH.	NORTH.	SOUTH.	SOUTH.
$\frac{1}{4}$	2° 48' 45"	N $\frac{1}{4}$ E	N $\frac{1}{4}$ W	S $\frac{1}{4}$ E	S $\frac{1}{4}$ W
$\frac{1}{2}$	5 37 30	N $\frac{1}{2}$ E	N $\frac{1}{2}$ W	S $\frac{1}{2}$ E	S $\frac{1}{2}$ W
$\frac{3}{4}$	8 26 15	N $\frac{3}{4}$ E	N $\frac{3}{4}$ W	S $\frac{3}{4}$ E	S $\frac{3}{4}$ W
1	11 15 0	N by E	N by W	S by E	S by W
$1\frac{1}{2}$	16 52 30	N by E $\frac{1}{2}$ E	N by W $\frac{1}{2}$ W	S by E $\frac{1}{2}$ E	S by W $\frac{1}{2}$ W
2	22 30 0	NNE	NNW	SSE	SSW
$2\frac{1}{2}$	28 7 30	NNE $\frac{1}{2}$ E	NNW $\frac{1}{2}$ W	SSE $\frac{1}{2}$ E	SSW $\frac{1}{2}$ W
3	33 45 0	NE by N	NW by N	SE by S	SW by S
$3\frac{1}{2}$	39 22 30	NE $\frac{1}{2}$ N	NW $\frac{1}{2}$ N	SE $\frac{1}{2}$ S	SW $\frac{1}{2}$ S
4	45 0 0	NE	NW	SE	SW
$4\frac{1}{2}$	50 37 30	NE $\frac{1}{2}$ E	NW $\frac{1}{2}$ W	SE $\frac{1}{2}$ E	SW $\frac{1}{2}$ W
5	56 15 0	NE by E	NW by W	SE by E	SW by W
$5\frac{1}{2}$	61 52 30	ENE $\frac{1}{2}$ N	WNW $\frac{1}{2}$ N	ESE $\frac{1}{2}$ S	WSW $\frac{1}{2}$ S
6	67 30 0	ENE	WNW	ESE	WSW
$6\frac{1}{2}$	73 7 30	ENE $\frac{1}{2}$ E	WNW $\frac{1}{2}$ W	ESE $\frac{1}{2}$ E	WSW $\frac{1}{2}$ W
7	78 45 0	E by N	W by N	E by S	W by S
$7\frac{1}{2}$	84 22 30	E $\frac{1}{2}$ N	W $\frac{1}{2}$ N	E $\frac{1}{2}$ S	W $\frac{1}{2}$ S
8	90 0 0	EAST	WEST	EAST	WEST



TABLE 4.—LOGARITHMS OF NUMBERS, FROM 1 TO 10,000.\*

N.	0	1	2	3	4	5	6	7	8	9	N.
0	—	000000	301030	477121	602060	698970	778151	845098	903090	954243	0
1	000000	041393	079181	113943	146128	176091	204120	230449	255273	278754	1
2	301030	322219	342423	361728	380211	397940	414973	431364	447158	462398	2
3	477121	491362	505150	518514	531479	544068	556303	568202	579784	591065	3
4	602060	612784	623249	633468	643453	653213	662758	672098	681241	690196	4
5	698970	707570	716003	724276	732394	740363	748188	755875	763428	770852	5
6	778151	785330	792392	799341	806180	812913	819544	826075	832509	838849	6
7	845098	851258	857332	863323	869232	875061	880814	886491	892095	897627	7
8	903090	908485	913814	919078	924279	929419	934498	939519	944483	949390	8
9	954243	959041	963788	968483	973128	977724	982271	986772	991226	995635	9
N.	0	1	2	3	4	5	6	7	8	9	N.
N.	0	1	2	3	4	5	6	7	8	9	D.
100	000000	000434	000868	001301	001734	002166	002598	003029	003461	003891	432
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105	021189	021603	022016	022428	022841	023252	023664	024075	024486	024896	411
106	025306	025715	026125	026533	026942	027350	027757	028164	028571	028978	408
107	029384	029789	030195	030600	031004	031408	031812	032216	032619	033021	404
108	033424	033826	034227	034628	035029	035430	035830	036230	036629	037028	400
109	037426	037825	038223	038620	039017	039414	039811	040207	040602	040998	396
110	041393	041787	042182	042576	042969	043362	043755	044148	044540	044932	393
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\* See Introduction, ante, p. 2.

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113	053078	053463	053846	054230	054613	054996	055378	055760	056142	056524	383
114	056905	057286	057666	058046	058426	058805	059185	059563	059942	060320	379
115	060698	061075	061452	061829	062206	062582	062958	063333	063709	064083	376
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117	068186	068557	068928	069298	069668	070038	070407	070776	071145	071514	369
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119	075547	075912	076276	076640	077004	077368	077731	078094	078457	078819	363
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121	082785	083144	083503	083861	084219	084576	084934	085291	085647	086004	357
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125	096910	097257	097604	097951	098298	098644	098990	099335	099681	100026	346
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130	113943	114277	114611	114944	115278	115611	115943	116276	116608	116940	332
131	117271	117603	117934	118265	118595	118926	119256	119586	119915	120245	330
132	120574	120903	121231	121560	121888	122216	122544	122871	123198	123525	327
133	123852	124178	124504	124830	125156	125481	125806	126131	126456	126781	325
134	127105	127429	127753	128076	128399	128722	129045	129368	129690	130012	322
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143	155336	155640	155943	156246	156549	156852	157154	157457	157759	158061	302
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147	167317	167613	167908	168203	168497	168792	169086	169380	169674	169968	294
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154	187521	187803	188084	188366	188647	188928	189209	189489	189771	190051	281
155	190332	190612	190892	191171	191451	191730	192010	192289	192567	192846	279
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157	195900	196176	196453	196729	197005	197281	197556	197832	198107	198382	275
158	198657	198932	199206	199481	199755	200029	200303	200577	200850	201124	274
159	201397	201670	201943	202216	202488	202761	203033	203305	203577	203848	272
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184	264818	265054	265290	265525	265761	265996	266232	266467	266702	266937	235
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883	945961	946010	946059	946108	946157	946207	946256	946305	946354	946403	49
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952	978637	978683	978728	978774	978819	978865	978911	978956	979002	979047	46
953	979093	979138	979184	979230	979275	979321	979366	979412	979457	979503	46
954	979548	979594	979639	979685	979730	979776	979821	979867	979912	979958	46
955	980003	980049	980094	980140	980185	980231	980276	980322	980367	980412	45
956	980458	980503	980549	980594	980640	980685	980730	980776	980821	980867	45
957	980912	980957	981003	981048	981093	981139	981184	981229	981275	981320	45
958	981366	981411	981456	981501	981547	981592	981637	981683	981728	981773	45
959	981819	981864	981909	981954	982000	982045	982090	982135	982181	982226	45
960	982271	982316	982362	982407	982452	982497	982543	982588	982633	982678	45
N.	0	1	2	3	4	5	6	7	8	9	D.

N.	0	1	2	3	4	5	6	7	8	9	D.
961	982723	982769	982814	982859	982904	982949	982994	983040	983085	983130	45
962	983175	983220	983265	983310	983356	983401	983446	983491	983536	983581	45
963	983626	983671	983716	983762	983807	983852	983897	983942	983987	984032	45
964	984077	984122	984167	984212	984257	984302	984347	984392	984437	984482	45
965	984527	984572	984617	984662	984707	984752	984797	984842	984887	984932	45
966	984977	985022	985067	985112	985157	985202	985247	985292	985337	985382	45
967	985426	985471	985516	985561	985606	985651	985696	985741	985786	985830	45
968	985875	985920	985965	986010	986055	986100	986144	986189	986234	986279	45
969	986324	986369	986413	986458	986503	986548	986593	986637	986682	986727	45
970	986772	986817	986861	986906	986951	986996	987040	987085	987130	987175	45
971	987219	987264	987309	987353	987398	987443	987488	987532	987577	987622	45
972	987666	987711	987756	987800	987845	987890	987934	987979	988024	988068	45
973	988113	988157	988202	988247	988291	988336	988381	988425	988470	988514	45
974	988559	988604	988648	988693	988737	988782	988826	988871	988916	988960	45
975	989005	989049	989094	989138	989183	989227	989272	989316	989361	989405	45
976	989450	989494	989539	989583	989628	989672	989717	989761	989806	989850	44
977	989895	989939	989983	990028	990072	990117	990161	990206	990250	990294	44
978	990339	990383	990428	990472	990516	990561	990605	990650	990694	990738	44
979	990783	990827	990871	990916	990960	991004	991049	991093	991137	991182	44
980	991226	991270	991315	991359	991403	991448	991492	991536	991580	991625	44
981	991669	991713	991758	991802	991846	991890	991935	991979	992023	992067	44
982	992111	992156	992200	992244	992288	992333	992377	992421	992465	992509	44
983	992554	992598	992642	992686	992730	992774	992819	992863	992907	992951	44
984	992995	993039	993083	993127	993172	993216	993260	993304	993348	993392	44
985	993436	993480	993524	993568	993613	993657	993701	993745	993789	993833	44
N.	0	1	2	3	4	5	6	7	8	9	D.

N.	0	1	2	3	4	5	6	7	8	9	D.
986	993877	993921	993965	994009	994053	994097	994141	994185	994229	994273	44
987	994317	994361	994405	994449	994493	994537	994581	994625	994669	994713	44
988	994757	994801	994845	994889	994933	994977	995021	995065	995108	995152	44
989	995196	995240	995284	995328	995372	995416	995460	995504	995547	995591	44
990	995635	995679	995723	995767	995811	995854	995898	995942	995986	996030	44
991	996074	996117	996161	996205	996249	996293	996337	996380	996424	996468	44
992	996512	996555	996599	996643	996687	996731	996774	996818	996862	996906	44
993	996949	996993	997037	997080	997124	997168	997212	997255	997299	997343	44
994	997386	997430	997474	997517	997561	997605	997648	997692	997736	997779	44
995	997823	997867	997910	997954	997998	998041	998085	998129	998172	998216	44
996	998259	998303	998347	998390	998434	998477	998521	998564	998608	998652	44
997	998695	998739	998782	998826	998869	998913	998956	999000	999043	999087	44
998	999131	999174	999218	999261	999305	999348	999392	999435	999479	999522	44
999	999565	999609	999652	999696	999739	999783	999826	999870	999913	999957	43
N.	0	1	2	3	4	5	6	7	8	9	D.

TABLE 5.—HYPERBOLIC LOGARITHMS OF NUMBERS  
FROM 1.01 TO 20.\*

No.	Log.	No.	Log.	No.	Log.	No.	Log.
1.01	.0099	1.42	.3507	1.83	.6043	2.24	.8065
1.02	.0198	1.43	.3577	1.84	.6098	2.25	.8109
1.03	.0296	1.44	.3646	1.85	.6152	2.26	.8154
1.04	.0392	1.45	.3716	1.86	.6206	2.27	.8198
1.05	.0488	1.46	.3784	1.87	.6259	2.28	.8242
1.06	.0583	1.47	.3853	1.88	.6313	2.29	.8286
1.07	.0677	1.48	.3920	1.89	.6366	2.30	.8329
1.08	.0770	1.49	.3988	1.90	.6419	2.31	.8372
1.09	.0862	1.50	.4055	1.91	.6471	2.32	.8416
1.10	.0953	1.51	.4121	1.92	.6523	2.33	.8458
1.11	.1044	1.52	.4187	1.93	.6575	2.34	.8502
1.12	.1133	1.53	.4253	1.94	.6627	2.35	.8544
1.13	.1222	1.54	.4318	1.95	.6678	2.36	.8587
1.14	.1310	1.55	.4383	1.96	.6729	2.37	.8629
1.15	.1398	1.56	.4447	1.97	.6780	2.38	.8671
1.16	.1484	1.57	.4511	1.98	.6831	2.39	.8713
1.17	.1570	1.58	.4574	1.99	.6881	2.40	.8755
1.18	.1655	1.59	.4637	2.00	.6931	2.41	.8796
1.19	.1740	1.60	.4700	2.01	.6981	2.42	.8838
1.20	.1823	1.61	.4762	2.02	.7031	2.43	.8879
1.21	.1906	1.62	.4824	2.03	.7080	2.44	.8920
1.22	.1988	1.63	.4886	2.04	.7129	2.45	.8961
1.23	.2070	1.64	.4947	2.05	.7178	2.46	.9002
1.24	.2151	1.65	.5008	2.06	.7227	2.47	.9042
1.25	.2231	1.66	.5068	2.07	.7275	2.48	.9083
1.26	.2311	1.67	.5128	2.08	.7324	2.49	.9123
1.27	.2390	1.68	.5188	2.09	.7372	2.50	.9163
1.28	.2469	1.69	.5247	2.10	.7419	2.51	.9203
1.29	.2546	1.70	.5306	2.11	.7467	2.52	.9243
1.30	.2624	1.71	.5365	2.12	.7514	2.53	.9282
1.31	.2700	1.72	.5423	2.13	.7561	2.54	.9322
1.32	.2776	1.73	.5481	2.14	.7608	2.55	.9361
1.33	.2852	1.74	.5539	2.15	.7655	2.56	.9400
1.34	.2927	1.75	.5596	2.16	.7701	2.57	.9439
1.35	.3001	1.76	.5653	2.17	.7747	2.58	.9478
1.36	.3075	1.77	.5710	2.18	.7793	2.59	.9517
1.37	.3148	1.78	.5766	2.19	.7839	2.60	.9555
1.38	.3221	1.79	.5822	2.20	.7885	2.61	.9594
1.39	.3293	1.80	.5878	2.21	.7930	2.62	.9632
1.40	.3365	1.81	.5933	2.22	.7975	2.63	.9670
1.41	.3436	1.82	.5988	2.23	.8020	2.64	.9708

\* See Introduction, *ante*, p. 6.



No.	Log.	No.	Log.	No.	Log.	No.	Log.
2·65	·9746	3·08	1·1249	3·51	1·2556	3·94	1·3712
2·66	·9783	3·09	1·1282	3·52	1·2585	3·95	1·3737
2·67	·9821	3·10	1·1314	3·53	1·2613	3·96	1·3762
2·68	·9858	3·11	1·1346	3·54	1·2641	3·97	1·3788
2·69	·9895	3·12	1·1378	3·55	1·2669	3·98	1·3813
2·70	·9933	3·13	1·1410	3·56	1·2698	3·99	1·3838
2·71	·9969	3·14	1·1442	3·57	1·2726	4·00	1·3863
2·72	1·0006	3·15	1·1474	3·58	1·2754	4·01	1·3888
2·73	1·0043	3·16	1·1506	3·59	1·2782	4·02	1·3913
2·74	1·0080	3·17	1·1537	3·60	1·2809	4·03	1·3938
2·75	1·0116	3·18	1·1569	3·61	1·2837	4·04	1·3962
2·76	1·0152	3·19	1·1600	3·62	1·2865	4·05	1·3987
2·77	1·0188	3·20	1·1632	3·63	1·2892	4·06	1·4012
2·78	1·0225	3·21	1·1663	3·64	1·2920	4·07	1·4036
2·79	1·0260	3·22	1·1694	3·65	1·2947	4·08	1·4061
2·80	1·0296	3·23	1·1725	3·66	1·2975	4·09	1·4085
2·81	1·0332	3·24	1·1756	3·67	1·3002	4·10	1·4110
2·82	1·0367	3·25	1·1787	3·68	1·3029	4·11	1·4134
2·83	1·0403	3·26	1·1817	3·69	1·3056	4·12	1·4159
2·84	1·0438	3·27	1·1848	3·70	1·3083	4·13	1·4183
2·85	1·0473	3·28	1·1878	3·71	1·3110	4·14	1·4207
2·86	1·0508	3·29	1·1909	3·72	1·3137	4·15	1·4231
2·87	1·0543	3·30	1·1939	3·73	1·3164	4·16	1·4255
2·88	1·0578	3·31	1·1969	3·74	1·3191	4·17	1·4279
2·89	1·0613	3·32	1·1999	3·75	1·3218	4·18	1·4303
2·90	1·0647	3·33	1·2030	3·76	1·3244	4·19	1·4327
2·91	1·0682	3·34	1·2060	3·77	1·3271	4·20	1·4351
2·92	1·0716	3·35	1·2090	3·78	1·3297	4·21	1·4375
2·93	1·0750	3·36	1·2119	3·79	1·3324	4·22	1·4398
2·94	1·0784	3·37	1·2149	3·80	1·3350	4·23	1·4422
2·95	1·0818	3·38	1·2179	3·81	1·3376	4·24	1·4446
2·96	1·0852	3·39	1·2208	3·82	1·3403	4·25	1·4469
2·97	1·0886	3·40	1·2238	3·83	1·3429	4·26	1·4493
2·98	1·0919	3·41	1·2267	3·84	1·3455	4·27	1·4516
2·99	1·0953	3·42	1·2296	3·85	1·3481	4·28	1·4540
3·00	1·0986	3·43	1·2326	3·86	1·3507	4·29	1·4563
3·01	1·1019	3·44	1·2355	3·87	1·3533	4·30	1·4586
3·02	1·1053	3·45	1·2384	3·88	1·3558	4·31	1·4609
3·03	1·1086	3·46	1·2413	3·89	1·3584	4·32	1·4633
3·04	1·1119	3·47	1·2442	3·90	1·3610	4·33	1·4656
3·05	1·1151	3·48	1·2470	3·91	1·3635	4·34	1·4679
3·06	1·1184	3·49	1·2499	3·92	1·3661	4·35	1·4702
3·07	1·1217	3·50	1·2528	3·93	1·3686	4·36	1·4725

No.	Log.	No.	Log.	No.	Log.	No.	Log.
4-37	1-4748	4-80	1-5686	5-23	1-6544	5-66	1-7334
4-38	1-4770	4-81	1-5707	5-24	1-6563	5-67	1-7352
4-39	1-4793	4-82	1-5728	5-25	1-6582	5-68	1-7370
4-40	1-4816	4-83	1-5748	5-26	1-6601	5-69	1-7387
4-41	1-4839	4-84	1-5769	5-27	1-6620	5-70	1-7405
4-42	1-4861	4-85	1-5790	5-28	1-6639	5-71	1-7422
4-43	1-4884	4-86	1-5810	5-29	1-6658	5-72	1-7440
4-44	1-4907	4-87	1-5831	5-30	1-6677	5-73	1-7457
4-45	1-4929	4-88	1-5851	5-31	1-6696	5-74	1-7475
4-46	1-4951	4-89	1-5872	5-32	1-6715	5-75	1-7492
4-47	1-4974	4-90	1-5892	5-33	1-6734	5-76	1-7509
4-48	1-4996	4-91	1-5913	5-34	1-6752	5-77	1-7527
4-49	1-5019	4-92	1-5933	5-35	1-6771	5-78	1-7544
4-50	1-5041	4-93	1-5953	5-36	1-6790	5-79	1-7561
4-51	1-5063	4-94	1-5974	5-37	1-6808	5-80	1-7579
4-52	1-5085	4-95	1-5994	5-38	1-6827	5-81	1-7596
4-53	1-5107	4-96	1-6014	5-39	1-6845	5-82	1-7613
4-54	1-5129	4-97	1-6034	5-40	1-6864	5-83	1-7630
4-55	1-5151	4-98	1-6054	5-41	1-6882	5-84	1-7647
4-56	1-5173	4-99	1-6074	5-42	1-6901	5-85	1-7664
4-57	1-5195	5-00	1-6094	5-43	1-6919	5-86	1-7681
4-58	1-5217	5-01	1-6114	5-44	1-6938	5-87	1-7699
4-59	1-5239	5-02	1-6134	5-45	1-6956	5-88	1-7716
4-60	1-5261	5-03	1-6154	5-46	1-6974	5-89	1-7733
4-61	1-5282	5-04	1-6174	5-47	1-6993	5-90	1-7750
4-62	1-5304	5-05	1-6194	5-48	1-7011	5-91	1-7766
4-63	1-5326	5-06	1-6214	5-49	1-7029	5-92	1-7783
4-64	1-5347	5-07	1-6233	5-50	1-7047	5-93	1-7800
4-65	1-5369	5-08	1-6253	5-51	1-7066	5-94	1-7817
4-66	1-5390	5-09	1-6273	5-52	1-7084	5-95	1-7834
4-67	1-5412	5-10	1-6292	5-53	1-7102	5-96	1-7851
4-68	1-5433	5-11	1-6312	5-54	1-7120	5-97	1-7867
4-69	1-5454	5-12	1-6332	5-55	1-7138	5-98	1-7884
4-70	1-5476	5-13	1-6351	5-56	1-7156	5-99	1-7901
4-71	1-5497	5-14	1-6371	5-57	1-7174	6-00	1-7918
4-72	1-5518	5-15	1-6390	5-58	1-7192	6-01	1-7934
4-73	1-5539	5-16	1-6409	5-59	1-7210	6-02	1-7951
4-74	1-5560	5-17	1-6429	5-60	1-7228	6-03	1-7967
4-75	1-5581	5-18	1-6448	5-61	1-7246	6-04	1-7984
4-76	1-5602	5-19	1-6467	5-62	1-7263	6-05	1-8001
4-77	1-5623	5-20	1-6487	5-63	1-7281	6-06	1-8017
4-78	1-5644	5-21	1-6506	5-64	1-7299	6-07	1-8034
4-79	1-5665	5-22	1-6525	5-65	1-7317	6-08	1-8050

No.	Log.	No.	Log.	No.	Log.	No.	Log.
6-09	1-8066	6-52	1-8749	6-95	1-9387	7-38	1-9988
6-10	1-8083	6-53	1-8764	6-96	1-9402	7-39	2-0001
6-11	1-8099	6-54	1-8779	6-97	1-9416	7-40	2-0015
6-12	1-8116	6-55	1-8795	6-98	1-9430	7-41	2-0028
6-13	1-8132	6-56	1-8810	6-99	1-9445	7-42	2-0042
6-14	1-8148	6-57	1-8825	7-00	1-9459	7-43	2-0055
6-15	1-8165	6-58	1-8840	7-01	1-9473	7-44	2-0069
6-16	1-8181	6-59	1-8856	7-02	1-9488	7-45	2-0082
6-17	1-8197	6-60	1-8871	7-03	1-9502	7-46	2-0096
6-18	1-8213	6-61	1-8886	7-04	1-9516	7-47	2-0109
6-19	1-8229	6-62	1-8901	7-05	1-9530	7-48	2-0122
6-20	1-8245	6-63	1-8916	7-06	1-9544	7-49	2-0136
6-21	1-8262	6-64	1-8931	7-07	1-9559	7-50	2-0149
6-22	1-8278	6-65	1-8946	7-08	1-9573	7-51	2-0162
6-23	1-8294	6-66	1-8961	7-09	1-9587	7-52	2-0176
6-24	1-8310	6-67	1-8976	7-10	1-9601	7-53	2-0189
6-25	1-8326	6-68	1-8991	7-11	1-9615	7-54	2-0202
6-26	1-8342	6-69	1-9006	7-12	1-9629	7-55	2-0215
6-27	1-8358	6-70	1-9021	7-13	1-9643	7-56	2-0229
6-28	1-8374	6-71	1-9036	7-14	1-9657	7-57	2-0242
6-29	1-8390	6-72	1-9051	7-15	1-9671	7-58	2-0255
6-30	1-8405	6-73	1-9066	7-16	1-9685	7-59	2-0268
6-31	1-8421	6-74	1-9081	7-17	1-9699	7-60	2-0281
6-32	1-8437	6-75	1-9095	7-18	1-9713	7-61	2-0295
6-33	1-8453	6-76	1-9110	7-19	1-9727	7-62	2-0308
6-34	1-8469	6-77	1-9125	7-20	1-9741	7-63	2-0321
6-35	1-8485	6-78	1-9140	7-21	1-9755	7-64	2-0334
6-36	1-8500	6-79	1-9155	7-22	1-9769	7-65	2-0347
6-37	1-8516	6-80	1-9169	7-23	1-9782	7-66	2-0360
6-38	1-8532	6-81	1-9184	7-24	1-9796	7-67	2-0373
6-39	1-8547	6-82	1-9199	7-25	1-9810	7-68	2-0386
6-40	1-8563	6-83	1-9213	7-26	1-9824	7-69	2-0399
6-41	1-8579	6-84	1-9228	7-27	1-9838	7-70	2-0412
6-42	1-8594	6-85	1-9242	7-28	1-9851	7-71	2-0425
6-43	1-8610	6-86	1-9257	7-29	1-9865	7-72	2-0438
6-44	1-8625	6-87	1-9272	7-30	1-9879	7-73	2-0451
6-45	1-8641	6-88	1-9286	7-31	1-9892	7-74	2-0464
6-46	1-8656	6-89	1-9301	7-32	1-9906	7-75	2-0477
6-47	1-8672	6-90	1-9315	7-33	1-9920	7-76	2-0490
6-48	1-8687	6-91	1-9330	7-34	1-9933	7-77	2-0503
6-49	1-8703	6-92	1-9344	7-35	1-9947	7-78	2-0516
6-50	1-8718	6-93	1-9359	7-36	1-9961	7-79	2-0528
6-51	1-8733	6-94	1-9373	7-37	1-9974	7-80	2-0541

No.	Log.	No.	Log.	No.	Log.	No.	Log.
7-81	2-0554	8-24	2-1090	8-67	2-1599	9-10	2-2083
7-82	2-0567	8-25	2-1102	8-68	2-1610	9-11	2-2094
7-83	2-0580	8-26	2-1114	8-69	2-1622	9-12	2-2105
7-84	2-0592	8-27	2-1126	8-70	2-1633	9-13	2-2116
7-85	2-0605	8-28	2-1138	8-71	2-1645	9-14	2-2127
7-86	2-0618	8-29	2-1150	8-72	2-1656	9-15	2-2138
7-87	2-0631	8-30	2-1163	8-73	2-1668	9-16	2-2148
7-88	2-0643	8-31	2-1175	8-74	2-1679	9-17	2-2159
7-89	2-0656	8-32	2-1187	8-75	2-1691	9-18	2-2170
7-90	2-0669	8-33	2-1199	8-76	2-1702	9-19	2-2181
7-91	2-0681	8-34	2-1211	8-77	2-1713	9-20	2-2192
7-92	2-0694	8-35	2-1223	8-78	2-1725	9-21	2-2203
7-93	2-0707	8-36	2-1235	8-79	2-1736	9-22	2-2214
7-94	2-0719	8-37	2-1247	8-80	2-1748	9-23	2-2225
7-95	2-0732	8-38	2-1258	8-81	2-1759	9-24	2-2235
7-96	2-0744	8-39	2-1270	8-82	2-1770	9-25	2-2246
7-97	2-0757	8-40	2-1282	8-83	2-1782	9-26	2-2257
7-98	2-0769	8-41	2-1294	8-84	2-1793	9-27	2-2268
7-99	2-0782	8-42	2-1306	8-85	2-1804	9-28	2-2279
8-00	2-0794	8-43	2-1318	8-86	2-1815	9-29	2-2289
8-01	2-0807	8-44	2-1330	8-87	2-1827	9-30	2-2300
8-02	2-0819	8-45	2-1342	8-88	2-1838	9-31	2-2311
8-03	2-0832	8-46	2-1353	8-89	2-1849	9-32	2-2322
8-04	2-0844	8-47	2-1365	8-90	2-1861	9-33	2-2332
8-05	2-0857	8-48	2-1377	8-91	2-1872	9-34	2-2343
8-06	2-0869	8-49	2-1389	8-92	2-1883	9-35	2-2354
8-07	2-0882	8-50	2-1401	8-93	2-1894	9-36	2-2364
8-08	2-0894	8-51	2-1412	8-94	2-1905	9-37	2-2375
8-09	2-0906	8-52	2-1424	8-95	2-1917	9-38	2-2386
8-10	2-0919	8-53	2-1436	8-96	2-1928	9-39	2-2396
8-11	2-0931	8-54	2-1448	8-97	2-1939	9-40	2-2407
8-12	2-0943	8-55	2-1459	8-98	2-1950	9-41	2-2418
8-13	2-0956	8-56	2-1471	9-99	2-1961	9-42	2-2428
8-14	2-0968	8-57	2-1483	9-00	2-1972	9-43	2-2439
8-15	2-0980	8-58	2-1494	9-01	2-1983	9-44	2-2450
8-16	2-0992	8-59	2-1506	9-02	2-1994	9-45	2-2460
8-17	2-1005	8-60	2-1518	9-03	2-2006	9-46	2-2471
8-18	2-1017	8-61	2-1529	9-04	2-2017	9-47	2-2481
8-19	2-1029	8-62	2-1541	9-05	2-2028	9-48	2-2492
8-20	2-1041	8-63	2-1552	9-06	2-2039	9-49	2-2502
8-21	2-1054	8-64	2-1564	9-07	2-2050	9-50	2-2513
8-22	2-1066	8-65	2-1576	9-08	2-2061	9-51	2-2523
8-23	2-1078	8-66	2-1587	9-09	2-2072	9-52	2-2534

No.	Log.	No.	Log.	No.	Log.	No.	Log.
9.53	2.2544	9.73	2.2752	9.93	2.2956	13.25	2.5840
9.54	2.2555	9.74	2.2762	9.94	2.2966	13.50	2.6027
9.55	2.2565	9.75	2.2773	9.95	2.2976	13.75	2.6211
9.56	2.2576	9.76	2.2783	9.96	2.2986	14.00	2.6391
9.57	2.2586	9.77	2.2793	9.97	2.2996	14.25	2.6567
9.58	2.2597	9.78	2.2803	9.98	2.3006	14.50	2.6740
9.59	2.2607	9.79	2.2814	9.99	2.3016	14.75	2.6913
9.60	2.2618	9.80	2.2824	10.00	2.3026	15.00	2.7081
9.61	2.2628	9.81	2.2834	10.25	2.3279	15.50	2.7408
9.62	2.2638	9.82	2.2844	10.50	2.3513	16.00	2.7726
9.63	2.2649	9.83	2.2854	10.75	2.3749	16.50	2.8034
9.64	2.2659	9.84	2.2865	11.00	2.3979	17.00	2.8332
9.65	2.2670	9.85	2.2875	11.25	2.4201	17.50	2.8621
9.66	2.2680	9.86	2.2885	11.50	2.4430	18.00	2.8904
9.67	2.2690	9.87	2.2895	11.75	2.4636	18.50	2.9173
9.68	2.2701	9.88	2.2905	12.00	2.4849	19.00	2.9444
9.69	2.2711	9.89	2.2915	12.25	2.5052	19.50	2.9703
9.70	2.2721	9.90	2.2925	12.50	2.5262	20.00	2.9957
9.71	2.2732	9.91	2.2935	12.75	2.5455		
9.72	2.2742	9.92	2.2946	13.00	2.5649		

TABLE 6.—SINES AND COSINES OF ANGLES FROM  
0° TO 90°.\*

(RADIUS = 1.)

Sines of Angles.	Cosines of Angles.	Values.	Sines of Angles.	Cosines of Angles.	Values.
0	90	.00000	5.5	84.5	.09585
0.5	89.5	.00873	6	84	.10453
1	89	.01745	6.5	83.5	.11320
1.5	88.5	.02618	7	83	.12187
2	88	.03490	7.5	82.5	.13053
2.5	87.5	.04362	8	82	.13917
3	87	.05234	8.5	81.5	.14781
3.5	86.5	.06105	9	81	.15643
4	86	.06976	9.5	80.5	.16505
4.5	85.5	.07846	10	80	.17365
5	85	.08716	10.5	79.5	.18224

\* See Introduction, *ante*, p. 6.

Sines of Angles.	Cosines of Angles.	Values.	Sines of Angles.	Cosines of Angles.	Values.
°	°		°	°	
11	79	·19081	31·5	58·5	·52250
11·5	78·5	·19937	32	58	·52992
12	78	·20791	32·5	57·5	·53730
12·5	77·5	·21644	33	57	·54464
13	77	·22495	33·5	56·5	·55194
13·5	76·5	·23344	34	56	·55919
14	76	·24192	34·5	55·5	·56641
14·5	75·5	·25038	35	55	·57358
15	75	·25882	35·5	54·5	·58070
15·5	74·5	·26724	36	54	·58778
16	74	·27564	36·5	53·5	·59482
16·5	73·5	·28401	37	53	·60181
17	73	·29237	37·5	52·5	·60876
17·5	72·5	·30071	38	52	·61566
18	72	·30902	38·5	51·5	·62251
18·5	71·5	·31730	39	51	·62932
19	71	·32557	39·5	50·5	·63608
19·5	70·5	·33381	40	50	·64279
20	70	·34202	40·5	49·5	·64945
20·5	69·5	·35021	41	49	·65606
21	69	·35837	41·5	48·5	·66262
21·5	68·5	·36650	42	48	·66913
22	68	·37461	42·5	47·5	·67559
22·5	67·5	·38268	43	47	·68200
23	67	·39073	43·5	46·5	·68835
23·5	66·5	·39875	44	46	·69466
24	66	·40674	44·5	45·5	·70091
24·5	65·5	·41469	45	45	·70711
25	65	·42262	45·5	44·5	·71325
25·5	64·5	·43051	46	44	·71934
26	64	·43837	46·5	43·5	·72537
26·5	63·5	·44620	47	43	·73135
27	63	·45399	47·5	42·5	·73728
27·5	62·5	·46175	48	42	·74314
28	62	·46947	48·5	41·5	·74896
28·5	61·5	·47716	49	41	·75471
29	61	·48481	49·5	40·5	·76041
29·5	60·5	·49242	50	40	·76604
30	60	·50000	50·5	39·5	·77162
30·5	59·5	·50754	51	39	·77715
31	59	·51504	51·5	38·5	·78261

Sines of Angles.	Cosines of Angles.	Values.	Sines of Angles.	Cosines of Angles.	Values.
°	°		°	°	
52	38	·78801	71·5	18·5	·94832
52·5	37·5	·79335	72	18	·95106
53	37	·79864	72·5	17·5	·95372
53·5	36·5	·80386	73	17	·95630
54	36	·80902	73·5	16·5	·95882
54·5	35·5	·81412	74	16	·96126
55	35	·81915	74·5	15·5	·96363
55·5	34·5	·82413	75	15	·96593
56	34	·82904	75·5	14·5	·96815
56·5	33·5	·83389	76	14	·97030
57	33	·83867	76·5	13·5	·97237
57·5	32·5	·84339	77	13	·97437
58	32	·84805	77·5	12·5	·97630
58·5	31·5	·85264	78	12	·97815
59	31	·85717	78·5	11·5	·97992
59·5	30·5	·86163	79	11	·98163
60	30	·86602	79·5	10·5	·98325
60·5	29·5	·87036	80	10	·98481
61	29	·87462	80·5	9·5	·98629
61·5	28·5	·87882	81	9	·98769
62	28	·88295	81·5	8·5	·98902
62·5	27·5	·88701	82	8	·99027
63	27	·89101	82·5	7·5	·99144
63·5	26·5	·89493	83	7	·99255
64	26	·89879	83·5	6·5	·99357
64·5	25·5	·90258	84	6	·99452
65	25	·90631	84·5	5·5	·99540
65·5	24·5	·90996	85	5	·99619
66	24	·91354	85·5	4·5	·99692
66·5	23·5	·91706	86	4	·99756
67	23	·92050	86·5	3·5	·99813
67·5	22·5	·92388	87	3	·99863
68	22	·92718	87·5	2·5	·99905
68·5	21·5	·93042	88	2	·99939
69	21	·93358	88·5	1·5	·99966
69·5	20·5	·93667	89	1	·99985
70	20	·93969	89·5	0·5	·99996
70·5	19·5	·94264	90	0	1·00000
71	19	·94552			

TABLE 7.—TANGENTS AND COTANGENTS OF ANGLES FROM  
0° TO 90°.\*

(RADIUS = 1.)

Tangents of Angles.	Cotan- gents of Angles.	Values.	Tangents of Angles.	Cotan- gents of Angles.	Values.
0	90	·00000	18·5	71·5	·33459
0·5	89·5	·00873	19	71	·34433
1	89	·01745	19·5	70·5	·35412
1·5	88·5	·02619	20	70	·36397
2	88	·03492	20·5	69·5	·37388
2·5	87·5	·04366	21	69	·38386
3	87	·05241	21·5	68·5	·39391
3·5	86·5	·06116	22	68	·40403
4	86	·06993	22·5	67·5	·41421
4·5	85·5	·07870	23	67	·42447
5	85	·08749	23·5	66·5	·43481
5·5	84·5	·09629	24	66	·44523
6	84	·10510	24·5	65·5	·45573
6·5	83·5	·11394	25	65	·46631
7	83	·12278	25·5	64·5	·47698
7·5	82·5	·13165	26	64	·48773
8	82	·14054	26·5	63·5	·49858
8·5	81·5	·14945	27	63	·50952
9	81	·15838	27·5	62·5	·52057
9·5	80·5	·16734	28	62	·53171
10	80	·17633	28·5	61·5	·54296
10·5	79·5	·18534	29	61	·55431
11	79	·19438	29·5	60·5	·56577
11·5	78·5	·20345	30	60	·57735
12	78	·21256	30·5	59·5	·58904
12·5	77·5	·22169	31	59	·60086
13	77	·23087	31·5	58·5	·61280
13·5	76·5	·24008	32	58	·62487
14	76	·24933	32·5	57·5	·63708
14·5	75·5	·25862	33	57	·64941
15	75	·26795	33·5	56·5	·66189
15·5	74·5	·27732	34	56	·67451
16	74	·28674	34·5	55·5	·68728
16·5	73·5	·29621	35	55	·70021
17	73	·30573	35·5	54·5	·71329
17·5	72·5	·31530	36	54	·72654
18	72	·32492	36·5	53·5	·73996

\* See Introduction, *ante*, p. 6.



Tangents of Angles.	Cotan- gents of Angles.	Values.	Tangents of Angles.	Cotan- gents of Angles.	Values.
°	°		°	°	
37	53	·75355	57·5	32·5	1·56969
37·5	52·5	·76763	58	32	1·60033
38	52	·78129	58·5	31·5	1·63185
38·5	51·5	·79544	59	31	1·66428
39	51	·80978	59·5	30·5	1·69766
39·5	50·5	·82434	60	30	1·73205
40	50	·83910	60·5	29·5	1·76749
40·5	49·5	·85408	61	29	1·80405
41	49	·86929	61·5	28·5	1·84174
41·5	48·5	·88472	62	28	1·88073
42	48	·90040	62·5	27·5	1·92098
42·5	47·5	·91633	63	27	1·96261
43	47	·93251	63·5	26·5	2·00569
43·5	46·5	·94896	64	26	2·05030
44	46	·96569	64·5	25·5	2·09654
44·5	45·5	·98270	65	25	2·14451
45	45	1·00000	65·5	24·5	2·19430
45·5	44·5	1·01761	66	24	2·24604
46	44	1·03553	66·5	23·5	2·29984
46·5	43·5	1·05378	67	23	2·35585
47	43	1·07237	67·5	22·5	2·41421
47·5	42·5	1·09131	68	22	2·47509
48	42	1·11061	68·5	21·5	2·53865
48·5	41·5	1·13029	69	21	2·60509
49	41	1·15037	69·5	20·5	2·67462
49·5	40·5	1·17085	70	20	2·74748
50	40	1·19175	70·5	19·5	2·82391
50·5	39·5	1·21310	71	19	2·90421
51	39	1·23490	71·5	18·5	2·98868
51·5	38·5	1·25717	72	18	3·07768
52	38	1·27994	72·5	17·5	3·17159
52·5	37·5	1·30323	73	17	3·27085
53	37	1·32704	73·5	16·5	3·37594
53·5	36·5	1·35142	74	16	3·48741
54	36	1·37638	74·5	15·5	3·60588
54·5	35·5	1·40195	75	15	3·73205
55	35	1·42815	75·5	14·5	3·86671
55·5	34·5	1·45501	76	14	4·01078
56	34	1·48256	76·5	13·5	4·16530
56·5	33·5	1·51084	77	13	4·33148
57	33	1·53986	77·5	12·5	4·51071

Tangents of Angles.	Cotan- gents of Angles.	Values.	Tangents of Angles.	Cotan- gents of Angles.	Values.
°	°		°	°	
78	12	4.70463	84.5	5.5	10.38540
78.5	11.5	4.91516	85	5	11.43005
79	11	5.14455	85.5	4.5	12.70620
79.5	10.5	5.39552	86	4	14.30067
80	10	5.67128	86.5	3.5	16.34985
80.5	9.5	5.97576	87	3	19.08114
81	9	6.31375	87.5	2.5	22.90377
81.5	8.5	6.69116	88	2	28.63625
82	8	7.11537	88.5	1.5	38.18846
82.5	7.5	7.59575	89	1	57.28996
83	7	8.14435	89.5	0.5	114.58865
83.5	6.5	8.77689	90	0	infinite.
84	6	9.51436			

TABLE 8.—LENGTHS OF CIRCULAR ARCS FROM 1° TO 180°.\*  
(RADIUS = 1.)

Deg.	Length.	Deg.	Length.	Deg.	Length.	Deg.	Length.
1	.0175	20	.3491	39	.6807	58	1.0123
2	.0349	21	.3665	40	.6981	59	1.0297
3	.0524	22	.3840	41	.7156	60	1.0472
4	.0698	23	.4014	42	.7330	61	1.0647
5	.0873	24	.4189	43	.7505	62	1.0821
6	.1047	25	.4363	44	.7679	63	1.0996
7	.1222	26	.4538	45	.7854	64	1.1170
8	.1396	27	.4712	46	.8029	65	1.1345
9	.1571	28	.4887	47	.8203	66	1.1519
10	.1745	29	.5061	48	.8378	67	1.1694
11	.1920	30	.5236	49	.8552	68	1.1868
12	.2094	31	.5411	50	.8727	69	1.2043
13	.2269	32	.5585	51	.8901	70	1.2217
14	.2443	33	.5760	52	.9076	71	1.2392
15	.2618	34	.5934	53	.9250	72	1.2566
16	.2793	35	.6109	54	.9425	73	1.2741
17	.2967	36	.6283	55	.9599	74	1.2915
18	.3142	37	.6458	56	.9774	75	1.3090
19	.3316	38	.6632	57	.9948	76	1.3265

\* See Introduction, ante, p. 7.

Deg.	Length.	Deg.	Length.	Deg.	Length.	Deg.	Length.
77	1.3439	103	1.7977	129	2.2515	155	2.7053
78	1.3613	104	1.8151	130	2.2690	156	2.7227
79	1.3788	105	1.8326	131	2.2864	157	2.7402
80	1.3963	106	1.8500	132	2.3038	158	2.7576
81	1.4137	107	1.8675	133	2.3213	159	2.7751
82	1.4312	108	1.8850	134	2.3387	160	2.7925
83	1.4486	109	1.9024	135	2.3562	161	2.8100
84	1.4661	110	1.9199	136	2.3736	162	2.8274
85	1.4835	111	1.9373	137	2.3911	163	2.8449
86	1.5010	112	1.9548	138	2.4086	164	2.8623
87	1.5184	113	1.9722	139	2.4260	165	2.8798
88	1.5359	114	1.9897	140	2.4435	166	2.8912
89	1.5533	115	2.0071	141	2.4609	167	2.9147
90	1.5708	116	2.0246	142	2.4784	168	2.9321
91	1.5882	117	2.0420	143	2.4958	169	2.9496
92	1.6057	118	2.0595	144	2.5133	170	2.9671
93	1.6232	119	2.0769	145	2.5307	171	2.9845
94	1.6406	120	2.0944	146	2.5482	172	3.0020
95	1.6581	121	2.1118	147	2.5656	173	3.0194
96	1.6755	122	2.1293	148	2.5831	174	3.0369
97	1.6930	123	2.1468	149	2.6005	175	3.0543
98	1.7104	124	2.1642	150	2.6180	176	3.0718
99	1.7279	125	2.1817	151	2.6354	177	3.0892
100	1.7453	126	2.1991	152	2.6529	178	3.1067
101	1.7628	127	2.2166	153	2.6704	179	3.1241
102	1.7802	128	2.2304	154	2.6878	180	3.1416

TABLE 9.—LENGTHS OF CIRCULAR ARCS, UP TO A  
SEMI-CIRCLE.\*  
(CHORD = 1.)

Height.	Length.	Height.	Length.	Height.	Length.	Height.	Length.
.001	1.00002	.009	1.00022	.017	1.00078	.025	1.00167
.002	1.00002	.010	1.00027	.018	1.00081	.026	1.00182
.003	1.00003	.011	1.00032	.019	1.00097	.027	1.00196
.004	1.00004	.012	1.00038	.020	1.00107	.028	1.00210
.005	1.00007	.013	1.00045	.021	1.00117	.029	1.00225
.006	1.00010	.014	1.00053	.022	1.00128	.030	1.00240
.007	1.00013	.015	1.00061	.023	1.00140	.031	1.00256
.008	1.00017	.016	1.00069	.024	1.00153	.032	1.00272

\* See Introduction, *ante*, p. 7.

Height.	Length.	Height.	Length.	Height.	Length.	Height.	Length.
·033	1·00289	·076	1·01533	·119	1·03734	·162	1·06858
·034	1·00307	·077	1·01573	·120	1·03797	·163	1·06941
·035	1·00327	·078	1·01614	·121	1·03860	·164	1·07025
·036	1·00345	·079	1·01656	·122	1·03923	·165	1·07109
·037	1·00364	·080	1·01698	·123	1·03987	·166	1·07194
·038	1·00384	·081	1·01741	·124	1·04051	·167	1·07279
·039	1·00405	·082	1·01784	·125	1·04116	·168	1·07365
·040	1·00426	·083	1·01828	·126	1·04181	·169	1·07451
·041	1·00447	·084	1·01872	·127	1·04247	·170	1·07537
·042	1·00469	·085	1·01916	·128	1·04313	·171	1·07624
·043	1·00492	·086	1·01961	·129	1·04380	·172	1·07711
·044	1·00515	·087	1·02006	·130	1·04447	·173	1·07799
·045	1·00539	·088	1·02052	·131	1·04515	·174	1·07888
·046	1·00563	·089	1·02098	·132	1·04584	·175	1·07977
·047	1·00587	·090	1·02146	·133	1·04652	·176	1·08066
·048	1·00612	·091	1·02192	·134	1·04722	·177	1·08156
·049	1·00638	·092	1·02240	·135	1·04792	·178	1·08246
·050	1·00665	·093	1·02289	·136	1·04862	·179	1·08337
·051	1·00692	·094	1·02339	·137	1·04932	·180	1·08428
·052	1·00720	·095	1·02389	·138	1·05003	·181	1·08519
·053	1·00748	·096	1·02440	·139	1·05075	·182	1·08611
·054	1·00776	·097	1·02491	·140	1·05147	·183	1·08704
·055	1·00805	·098	1·02542	·141	1·05220	·184	1·08797
·056	1·00834	·099	1·02593	·142	1·05293	·185	1·08890
·057	1·00864	·100	1·02646	·143	1·05367	·186	1·08984
·058	1·00895	·101	1·02698	·144	1·05441	·187	1·09079
·059	1·00926	·102	1·02752	·145	1·05516	·188	1·09174
·060	1·00957	·103	1·02806	·146	1·05591	·189	1·09269
·061	1·00989	·104	1·02860	·147	1·05667	·190	1·09365
·062	1·01021	·105	1·02914	·148	1·05743	·191	1·09461
·063	1·01054	·106	1·02970	·149	1·05819	·192	1·09557
·064	1·01088	·107	1·03026	·150	1·05896	·193	1·09654
·065	1·01123	·108	1·03082	·151	1·05973	·194	1·09752
·066	1·01158	·109	1·03139	·152	1·06051	·195	1·09850
·067	1·01193	·110	1·03196	·153	1·06130	·196	1·09949
·068	1·01229	·111	1·03254	·154	1·06209	·197	1·10048
·069	1·01264	·112	1·03312	·155	1·06288	·198	1·10147
·070	1·01302	·113	1·03371	·156	1·06368	·199	1·10247
·071	1·01338	·114	1·03430	·157	1·06449	·200	1·10347
·072	1·01376	·115	1·03490	·158	1·06530	·201	1·10447
·073	1·01414	·116	1·03551	·159	1·06611	·202	1·10548
·074	1·01453	·117	1·03611	·160	1·06693	·203	1·10650
·075	1·01493	·118	1·03672	·161	1·06775	·204	1·10752

Height.	Length.	Height.	Length.	Height.	Length.	Height.	Length.
·205	1·10855	·248	1·15670	·291	1·21239	·334	1·27502
·206	1·10958	·249	1·15791	·292	1·21377	·335	1·27656
·207	1·11062	·250	1·15912	·293	1·21515	·336	1·27810
·208	1·11165	·251	1·16034	·294	1·21654	·337	1·27864
·209	1·11269	·252	1·16156	·295	1·21794	·338	1·28118
·210	1·11374	·253	1·16279	·296	1·21933	·339	1·28273
·211	1·11479	·254	1·16402	·297	1·22073	·340	1·28428
·212	1·11584	·255	1·16526	·298	1·22213	·341	1·28583
·213	1·11690	·256	1·16650	·299	1·22354	·342	1·28739
·214	1·11796	·257	1·16774	·300	1·22495	·343	1·28895
·215	1·11904	·258	1·16899	·301	1·22636	·344	1·29052
·216	1·12011	·259	1·17024	·302	1·22778	·345	1·29209
·217	1·12118	·260	1·17150	·303	1·22920	·346	1·29366
·218	1·12225	·261	1·17276	·304	1·23063	·347	1·29523
·219	1·12334	·262	1·17403	·305	1·23206	·348	1·29681
·220	1·12444	·263	1·17530	·306	1·23349	·349	1·29838
·221	1·12554	·264	1·17657	·307	1·23492	·350	1·29997
·222	1·12664	·265	1·17784	·308	1·23636	·351	1·30156
·223	1·12774	·266	1·17912	·309	1·23780	·352	1·30315
·224	1·12885	·267	1·18040	·310	1·23926	·353	1·30474
·225	1·12997	·268	1·18169	·311	1·24070	·354	1·30634
·226	1·13108	·269	1·18299	·312	1·24216	·355	1·30794
·227	1·13219	·270	1·18429	·313	1·24361	·356	1·30954
·228	1·13331	·271	1·18559	·314	1·24507	·357	1·31115
·229	1·13444	·272	1·18689	·315	1·24654	·358	1·31276
·230	1·13557	·273	1·18820	·316	1·24801	·359	1·31437
·231	1·13671	·274	1·18951	·317	1·24948	·360	1·31599
·232	1·13785	·275	1·19082	·318	1·25095	·361	1·31761
·233	1·13900	·276	1·19214	·319	1·25243	·362	1·31923
·234	1·14015	·277	1·19346	·320	1·25391	·363	1·32086
·235	1·14131	·278	1·19479	·321	1·25540	·364	1·32249
·236	1·14247	·279	1·19612	·322	1·25689	·365	1·32413
·237	1·14363	·280	1·19746	·323	1·25838	·366	1·32577
·238	1·14480	·281	1·19880	·324	1·25988	·367	1·32741
·239	1·14597	·282	1·20014	·325	1·26138	·368	1·32905
·240	1·14714	·283	1·20149	·326	1·26288	·369	1·33069
·241	1·14832	·284	1·20284	·327	1·26437	·370	1·33234
·242	1·14951	·285	1·20419	·328	1·26588	·371	1·33399
·243	1·15070	·286	1·20555	·329	1·26740	·372	1·33564
·244	1·15189	·287	1·20691	·330	1·26892	·373	1·33730
·245	1·15308	·288	1·20827	·331	1·27044	·374	1·33896
·246	1·15428	·289	1·20964	·332	1·27196	·375	1·34063
·247	1·15549	·290	1·21202	·333	1·27349	·376	1·34229

Height.	Length.	Height	Length.	Height.	Length.	Height.	Length.
·377	1·34396	·408	1·39724	·439	1·45327	·470	1·51185
·378	1·34563	·409	1·39900	·440	1·45512	·471	1·51378
·379	1·34731	·410	1·40077	·441	1·45697	·472	1·51571
·380	1·34899	·411	1·40254	·442	1·45883	·473	1·51764
·381	1·35068	·412	1·40432	·443	1·46069	·474	1·51958
·382	1·35237	·413	1·40610	·444	1·46255	·475	1·52152
·383	1·35406	·414	1·40788	·445	1·46441	·476	1·52346
·384	1·35575	·415	1·40966	·446	1·46628	·477	1·52541
·385	1·35744	·416	1·41145	·447	1·46815	·478	1·52736
·386	1·35914	·417	1·41324	·448	1·47002	·479	1·52931
·387	1·36084	·418	1·41503	·449	1·47189	·480	1·53126
·388	1·36254	·419	1·41682	·450	1·47377	·481	1·53322
·389	1·36425	·420	1·41861	·451	1·47565	·482	1·53518
·390	1·36596	·421	1·42041	·452	1·47753	·483	1·53714
·391	1·36767	·422	1·42221	·453	1·47942	·484	1·53910
·392	1·36939	·423	1·42402	·454	1·48131	·485	1·54106
·393	1·37111	·424	1·42583	·455	1·48320	·486	1·54302
·394	1·37283	·425	1·42764	·456	1·48509	·487	1·54499
·395	1·37455	·426	1·42945	·457	1·48699	·488	1·54696
·396	1·37628	·427	1·43127	·458	1·48889	·489	1·54893
·397	1·37801	·428	1·43309	·459	1·49079	·490	1·55091
·398	1·37974	·429	1·43491	·460	1·49269	·491	1·55289
·399	1·38148	·430	1·43673	·461	1·49460	·492	1·55487
·400	1·38322	·431	1·43856	·462	1·49651	·493	1·55685
·401	1·38496	·432	1·44039	·463	1·49842	·494	1·55884
·402	1·38671	·433	1·44222	·464	1·50033	·495	1·56083
·403	1·38846	·434	1·44405	·465	1·50224	·496	1·56282
·404	1·39021	·435	1·44589	·466	1·50416	·497	1·56481
·405	1·39196	·436	1·44773	·467	1·50608	·498	1·56681
·406	1·39372	·437	1·44957	·468	1·50800	·499	1·56881
·407	1·39548	·438	1·45142	·469	1·50992	·500	1·57080

TABLE 10.—AREAS OF CIRCULAR SEGMENTS, UP TO A SEMICIRCLE.\*

(DIAMETER OF CIRCLE = 1.)

Height.	Area.	Height.	Area.	Height.	Area.	Height.	Area.
·001	·000042	·005	·000471	·009	·001135	·013	·00197
·002	·000119	·006	·000619	·010	·00133	·014	·00220
·003	·000219	·007	·000779	·011	·00153	·015	·00244
·004	·000337	·008	·000952	·012	·00175	·016	·00268

\* See Introduction, *ante*, p. 7.

Height.	Area.	Height.	Area.	Height.	Area.	Height.	Area.
·017	·00294	·060	·01924	·103	·04269	·146	·07103
·018	·00320	·061	·01972	·104	·04330	·147	·07174
·019	·00347	·062	·02020	·105	·04391	·148	·07245
·020	·00375	·063	·02068	·106	·04452	·149	·07316
·021	·00403	·064	·02117	·107	·04514	·150	·07387
·022	·00432	·065	·02166	·108	·04576	·151	·07459
·023	·00461	·066	·02215	·109	·04638	·152	·07530
·024	·00492	·067	·02265	·110	·04701	·153	·07603
·025	·00523	·068	·02315	·111	·04763	·154	·07675
·026	·00555	·069	·02366	·112	·04826	·155	·07747
·027	·00587	·070	·02417	·113	·04889	·156	·07819
·028	·00619	·071	·02468	·114	·04953	·157	·07892
·029	·00653	·072	·02520	·115	·05016	·158	·07965
·030	·00687	·073	·02571	·116	·05080	·159	·08038
·031	·00721	·074	·02624	·117	·05145	·160	·08111
·032	·00756	·075	·02676	·118	·05209	·161	·08185
·033	·00792	·076	·02729	·119	·05274	·162	·08258
·034	·00828	·077	·02782	·120	·05338	·163	·08332
·035	·00864	·078	·02836	·121	·05404	·164	·08406
·036	·00901	·079	·02889	·122	·05469	·165	·08480
·037	·00939	·080	·02943	·123	·05535	·166	·08554
·038	·00977	·081	·02997	·124	·05600	·167	·08629
·039	·01015	·082	·03053	·125	·05666	·168	·08704
·040	·01054	·083	·03108	·126	·05733	·169	·08778
·041	·01093	·084	·03163	·127	·05799	·170	·08854
·042	·01133	·085	·03219	·128	·05866	·171	·08929
·043	·01173	·086	·03275	·129	·05933	·172	·09004
·044	·01214	·087	·03331	·130	·06000	·173	·09080
·045	·01255	·088	·03385	·131	·06067	·174	·09155
·046	·01297	·089	·03444	·132	·06135	·175	·09231
·047	·01340	·090	·03501	·133	·06203	·176	·09307
·048	·01382	·091	·03558	·134	·06271	·177	·09383
·049	·01425	·092	·03616	·135	·06339	·178	·09460
·050	·01468	·093	·03674	·136	·06407	·179	·09537
·051	·01512	·094	·03732	·137	·06476	·180	·09613
·052	·01556	·095	·03790	·138	·06545	·181	·09690
·053	·01601	·096	·03850	·139	·06614	·182	·09767
·054	·01646	·097	·03909	·140	·06683	·183	·09845
·055	·01691	·098	·03968	·141	·06753	·184	·09922
·056	·01737	·099	·04028	·142	·06822	·185	·09999
·057	·01783	·100	·04087	·143	·06892	·186	·10077
·058	·01830	·101	·04148	·144	·06963	·187	·10153
·059	·01877	·102	·04208	·145	·07033	·188	·10233

Height.	Area.	Height.	Area.	Height.	Area.	Height.	Area.
·189	·10317	·232	·13815	·275	·17554	·318	·21480
·190	·10390	·233	·13899	·276	·17644	·319	·21573
·191	·10469	·234	·13984	·277	·17733	·320	·21667
·192	·10547	·235	·14069	·278	·17823	·321	·21760
·193	·10626	·236	·14154	·279	·17912	·322	·21853
·194	·10705	·237	·14239	·280	·18002	·323	·21947
·195	·10784	·238	·14324	·281	·18092	·324	·22040
·196	·10864	·239	·14409	·282	·18182	·325	·22134
·197	·10943	·240	·14494	·283	·18272	·326	·22228
·198	·11023	·241	·14580	·284	·18362	·327	·22322
·199	·11102	·242	·14665	·285	·18452	·328	·22415
·200	·11182	·243	·14752	·286	·18542	·329	·22509
·201	·11262	·244	·14837	·287	·18633	·330	·22603
·202	·11343	·245	·14923	·288	·18723	·331	·22697
·203	·11423	·246	·15009	·289	·18814	·332	·22792
·204	·11504	·247	·15096	·290	·18905	·333	·22886
·205	·11584	·248	·15182	·291	·18996	·334	·22980
·206	·11665	·249	·15268	·292	·19086	·335	·23074
·207	·11746	·250	·15355	·293	·19177	·336	·23169
·208	·11827	·251	·15442	·294	·19268	·337	·23263
·209	·11908	·252	·15528	·295	·19360	·338	·23358
·210	·11990	·253	·15615	·296	·19451	·339	·23453
·211	·12071	·254	·15702	·297	·19543	·340	·23547
·212	·12153	·255	·15789	·298	·19634	·341	·23642
·213	·12235	·256	·15876	·299	·19725	·342	·23737
·214	·12317	·257	·15964	·300	·19817	·343	·23832
·215	·12399	·258	·16051	·301	·19908	·344	·23927
·216	·12481	·259	·16139	·302	·20000	·345	·24025
·217	·12563	·260	·16226	·303	·20092	·346	·24117
·218	·12646	·261	·16314	·304	·20184	·347	·24212
·219	·12729	·262	·16402	·305	·20276	·348	·24307
·220	·12811	·263	·16490	·306	·20368	·349	·24403
·221	·12894	·264	·16578	·307	·20460	·350	·24498
·222	·12977	·265	·16666	·308	·20553	·351	·24593
·223	·13060	·266	·16755	·309	·20645	·352	·24689
·224	·13144	·267	·16843	·310	·20738	·353	·24784
·225	·13227	·268	·16932	·311	·20830	·354	·24880
·226	·13311	·269	·17020	·312	·20923	·355	·24976
·227	·13395	·270	·17109	·313	·21015	·356	·25071
·228	·13478	·271	·17198	·314	·21108	·357	·25167
·229	·13562	·272	·17287	·315	·21201	·358	·25263
·230	·13646	·273	·17376	·316	·21294	·359	·25359
·231	·13731	·274	·17465	·317	·21387	·360	·25455



Height.	Area.	Height.	Area.	Height.	Area.	Height.	Area.
·361	·25551	·391	·28457	·421	·31403	·451	·34378
·362	·25647	·392	·28554	·422	·31502	·453	·34577
·363	·25743	·393	·28652	·423	·31600	·455	·34776
·364	·25839	·394	·28750	·424	·31699	·457	·34975
·365	·25936	·395	·28848	·425	·31798	·459	·35174
·366	·26032	·396	·28955	·426	·31897	·462	·35474
·367	·26128	·397	·29043	·427	·31996	·464	·35673
·368	·26225	·398	·29141	·428	·32095	·466	·35873
·369	·26321	·399	·29239	·429	·32194	·468	·36072
·370	·26418	·400	·29337	·430	·32293	·470	·36272
·371	·26514	·401	·29435	·431	·32392	·471	·36371
·372	·26611	·402	·29533	·432	·32491	·473	·36571
·373	·26708	·403	·29631	·433	·32590	·475	·36771
·374	·26805	·404	·29729	·434	·32689	·477	·36971
·375	·26901	·405	·29827	·435	·32788	·479	·37170
·376	·26998	·406	·29926	·436	·32887	·482	·37470
·377	·27095	·407	·30024	·437	·32987	·484	·37670
·378	·27192	·408	·30122	·438	·33086	·486	·37870
·379	·27289	·409	·30220	·439	·33185	·488	·38070
·380	·27386	·410	·30319	·440	·33284	·490	·38270
·381	·27483	·411	·30417	·441	·33384	·491	·38370
·382	·27580	·412	·30516	·442	·33483	·492	·38470
·383	·27678	·413	·30614	·443	·33582	·493	·38570
·384	·27775	·414	·30712	·444	·33682	·494	·38670
·385	·27872	·415	·30811	·445	·33781	·495	·38770
·386	·27969	·416	·30910	·446	·33880	·496	·38870
·387	·28070	·417	·31008	·447	·33980	·497	·38970
·388	·28164	·418	·31107	·448	·34079	·498	·39070
·389	·28262	·419	·31205	·449	·34179	·499	·39170
·390	·28359	·420	·31304	·450	·34278	·500	·39270

TABLE 11.—LENGTHS OF SEMI-ELLIPTIC ARCS.

(J. C. Trautwine.)\*

(SPAN = 1).

Height.	Length.	Height.	Length.	Height.	Length.	Height.	Length.
·02	1·003	·045	1·014	·07	1·029	·095	1·046
·025	1·004	·05	1·017	·075	1·032	·100	1·051
·03	1·006	·055	1·020	·08	1·036	·105	1·055
·035	1·008	·06	1·023	·085	1·039	·110	1·059
·04	1·011	·065	1·026	·09	1·043	·115	1·064

\* See Introduction, ante p. 7.

Height.	Length.	Height.	Length.	Height.	Length.	Height.	Length.
120	1.069	220	1.177	315	1.298	410	1.434
125	1.074	225	1.183	320	1.305	415	1.441
130	1.079	230	1.189	325	1.312	420	1.449
135	1.084	235	1.196	330	1.319	425	1.456
140	1.089	240	1.202	335	1.325	430	1.464
145	1.094	245	1.207	340	1.332	435	1.471
150	1.099	250	1.213	345	1.339	440	1.479
155	1.104	255	1.219	350	1.346	445	1.486
160	1.109	260	1.226	355	1.353	450	1.494
165	1.115	265	1.233	360	1.361	455	1.501
170	1.120	270	1.239	365	1.368	460	1.509
175	1.125	275	1.245	370	1.375	465	1.517
180	1.131	280	1.252	375	1.382	470	1.524
185	1.137	285	1.259	380	1.390	475	1.532
190	1.142	290	1.265	385	1.397	480	1.540
195	1.147	295	1.272	390	1.404	485	1.547
200	1.153	300	1.279	395	1.412	490	1.555
205	1.159	305	1.285	400	1.419	495	1.563
210	1.165	310	1.292	405	1.426	500	1.571
215	1.171						

## MEASUREMENT OF SURFACES AND SOLIDS.

### Plane Surfaces.

*The area of a triangle* is equal to half the product of the base by the perpendicular height.

*The area of a parallelogram* is equal to the product of the length by the height.

*The area of a trapezoid* (a parallel-sided figure of four sides, having two sides not parallel) is equal to the product of half the sum of the parallel sides by the distance between them.

*The area of any quadrilateral or four-sided figure*, is found by dividing the figure into two triangles; the sum of the areas of which is the area of the quadrilateral.

*The area of a square or a rhombus* (an oblique-angled equal-sided parallelogram) is equal to half the product of the diagonals.

*The area of a polygon or many-sided figure* is found by dividing the figure into triangles and trapezoids; the sum of the areas of these is the area of the figure.

*The area of a regular polygon* is half the product found by

multiplying the length of the side by the number of sides and by the perpendicular from the centre to one of the sides. In Table 12, columns 3 and 4 respectively are the lengths of the perpendiculars and the areas of the figures, when the length of the side is equal to 1; also the areas of polygons having an even number of sides, when the width across, between parallel sides (or twice the perpendicular length),

TABLE 12.—REGULAR POLYGONS.

Designation of Polygon.	Number of Sides.	Perpen- dicular. (Side=1.)	Area. (Side=1.)	Area. (Width across =1.)
1.	2.	3.	4.	5.
Equilateral triangle.	3	0·2887	0·4330	...
Square . . . . .	4	0·5000	1·0000	1·0000
Pentagon . . . . .	5	0·6882	1·7205	...
Hexagon . . . . .	6	0·8660	2·5981	0·8661
Heptagon . . . . .	7	1·0383	3·6339	...
Octagon . . . . .	8	1·2071	4·8284	0·3284
Nonagon . . . . .	9	1·3737	6·1818	...
Decagon . . . . .	10	1·5388	7·6942	0·8123
Undecagon . . . . .	11	1·7028	9·3656	...
Dodecagon . . . . .	12	1·8660	11·1962	0·8082
Circle . . . . .	infinite	infinite	infinite	0·7854

is equal to 1. A line is added to the table showing the relation of the circle as a polygon having an indefinitely great number of sides.

When the length of the side is other than 1, the perpendiculars and areas are to be calculated by squaring the given value of the side and multiplying the square by the corresponding coefficient in the table: column 3 for the perpendicular, column 4 for the area.

When the width across is other than 1, the area is to be calculated by squaring the value of the given width and multiplying the square by the corresponding coefficient in column 5.

A Regular Polygon may be inscribed in a circle. To supply a means of dividing the circumference of a circle into any number of equal parts, with a view to inscription of a polygon, the annexed tablet of angles at the centre subtended by the sides of polygons, expressed in degrees, is of general utility. Set off round the centre of the circle a succession of angles by means of the protractor, equal to the angle in the table due to a given number of sides. The radii so drawn divide the cir-

cumference into the same number of parts. The triangles thus formed are the elementary triangles of the polygon.

TABLE 13.—POLYGONAL ANGLES AT THE CENTRE.

Number of Sides of Polygon.	Elementary Angle at Centre.	Number of Sides of Polygon.	Elementary Angle at Centre.
Sides.	Degrees.	Sides.	Degrees.
3	120	12	30
4	90	13	$27\frac{2}{13}$
5	72	14	$25\frac{5}{7}$
6	60	15	24
7	$51\frac{3}{7}$	16	$22\frac{1}{2}$
8	45	17	$21\frac{3}{17}$
9	40	18	20
10	36	19	19 (exactly $18\frac{18}{19}$ )
11	$32\frac{8}{11}$	20	18

### Circle.

*The circumference of a circle* is 3.1416 times the diameter ; or, approximately,  $3\frac{1}{2}$  times. Or, the diameter is to the circumference as 7 to 22, approximately ; or as 113 to 355. Trigonometrically, the circle is divisible into 360 degrees.

When the *diameter* is 1, the area is equal to .7854, or approximately 4-5ths. The area of a circle of a given diameter is found by multiplying the square of the diameter by .7854.

*The length of an arc of a circle* is found by multiplying the number of degrees in the arc by the radius, and by .01745. Or, approximately, by subtracting the chord of the arc from eight times the chord of half the arc ; and taking one-third of the remainder.

*The area of a sector of a circle* is equal to the product of half the length of the arc of the sector by the radius. Or, multiply the number of degrees in the arc by the square of the radius, and by .008727.

*The area of a segment of a circle.* Find the area of the sector which has the same arc as the segment ; also the area of the triangle formed by the radial sides of the sector and the chord of the arc. The difference or the sum of these areas is the area of the segment, according as it is less or greater than a semicircle.

*The area of a ring.* Multiply the sum of the outer and inner diameters by their difference and by .7854.

*The area of a zone of a circle.* Find the areas of the two

segments cut off, and subtract the sum of these areas from the area of the whole circle, to give the area of the zone.

*The side of a square* equal in area to a given circle is equal to the product of the diameter by .8862.

*The side of a square inscribed* in a circle is equal to the product of the diameter by .7071.

*The area of an inscribed square* is equal to the product of the area of the circle by .6366.

*The diameter of a circle equal in area* to a given square is equal to the product of the side of the square by 1.1284, or  $1\frac{1}{8}$  approximately.

*The diameter of a circumscribing circle* is equal to the product of the side of the given square by 1.4142.

*The area of a circumscribing circle* is equal to the product of the area of the given square by 1.5708.

### Ellipse.

*The circumference of an ellipse* is equal to the product of the square root of half the sum of the squares of the two axes by 3.1416.

This rule is approximate. Mr. Trautwine proposes the following formula for the circumference of an ellipse, as more nearly exact, and sufficiently so for ordinary purposes. When the longer axis,  $D$ , is not more than five times the length of the shorter axis,  $d$ ,

$$\text{Circumference} = 3.1416 \sqrt{\frac{D^2 + d^2}{2} - \frac{(D - d)^2}{8.8}} \quad (1)$$

When the longer axis is more than five lengths of the shorter axis, the divisor 8.8 under the sign is to be replaced by the following divisors:—

When the longer axis is				Divisor.
6 times	the	shorter		9
"	"	7	"	9.2
"	"	8	"	9.3
"	"	9	"	9.35
"	"	10	"	9.4
"	"	12	"	9.5
"	"	14	"	9.6
"	"	16	"	9.68
"	"	18	"	9.75
"	"	20	"	9.8
"	"	25	"	9.87
"	"	30	"	9.92
"	"	40	"	9.98
"	"	50	"	10.00

*The area of an ellipse* is equal to the product of the two axes by .7854.

*The area of a segment of an ellipse*, the base of which is parallel to one of the axes of the ellipse. Divide the height of the segment by the axis of which it is a part, and find the area of a circular segment, in a table of circular segments, of which the height is equal to the quotient; multiply the area thus found by the two axes of the ellipse successively; the product is the area.

### Curvilinear Figures.

*The area of any curvilinear figure* bounded at the ends by parallel straight lines by Simpson's rule. Divide the length of the figure into any even number of equal parts, at the common distance D apart, and draw ordinates through the points of division, to touch the boundary lines. Add together the first and last ordinates, and call the sum A; add together the even ordinates, and call the sum B; add together the odd ordinates, except the first and last, and call the sum C. Then,

$$\text{area of the figure} = \frac{A + 4B + 2C}{3} \times D \quad (2)$$

*2nd Method.*—Divide the figure into any sufficient number,  $n$ , of equal parts; add together the first and last ordinates, making the sum A; add together all the intermediate ordinates, making the sum B. Putting L for the length of the figure. Then,

$$\text{area of the figure} = \frac{A + 2B}{2n} \times L \quad (3)$$

*3rd Method.*—Divide the figure into a sufficient number of equal parts, as before. Add together the mean depths of the several divisions, and divide the sum by the number of divisions, to give the average depth; multiply the average depth by the total length, to give the area.

The figure may, otherwise, be divided into two half-parts, one at each end, and a number of whole parts intermediately. The sum of the ordinates, excepting the extreme ordinates, divided by the number of them, gives the average depth, and the product of this by the length, gives the area.

The figures may be bounded at the ends by curves or angles. In this case, the extreme ordinates become nothing.

### Solids.

There are five species of regular solids, bounded by regular polygons, of which particulars are given in the annexed table:—

TABLE 14.—REGULAR SOLIDS.

Designation of Solid. 1	Number and Designation of Sides. 2	Superficial Area (Edge = 1) 3	Contents (Edge = 1) 4
Tetrahedron .	4 equilateral triangles .	1.7320	0.1178
Hexahedron, } or Cube }	6 squares . . . . .	6.0000	1.0000
Octahedron .	8 equilateral triangles .	3.4641	0.4714
Dodecahedron	12 pentagons . . . . .	20.6458	7.6631
Icosahedron .	20 equilateral triangles.	8.6603	2.1817

Regular solids may be circumscribed by spheres; and spheres may be inscribed in regular solids.

*To find the total area of surface of a regular solid*, multiply the square of the length of the edge by the tabular number given in column 3 of the table.

*To find the contents of a regular solid*, multiply the cube of the length of the edge by the tabular number in column 4 of the table.

The four leading solids are the cube, the cylinder, the sphere, and the cone. A cubic foot contains

- 1,728 cubic inches, or
- 2,200 cylindrical inches, or
- 3,300 spherical inches, or
- 6,600 conical inches.

These values supply an easy practical rule for finding, by proportion, the capacities of the "three round bodies."

*The surface of a cylinder, or of a prism*, is equal to the product of the perimeter of one end by the height; plus twice the area of one end.

*The cubic content of a cylinder, or of a prism*, is equal to the product of the area of the base by the length or height of the cylinder.

*The surface of a sphere* is equal to the product of the square of the diameter by 3.1416.

It is equal to four times the area of one of its great circles.

It is equal to the convex surface of its circumscribing cylinder.

The surfaces of spheres are to each other as the squares of their diameters.

*The curve surface of a segment, or a zone of a sphere*, is equal to the product of the diameter of the sphere by the height of the segment or zone, and by 3.1416. The curve

surfaces of segments or zones of a sphere are in the ratio of their heights.

*The content of a sphere* is equal to the product of the cube of the diameter by  $\cdot 5236$ . Or, it is the product of the surface by one-sixth of the diameter.

The content of a sphere is two-thirds of that of the circumscribing cylinder.

The contents of spheres are to each other as the cubes of the diameters.

*The cubic content of a segment of a sphere.* From three times the diameter of the sphere subtract twice the height of the segment; multiply the difference by the square of the height, and by  $\cdot 5236$ . Or, to three times the square of the radius of the base of the segment, add the square of its height; and multiply the sum by the height, and by  $\cdot 5236$ .

*The cubic content of a zone of a sphere.* To the sum of the squares of the radii of the ends add one-third of the square of the height; multiply the sum by the height, and by  $1\cdot 5708$ .

*The cubic content of a spheroid* is equal to the product of the square of the revolving axis by the fixed axis, and by  $\cdot 5236$ . The content of a spheroid is two-thirds of that of the circumscribing cylinder.

*The cubic content of a segment of a spheroid.* 1. When the base is parallel to the revolving axis, multiply the difference between three times the fixed axis and twice the height of the segment, by the square of the height, and by  $\cdot 5236$ . Multiply the product by the square of the revolving axis, and divide by the square of the fixed axis.

2. When the base is perpendicular to the revolving axis, multiply the difference between three times the revolving axis and twice the height of the segment, by the square of the height, and by  $\cdot 5236$ . Multiply the product by the length of the fixed axis, and divide by the length of the revolving axis.

*The cubic content of the middle frustum of a spheroid.* 1. When the ends are circular, or parallel to the revolving axis. To twice the square of the middle diameter, add the square of the diameter of one end; multiply the sum by the length of the frustum, and by  $\cdot 2618$ .

2. When the ends are elliptical, or perpendicular to the revolving axis. To twice the product of the transverse and conjugate diameters of the middle section, add the product of the transverse and conjugate diameters of one end; multiply the sum by the length of the frustum, and by  $\cdot 2618$ .

*The cubic content of a parabolic conoid* (generated by the revolution of a parabola on its axis). Multiply the area of the base by half the height.



Or, multiply the square of the diameter of the base by the height, and by  $\cdot 392$ .

*The cubic content of a frustum of a parabolic conoid.* Multiply half the sum of the areas of the two ends by the height.

*The cubic content of a parabolic spindle* (generated by the revolution of a parabola on its base). Multiply the square of the middle diameter by the length, and by  $\cdot 4189$ .

The content of a parabolic spindle is to that of a cylinder of the same height and diameter, as 8 to 15.

*The cubic content of the middle frustum of a parabolic spindle.* Add together 8 times the square of the maximum diameter, 3 times the square of the end diameter, and 4 times the product of the diameters; multiply the sum by the length of the frustum, and by  $\cdot 05236$ .

This rule is applicable for calculating the content of casks of parabolic form.

*To find the cubic content of a cask of any form.* Add together 39 times the square of the bung diameter, 25 times the square of the head diameter, and 26 times the product of the diameters; multiply the sum by the length, and divide by 31,773 for the content in imperial gallons.

This rule was framed by Dr. Hutton, on the supposition that the middle third of the length of the cask was a frustum of a parabolic spindle, and each outer third was a frustum of a cone.

*To find the ullage of a cask,* the quantity of liquor in it when it is not full. 1. For a *lying cask*. Divide the number of wet or dry inches by the bung diameter in inches. If the quotient is less than  $\cdot 5$ , deduct from it one-fourth part of what it wants of  $\cdot 5$ . If it exceeds  $\cdot 5$ , add to it one-fourth part of the excess above  $\cdot 5$ . Multiply the remainder or the sum by the whole content of the cask. The product is the quantity of liquor in the cask, in gallons, when the dividend is *wet inches* or the empty space, if *dry inches*.

2. For a *standing cask*. Divide the number of wet or dry inches by the length of the cask. If the quotient exceeds  $\cdot 5$ , add to it one-tenth of its excess above  $\cdot 5$ ; if less than  $\cdot 5$ , subtract from it one-tenth of what it wants of  $\cdot 5$ . Multiply the sum or the remainder by the whole content of the cask. The product is the quantity of liquor in the cask, when the dividend is *wet inches*; or the empty space if *dry inches*.

*The surface of a cone or of a pyramid* is equal to the product of the perimeter of the base by half the slant height, plus the area of the base.

*The content of a cone or of a pyramid* is equal to the product of the area of the base by one-third of the perpendicular height.

*The surface of a frustum of a cone or a pyramid* is equal to the product of the sum of the perimeters of the ends by half the slant height, plus the areas of the ends.

*The content of a frustum of a cone or a pyramid* is found by adding together the areas of the ends and the mean proportional between them (the square root of their product), and multiplying the sum by one-third of the perpendicular height.

Or, in the case of a conical frustum, add together the squares of the diameters and the product of the diameters and multiply the sum by .7854, and by one-third of the height.

*The content of a wedge* is found by adding together twice the length of the base and the length of the edge, and multiplying the sum by the breadth of the base, and by one-sixth of the height.

*The content of a prismoid* (a solid having three or more inclined sides, and similar parallel ends) is found by adding together the areas of the ends, and four times the intermediate sectional area equally distant from the ends; and multiplying the sum by one-sixth of the length.

*The content of an irregular solid* may be found by dividing it into parts measurable by the ordinary rules, and adding together the contents of them; the sum is the content of the solid.

*Piles of equal spheres or balls.* Ranged usually in pyramidal piles, on a square or a triangular base; or in oblong piles on a rectangular base:—

1. *To find the number of balls in a pile on a square base.* Let  $n$  = the number of horizontal strata or layers of spheres in the piles, comprising the highest stratum, which consists of one sphere. The number,  $S$ , of spheres is

$$S = \frac{2n^3 + 3n^2 + n}{6} \quad . \quad . \quad . \quad (4)$$

The value  $n$  expresses also the number of spheres in one side of the base. If, for example,  $n=10$ , the number of balls,  $S$ , is, by the formula,  $(2,000 + 300 + 10) \div 6 = 385$ .

2. *On a triangular base.*

$$S = \frac{n(n+1)(n+2)}{6} \quad . \quad . \quad . \quad (5)$$

If  $n$  is equal to 10,  $S$  is equal to 220.

3. *Oblong pile on a rectangular base.* The uppermost stratum is a row of balls, say  $m$  in number,

$$S = \frac{n(n+1)(3m+2n)-2}{6} \quad . \quad . \quad . \quad (6)$$

Supposing  $m$  and  $n$  each equal to 10,  $S$  is equal to 880.

# DESCRIPTION OF CIRCULAR SEGMENTS, CONIC SECTIONS AND CYCLOIDS.

To describe a Circle passing through three given points, when the Centre is not available. From the extreme points A, B, fig. 1, as centres describe arcs AH, BG. Through the third point C draw AE, BF. Divide AF and BE into any

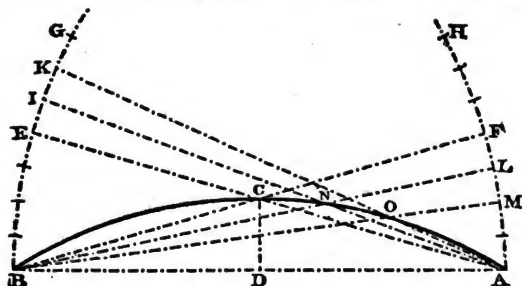


FIG. 1.—To describe a Circular Arc through three points.

convenient number of equal parts, and set off a series of equal parts of the same length on the upper portions of the arcs, beyond the points E, F. Draw straight lines BL, BM, &c., to the divisions in AF; and AI, AK, &c., to the division in EG. The successive intersections at N, O, &c., of these lines, are points in the circle required, between the given points A and C, which may be traced in accordingly. Similarly, the remaining part of the curve may be described.

*2nd Method.* Let A, D, B, fig. 2, be the given points. Draw AB, AD, and DB; and *ef* parallel to AB. Divide AD into a number of equal parts, at 1, 2, 3, &c., and from D

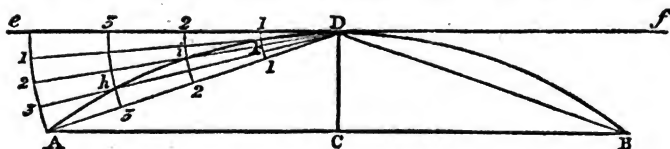


FIG. 2.—To describe a Circular Arc through three points.

describe arcs through these points. Divide the arc *Ae* into the same number of equal parts, and draw straight lines from D to the points of division. The intersections of these lines successively with the arcs 1, 2, 3, &c., are points in the circle.

*Note.*—The second method is not exact, but it is sufficiently near to exactness for arcs less than one-fourth of a circle.

The Ellipse is a Curve such that the sum of the distances of any point in the curve from two fixed points or foci, is constant.

*To describe an Ellipse*, when the length and width are given.

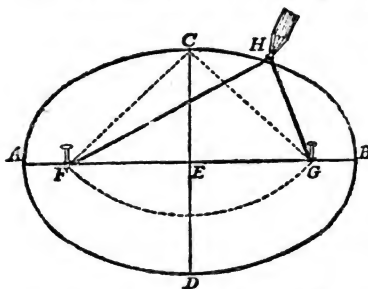


FIG. 3.—To describe an Ellipse.

On the centre C, fig. 3, with AE as radius, cut the axis AB at F and G, the foci. Fix a couple of pins into the axis at F and G, and loop a thread or cord upon them equal in length to the axis AB, so as, when stretched, to reach to the extremity C of the conjugate axis. With a pencil or draw-point inside the cord, as at H, guide the pencil in tension

about the pins F and G, and so describe the ellipse.

*2nd Method.* Bisect the transverse axis, fig. 4 at C, and through C draw the perpendicular DE, making CD and CE each equal to half the conjugate axis. From D or E, with the

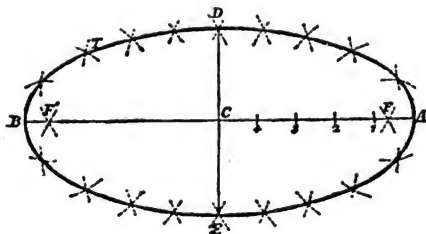


Fig. 4.—To describe an Ellipse.

radius AC cut the transverse axis at F, F', for the foci. Divide AC into any number of parts at 1, 2, 3, &c. With the radius A1, on F and F' as centres, describe arcs; and with the radius B1 on the same centres, cut these arcs, as shown. Repeat the operation for the other points of division of the transverse axis. The series of intersections thus made are points in the curve, through which the curve may be traced.

**3rd Method (approximate).** With arcs of two radii, fig. 5. Lay down the axes AB and CD, and set off  $oa$  and  $oc$  equal to the difference of the lengths of the axes. Draw  $ac$  and set off half of  $ac$  to  $d$ , and  $oe$  equal to  $od$ . Draw  $di$ ,  $ei$ , and parallels intersecting at  $m$ . From the centres  $m$  and  $i$ , describe arcs through C and D; and from  $d$  and  $e$ , describe arcs through A and B. The four arcs form the ellipse.

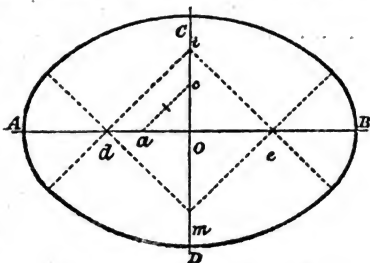


FIG. 5.—To describe an Ellipse.

*Note.* — This method is applicable when the conjugate axis is at least two-thirds of the transverse axis.

**4th Method (approximate).** With arcs of three radii, fig. 6.

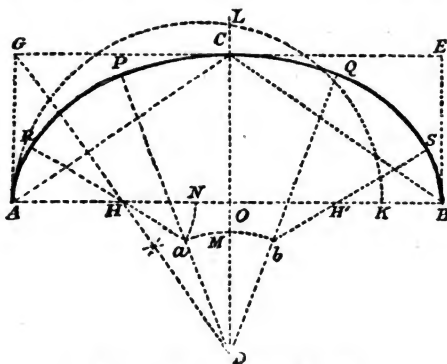


FIG. 6.—To describe an Ellipse.

On the transverse axis AB, draw the rectangle BG, on the height OC, of the semi-conjugate axis. To the diagonal AC draw the perpendicular GHD; set off OK equal to OC, and describe a semicircle on AK, and produce OC to L. Set off OM equal CL, and on D describe an arc with the radius DM. On A with radius OL, cut this arc at A. The five centres D,  $a$ ,  $b$ , H, H', are found, from which the arcs are described to form the ellipse.

*Note.*—This process works well for nearly all proportions of ellipses.

The parabola is a curve such that the distance of any point in the curve from a fixed point, the focus, is equal to its distance from a straight line, the directrix.

*To describe a Parabola*, when an absciss and its ordinate, or the height and the base, are given. Bisect the given ordinate  $BC$ , fig. 7, at  $a$ ; draw  $Aa$ , and then  $ab$  perpendicular to it, meeting the axis at  $b$ . Set off  $Ae$ ,  $AF$ , each equal to  $Bb$ , and draw  $KcL$  at right angles to the axis. Then  $KL$  is the directrix and  $F$  is the focus. Through  $F$  and any number of points  $o, o', \&c.$ , in the axis, draw double ordinates  $non, \&c.$ , and on the centre  $F$ , with the radii  $Fe, oe, \&c.$ , cut the respective ordinates

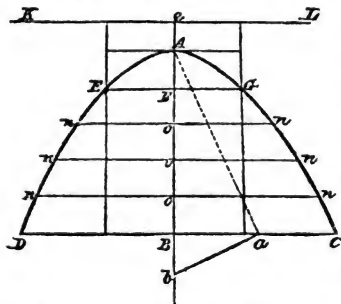


FIG. 7.—To describe a Parabola.

at  $E, G, n, n, \&c.$  The curve is traced through these points of intersection.

*2nd Method.* Place a straight-edge to the directrix  $EN$ , fig. 8, and apply to it a square  $LEG$ . Fasten to the end  $G$  one end of a thread or cord, shown in dot-lining, equal in length to the edge  $EG$ , and attach the other end to the focus  $F$ . Slide the square along the straight-edge, holding the cord taut against the edge of the square by a drawpoint or pencil  $D$ , by which the curve is described.

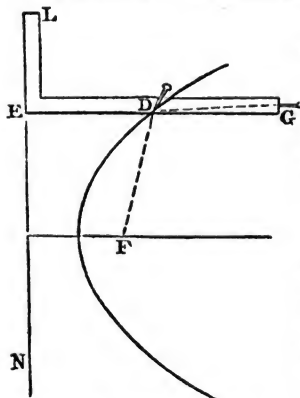


FIG. 8.—To describe a Parabola.

*3rd Method.* Through the vertex  $A$ , fig. 9, draw  $EF$  parallel to  $CD$  the base, and through  $c$  and  $D$  draw  $CE$  and  $DF$  parallel to the axis  $AB$ . Divide  $BC$  and  $BD$  into any number of equal parts, at  $a, b, \&c.$ , and divide  $CE$  and  $DF$  into the same number of equal parts.

Through the points  $a, b, c, d$ , in the base  $CD$ , draw perpendiculars, and through  $a, b, c, d$  in  $CE$  and  $DF$  draw lines to the vertex  $A$ , cutting the perpendiculars at  $e, f, g, h$ . These are points of the curve, which may be traced through them.

The nature of the parabola is such that the abscissæ vary in length as the squares of the ordinates. Inversely, the ordinates vary as the square roots of the abscissæ. By means of these

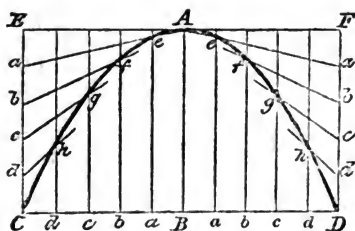


FIG. 9.—To describe a Parabola.

relations any number of points in the curve may be determined, and the curve constructed.

The hyperbola is a curve such that the difference of the distances of any point in the curve from two fixed points, the foci, is equal to a constant, the transverse axis. The vertices A, B, fig. 10, of opposite hyperbolas, are the heads of the

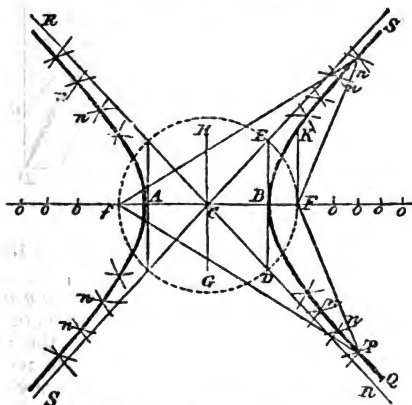


FIG. 10.—To describe a Hyperbola.

curves, in their axial lines. The transverse axis AB is the distance between the vertices. The conjugate axis GH passes through the centre C, at right angles to the transverse axis.

*To describe a Hyperbola.* Let the ends of two threads  $fPQ$ ,  $FPQ$ , fig. 10, be fastened at the points  $f$  and  $F$ , and passed through a small bead or pin  $P$ , and knotted together at  $Q$ . Take hold of  $Q$  and draw the threads taut; move the bead along the threads, and the point  $P$  will describe the curve.

*2nd Method.* When the base  $CD$ , height  $AB$ , and transverse axis  $AA'$ , fig. 11, are given. Divide the base  $CD$  into a number of equal parts on each side of the axis at  $a$ ,  $b$ , &c.; and divide the parallels  $CE$ ,  $DF$ , into the same number of equal parts at  $a$ ,  $b$ , &c. From the points  $a$ ,  $b$ , &c., in the base, draw lines to  $A'$ ; and from the points  $a$ ,  $b$ , &c., in the verticals, draw

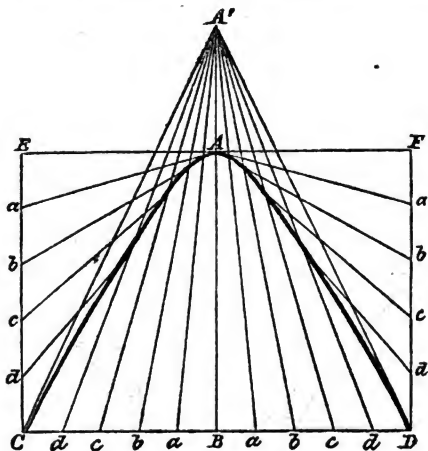


FIG. 11.—To describe a Hyperbola.

lines to  $A$ , cutting the respective lines from the base. Trace the curve through the intersections.

*To describe a Right-angled Hyperbola, given a point in the curve.* Let  $E$ , fig. 12, be a point in the curve, of which  $AB$  and  $AC$ , at right angles to each other, are the asymptotes. Draw the parallels  $DE$  and  $DC$  to complete the rectangle  $AE$ . Set off  $Dd$  on the base line equal to  $AD$ , and draw the vertical  $de$ . Bisect  $AC$  at  $b$ , and draw  $be$  parallel to the base; the point of intersection,  $e$ , is a point in the curve. Similarly, bisecting  $Ab$  at  $c$ , and  $Ac$  at  $n$ ; doubling  $Ad$  to  $d'$ , and  $Ad'$  to  $d''$ ; and completing the rectangles  $d'e'$  and  $d''e''$ ; and again bisecting and doubling; the points  $e'$  and  $e''$ , and  $e'''$  in the curve are found. By a like process of dividing and multiplying in-



versely, any additional number of points may be found, and the curve may be traced through the points.

This curve possesses the useful property that the elementary rectangles are equal in area.

The cycloid ADB, fig. 13, is the curved path described by

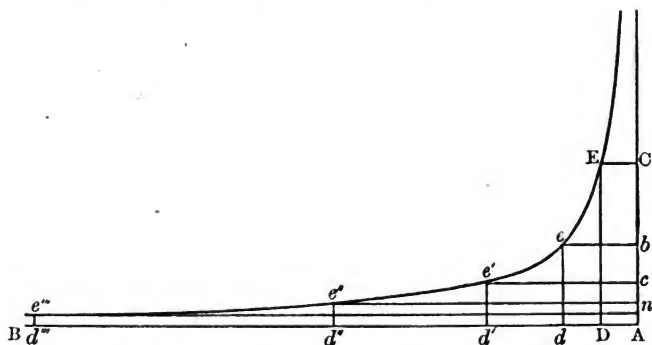


FIG. 12.—To describe a Right-Angled Hyperbola.

any point D in the circumference of a wheel or a circle DGC which rolls along a straight line. The base AB for a complete

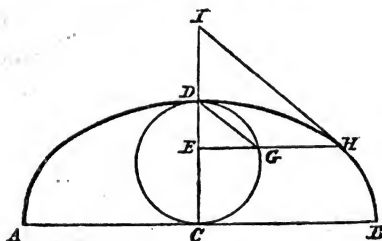


FIG. 13.—Cycloid.

revolution of the wheel, is equal in length to the circumference of the circle ; the length of the curve is equal to four times the diameter of the circle ; the area of the cycloid, ADBA, is equal to three times the area of the circle.

The exterior epicycloid ADB, fig. 14, is the curve described by any point in the circumference of one circle, DC, rolling over another circle, ACB, on the outside of the circumference.

The hypocycloid, or interior epicycloid, ADB, fig. 15, is the

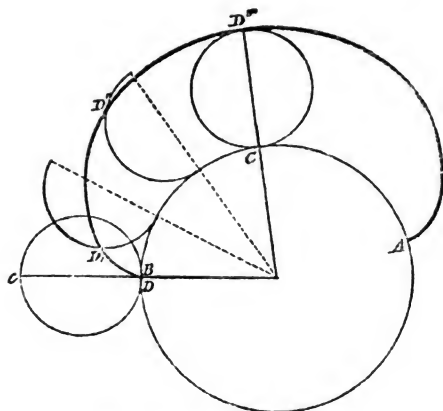


FIG. 14.—Exterior Epicycloid.

curve ADB described by a point in the circumference of a circle rolling on the inside of the circumference of another

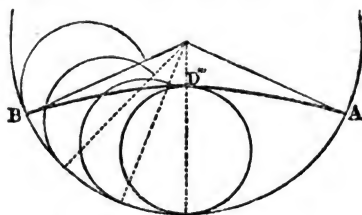


FIG. 15.—Interior Epicycloid.

circle. When the diameter of the rolling circle is equal to half the diameter of the fixed circle, the curve becomes a straight line, or a diameter of the fixed circle.

## WEIGHTS AND MEASURES.

THE yard and the pound are the units of English measure and weight.

The imperial standard yard is a solid square bar, 38 inches long, 1 inch square, of bronze or gun-metal, deposited in the Standards Department of the Board of Trade. The length of the yard is defined by lines inscribed on two gold plugs inserted near each end of the bar.

The imperial standard pound is a cylinder of platinum, nearly 1·35 inches in height, and 1·15 inches in diameter, having a groove or channel round it, near the top, by which it may be lifted.

Copies of the standard yard and the standard pound have been deposited in the Royal Mint and the Greenwich Observatory; copies have been immured in the New Palace at Westminster; and copies have been delivered to the Royal Society of London.

The unit or standard measure of capacity, for liquids as for dry goods, is the gallon, capable of containing ten imperial standard pounds weight of distilled water weighed in air against brass weights, at the temperature of 62° F., with the barometer at 30 inches. The standard measure is cylindrical, on a plane base, and the height is equal to the diameter.

The standard bushel, as a measure of capacity, is cylindrical, about 17·8 inches in diameter, with a plane base; the depth is half the diameter, about 8·9 inches. It has a capacity equal to 8 gallons.

In using an imperial measure of capacity, it is not to be heaped; but is either to be stricken with a round stick or cylindrical roller; or, if the article cannot be conveniently stricken, it is to be filled in all parts as nearly to the level of the brim as the size and shape of the article admits.

### LIST OF GAUGES DEPOSITED AT THE STANDARDS OFFICE BY SIR JOSEPH WHITWORTH.

1 set, External plane gauges, containing 91 sizes, from ·01 to 0·1, rising by ·001 inch.

6 sets, Internal and External Cylindrical gauges, containing the following fractional sizes:—

1 set containing 15 gauges from $\frac{1}{8}$ inch to 1 inch, increasing by $\frac{1}{16}$ inch.		
1 „ „ 8 „ „ $1\frac{1}{8}$ inches to 2 inches, increasing by $\frac{1}{8}$ inch.		

1 set containing 8 gauges from $2\frac{1}{8}$ inches to 3 inches, increasing by $\frac{1}{8}$ inch.
1    "            "       8    "        " $3\frac{1}{8}$ inches to 4 inches, increasing by $\frac{1}{8}$ inch.
1    "            "       4    "        " $4\frac{1}{4}$ inches to 5 inches, increasing by $\frac{1}{4}$ inch.
1    "            "       4    "        " $5\frac{1}{4}$ inches to 6 inches, increasing by $\frac{1}{4}$ inch.

6 sets, containing the following decimal sizes :—

1 set containing 15 gauges, sizes, 0·10, 0·15, 0·2, 0·3, 0·35, 0·4, 0·45, 0·55, 0·60, 0·65, 0·7, 0·8, 0·85, 0·9, 0·95 inch.
1    "            "       8    "        "    1·1, 1·2, 1·3, 1·4, 1·6, 1·7, 1·8, 1·9 inches.
1    "            "       8    "        "    2·1, 2·2, 2·3, 2·4, 2·6, 2·7, 2·8, 2·9 inches.
1    "            "       8    "        "    3·1, 3·2, 3·3, 3·4, 3·6, 3·7, 3·8, 3·9 inches.
1    "            "       4    "        "    4·2, 4·4, 4·6, 4·8 inches.
1    "            "       4    "        "    5·2, 5·4, 5·6, 5·8 inches.

From 6 inches to 2 inches inclusive, the gauges are made of cast iron ; and below 2 inches they are made of steel.

The above collection of gauges is denominated as follows:—

- (1.) Whitworth's External Cylindrical Gauges : external diameters in terms of the inch.
  - 15 gauges from  $\frac{1}{8}$  inch to 1 inch, increasing by sixteenths of an inch.
  - 24 gauges from  $1\frac{1}{8}$  inches to 4 inches, increasing by eighths of an inch.
  - 8 gauges from  $4\frac{1}{4}$  inches to 6 inches, increasing by quarters of an inch.
  - 19 gauges from 0·1 inch to 1 inch, increasing by five one-hundredths of an inch.
  - 30 gauges from 1·1 inches to 4 inches, increasing by tenths of an inch.
  - 10 gauges from 4·2 inches to 6 inches, increasing by fifths of an inch.
- (2.) Whitworth's Internal Cylindrical Gauges : internal diameters in terms of the inch : a repetition of section (1) preceding.
- (3.) Whitworth's External Plane Gauges : thickness in terms of the inch.
  - 91 gauges from 0·01 inch to 0·1 inch, increasing by thousandths of an inch.

TABLE 15.—ENGLISH MEASURES OF LENGTH.

French Equivalents.

12 lines	{	1 inch	25·4 millimetres.
72 points			
1000 mils	{	1 link	·2012 metre.
7·92 inches			
12 inches	{	1 foot	·3048 metre.
3 feet			
6 feet	{	1 yard	·91439 "
5½ yards			
100 links	{	1 fathom	1·82878 "
66 feet			
220 yards	{	1 rod, pole, or perch	5·02915 "
40 poles			
10 chains	{	1 chain	20·1166 "
8 furlongs			
80 chains	{	1 furlong	{ 201·1662 metres.
1,760 yards			
5,280 feet	{	1 mile	{ 0·20117 kilometre.
1·1515 miles			
6080 feet	{	1 Admiralty knot or nautical mile	{ 1609·3296 metres. 1·60933 kilometres.
	{	1 mile	{ 1·85315 kilometres.

English Measures of Surface.

TABLE 16.—ORDINARY SUPERFICIAL MEASUREMENT.

1 square inch	{	645·15 square millimetres. 6·4515 square centimetres.
144 square inches		
183·35 circular inches	{	1 square foot
9 square feet		
100 square feet (for roofing and flooring)	{	·0929 square metre. ·8361 square metre.
30¼ square yards		
40 square poles	{	1 square
4 roods		
4840 square yards	{	9·2901 square metres.
640 acres		
	{	1 square pole, rod, or perch
	{	1 rood
	{	1 acre*
	{	1 square mile

The side of a square acre is equal to 69·57 lineal yards.

**English Measures of Volume and Capacity.****TABLE 17.—SOLID OR CUBIC MEASURE.**

1 cubic inch	.	.	.	.	16·387 cubic centimetres.
1728 cubic inches	}	1 cubic foot	{	28·3153 cubic deci-	
2200·15 cylindrical inches				metres.	
3300·23 spherical inches				·028315 cubic metre.	
6600·45 conical inches					
27 cubic feet	.	1 cubic yard	.	.	·764513 cubic metre.
1·308 cubic yard	}				1 cubic metre.
31·3156 cubic feet					

**TABLE 18.—DRY MEASURE.**

	1 pint . . . . .	·5679 litre.
2 pints . . . . .	1 quart . . . . .	1·1359 litres.
4 quarts (277·274 cubic inches)	1 gallon . . . . .	4·5435 litres.
2 gallons . . . . .	1 peck . . . . .	9·0869 litres.
4 pecks (1·28366 cubic feet)	1 bushel . . . . .	36·3477 litres.
8 bushels . . . . .	1 quarter . . . . .	290·782 litres.
4 quarters (41·077 cubic feet)	1 chaldron . . . . .	{ 1·1631 cubic
		metres.
5 quarters . . . . .	1 load, or way . . . . .	{ 1·4539 cubic
		metres.
2 loads . . . . .	1 last . . . . .	{ 2·9078 cubic
		metres.

**Builders' Measurement.****TABLE 19.—LINEAL MEASURE.**

12 inches . . . . .	1 foot.
3 feet . . . . .	1 yard.
16½ feet . . . . .	1 rod.

The rod of 16½ feet lineal is used for measuring park-fencing.

Rubble-walling, in some parts of England, is measured by the rod of 16½ feet, by 1 foot high; and the various thicknesses are stated.

**TABLE 20.—SUPERFICIAL MEASURE.**

1 part . . . . .	1 square inch.
12 parts . . . . .	1 inch (12 square inches).
12 inches . . . . .	1 foot.
9 feet . . . . .	1 yard.
100 feet . . . . .	1 square.
272½ feet . . . . .	1 rod.

Brickwork generally is measured by the rod of 272 feet superficial (not 272½ feet) reduced to 1½ bricks in thickness.

But, for engineering works, it is measured by the cubic yard of 27 cubic feet.

Flooring, slating, and tiling, are measured by the square.

Paving, painting, plastering, &c., are measured by the yard.

TABLE 21.—CUBIC MEASURE.

1 third . . . . .	1 cubic inch.
12 thirds . . . . .	1 part (12 cubic inches).
12 parts . . . . .	1 inch (144 cubic inches).
12 inches . . . . .	1 foot (1728 cubic inches).
27 feet . . . . .	1 yard.

Excavation, concrete, &c., are measured by the cubic yard.

Masonry, square-sided timber, &c., are measured by the cubic foot.

### Timber.

The inscribed square in the section of a round tree gives the maximum of sectional area, but not the maximum of transverse strength. To find the strongest section, draw a diameter  $a b$ ; from the centre  $o$  set off  $o c$ , one-third of the radius  $o b$ , and draw the perpendicular  $c d$ . Draw  $d b$  and  $d a$ , and complete the parallelogram. The area of the parallelogram is 6 per cent. less than that of the square section; but it is 9 per cent. stronger.

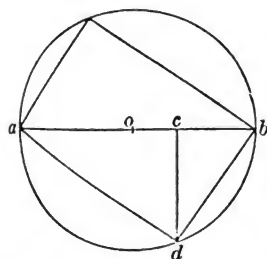


FIG. 16.—To find Strongest Section of Round Tree.

TABLE 22.—LIQUID MEASURE.

8·665 cubic inches . . . . .	1 gill or quarten . . . . .	·1420 litre.
4 gills . . . . .	1 pint . . . . .	·5679 litre.
2 pints . . . . .	1 quart . . . . .	1·1359 litres.
4 pints . . . . .	1 pottle . . . . .	2·2718 litres.
8 pints { (277·274 cubic inches) }	1 gallon . . . . .	4·5435 litres.
4 quarts { }		
6·2355 gallons . . . . .	1 cubic foot.	
168·3765 gallons . . . . .	1 cubic yard.	
220·09 gallons . . . . .		1 cubic metre.

TABLE 23.—OLD WINE AND SPIRIT MEASURE.

4 gills or quarterns . . . . .	1 pint.	
2 pints . . . . .	1 quart.	
4 quarts (231·06 cubic inches) 1 gallon	=	·8333, or $\frac{5}{6}$ .

Imperial Gallons.

		Imperial gallons.
31½ gallons	1 barrel	= 26·25.
63 gallons } 2 barrels }	1 hogshead	= 52·5.
84 gallons	1 puncheon	= 70.
126 gallons	1 pipe or butt	= 105.
2 pipes	1 tun	= 210.

Wines, spirits, oils, &c., are measured by this scale ; but the contents of casks are reckoned in imperial gallons when sold.

TABLE 24.—APOTHECARIES' FLUID MEASURE (ENGLISH).

60 minims (m)	1 fluid drachm (f 3).
8 drachms (water 1·732 cubic inches, 437½ grains)	1 fluid ounce (f 3).
20 ounces	1 pint (o).
80 pints (water, 70,000 grains)	1 gallon (gall.)
4 drachms	1 tablespoonful.
2 ounces (water, 875 grains)	1 wineglassful.
3 ounces	1 teacupful.

TABLE 25.—AVOIRDUPOIS WEIGHT.

1 grain .	.	.	.	·0648 gramme.
27·344 grains .	1 drachm .	.	.	1·7718 grammes.
16 drachms } 437½ grains }	1 ounce .	.	.	28·3495 grammes.
16 ounces } 7000 grains }	1 pound .	.	{	453·5926 grammes. 453·59 kilogrammes.
14 pounds .	1 stone .	.	.	6·3503 kilogrammes.
28 pounds .	1 quarter .	.	.	12·7006 kilogrammes.
4 quarters } 112 pounds }	1 hundredweight	.	.	50·8024 kilogrammes.
20 hundredweights } 2240 pounds }	1 ton .	.	{	1016·048 kilogrammes. 1·01605 metric ton.

TABLE 26.—TROY WEIGHT.

24 grains	1 pennyweight	1·5552 grammes.
20 pennyweights } 480 grains }	1 troy ounce	31·1035 grammes.
12 troy ounces } 5760 grains }	1 troy pound	{ 373·2419 grammes. 373·24 kilogramme.
25 pounds	1 troy quarter	9·3310 kilogrammes.
4 quarters } 100 pounds }	1 troy hundredweight	37·3242 kilogrammes.



TABLE 27.—COAL WEIGHT (ENGLISH).

14 pounds	1 stone	6·3503 kilogrammes.
88 pounds	1 bushel	
1 sack of 112 pounds	1 hundredweight	50·8024 kilogrammes.
20 hundredweights	1 ton	1·01605 metric ton.
26½ hundredweights	{ 1 chaldron (London) }	1·3462 metric ton.
53 hundredweights	{ 1 chaldron (Newcastle) }	2·6924 metric tons.

*Sundry bushels of coal.*—Cornish, 90 or 94 pounds; heaped, 101 pounds; Welsh, 93 pounds; Newcastle, 80 or 84 pounds; London, 80 or 84 pounds.

The “colliery ton” is 21 cwt. of 120 lbs. each.

TABLE 28.—HAY AND STRAW WEIGHT (ENGLISH).

1 truss of straw	36 pounds.
1 load of straw	11 hundredweights, 64 pounds.
1 truss of old hay	56 pounds.
1 load of old hay	18 hundredweights.
1 truss of new hay	60 pounds.
1 load of new hay	19 hundredweights, 32 pounds.
1 cubic yard of compact old hay.	15 stones.

Loose hay, 5 pounds per cubic foot; ordinarily pressed, as in a stack, 8 pounds; close pressed, as in a bale, 12 to 14 pounds; ordinarily pressed, as in a waggon-load, from 450 to 500 cubic feet weigh 1 ton.—*Haswell.*

TABLE 29.—CORN AND FLOUR WEIGHT (ENGLISH).

1 peck, or stone, of flour	14 pounds
10 pecks	1 boll 140 ”
2 bolls.	1 sack 280 ”
14 pecks	1 barrel 196 ”
1 bushel of wheat.	60 ”
1 bushel of barley	47 ”
1 bushel of oats	40 ”
80 bushels of corn	1 last.

Six bushels of wheat should yield one sack of flour.

TABLE 30.—TIMBER MEASURES FOR BUILDING PURPOSES (ENGLISH).

Load of timber, unhewn or rough	40 cubic feet.
Load, hewn or squared	{ 50 cubic feet, reckoned to weigh 20 cwt.

Stack of wood . . . . .	108 cubic feet.
Cord of wood . . . . .	128 "
(In dockyards, 40 cubic feet of hewn timber are reckoned to weigh 20 cwt.; 50 cubic feet is a load.)	
100 superficial feet of boarding or flooring . . . . .	1 square.
Hundred of deals . . . . .	120 deals.
Load of 1-inch plank . . . . .	600 square feet.
Load of $1\frac{1}{2}$ -inch plank . . . . .	400 "
Load of 2-inch . . . . .	300 "
Load of $2\frac{1}{2}$ -inch . . . . .	240 "
Load of 3-inch . . . . .	200 "
Load of $3\frac{1}{2}$ -inch . . . . .	170 "
Load of 4-inch . . . . .	150 "
Planks, section . . . . .	11 by 3 inches.
Deals, section . . . . .	9 by 3 "
Battens, section . . . . .	7 by $2\frac{1}{2}$ "
A reduced deal is $1\frac{1}{2}$ inches thick, 11 inches wide, and 12 feet long.	
Bundle of 4 feet oak-heart laths . . . . .	120 laths.
Load of " " " " " " . . . . .	$37\frac{1}{2}$ bundles.
Bundle of 5 feet oak-heart laths . . . . .	100 laths.
Load of " " " " " " . . . . .	30 bundles.

*Sundry Building Materials.*

Load of statute bricks . . . . .	500.
Load of plain tiles . . . . .	1000.
Load of lime . . . . .	32 bushels.
Load of sand . . . . .	36 "
Hundred of lime . . . . .	35 "
Hundred of nails, or tacks . . . . .	120.
Thousand of nails, or tacks . . . . .	1200.
Fodder of lead . . . . .	$19\frac{1}{2}$ cwt.
Sheet lead . . . . .	{ 6 to 10 pounds per sq. ft.
Hundred of lead . . . . .	112 pounds.
Table of glass . . . . .	5 feet.
Case of glass . . . . .	45 tables.
Case of glass . . . . .	{ (Newcastle and Normandy glass, 25 tables.)
Stone of glass . . . . .	5 pounds.
Seam of glass . . . . .	24 stone.

TABLE 31.—ENGLISH BRICKWORK MEASURES (Mackrow).

	ins.	ins.	ins.	Weight.
London stock bricks . . . . .	$8\frac{3}{4}$	$4\frac{1}{4}$	$2\frac{3}{4}$	6.81 lbs.
Red kiln . . . . .	$8\frac{3}{4}$	$4\frac{1}{4}$	$2\frac{3}{4}$	7.00 "
Welsh fire . . . . .	9	$4\frac{1}{2}$	$2\frac{3}{4}$	7.84 "

	ins.	ins.	ins.	Weight.
Paving . . . . .	9	$4\frac{1}{2}$	$1\frac{3}{4}$	5·00 lbs.
Square tiles . . . . .	$9\frac{3}{4}$	$9\frac{3}{4}$	1	5·70 "
do. . . . .	6	6	1	2·16 "

A rod of brickwork is,—

$16\frac{1}{2}$  feet  $\times$   $16\frac{1}{2}$  feet  $\times$   $1\frac{1}{2}$  bricks thick ;  
 306 cubic feet, or  $11\frac{1}{2}$  cubic yards ;  
 272 superficial feet  $1\frac{1}{2}$  bricks thick ;  
 4352 stock bricks, 4 courses 1 foot high.

Bricks absorb about  $\frac{1}{10}$ th of their weight of water.

A rod of brick-work requires about 3 cubic yards of mortar, or  $1\frac{1}{2}$  cubic yards of chalk lime and 3 loads of sand, or 1 cubic yard of stone lime and  $3\frac{1}{2}$  loads of sand, or 36 bushels of cement and an equal quantity of sand.

A load of mortar or of sand is 1 cubic yard.

A bag of cement is 3 bushels.

A sack of cement is 5 bushels.

A load of mortar requires about 9 bushels of lime and 1 cubic yard or load of sand.

One load of bricks, 500 bricks.

330 stock bricks weigh 1 ton.

1000 bricks loosely stacked occupy about 72 cubic feet (14 bricks per cubic foot).

1000 bricks closely stacked occupy about 56 cubic feet (18 bricks per cubic foot).

Mortar is composed of 1 part of lime to 3 or  $3\frac{1}{2}$  parts of sharp-sand.

Concrete is composed of 1 part of lime, 4 parts of gravel, and 2 parts of sand.

Cement is composed of 1 part of Portland cement to 3 parts of sand. Or cement alone may be used.

TABLE 32.—TONNAGE OF SHIPS (ENGLISH).

1 ton, displacement of a ship . . . . .	35 cubic feet.
1 ton, freight by measurement . . . . .	40 "
1 ton, registered internal capacity of a ship . . . . .	100 "
1 ton, shipbuilders' old measurement . . . . .	94 "

### Wire-Gauges.

The oldest and best-known Birmingham Wire-Gauge is that of which the numbers were carefully measured by Mr. Holtzapffel, and published by him in 1847. He gives 40 measurements ranging from  $\cdot 454$  inch to  $\cdot 004$  inch, as recorded in Table 33. It was accepted by the Standards Depart-

ment of the Board of Trade. Although there are only 40 marks in the table, there were 60 different sizes of wire made, for which intermediate sizes were added to the gauge.

TABLE 33.—BIRMINGHAM WIRE-GAUGE.

(Stubs.)

Mark.	Size.	Mark.	Size.	Mark.	Size.	Mark.	Size.
No.	Inch.	No.	Inch.	No.	Inch.	No.	Inch.
4/0	·454	7	·180	17	·058	27	·016
3/0	·425	8	·165	18	·049	28	·014
2/0	·380	9	·148	19	·042	29	·013
0	·340	10	·134	20	·035	30	·012
1	·300	11	·120	21	·032	31	·010
2	·284	12	·109	22	·028	32	·009
3	·259	13	·095	23	·025	33	·008
4	·238	14	·083	24	·022	34	·007
5	·220	15	·072	25	·020	35	·005
6	·203	16	·065	26	·018	36	·004

The wire-gauge that has been in common use by the sheet-rollers of South Staffordshire, ranges from  $\frac{5}{16}$  inch to  $\frac{1}{80}$  inch in thickness, according to the following Table :—

TABLE 34.—BIRMINGHAM WIRE-GAUGE.

*For Iron Sheets chiefly.*

No.	Size.	No.	Size.	No.	Size.	No.	Size.
	Inch.		Inch.		Inch.		Inch.
1	·3125 ( $\frac{5}{16}$ )	9	·15625	17	·05625	25	·02344
2	·28125	10	·140625	18	·05 ( $\frac{1}{20}$ )	26	·021875
3	·25 ( $\frac{1}{4}$ )	11	·125 ( $\frac{1}{8}$ )	19	·04375	27	·020312
4	·234375	12	·1125	20	·0375	28	·01875
5	·21875	13	·10 ( $\frac{1}{10}$ )	21	·034375	29	·01719
6	·203125	14	·0875	22	·03125 ( $\frac{1}{32}$ )	30	·015625
7	·1875 ( $\frac{3}{16}$ )	15	·075	23	·028125	31	·01406
8	·171875	16	·0625 ( $\frac{1}{16}$ )	24	·025 ( $\frac{1}{40}$ )	32	·0125 ( $\frac{1}{80}$ )

Sir Joseph Whitworth, in 1857, promulgated his Standard Wire-Gauge, ranging from half an inch to one-thousandth of an inch, and comprising 62 measurements, given in Table 35. The sizes are designated or marked by their respective values. The Whitworth gauge has been in general use.

TABLE 35.—WHITWORTH WIRE-GAUGE, 1857.

Mark.	Size.	Mark.	Size.	Mark.	Size.	Mark.	Size.
No.	Inch.	No.	Inch.	No.	Inch.	No.	Inch.
1	·001	17	·017	55	·055	200	·200
2	·002	18	·018	60	·060	220	·220
3	·003	19	·019	65	·065	240	·240
4	·004	20	·020	70	·070	260	·260
5	·005	22	·022	75	·075	280	·280
6	·006	24	·024	80	·080	300	·300
7	·007	26	·026	85	·085	325	·325
8	·008	28	·028	90	·090	350	·350
9	·009	30	·030	95	·095	375	·375
10	·010	32	·032	100	·100	400	·400
11	·011	34	·034	110	·110	425	·425
12	·012	36	·036	120	·120	450	·450
13	·013	38	·038	135	·135	475	·475
14	·014	40	·040	150	·150	500	·500
15	·015	45	·045	165	·165		
16	·016	50	·050	180	·180		

TABLE 36.—IMPERIAL STANDARD WIRE-GAUGE.

Descriptive Number.	Equivalents in Parts of an Inch.	Metric Equivalents.	Sectional Area of Wire.	
No.	Inch.	Millimetres.	Square Inch.	Square Millimetres.
7/0	·500	12·700	·1963	126·67
6/0	·464	11·785	·1691	109·09
5/0	·432	10·973	·1466	94·56
4/0	·400	10·160	·1257	81·07
3/0	·372	9·449	·1087	70·12
2/0	·348	8·839	·0951	61·36
0	·324	8·229	·0824	53·19
1	·300	7·620	·0707	45·60
2	·276	7·010	·0598	38·58
3	·252	6·401	·0499	32·18
4	·232	5·893	·0423	27·27
5	·212	5·385	·0353	22·77
6	·192	4·877	·0289	18·68
7	·176	4·470	·0243	15·70
8	·160	4·064	·0201	12·97
9	·144	3·658	·0163	10·51

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TABLE 36.—IMPERIAL STANDARD WIRE-GAUGE (*continued*).

Descriptive Number.	Equivalents in Parts of an Inch.	Metric Equivalents.	Sectional Area of Wire.	
			Square Inch.	Square Millimetres.
No.	Inch.	Millimetres.		
10	·128	3·251	·0129	8·30
11	·116	2·946	·0106	6·82
12	·104	2·642	·00849	5·48
13	·092	2·337	·00665	4·29
14	·080	2·032	·00503	3·24
15	·072	1·829	·00407	2·63
16	·064	1·626	·00322	2·07
17	·056	1·422	·00246	1·59
18	·048	1·219	·00181	1·17
19	·040	1·016	·00126	·811
20	·036	·914	·00102	·657
21	·032	·813	·000804	·519
22	·028	·711	·000616	·397
23	·024	·610	·000452	·292
24	·022	·559	·000380	·245
25	·020	·508	·000314	·203
26	·018	·457	·000254	·164
27	·0164	·4166	·000211	·136
28	·0148	·3759	·000173	·111
29	·0136	·3454	·000145	·0937
30	·0124	·3150	·000121	·0779
31	·0116	·2946	·000106	·0682
32	·0108	·2743	·0000916	·0591
33	·0100	·2540	·0000785	·0507
34	·0092	·2337	·0000665	·0429
35	·0084	·2134	·0000554	·0357
36	·0076	·1930	·0000454	·0293
37	·0068	·1727	·0000363	·0234
38	·0060	·1524	·0000283	·0182
39	·0052	·1321	·0000212	·0137
40	·0048	·1219	·0000181	·0117
41	·0044	·1118	·0000152	·00982
42	·0040	·1016	·0000126	·00811
43	·0036	·0914	·0000102	·00656
44	·0032	·0813	·00000804	·00519
45	·0028	·0711	·00000616	·00397
46	·0024	·0610	·00000452	·00292
47	·0020	·0508	·00000314	·00203
48	·0016	·0406	·00000201	·00129
49	·0012	·0305	·00000113	·00073
50	·0010	·0254	·000000785	·00051

TABLE 37.—WARRINGTON WIRE GAUGE.  
(Rylands Brothers.)  
(Rarely used now.)

Mark.	Size.	Mark.	Size.	Mark.	Size.
No.	Inch.	No.	Inch.	No.	Inch.
7/0	$\frac{1}{32}$	4	·229	13	·090
6/0	$\frac{1}{32}$	5	·209	14	·079
5/0	$\frac{1}{16}$	6	·191	15	·069
4/0	$\frac{1}{16}$	7	·174	16	·0625 or $\frac{1}{16}$
3/0	$\frac{1}{8}$	8	·159	17	·053
2/0	$\frac{1}{8}$	9	·146	18	·047
0	·326	10	·135	19	·041
1	·300	10½	·125 or $\frac{1}{8}$	20	·036
2	·274	11	·117	21	·0315 or $\frac{1}{32}$
3	·250 or $\frac{1}{4}$	12	·100 or $\frac{1}{10}$	22	·028

TABLE 38.—HOLTZAPFFEL'S LANCASHIRE GAUGE.  
(For Round Steel Wire and Pinion Wire.)

Mark.	Size.	Mark.	Size.	Mark.	Size.	Mark.	Size.	Mark.	Size.
No.	Inch.	No.	Inch.	No.	Inch.	No.	Inch.	No.	Inch.
80	·013	57	·042	34	·109	11	·189	M	·295
79	·014	56	·044	33	·111	10	·190	N	·302
78	·015	55	·050	32	·115	9	·191	O	·316
77	·016	54	·055	31	·118	8	·192	P	·323
76	·018	53	·058	30	·125	7	·195	Q	·332
75	·019	52	·060	29	·134	6	·198	R	·339
74	·022	51	·064	28	·138	5	·201	S	·348
73	·023	50	·067	27	·141	4	·204	T	·358
72	·024	49	·070	26	·143	3	·209	U	·368
71	·026	48	·073	25	·146	2	·219	V	·377
70	·027	47	·076	24	·148	1	·227	W	·386
69	·029	46	·078	23	·150	A	·234	X	·397
68	·030	45	·080	22	·152	B	·238	Y	·404
67	·031	44	·084	21	·157	C	·242	Z	·413
66	·032	43	·086	20	·160	D	·246	A1	·420
65	·033	42	·091	19	·164	E	·250	B1	·431
64	·034	41	·095	18	·167	F	·257	C1	·443
63	·035	40	·096	17	·169	G	·261	D1	·452
62	·036	39	·098	16	·174	H	·266	E1	·462
61	·038	38	·100	15	·175	I	·272	F1	·475
60	·039	37	·102	14	·177	Kj	·277	G1	·484
59	·040	36	·105	13	·180	K	·281	HL	·494
58	·041	35	·107	12	·185	L	·290		

The Imperial Standard Wire-Gauge was legally established March 1, 1884. It is given in Table 36.

The Warrington Wire-Gauge, formerly practised by Rylands Brothers, is given in Table 37. It is rarely used now.

The Lancashire Gauge, Table 38, arranged by Holtzapffel, is employed for the manufacture of bright steel wire in Lancashire, and steel pinion-wire used in clocks and watches. The larger sizes, distinguished by letters, form the *Letter-Gauge*.

There are also the Needle-gauge, for needle-wire, and the Music Wire-gauge, for the strings of pianofortes.

TABLE 39.—ADMIRALTY KNOTS AND STATUTE MILES.

Knots.	Miles.	Knots.	Miles.	Knots.	Miles.	Knots.	Miles.
10	1152	50	63333	25	141061	18	215909
20	2303	55	66212	50	143939	19	218788
30	3455	60	69091	75	146818	22	221667
40	4606	65	71970	100	149697	25	224545
50	5758	70	74848	125	152576	28	227424
60	6909	75	77727	150	155455	30	230303
70	8061	80	80606	175	158333	32	233182
80	9212	85	83485	200	161212	35	236061
90	10363	90	86364	225	164091	38	238940
100	11515	95	89242	250	166970	40	241818
125	14394	100	92121	275	169848	42	244697
150	17273	105	95000	300	172727	45	247576
175	20152	110	97879	325	175606	48	250455
200	23030	115	100758	350	178485	50	253333
225	25909	120	103636	375	181364	52	256212
250	28788	125	106515	400	184242	55	259091
275	31667	130	109394	425	187121	58	261970
300	34546	135	112273	450	190000	60	264848
325	37424	140	115152	475	192879	62	267727
350	40303	145	118030	500	195758	65	270606
375	43182	150	120909	525	198636	68	273485
400	46061	155	123788	550	201515	70	276364
425	48939	160	126667	575	204394	72	279242
450	51818	165	129545	600	207273	75	282121
475	54697	170	132424	625	210152	78	284999
500	57576	175	135303	650	213030	80	287878
525	60455	180	138182				



TABLE 40.—VULGAR FRACTIONS OF A LINEAL INCH IN DECIMAL FRACTIONS.

*Advancing by Eighths.*

Eighths.	Fractions.	Decimals of an Inch.	Eighths.	Fractions.	Decimals of an Inch.
1	$\frac{1}{8}$	·125	5	$\frac{5}{8}$	·625
2	$\frac{1}{4}$	·25	6	$\frac{3}{4}$	·75
3	$\frac{3}{8}$	·375	7	$\frac{7}{8}$	·875
4	$\frac{1}{2}$	·5	8	1	1·0

*Advancing by Twelfths.*

Twelfths.	Fractions.	Decimals of an Inch.	Twelfths.	Fractions.	Decimals of an Inch.
1	$\frac{1}{12}$	·0833	7	$\frac{7}{12}$	·5833
2	$\frac{1}{6}$	·1666	8	$\frac{2}{3}$	·6666
3	$\frac{1}{4}$	·25	9	$\frac{3}{4}$	·75
4	$\frac{1}{3}$	·3333	10	$\frac{5}{6}$	·8333
5	$\frac{5}{12}$	·4166	11	$\frac{11}{12}$	·9166
6	$\frac{1}{2}$	·5	12	1	1·0

*Advancing by Sixteenths.*

Six- teenths.	Fractions.	Decimals of an Inch.	Six- teenths.	Fractions.	Decimals of an Inch.
1	$\frac{1}{16}$	·0625	9	$\frac{9}{16}$	·5625
2	$\frac{1}{8}$	·125	10	$\frac{5}{8}$	·625
3	$\frac{3}{16}$	·1875	11	$\frac{11}{16}$	·6875
4	$\frac{1}{4}$	·25	12	$\frac{3}{4}$	·75
5	$\frac{5}{16}$	·3125	13	$\frac{13}{16}$	·8125
6	$\frac{3}{8}$	·375	14	$\frac{7}{8}$	·875
7	$\frac{7}{16}$	·4375	15	$\frac{15}{16}$	·9375
8	$\frac{1}{2}$	·5	16	1	1·0

TABLE 40.—VULGAR FRACTIONS OF A LINEAL INCH IN DECIMAL FRACTIONS (*continued*).*Advancing by Thirty-seconds.*

Thirty-seconds.	Fractions.	Decimals of an Inch.	Thirty-seconds.	Fractions.	Decimals of an Inch.
1	$\frac{1}{32}$	·03125	17	$\frac{17}{32}$	·53125
2	$\frac{1}{16}$	·0625	18	$\frac{9}{16}$	·5625
3	$\frac{3}{32}$	·09375	19	$\frac{19}{32}$	·59375
4	$\frac{1}{8}$	·125	20	$\frac{5}{8}$	·625
5	$\frac{5}{32}$	·15625	21	$\frac{21}{32}$	·65625
6	$\frac{3}{16}$	·1875	22	$\frac{11}{16}$	·6875
7	$\frac{7}{32}$	·21875	23	$\frac{23}{32}$	·71875
8	$\frac{1}{4}$	·25	24	$\frac{3}{4}$	·75
9	$\frac{9}{32}$	·28125	25	$\frac{25}{32}$	·78125
10	$\frac{5}{16}$	·3125	26	$\frac{13}{16}$	·8125
11	$\frac{11}{32}$	·34375	27	$\frac{27}{32}$	·84375
12	$\frac{3}{8}$	·375	28	$\frac{7}{8}$	·875
13	$\frac{13}{32}$	·40625	29	$\frac{29}{32}$	·90625
14	$\frac{7}{16}$	·4375	30	$\frac{15}{16}$	·9375
15	$\frac{15}{32}$	·46875	31	$\frac{31}{32}$	·96875
16	$\frac{1}{2}$	·5	32	1	1·0

*Advancing by odd Sixty-fourths.*

Sixty-fourths.		Decimals of an Inch.	Sixty-fourths.		Decimals of an Inch.
1		·015625	35		·546875
3		·031250	37		·578125
5		·078125	39		·609375
7		·109375	41		·640625
9		·140625	43		·671875
11		·171875	45		·703125
13		·203125	47		·734375
15		·234375	49		·765625
17		·265625	51		·796875
19		·296875	53		·828125
21		·328125	55		·859375
23		·359375	57		·890625
25		·390625	59		·921875
27		·421875	61		·953125
29		·453125	63		·984375
31		·484375	64		1·0
33		·515625			

TABLE 41.—LINEAL INCHES IN DECIMAL FRACTIONS OF A LINEAL FOOT.

Lineal Inches.	Lineal Foot.	Lineal Inches.	Lineal Foot.	Lineal Inches.	Lineal Foot.
$\frac{1}{64}$	·001302083	$1\frac{1}{8}$	·15625	$6\frac{1}{2}$	·5416
$\frac{1}{32}$	·00260416	2	·1666	$6\frac{3}{4}$	·5625
$\frac{1}{16}$	·0052083	$2\frac{1}{8}$	·177083	7	·5833
$\frac{1}{8}$	·010416	$2\frac{1}{4}$	·1875	$7\frac{1}{4}$	·60416
$\frac{3}{16}$	·015625	$2\frac{3}{8}$	·197916	$7\frac{1}{2}$	·625
$\frac{1}{4}$	·02083	$2\frac{1}{2}$	·2083	$7\frac{3}{4}$	·64583
$\frac{5}{16}$	·0260416	$2\frac{5}{8}$	·21875	8	·6666
$\frac{3}{8}$	·03125	$2\frac{3}{4}$	·22916	$8\frac{1}{4}$	·6875
$\frac{7}{16}$	·0364583	$2\frac{7}{8}$	·239583	$8\frac{1}{2}$	·7083
$\frac{1}{2}$	·0416	3	·25	$8\frac{3}{4}$	·72916
$\frac{9}{16}$	·046875	$3\frac{1}{4}$	·27083	9	·75
$\frac{5}{8}$	·052083	$3\frac{1}{2}$	·2916	$9\frac{1}{4}$	·77083
$\frac{11}{16}$	·0572916	$3\frac{3}{4}$	·3125	$9\frac{1}{2}$	·7916
$\frac{3}{4}$	·0625	4	·3333	$9\frac{3}{4}$	·8125
$\frac{13}{16}$	·0677083	$4\frac{1}{4}$	·35416	10	·8333
$\frac{7}{8}$	·072916	$4\frac{1}{2}$	·375	$10\frac{1}{4}$	·85416
$\frac{15}{16}$	·078125	$4\frac{3}{4}$	·39583	$10\frac{1}{2}$	·875
1	·0833	5	·4166	$10\frac{3}{4}$	·89583
$1\frac{1}{8}$	·09375	$5\frac{1}{4}$	·4375	11	·9166
$1\frac{1}{4}$	·10416	$5\frac{1}{2}$	·4583	$11\frac{1}{4}$	·9375
$1\frac{3}{8}$	·114583	$5\frac{3}{4}$	·47916	$11\frac{1}{2}$	·9583
$1\frac{1}{2}$	·125	6	·5	$11\frac{3}{4}$	·97916
$1\frac{5}{8}$	·135416	$6\frac{1}{4}$	·52083	12	1·0000
$1\frac{3}{4}$	·14583				

TABLE 42.—SQUARE INCHES IN DECIMAL FRACTIONS OF A SQUARE FOOT.

Square Inches.	Square Foot.	Square Inches.	Square Foot.	Square Inches.	Square Foot.	Square Inches.	Square Foot.
10	0006944	24	16666	65	45138	105	72916
15	0010416	25	17361	66	45833	106	73611
20	001388	26	18055	67	46527	107	74305
25	0017361	27	18750	68	47222	108	75000
30	002083	28	19444	69	47916	109	75694
35	0024305	29	20138	70	48611	110	76388
40	002777	30	20833	71	49305	111	77083
45	00311249	31	21527	72	50000	112	77777
50	003472	32	22222	73	50694	113	78472
55	0038194	33	22916	74	51388	114	79166
60	004166	34	23611	75	52083	115	79861
65	0045138	35	24305	76	52777	116	80555
70	004861	36	25000	77	53472	117	81249
75	0052083	37	25694	78	54166	118	81944
80	005555	38	26388	79	54861	119	82638
85	0059027	39	27083	80	55555	120	83333
90	006250	40	27777	81	56249	121	84027
95	0065972	41	28472	82	56944	122	84722
1	006944	42	29166	83	57638	123	85416
2	01388	43	29861	84	58333	124	86111
3	02083	44	30555	85	59027	125	86805
4	02777	45	31249	86	59722	126	87500
5	03472	46	31944	87	60416	127	88194
6	04166	47	32638	88	61111	128	88888
7	04861	48	33333	89	61805	129	89583
8	05555	49	34027	90	62500	130	90277
9	06250	50	34722	91	63194	131	90972
10	06944	51	35416	92	63888	132	91666
11	07638	52	36111	93	64583	133	92361
12	08333	53	36805	94	65277	134	93055
13	09027	54	37500	95	65972	135	93750
14	09722	55	38194	96	66666	136	94444
15	10416	56	38888	97	67361	137	95138
16	11111	57	39583	98	68055	138	95833
17	11805	58	40277	99	68750	139	96527
18	12500	59	40972	100	69444	140	97222
19	13194	60	41666	101	70138	141	97916
20	13888	61	42361	102	70833	142	98611
21	14583	62	43055	103	71527	143	99305
22	15277	63	43750	104	72222	144	100000
23	15972	64	44444				

TABLE 43.—DECIMAL FRACTIONS OF A SQUARE FOOT IN SQUARE INCHES.

Square Foot.	Square Inches.	Square Foot.	Square Inches.	Square Foot.	Square Inches.	Square Foot.	Square Inches.
·01	1·44	·26	37·4	·51	73·4	·76	109·4
·02	2·88	·27	38·9	·52	74·9	·77	110·9
·03	4·32	·28	40·3	·53	76·3	·78	112·3
·04	5·76	·29	41·8	·54	77·8	·79	113·8
·05	7·20	·30	43·2	·55	79·2	·80	115·2
·06	8·64	·31	44·6	·56	80·6	·81	116·6
·07	10·1	·32	46·1	·57	82·1	·82	118·1
·08	11·5	·33	47·5	·58	83·5	·83	119·5
·09	13·0	·34	49·0	·59	85·0	·84	121·0
·10	14·4	·35	50·4	·60	86·4	·85	122·4
·11	15·8	·36	51·8	·61	87·8	·86	123·8
·12	17·3	·37	53·3	·62	89·3	·87	125·3
·13	18·7	·38	54·7	·63	90·7	·88	126·7
·14	20·2	·39	56·2	·64	92·2	·89	128·2
·15	21·6	·40	57·6	·65	93·6	·90	129·6
·16	23·0	·41	58·0	·66	95·0	·91	131·0
·17	24·5	·42	60·5	·67	96·5	·92	132·5
·18	25·9	·43	61·9	·68	97·9	·93	133·9
·19	27·4	·44	63·4	·69	99·4	·94	135·4
·20	28·8	·45	64·8	·70	100·8	·95	136·8
·21	30·2	·46	66·2	·71	102·2	·96	138·2
·22	31·7	·47	67·7	·72	103·7	·97	139·7
·23	33·1	·48	69·1	·73	105·1	·98	141·1
·24	34·6	·49	70·6	·74	106·6	·99	142·6
·25	36·0	·50	72·0	·75	108·0	1·00	144·0

TABLE 44.—CORRELATIVE RATES OF MEASUREMENT (ENGLISH).

100 lbs. per cubic foot	. . .	{	·926 ounce per cubic inch.
			24·107 cwt. per cubic yard.
			1·2053 tons per cubic yard.
1 cwt. per cubic yard	. . .		4·148 lbs. per cubic foot.
1 ton per cubic yard	. . .		82·963 lbs. per cubic foot.
1 grain per gallon (1 in	{		6·2321 grains per cubic foot.
70,000 parts, by weight, of			168·36 grains per cubic yard.
water)			220·09 grains per cubic metre.
1 lb. per lineal yard	. . .		·7857 ton per mile.

TABLE 44.—CORRELATIVE RATES (ENGLISH)—(*continued*).

	144 lbs. per square foot.
	1296 lbs. per square yard.
	·5786 ton per square yard.
1 lb. per square inch . . .	2·0355 inches of mercury at 32° F.
	2·0416 inches of mercury at 62° F.
	2·309 feet of water at 62° F.
	27·71 inches of water at 62° F.
1 atmosphere (14·7 lbs. per square inch) . . .	2116·4 lbs. per square foot.
	8·503 tons per square yard.
	33·947 feet of water at 62° F.
	10·347 metres of water at 62° F.
	30 inches of mercury at 62° F.
1 lb. per square foot . . .	·00694 lb. per square inch.
	·1111 ounce per square inch.
	·0804 cwt. per square yard.
1 inch of water at 62° F. . .	·5773 ounce per square inch.
	·0361 lb. per square inch.
	5·20 lbs. per square foot.
	·0736 inch of mercury at 62° F.
1 foot of water at 62° F. . .	·433 lb. per square inch.
	62·355 lbs. per square foot.
	·883 inch of mercury at 62° F.
1 inch of mercury at 62° F. . .	·49 lb. per square inch.
	70·56 lbs. per square foot.
	1·165 feet of water at 62° F.
	14 inches of water at 62° F.
1 cubic foot per second . . .	2·222 cubic yards per minute.
	133·333 cubic yards per hour.
1 cubic foot per minute . . .	2·222 cubic yards per hour.
·45 cubic foot per minute . . .	1 cubic yard per hour.
1 cubic inch per second . . .	2·083 cubic feet per hour.
	12·984 gallons per hour.
1 mile per hour . . . . .	1·467 feet per second.
	88 feet per minute.
1 foot per second . . . . .	·682 mile per hour.
1 foot per minute . . . . .	·01136 mile per hour.
	·20 inch per second.
1 inch per second . . . . .	5 feet per minute.

TABLE 45.—WATER.

	277·274 cubic inches.
	·1604 cubic foot.
1 Imperial gallon . . . . .	10 pounds of water at 62° F.
	70,000 grains of water at 62° F.
	1·20 U.S. gallons.
	4·544 litres.
	231 cubic inches.
	·1337 cubic foot.
1 U. S. gallon . . . . .	8·333 pounds of water at 62° F.
	·8333 imperial gallon ( $\frac{1}{8}$ ths).
	3·786 litres.
	·03608 pound.
	·5773 ounce.
1 cubic inch of water at 62° F. . . . .	252·6 grains.
	·003607 imperial gallon.
	·004326 U.S. gallon.
	·01638 litre.
	62·355 pounds.
	997·68 ounces (about 1000).
	·557 cwt.
	·0278 ton.
1 cubic foot of water at 62° F.	6·2355 imperial gallons.
	49·884 imperial pints (about 50).
	7·4805 U.S. gallons.
	28·315 litres.
	·02832 cubic metre.
1 cylindrical inch of water at 62° F. . . . .	·02833 pound.
	·4533 ounce.
	·7854 cubic inch.
	48·973 pounds (about 50).
	783·57 ounces.
	·437 cwt.
	·0219 ton.
1 cylindrical foot of water at 62° F. . . . .	4·8973 imperial gallons.
	5·8758 U.S. gallons.
	22·2380 litres.
	·02224 cubic metre.
	1684·8 pounds.
1 cubic yard of water . . . . .	15·043 cwt., or 15 cwt. 4·8 pounds.
	·7645 cubic metre.
	2·2046 pounds at 62° F.
	·2201 imperial gallon.
1 litre of water . . . . .	1·761 imperial pint.
	·2641 U.S. gallon.
	61·025 cubic inches.
	·0353 cubic foot.

TABLE 45.—WATER (*continued*).

	1 tonne, or 1000 kilogrammes at 39·1° F. or 4° C.
	2204·62 pounds at 39·1° F. or 4° C.
	2203·7 pounds at 62·4 pounds per cubic foot.
	1 ton of 2240 pounds, nearly.
1 cubic metre of water .	1 tun of 4 hogsheads or 2100 pounds, nearly.
	220·1 imperial gallons.
	264·2 U.S. gallons.
	1·308 cubic yards.
	35·3156 cubic feet.
	1000 litres.

The weight of fresh water is commonly assumed, in ordinary calculations, to be 62·4 pounds per cubic foot, which is the weight at 52·3° F. It is frequently taken as  $62\frac{1}{2}$  pounds or 1000 ounces per cubic foot.

The volumes of given weights of water, at the rate of 62·4 pounds per cubic foot, are as follows :—

1 ton . . . . .	35·90 cubic feet (about 36).
1 cwt. . . . .	1·795     "
1 pound . . . . .	{ .016     "
	27·692 cubic inches.
1 ounce . . . . .	1·731     "
1 tonne, at 39·1° F. or 4° C. .	35·3156 cubic feet.
1 kilogramme     "     "	{ .0353     "
	61·025 cubic inches.
1 tonne, at 52·3° F. (62·4 pounds per cubic foot) . . . . .	35·330 cubic feet.

A pipe 1 yard in length holds about as many pounds of water of ordinary temperatures as the square of its diameter in inches (about two per cent. more).

A column of water at 62° F. 1 foot high, is equivalent to a pressure of 4·33 pound, or 6·928 ounces per square inch of base, or to 62·355 pounds per square foot.

A column of water 1 inch high, is equivalent to a pressure of ·5773 ounce, or ·03608 pound per square inch; or to 5·196 pounds per square foot.

A column of water 100 feet high is equivalent to  $43\frac{1}{2}$  pounds per square inch; or 2·786 tons per square foot.

A column of water 1 mile deep; weighing 62·4 pounds per cubic foot, is equivalent to a pressure of about 1 ton per square inch.



1 pound per square inch is equivalent to a column of water at 62° F. 2·31 feet or 27·72 inches high.

### Sea Water.

1 cubic foot at 62° F. . . .	64 pounds.
1 cubic yard . . . . .	15½ cwt. nearly (8 pounds less).
1 cubic metre . . . . .	1 ton fully (20 pounds more).
1 ton . . . . .	35 cubic feet.
Ratio of weight of fresh water to that of sea water . . . }	39 to 40, or 1 to 1·028.

### Ice and Snow.

1 cubic foot of ice at 32° F.	57·50 pounds.
1 pound of ice     "     "     {	·0174 cubic foot, or 30·067 cubic inches.
Specific density of ice, ·922; that of water at 62° F. being 1.	
1 cubic foot of fresh snow, according to humidity of atmosphere: 5 pounds to 12 pounds (Trautwine).	
1 cubic foot of snow moistened and com- pacted by rain . . . }	15 pounds to 50 pounds (Trautwine).

TABLE\*46.—AIR.

	·080728 pound at 32° F.
1 cubic foot, at 14·7 lbs. per square inch, or 1 atmosphere . . . . .	1·29 ounce     "     " 565·1 grains     "     " ·076097 pound at 62° F. 1·217 ounce     "     " 532·7 grains     "     "
1 litre, under one atmosphere . . . . .	1·293 grammes at 32° F. 19·955 grains     "     "
1 pound of air at 62° F. . . . .	13·141 cubic feet.
The weights of equal volumes of mercury, water and air at 62° F. under 1 atmosphere, are as 11140·56, 819·4 and 1.	
	14·7 lbs. per square inch. 2116·4 lbs. per square foot. 1·0335 kilogrammes per square centimetre.
1 atmosphere of pressure . . . . .	29·922 inches of mercury at 32° F. 76 centimetres of mercury at 32° F. 30 inches of mercury at 62° F. 33·947 feet of water at 62° F. 10·347 metres of water at 62° F.

TABLE 46.—AIR (*continued*).

	2.035 inches of mercury at 32° F.
	51.7 millimetres
1 lb. per square inch .	2.04 inches of mercury at 62° F
	2.31 feet of water at 62° F.
	27.72 inches   "   "
1 ounce per square inch .	1.732 inches   "   "
	1.925 inch   "   "
lb. per square foot .	.01417 inch of mercury at 62° F.

**French Metric Weights and Measures.**

The metre, equal to 39.37043 inches, and the kilogramme, equal to 2.20462 pounds, are the only standards of weight and measure in France. The kilogramme is defined as the weight of a cubic decimetre of distilled water at its maximum density, at 4.0° C., or 39.1° F. It is legally taken to be 2.20462125 pounds. The gramme, of which there are one thousand in the kilogramme, is the unit of weight. It is the weight of one cubic centimetre of water under the conditions above defined.

The metric unit of capacity is the litre, defined as equal to a cubic decimetre. It is equal to 0.22009 gallon.

The French metric system has been compulsorily adopted by France and Belgium in 1801; Holland in 1819; Greece in 1836; Italy and Spain, in 1859; Portugal in 1860—68; the German Empire, in 1872; Colombia, Venezuela, in 1872. The system is established in France and her Colonies, Belgium, Holland and her Colonies, Germany, Sweden, Norway, Austro-Hungary, Italy, Spain, Portugal, Turkey, Roumania, Greece, Brazil, Colombia, Uruguay, Ecuador, Peru, Chili, the Argentine Republic. It has been made legally optional in Great Britain and Ireland, the United States of North America and Canada. It is admitted in principle, or partially for customs, in British India, Russia, and Venezuela. Switzerland, in 1856, legalised the foot of three decimetres as the unit of length, with a decimal scale; with a unit of weight, the pound of 500 grammes, or half a kilogramme, with two distinct scales of multiples and parts, one decimal, the other on the old system. Denmark adopted the metric system so far as the pound of 500 grammes.



Figs. 17, 18.—French and English Measures compared.

TABLE 47.—FRENCH MEASURES OF LENGTH.

		Metres.	English Equivalents.
1 millimetre =		·001	= ·03937 in., or $\frac{1}{25}$ in. nearly.
10 millimetres	= 1 centimetre =	·01	= ·3937 inch.
10 centimetres	= 1 decimetre =	·1	= 3·93704 in., or 4 ins. nearly
10 decimetres	} = 1 METRE =	1	{ 39·3704 ins. 3·2809 feet.
100 centimetres			
1000 millimetres			
10 metres	= 1 decametre =	10	= 32·8087 feet.
10 decametres	= 1 hectometre =	100	{ 328·0869 feet. 109·3623 yds.
10 hectometres	= 1 KILOMETRE =	1000	{ 3280·869 feet. 1093·623 yds.
10 kilometres	= 1 myriametre = 10,000 =		{ ·62138mle. 6·21377 miles.

TABLE 48.—FRENCH MEASURES OF SURFACE.

		Sq. Metres.	English Equivalents.
1 sq. millimetre		·000001	·00155 sq. in.
100 square millimetres	} 1 sq. centimetre . }	·0001	·155 sq. in.
100 square centimetres.			
100 square decimetres.	} 1 sq. decimetre . }	·01	15·5003 sq. ins.
10,000 square centimetres.			
100 square metres.	} 1 square metre or centiare . . }	1	{ 10·7641 sq. ft. 1·1960 sq. yds.
100 square decametres.			
100 square metres.	} 1 sq. decametre, or are . . . }	100	{ 1076·41 sq. ft. 119·601 sq. yds.
100 square decametres.			
100 square hectometres.	} 1 sq. hectometre or hectare, or metrical acre . }	10,000	{ 11,960·11 sq. yds. 2·4711 acres.
100 square kilometres.			
100 square kilometres.	} 1 sq. kilometre . }	1,000,000	{ 1,196,014 sq. yds. ·38611 sq. mile.
100 square kilometres.			
100 square kilometres.	} 1 sq. myriametre . }	100,000,000	= 38·611 sq. miles
100 square kilometres.			

Land is measured in terms of the centiare, the are, and the hectare.

#### Wood (France).

The large pieces of timber, cut from the trees, are of the following ordinary squared sizes.

	Metre.	Inches.
Oak . . . . .	·10 to ·30	3·94 to 11·8
Small stowage ( <i>Petit arrimage</i> ) . . . . .	·30 to ·40	11·8 to 15·7

	Metre.	Inches.
Large stowage ( <i>Gros arrimage</i> ) . .	40 to 60	15.7 to 23.6
Fir . . . . .	18 to 27	7.1 to 10.6
do. beams . . . . .	27 to 36	10.6 to 14.2
do. large wood . . . . .	36 to 60	14.2 to 23.6

TABLE 49.—OAK SCANTLINGS IN COMMERCIAL USE (FRANCE).

Description.	Width.		Thickness.		Length.	
	Milli-metres.	Inches.	Milli-metres.	Inches.	Metres.	Feet.
Echantillon } (sample)	25	98	42	1.65	1.5 to 4	4.9 to 13.2
Membrure } (frame)	167	6.57	83	3.27	2 to 4	6.6 to 13.2
Doublette } (principal)	333	11.93	63	2.48	2.5 to 4	8.2 to 13.2
Grand Bat- } tant (large doorframe)	333	11.93	126	4.96	4 to 6	13.1 to 19.7
Petit Bat- } tant (small doorframe)	25	98	83	3.27	3 to 6	9.8 to 19.7
Entrevous } (between joists)	25	98	28	1.10	1.5 to 4	4.9 to 13.2
Chevron } (joist)	83	3.27	83	3.27	2 to 4	6.6 to 13.2
Membrette .	167	6.57	56	2.20	1.5 to 4	4.9 to 13.2
Panneau } (panel)	216 to 243	8.51 to 9.57	20 to 22	.79 to .87	2 to 4	6.6 to 13.2
Volige (thin } plank)	216 to 243	8.51 to 9.57	13 to 15	.51 to .59	2 to 4	6.6 to 13.2
Feuillet } (edge of panel)	216 to 243	8.51 to 9.57	6 to 7	.24 to .28	2 to 4	6.6 to 13.2
FIR SCANTLINGS.						
Madrier } (plank- principal piece)	220	8.66	80	3.15	...	...
Petit } Madrier (smaller piece)	220	8.66	54	2.13	...	...
Planche } (board)	220 or 320	8.66 or 12.60	27	1.06	...	...

TABLE 50.—FRENCH MEASURES OF VOLUME.

**Cubic Measure.**

		Cubic Metres.	English Equivalents.
1 cubic milli-	}	.000000001	.000061 cubic inch.
metre			
1000 cubic } 1 cubic centi-	}	.000001	.061025 cubic inch.
millimetres. } metre			
1000 cubic } 1 cubic deci-	}	.001	{ 61.02524 cubic ins. } .0353156 cubic ft.
centimetres. } metre			
1000 cubic } 1 cubic metre 1	}	1	{ 35.3156 cubic feet. } 1.308 cubic yards.
decimeters. } metre			
1000 cubic } 1 cubic deca-	}	1,000	1308 cubic yards.
metres. } metre.			

**Firewood Measure (French).**

		Cubic Metres.	
1 decistère	.	0.1	3.532 cubic feet.
10 decistères	{ 1 stère (cubic metre).	1	35.3156 cubic feet.
1 vois (Paris)	2 stères	2	70.6312 cubic feet.
1 vois de charbon (charcoal)	0.2 stère	0.2	7.063 cubic feet.
1 corde	4 stères	4	141.2624 „
1 decastère	10 stères	10	353.156 „

The stère measures 1.14 metres  $\times$  0.88 metre, by 1 metre, the billets being 1.14 metres in length.

**Liquid Measure.**

		Litres.	
1 centilitre	}	.01	{ .61025 cubic inch. } .0704 gill.
10 cubic centimetres			
10 centilitres	1 décilitre	0.1	{ 6.1025 cubic inches. } .1761 pint.
10 décilitres	{ 1 LITRE (1 cubic decimetre)	1	{ 61.02524 cubic ins. } .2201 gallon.
10 litres	1 décalitre	10	2.2009 gallons.
10 décalitres	1 hectolitre	100	22.009 gallons.

**Dry Measure.**

10 litres	1 décalitre	10	2.2009 gallons.
10 décalitres	1 hectolitre	100	{ 22.009 gallons. } 2.7511 bushels.
10 hectolitres	{ 1 kilolitre. (1 cubic metre)	1000	{ 220.09 gallons. } 27.511 bushels.

The use of measures equal to a *double-litre*, a *half-litre*, a *double-décilitre*, a *half-décilitre*, is sanctioned by law.

TABLE 51.—FRENCH MEASURES OF WEIGHT.

		Grammes. English Equivalents.	
	1 milligramme .	·001	·0154 grain.
10 milligrammes .	1 centigramme .	·01	·1543 grain.
10 centigrammes .	1 decigramme .	0·1	1·5432 grains.
10 decigrammes .	{ 1 GRAMME (unit of weight) }	1	15·4323 grains.
10 grammes .	1 décagramme .	10	{ 154·3235 grains. ·3527 ounce.
10 décagrammes .	1 hectogramme	100	{ 1543·2349 grains. 3·5274 ounces.
10 hectogrammes .	1 KILOGRAMME	1000	2·2046 pounds.
100 kilogrammes .	1 metric quintal		220·4621 pounds.
10 quintals, or	{ 1 millier, or		{ 2204·6212 pounds. 19·6841 cwt.
1000 kilogrammes }	tonne .		{ .9842 ton.

TABLE 52.—MILLIMETRES IN LINEAL INCHES.

Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.
1	·0394	26	1·0236	51	2·0079	76	2·9922
2	·0787	27	1·0630	52	2·0473	77	3·0315
3	·1181	28	1·1024	53	2·0866	78	3·0709
4	·1575	29	1·1417	54	2·1260	79	3·1103
5	·1968	30	1·1811	55	2·1654	80	3·1496
6	·2362	31	1·2205	56	2·2047	81	3·1890
7	·2756	32	1·2598	57	2·2441	82	3·2284
8	·3150	33	1·2992	58	2·2835	83	3·2677
9	·3543	34	1·3386	59	2·3228	84	3·3071
10	·3937	35	1·3780	60	2·3622	85	3·3465
11	·4331	36	1·4173	61	2·4016	86	3·3859
12	·4724	37	1·4567	62	2·4410	87	3·4252
13	·5118	38	1·4961	63	2·4803	88	3·4646
14	·5512	39	1·5354	64	2·5197	89	3·5040
15	·5906	40	1·5748	65	2·5591	90	3·5433
16	·6299	41	1·6142	66	2·5984	91	3·5827
17	·6693	42	1·6536	67	2·6378	92	3·6221
18	·7087	43	1·6929	68	2·6772	93	3·6614
19	·7480	44	1·7323	69	2·7166	94	3·7008
20	·7874	45	1·7717	70	2·7559	95	3·7402
21	·8268	46	1·8110	71	2·7953	96	3·7796
22	·8661	47	1·8504	72	2·8347	97	3·8189
23	·9055	48	1·8898	73	2·8740	98	3·8583
24	·9449	49	1·9291	74	2·9134	99	3·8977
25	·9843	50	1·9685	75	2·9528	100	3·9370

TABLE 52.—MILLIMETRES IN LINEAL INCHES (*continued*).

Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.
101	3.9764	143	5.6300	185	7.2835	227	8.9371
102	4.0158	144	5.6693	186	7.3229	228	8.9765
103	4.0552	145	5.7087	187	7.3623	229	9.0158
104	4.0945	146	5.7481	188	7.4016	230	9.0552
105	4.1339	147	5.7874	189	7.4410	231	9.0946
106	4.1733	148	5.8268	190	7.4804	232	9.1339
107	4.2126	149	5.8662	191	7.5198	233	9.1733
108	4.2520	150	5.9056	192	7.5591	234	9.2127
109	4.2914	151	5.9449	193	7.5985	235	9.2521
110	4.3307	152	5.9843	194	7.6379	236	9.2914
111	4.3701	153	6.0237	195	7.6772	237	9.3308
112	4.4095	154	6.0630	196	7.7166	238	9.3702
113	4.4489	155	6.1024	197	7.7560	239	9.4095
114	4.4882	156	6.1418	198	7.7954	240	9.4489
115	4.5276	157	6.1812	199	7.8347	241	9.4883
116	4.5670	158	6.2205	200	7.8741	242	9.5277
117	4.6063	159	6.2599	201	7.9135	243	9.5670
118	4.6457	160	6.2993	202	7.9528	244	9.6064
119	4.6851	161	6.3386	203	7.9922	245	9.6458
120	4.7245	162	6.3780	204	8.0316	246	9.6851
121	4.7638	163	6.4174	205	8.0709	247	9.7245
122	4.8032	164	6.4568	206	8.1103	248	9.7639
123	4.8426	165	6.4961	207	8.1497	249	9.8032
124	4.8819	166	6.5355	208	8.1891	250	9.8426
125	4.9213	167	6.5749	209	8.2284	251	9.8820
126	4.9607	168	6.6142	210	8.2678	252	9.9214
127	5.0000	169	6.6536	211	8.3072	253	9.9607
128	5.0394	170	6.6930	212	8.3465	254	10.0001
129	5.0788	171	6.7323	213	8.3859	255	10.0395
130	5.1182	172	6.7717	214	8.4253	256	10.0788
131	5.1575	173	6.8111	215	8.4646	257	10.1182
132	5.1969	174	6.8505	216	8.5040	258	10.1576
133	5.2363	175	6.8898	217	8.5434	259	10.1970
134	5.2756	176	6.9292	218	8.5828	260	10.2363
135	5.3150	177	6.9686	219	8.6221	261	10.2757
136	5.3544	178	7.0079	220	8.6615	262	10.3151
137	5.3938	179	7.0473	221	8.7009	263	10.3544
138	5.4331	180	7.0867	222	8.7402	264	10.3938
139	5.4725	181	7.1261	223	8.7796	265	10.4332
140	5.5119	182	7.1654	224	8.8190	266	10.4725
141	5.5512	183	7.2048	225	8.8584	267	10.5119
142	5.5906	184	7.2442	226	8.8977	268	10.5513

TABLE 52.—MILLIMETRES IN LINEAL INCHES (*continued*).

Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.
269	10·5907	311	12·2442	353	13·8978	395	15·5513
270	10·6300	312	12·2836	354	13·9371	396	15·5907
271	10·6694	313	12·3229	355	13·9765	397	15·6300
272	10·7088	314	12·3623	356	14·0159	398	15·6694
273	10·7481	315	12·4017	357	14·0552	399	15·7088
274	10·7875	316	12·4410	358	14·0946	400	15·7482
275	10·8269	317	12·4804	359	14·1340	401	15·7875
276	10·8663	318	12·5198	360	14·1733	402	15·8269
277	10·9056	319	12·5592	361	14·2127	403	15·8663
278	10·9450	320	12·5985	362	14·2521	404	15·9056
279	10·9844	321	12·6379	363	14·2915	405	15·9450
280	11·0237	322	12·6773	364	14·3308	406	15·9844
281	11·0361	323	12·7166	365	14·3702	407	16·0238
282	11·1025	324	12·7560	366	14·4096	408	16·0631
283	11·1419	325	12·7954	367	14·4489	409	16·1025
284	11·1812	326	12·8348	368	14·4883	410	16·1419
285	11·2206	327	12·8741	369	14·5277	411	16·1812
286	11·2600	328	12·9135	370	14·5670	412	16·2206
287	11·2993	329	12·9529	371	14·6064	413	16·2600
288	11·3387	330	12·9922	372	14·6458	414	16·2993
289	11·3781	331	13·0316	373	14·6852	415	16·3387
290	11·4174	332	13·0710	374	14·7245	416	16·3781
291	11·4568	333	13·1103	375	14·7639	417	16·4175
292	11·4962	334	13·1497	376	14·8033	418	16·4568
293	11·5356	335	13·1891	377	14·8426	419	16·4962
294	11·5749	336	13·2285	378	14·8820	420	16·5356
295	11·6143	337	13·2678	379	14·9214	421	16·5749
296	11·6537	338	13·3072	380	14·9608	422	16·6143
297	11·6930	339	13·3466	381	15·0001	423	16·6537
298	11·7324	340	13·3859	382	15·0395	424	16·6930
299	11·7718	341	13·4253	383	15·0789	425	16·7324
300	11·8111	342	13·4647	384	15·1182	426	16·7718
301	11·8505	343	13·5040	385	15·1576	427	16·8112
302	11·8899	344	13·5434	386	15·1970	428	16·8505
303	11·9292	345	13·5828	387	15·2363	429	16·8899
304	11·9686	346	13·6222	388	15·2757	430	16·9293
305	12·0080	347	13·6615	389	15·3151	431	16·9686
306	12·0473	348	13·7009	390	15·3545	432	17·0080
307	12·0867	349	13·7403	391	15·3938	433	17·0474
308	12·1261	350	13·7790	392	15·4332	434	17·0868
309	12·1655	351	13·8190	393	15·4726	435	17·1261
310	12·2048	352	13·8584	394	15·5119	436	17·1655



TABLE 52.—MILLIMETRES IN LINEAL INCHES (*continued*).

Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.	Milli- metres.	Inches.
437	17.2049	456	17.9529	475	18.7009	494	19.4490
438	17.2442	457	17.9923	476	18.7403	495	19.4883
439	17.2836	458	18.0316	477	18.7797	496	19.5277
440	17.3230	459	18.0710	478	18.8191	497	19.5671
441	17.3623	460	18.1104	479	18.8584	498	19.6065
442	17.4017	461	18.1498	480	18.8978	499	19.6458
443	17.4411	462	18.1891	481	18.9372	500	19.6852
444	17.4805	463	18.2285	482	18.9765	550	21.6537
445	17.5198	464	18.2679	483	19.0159	600	23.6223
446	17.5592	465	18.3072	484	19.0553	650	25.5908
447	17.5986	466	18.3466	485	19.0946	700	27.5593
448	17.6379	467	18.3860	486	19.1340	750	29.5278
449	17.6773	468	18.4253	487	19.1734	800	31.4963
450	17.7167	469	18.4647	488	19.2128	850	33.4649
451	17.7561	470	18.5041	489	19.2521	900	35.4334
452	17.7954	471	18.5435	490	19.2915	950	37.4019
453	17.8350	472	18.5828	491	19.3309	1000	39.3704
454	17.8742	473	18.6222	492	19.3702		= 1
455	17.9135	474	18.6616	493	19.4096		metre.

By means of the above Table, and the following Table 53, the equivalent values of inches in centimetres and decimetres, and even in metres, may be found by simply altering the position of the decimal point. Take for example the tabular value of 2 millimetres, Table 52, and shift the decimal point successively, by one digit, towards the right-hand side; the values of two centimetres, two decimetres, and two metres are thereby expressed in inches, as follows:—

2 millimetres	. . . . .	0.787 inches.
2 centimetres	. . . . .	0.787 "
2 decimetres	. . . . .	7.87 "
2 metres	. . . . .	78.7 "

At the same time, it appears that, by selecting the tabular value of 20 millimetres, the value of its multiples are given more accurately, thus,—

20 millimetres, or 2 centimetres	. . . . .	0.7874 inches.
2 decimetres	. . . . .	7.874 "
2 metres	. . . . .	78.74 "

Again :—

200 millimetres, or 2 decimetres = 7·8741 inches

2 metres . . . . . = 78·741 "

Similarly, for example :—

·32 inch = 8·128 millimetres.

3·2 " = 81·28 "

32·0 " =  $\begin{cases} 812·8 & \text{"} \\ \cdot 8128 & \text{metre.} \end{cases}$  or

Like functional expansions of the following tables of relative French and English measures and weight, are available for practice : greatly extending the utility of the tables.

TABLE 53.—DECIMAL FRACTIONS OF A LINEAL INCH IN MILLIMETRES.

Inch.	Milli- metres.	Inch.	Milli- metres.	Inch.	Milli- metres.	Inches.	Milli- metres.
·01	·254	·29	7·366	·57	14·478	·85	21·590
·02	·508	·30	7·620	·58	14·732	·86	21·844
·03	·762	·31	7·874	·59	14·986	·87	22·098
·04	1·016	·32	8·128	·60	15·240	·88	22·352
·05	1·270	·33	8·382	·61	15·494	·89	22·606
·06	1·524	·34	8·636	·62	15·748	·90	22·860
·07	1·778	·35	8·890	·63	16·002	·91	23·114
·08	2·032	·36	9·144	·64	16·256	·92	23·368
·09	2·286	·37	9·398	·65	16·510	·93	23·622
·10	2·540	·38	9·652	·66	16·764	·94	23·876
·11	2·794	·39	9·906	·67	17·018	·95	24·130
·12	3·048	·40	10·160	·68	17·272	·96	24·384
·13	3·302	·41	10·414	·69	17·526	·97	24·638
·14	3·556	·42	10·668	·70	17·780	·98	24·892
·15	3·810	·43	10·922	·71	18·034	·99	25·146
·16	4·064	·44	11·176	·72	18·288	1·00	25·400
·17	4·318	·45	11·430	·73	18·542	2·00	50·799
·18	4·572	·46	11·684	·74	18·796	3·00	76·199
·19	4·826	·47	11·938	·75	19·050	4·00	101·598
·20	5·080	·48	12·192	·76	19·304	5·00	126·998
·21	5·334	·49	12·446	·77	19·558	6·00	152·397
·22	5·588	·50	12·700	·78	19·812	7·00	177·797
·23	5·842	·51	12·954	·79	20·066	8·00	203·196
·24	6·096	·52	13·208	·80	20·320	9·00	228·596
·25	6·350	·53	13·462	·81	20·574	10·00	253·995
·26	6·604	·54	13·716	·82	20·828	11·00	279·395
·27	6·858	·55	13·970	·83	21·082	12·00	304·794
·28	7·112	·56	14·224	·84	21·336	= 1 foot }	

TABLE 54.—VULGAR FRACTIONS OF A LINEAL INCH IN MILLIMETRES.

Eighths of an Inch.	Millimetres.	Eighths of an Inch.	Millimetres.	Eighths of an Inch.	Millimetres.
1	3.175	4	12.700	7	22.225
2	6.350	5	15.875	8	25.400
3	9.525	6	19.050		
Twelfths of an Inch.	Millimetres.	Twelfths of an Inch.	Millimetres.	Twelfths of an Inch.	Millimetres.
1	2.117	5	10.583	9	19.050
2	4.233	6	12.700	10	21.166
3	6.350	7	14.816	11	23.283
4	8.466	8	16.933	12	25.400
Sixteenths of an Inch.	Millimetres.	Sixteenths of an Inch.	Millimetres.	Sixteenths of an Inch.	Millimetres.
1	1.587	7	11.112	13	20.637
3	4.762	9	14.287	15	23.812
5	7.937	11	17.462		
Thirty-seconds of an Inch.	Millimetres.	Thirty-seconds of an Inch.	Millimetres.	Thirty-seconds of an Inch.	Millimetres.
1	0.794	13	10.319	25	19.843
3	2.381	15	11.906	27	21.431
5	3.969	17	13.493	29	23.018
7	5.556	19	15.081	31	24.605
9	7.144	21	16.668		
11	8.731	23	18.256		
Sixty-fourths of an Inch.	Millimetres.	Sixty-fourths of an Inch.	Millimetres.	Sixty-fourths of an Inch.	Millimetres.
1	0.397	23	9.128	45	17.859
3	1.191	25	9.922	47	18.653
5	1.984	27	10.715	49	19.447
7	2.778	29	11.509	51	20.240
9	3.572	31	12.303	53	21.034
11	4.366	33	13.097	55	21.828
13	5.159	35	13.890	57	22.621
15	5.953	37	14.684	59	23.415
17	6.747	39	15.478	61	24.209
19	7.540	41	16.272	63	25.003
21	8.334	43	17.065		

TABLE 55.—METRES IN LINEAL FEET AND IN YARDS.

Metres.	Feet.	Yards.	Metres.	Feet.	Yards.
1	3·2809	1·0936	44	144·3596	48·1193
2	6·5618	2·1872	45	147·6405	49·2129
3	9·8427	3·2809	46	150·9214	50·3065
4	13·1236	4·3745	47	154·2023	51·4001
5	16·4045	5·4681	48	157·4832	52·4938
6	19·6854	6·5617	49	160·7641	53·5874
7	22·9663	7·6553	50	164·0450	54·6810
8	26·2472	8·7490	51	167·3259	55·7746
9	29·5281	9·8426	52	170·6068	56·8682
10	32·8090	10·9362	53	173·8877	57·9619
11	36·0899	12·0298	54	177·1686	59·0555
12	39·3708	13·1234	55	180·4495	60·1491
13	42·6517	14·2171	56	183·7304	61·2427
14	45·9326	15·3107	57	187·0113	62·3363
15	49·2135	16·4043	58	190·2922	63·4300
16	52·4944	17·4979	59	193·5731	64·5236
17	55·7753	18·5915	60	196·8540	65·6172
18	59·0562	19·6852	61	200·1349	66·7108
19	62·3371	20·7788	62	203·4158	67·8044
20	65·6180	21·8724	63	206·6967	68·8981
21	68·8989	23·9660	64	209·9776	69·9917
22	72·1798	24·0596	65	213·2585	71·0853
23	75·4607	25·1533	66	216·5394	72·1789
24	78·7416	26·2469	67	219·8203	73·2725
25	82·0225	27·3405	68	223·1012	74·3662
26	85·3034	28·4341	69	226·3821	75·4598
27	88·5843	29·5277	70	229·6630	76·5534
28	91·8652	30·6214	71	232·9439	77·6470
29	95·1461	31·7150	72	236·2248	78·7406
30	98·4270	32·8086	73	239·5057	79·8343
31	101·7079	33·9022	74	242·7866	80·9279
32	104·9888	34·9958	75	246·0675	82·0215
33	108·2697	36·0895	76	249·3484	83·1151
34	111·5506	37·1831	77	252·6293	84·2087
35	114·8315	38·2767	78	255·9102	85·3024
36	118·1124	39·3703	79	259·1911	86·3960
37	121·3933	40·4639	80	262·4720	87·4896
38	124·6742	41·5576	81	265·7529	88·5832
39	127·9551	42·6512	82	269·0338	89·6768
40	131·2360	43·7448	83	272·3147	90·7705
41	134·5169	44·8384	84	275·5956	91·8641
42	137·7978	45·9320	85	278·8765	92·9577
43	141·0787	47·0257	86	282·1574	94·0513

TABLE 55.—METRES IN LINEAL FEET AND IN YARDS  
(continued).

Metres.	Feet.	Yards.	Metres.	Feet.	Yards.
87	285·4383	95·1449	94	308·4046	102·8003
88	288·7192	96·2386	95	311·6855	103·8939
89	292·0001	97·3322	96	314·9664	104·9875
90	295·2810	98·4258	97	318·2473	106·0811
91	298·5619	99·5194	98	321·5282	107·1748
92	301·8428	100·6130	99	324·8091	108·2684
93	305·1237	101·7067	100	328·0900	109·3620

TABLE 56.—LINEAL FEET IN METRES.

Feet.	Metres.	Feet.	Metres.	Feet.	Metres.	Feet.	Metres.
1	·3048	26	7·9248	51	15·5448	76	23·1648
2	·6096	27	8·2296	52	15·8496	77	23·4696
3	·9144	28	8·5344	53	16·1544	78	23·7744
4	1·2192	29	8·8392	54	16·4592	79	24·0792
5	1·5240	30	9·1440	55	16·7640	80	24·3840
6	1·8288	31	9·4488	56	17·0688	81	24·6888
7	2·1336	32	9·7536	57	17·3736	82	24·9936
8	2·4384	33	10·0584	58	17·6784	83	25·2984
9	2·7432	34	10·3632	59	17·9832	84	25·6032
10	3·0480	35	10·6680	60	18·2880	85	25·9080
11	3·3528	36	10·9728	61	18·5928	86	26·2128
12	3·6576	37	11·2776	62	18·8976	87	26·5176
13	3·9624	38	11·5824	63	19·2024	88	26·8224
14	4·2672	39	11·8872	64	19·5072	89	27·1272
15	4·5720	40	12·1920	65	19·8120	90	27·4320
16	4·8768	41	12·4968	66	20·1168	91	27·7368
17	5·1816	42	12·8016	67	20·4216	92	28·0416
18	5·4864	43	13·1064	68	20·7264	93	28·3464
19	5·7912	44	13·4112	69	21·0312	94	28·6512
20	6·0960	45	13·7160	70	21·3360	95	28·9560
21	6·4008	46	14·0208	71	21·6408	96	29·2608
22	6·7056	47	14·3256	72	21·9456	97	29·5656
23	7·0104	48	14·6304	73	22·2504	98	29·8704
24	7·3152	49	14·9352	74	22·5552	99	30·1752
25	7·6200	50	15·2400	75	22·8600	100	30·4800

TABLE 57.—LINEAL YARDS IN METRES.

Yards.	Metres.	Yards.	Metres.	Yards.	Metres.	Yards.	Metres.
1	·9144	26	23·7741	51	46·6339	76	69·4936
2	1·8288	27	24·6885	52	47·5483	77	70·4080
3	2·7432	28	25·6029	53	48·4627	78	71·3224
4	3·6576	29	26·5173	54	49·3771	79	72·2368
5	4·5719	30	27·4317	55	50·2914	80	73·1512
6	5·4863	31	28·3461	56	51·2058	81	74·0656
7	6·4007	32	29·2605	57	52·1202	82	74·9800
8	7·3151	33	30·1749	58	53·0346	83	75·8944
9	8·2295	34	31·0893	59	53·9490	84	76·8088
10	9·1439	35	32·0036	60	54·8634	85	77·7231
11	10·0583	36	32·9180	61	55·7778	86	78·6375
12	10·9727	37	33·8324	62	56·6922	87	79·5519
13	11·8871	38	34·7468	63	57·6066	88	80·4663
14	12·8015	39	35·6612	64	58·5210	89	81·3807
15	13·7158	40	36·5756	65	59·4353	90	82·2951
16	14·6302	41	37·4900	66	60·3497	91	83·2095
17	15·5446	42	38·4044	67	61·2641	92	84·1239
18	16·4590	43	39·3188	68	62·1785	93	85·0383
19	17·3734	44	40·2332	69	63·0929	94	85·9527
20	18·2878	45	41·1475	70	64·0073	95	86·8670
21	19·2022	46	42·0619	71	64·9217	96	87·7814
22	20·1166	47	42·9763	72	65·8361	97	88·6958
23	21·0310	48	43·8907	73	66·7505	98	89·6102
24	21·9454	49	44·8051	74	67·6649	99	90·5246
25	22·8600	50	45·7195	75	68·5792	100	91·4390

TABLE 58.—KILOGRAMMES IN POUNDS.

Kilos.	Pounds.	Kilos.	Pounds.	Kilos.	Pounds.	Kilos.	Pounds.
1	2·2046	13	28·6601	25	55·1155	37	81·5710
2	4·4092	14	30·8647	26	57·3201	38	83·7756
3	6·6139	15	33·0693	27	59·5248	39	85·9802
4	8·8185	16	35·2739	28	61·7294	40	88·1848
5	11·0231	17	37·4786	29	63·9340	41	90·3895
6	13·2277	18	39·6832	30	66·1386	42	92·5941
7	15·4323	19	41·8878	31	68·3433	43	94·7987
8	17·6370	20	44·0924	32	70·5479	44	97·0033
9	19·8416	21	46·2970	33	72·7525	45	99·2079
10	22·0462	22	48·5017	34	74·9571	46	101·4126
11	24·2508	23	50·7063	35	77·1617	47	103·6172
12	26·4555	24	52·9109	36	79·3664	48	105·8218

TABLE 58.—KILOGRAMMES IN POUNDS (*continued*).

Kilos.	Pounds.	Kilos.	Pounds.	Kilos.	Pounds.	Kilos.	Pounds.
49	108·0264	62	136·4865	75	165·3466	88	194·0066
50	110·2310	63	138·8911	76	167·5512	89	196·2113
51	112·4357	64	141·0957	77	169·7558	90	198·4159
52	114·6403	65	143·3004	78	171·9604	91	200·6205
53	116·8449	66	145·5050	79	174·1651	92	202·8251
54	119·0495	67	147·7096	80	176·3697	93	205·0298
55	121·2542	68	149·9142	81	178·5743	94	207·2344
56	123·4588	69	152·1188	82	180·7789	95	209·4390
57	125·6634	70	154·3235	83	182·9835	96	211·6436
58	127·8680	71	156·5281	84	185·1182	97	213·8482
59	130·0726	72	158·7327	85	187·3928	98	216·0529
60	132·2773	73	160·9373	86	189·5974	99	218·2575
61	134·4819	74	163·1420	87	191·8020	100	220·4621

TABLE 59.—POUNDS IN KILOGRAMMES.

Pounds.	Kilogs.	Pounds.	Kilogs.	Pounds.	Kilogs.	Pounds.	Kilogs.
1	·4536	26	11·7934	51	23·1332	76	34·4731
2	·9072	27	12·2470	52	23·5868	77	34·9267
3	1·3608	28	12·7006	53	24·0404	78	35·3803
4	1·8144	29	13·1542	54	24·4940	79	35·8338
5	2·2680	30	13·6078	55	24·9476	80	36·2874
6	2·7216	31	14·0614	56	25·4012	81	36·7410
7	3·1752	32	14·5150	57	25·8548	82	37·1946
8	3·6287	33	14·9686	58	26·3084	83	37·6482
9	4·0823	34	15·4222	59	26·7620	84	38·1018
10	4·5359	35	15·8758	60	27·2156	85	38·5554
11	4·9895	36	16·3293	61	27·6692	86	39·0090
12	5·4431	37	16·7829	62	28·1227	87	39·4626
13	5·8967	38	17·2365	63	28·5764	88	39·9162
14	6·3503	39	17·6901	64	29·0300	89	40·3700
15	6·8039	40	18·1437	65	29·4835	90	40·8234
16	7·2575	41	18·5973	66	29·9371	91	41·2770
17	7·7111	42	19·0509	67	30·3907	92	41·7306
18	8·1647	43	19·5045	68	30·8443	93	42·1841
19	8·6183	44	19·9581	69	31·2979	94	42·6377
20	9·0719	45	20·4117	70	31·7515	95	43·0913
21	9·5255	46	20·8653	71	32·2051	96	43·5449
22	9·9790	47	21·3189	72	32·6587	97	43·9985
23	10·4326	48	21·7725	73	33·1123	98	44·4521
24	10·8862	49	22·2261	74	33·5659	99	44·9057
25	11·3398	50	22·6796	75	34·0195	100	45·3593

TABLE 60.—SQUARE METRES IN SQUARE FEET AND SQUARE YARDS.

Square Metres.	Square Feet.	Square Yards.	Square Metres.	Square Feet.	Square Yards.
1	10·7641	1·1960	42	452·0930	50·2320
2	21·5282	2·3920	43	462·8572	51·4280
3	32·2924	3·5880	44	473·6213	52·6240
4	43·0565	4·7840	45	484·3854	53·8200
5	53·8206	5·9800	46	495·1495	55·0160
6	64·5847	7·1760	47	505·9136	56·2120
7	75·3458	8·3720	48	516·6778	57·4080
8	86·1130	9·5680	49	527·4419	58·6040
9	96·8771	10·7640	50	538·2060	59·8000
10	107·6412	11·9600	51	548·9701	60·9960
11	118·4053	13·1560	52	559·7342	62·1920
12	129·1694	14·3520	53	570·4984	63·3880
13	139·9336	15·5480	54	581·2625	64·5840
14	150·6977	16·7440	55	592·0266	65·7800
15	161·4618	17·9400	56	602·7907	66·9760
16	172·2259	19·1360	57	613·5548	68·1720
17	182·9900	20·3320	58	624·3190	69·3680
18	193·7542	21·5280	59	635·0831	70·5640
19	204·5183	22·7240	60	645·8472	71·7600
20	215·2824	23·9200	61	656·6113	72·9560
21	226·0465	25·1160	62	667·3754	74·1520
22	236·8106	26·3120	63	678·1396	75·3480
23	247·5748	27·5080	64	688·9037	76·5440
24	258·3389	28·7040	65	699·6678	77·7400
25	269·1030	29·9000	66	710·4319	78·9360
26	279·8671	31·0960	67	721·1960	80·1320
27	290·6312	32·2920	68	731·9602	81·3280
28	301·3954	33·4880	69	742·7243	82·5240
29	312·1595	34·6840	70	753·4884	83·7200
30	322·9236	35·8800	71	764·2525	84·9160
31	333·6877	37·0760	72	775·0166	86·1120
32	344·4518	38·2720	73	785·7808	87·3080
33	355·2160	39·4680	74	796·5449	88·5040
34	365·9801	40·6640	75	807·3090	89·7000
35	376·7442	41·8600	76	818·0731	90·8960
36	387·5083	43·0560	77	828·8372	92·0920
37	398·2724	44·2520	78	839·6014	93·2880
38	409·0366	45·4480	79	850·3655	94·4840
39	419·8007	46·6440	80	861·1296	95·6800
40	430·5648	47·8400	81	871·8937	96·8760
41	441·3289	49·0360	82	882·6578	98·0720



TABLE 60.—SQUARE METRES IN SQUARE FEET AND SQUARE YARDS (*continued*).

Square Metres.	Square Feet.	Square Yards.	Square Metres.	Square Feet.	Square Yards.
83	893·4220	99·2680	92	990·2990	110·0320
84	904·1861	100·4640	93	1001·0632	111·2280
85	914·9502	101·6600	94	1011·8273	112·4240
86	925·7143	102·8560	95	1022·5914	113·6200
87	936·4784	104·0520	96	1033·3555	114·8160
88	947·2426	105·2480	97	1044·1196	116·0120
89	958·0067	106·4440	98	1054·8838	117·2080
90	968·7708	107·6400	99	1065·6479	118·4040
91	979·5349	108·8360	100	1076·4120	119·6000

TABLE 61.—SQUARE FEET IN SQUARE METRES.

Square Feet.	Square Metres.	Square Feet.	Square Metres.	Square Feet.	Square Metres.	Square Feet.	Square Metres.
1	·0929	26	2·4154	51	4·7380	76	7·0605
2	·1858	27	2·5083	52	4·8309	77	7·1534
3	·2787	28	2·6012	53	4·9238	78	7·2463
4	·3716	29	2·6941	54	5·0167	79	7·3392
5	·4645	30	2·7870	55	5·1096	80	7·4321
6	·5574	31	2·8799	56	5·2025	81	7·5250
7	·6503	32	2·9728	57	5·2954	82	7·6179
8	·7432	33	3·0657	58	5·3883	83	7·7108
9	·8361	34	3·1586	59	5·4812	84	7·8037
10	·9290	35	3·2515	60	5·5741	85	7·8966
11	1·0219	36	3·3444	61	5·6670	86	7·9895
12	1·1148	37	3·4373	62	5·7599	87	8·0824
13	1·2077	38	3·5302	63	5·8528	88	8·1753
14	1·3006	39	3·6231	64	5·9457	89	8·2682
15	1·3935	40	3·7160	65	6·0386	90	8·3611
16	1·4864	41	3·8089	66	6·1315	91	8·4540
17	1·5793	42	3·9018	67	6·2244	92	8·5469
18	1·6722	43	3·9947	68	6·3173	93	8·6398
19	1·7651	44	4·0876	69	6·4102	94	8·7327
20	1·8580	45	4·1805	70	6·5031	95	8·8256
21	1·9509	46	4·2734	71	6·5960	96	8·9185
22	2·0438	47	4·3663	72	6·6889	97	9·0114
23	2·1367	48	4·4592	73	6·7818	98	9·1043
24	2·2296	49	4·5521	74	6·8747	99	9·1972
25	2·3225	50	4·6450	75	6·9676	100	9·2901

TABLE 62.—SQUARE YARDS IN SQUARE METRES.

Square Yards.	Square Metres.	Square Yards.	Square Metres.	Square Yards.	Square Metres.	Square Yards.	Square Metres.
1	·8361	26	21·7389	51	42·6417	76	63·5445
2	1·6722	27	22·5750	52	43·4778	77	64·3806
3	2·5083	28	23·4111	53	44·3139	78	65·2167
4	3·3444	29	24·2472	54	45·1500	79	66·0528
5	4·1806	30	25·0834	55	45·9862	80	66·8890
6	5·0167	31	25·9195	56	46·8223	81	67·7251
7	5·8528	32	26·7556	57	47·6584	82	68·5612
8	6·6889	33	27·5917	58	48·4945	83	69·3973
9	7·5250	34	28·4278	59	49·3306	84	70·2334
10	8·3611	35	29·2639	60	50·1667	85	71·0695
11	9·1972	36	30·1000	61	51·0028	86	71·9056
12	10·0333	37	30·9361	62	51·8389	87	72·7417
13	10·8695	38	31·7723	63	52·6751	88	73·5779
14	11·7056	39	32·6084	64	53·5112	89	74·4140
15	12·5417	40	33·4445	65	54·3473	90	75·2501
16	13·3778	41	34·2806	66	55·1834	91	76·0862
17	14·2139	42	35·1167	67	56·0195	92	76·9223
18	15·0500	43	35·9528	68	56·8556	93	77·7584
19	15·8861	44	36·7889	69	57·6917	94	78·5945
20	16·7222	45	37·6250	70	58·5278	95	79·4306
21	17·5584	46	38·4612	71	59·3640	96	80·2668
22	18·3945	47	39·2973	72	60·2001	97	81·1029
23	19·2306	48	40·1334	73	61·0362	98	81·9390
24	20·0667	49	40·9695	74	61·8723	99	82·7751
25	20·9028	50	41·8056	75	62·7085	100	83·6112

TABLE 63.—CUBIC METRES IN CUBIC FEET AND CUBIC YARDS.

Cubic Metres.	Cubic Feet.	Cubic Yards.	Cubic Metres.	Cubic Feet.	Cubic Yards.
1	35·3156	1·3080	10	353·1560	13·0800
2	70·6312	2·6160	11	388·4716	14·3880
3	105·9468	3·9240	12	423·7872	15·6960
4	141·2624	5·2320	13	459·1028	17·0040
5	176·5780	6·5400	14	494·4184	18·3120
6	211·8936	7·8480	15	529·7340	19·6200
7	247·2092	9·1560	16	565·0496	20·9280
8	282·5248	10·4640	17	600·3652	22·2360
9	317·8404	11·7720	18	635·6808	23·5440

TABLE 63.—CUBIC METRES IN CUBIC FEET AND CUBIC YARDS (*continued*).

Cubic Metres.	Cubic Feet.	Cubic Yards.	Cubic Metres.	Cubic Feet.	Cubic Yards.
19	670·9964	24·8520	60	2118·9360	78·4800
20	706·3120	26·1600	61	2154·2516	79·7880
21	741·6276	27·4680	62	2189·5672	81·0960
22	776·9432	28·7760	63	2224·8828	82·4040
23	812·2588	30·0840	64	2260·1984	83·7120
24	847·5744	31·3920	65	2295·5140	85·0200
25	882·8900	32·7000	66	2330·8296	86·3280
26	918·2056	34·0080	67	2366·1452	87·6360
27	953·5212	35·3160	68	2401·4608	88·9440
28	988·8368	36·6240	69	2436·7764	90·2520
29	1024·1524	37·9320	70	2472·0920	91·5600
30	1059·4680	39·2400	71	2507·4076	92·8680
31	1094·7836	40·5480	72	2542·7232	94·1760
32	1130·0992	41·8560	73	2578·0388	95·4840
33	1165·4148	43·1640	74	2613·3544	96·7920
34	1200·7304	44·4720	75	2648·6700	98·1000
35	1236·0460	45·7800	76	2683·9856	99·4080
36	1271·3616	47·0880	77	2719·3012	100·7160
37	1306·6772	48·3960	78	2754·6168	102·0240
38	1341·9928	49·7040	79	2789·9324	103·3320
39	1377·3084	51·0120	80	2825·2480	104·6400
40	1412·6240	52·3200	81	2860·5636	105·9480
41	1447·9396	53·6280	82	2895·8792	107·2560
42	1483·2552	54·9360	83	2931·1948	108·5640
43	1518·5708	56·2440	84	2966·5104	109·8720
44	1553·8864	57·5520	85	3001·8260	111·1800
45	1589·2020	58·8600	86	3037·1416	112·4880
46	1624·5176	60·1680	87	3072·4572	113·7960
47	1659·8332	61·4760	88	3107·7728	115·1040
48	1695·1488	62·7840	89	3143·0884	116·4120
49	1730·4644	64·0920	90	3178·4040	117·7200
50	1765·7800	65·4000	91	3213·7196	119·0280
51	1801·0956	66·7080	92	3249·0352	120·3360
52	1836·4112	68·0160	93	3284·3508	121·6440
53	1871·7268	69·3240	94	3319·6664	122·9520
54	1907·0424	70·6320	95	3354·9820	124·2600
55	1942·3580	71·9400	96	3390·2976	125·5680
56	1977·6736	73·2480	97	3425·6132	126·8760
57	2012·9892	74·5560	98	3460·9288	128·1840
58	2048·3048	75·8640	99	3496·2444	129·4920
59	2083·6204	77·1720	100	3531·5600	130·8000

TABLE 64.—CUBIC FEET IN CUBIC METRES.

Cubic Feet.	Cubic Metres.	Cubic Feet.	Cubic Metres.	Cubic Feet.	Cubic Metres.	Cubic Feet.	Cubic Metres.
1	·0283	26	·7362	51	1·4450	76	2·1519
2	·0566	27	·7645	52	1·4724	77	2·1803
3	·0849	28	·7928	53	1·5007	78	2·2086
4	·1133	29	·8211	54	1·5290	79	2·2369
5	·1416	30	·8494	55	1·5573	80	2·2652
6	·1699	31	·8778	56	1·5856	81	2·2935
7	·1982	32	·9061	57	1·6140	82	2·3218
8	·2265	33	·9344	58	1·6423	83	2·3501
9	·2548	34	·9627	59	1·6706	84	2·3785
10	·2831	35	·9910	60	1·6989	85	2·4068
11	·3115	36	1·0193	61	1·7272	86	2·4351
12	·3398	37	1·0477	62	1·7555	87	2·4634
13	·3681	38	1·0760	63	1·7838	88	2·4917
14	·3964	39	1·1043	64	1·8122	89	2·5200
15	·4247	40	1·1326	65	1·8405	90	2·5483
16	·4530	41	1·1609	66	1·8688	91	2·5767
17	·4814	42	1·1892	67	1·8971	92	2·6050
18	·5097	43	1·2175	68	1·9254	93	2·6333
19	·5380	44	1·2459	69	1·9537	94	2·6616
20	·5663	45	1·2742	70	1·9820	95	2·6899
21	·5946	46	1·3025	71	2·0104	96	2·7182
22	·6229	47	1·3308	72	2·0387	97	2·7466
23	·6512	48	1·3591	73	2·0670	98	2·7749
24	·6795	49	1·3874	74	2·0953	99	2·8032
25	·7079	50	1·4157	75	2·1236	100	2·8315

TABLE 65.—CUBIC YARDS IN CUBIC METRES.

Cubic Yards.	Cubic Metres.	Cubic Yards.	Cubic Metres.	Cubic Yards.	Cubic Metres.	Cubic Yards.	Cubic Metres.
1	·7645	11	8·4096	21	16·0548	31	23·6999
2	1·5290	12	9·1742	22	16·8193	32	24·4644
3	2·2935	13	9·9387	23	17·5838	33	25·2289
4	3·0581	14	10·7032	24	18·3483	34	25·9934
5	3·8226	15	11·4677	25	19·1128	35	26·7580
6	4·5871	16	12·2322	26	19·8773	36	27·5225
7	5·3516	17	12·9967	27	20·6419	37	28·2870
8	6·1161	18	13·7612	28	21·4064	38	29·0515
9	6·8806	19	14·5257	29	22·1709	39	29·8160
10	7·6451	20	15·2903	30	22·9354	40	30·5805

TABLE 65.—CUBIC YARDS IN CUBIC METRES (*continued*).

Cubic Yards.	Cubic Metres.	Cubic Yards.	Cubic Metres.	Cubic Yards.	Cubic Metres.	Cubic Yards.	Cubic Metres.
41	31·3450	56	42·8127	71	54·2804	86	65·7481
42	32·1095	57	43·5772	72	55·0449	87	66·5126
43	32·8741	58	44·3418	73	55·8094	88	67·2771
44	33·6386	59	45·1063	74	56·5740	89	68·0417
45	34·4031	60	45·8708	75	57·3385	90	68·8062
46	35·1676	61	46·6353	76	58·1030	91	69·5707
47	35·9321	62	47·3998	77	58·8675	92	70·3352
48	36·6966	63	48·1643	78	59·6320	93	71·0997
49	37·4611	64	48·9288	79	60·3965	94	71·8642
50	38·2256	65	49·6933	80	61·1610	95	72·6287
51	38·9902	66	50·4579	81	61·9256	96	73·3932
52	39·7547	67	51·2224	82	62·6901	97	74·1578
53	40·5192	68	51·9869	83	63·4546	98	74·9223
54	41·2837	69	52·7514	84	64·2191	99	75·6868
55	42·0482	70	53·5159	85	64·9836	100	76·4513

TABLE 66.—APPROXIMATE EQUIVALENTS OF FRENCH AND ENGLISH MEASURES.

1 chain (22 yards).	20 metres (exactly 20·1166 metres).
5 furlongs . . . . .	{ 1 kilometre (exactly 1·0058 kilometres).
	{ 3 decimetres (exactly 3·048 decimetres).
1 foot . . . . .	{ 30 centimetres.
	{ 3·28 feet.
1 metre . . . . .	{ 3 feet 3 inches $\frac{3}{4}$ inch ( $\frac{1}{512}$ inch less).
	{ 40 inches (1·6 per cent. less).
1 inch . . . . .	25 millimetres (exactly 25·4).
1 yard . . . . .	$\frac{11}{12}$ metre.
11 metres . . . . .	12 yards.
To convert metres into yards . . . . .	{ Add $\frac{1}{11}$ th.
1 kilometre . . . . .	$\frac{5}{8}$ mile.
1 mile . . . . .	1·6 or $1\frac{3}{5}$ kilometres.
1 square inch . . . . .	6·5 square centimetres.
1 square metre . . . . .	{ 10 $\frac{3}{4}$ square feet.
	{ 1 $\frac{1}{3}$ square yards.
1 square yard . . . . .	$\frac{9}{7}$ square metre.
1 acre . . . . .	{ 4000 square metres (1·2 per cent. more).
1 square mile . . . . .	260 hectares (0·4 per cent. less).

1 cubic yard . . . .	$\frac{3}{4}$ cubic metre (2 per cent. more).
1 cubic metre . . . .	$1\frac{1}{4}$ cubic yard ( $1\frac{1}{2}$ per cent. less).
1 cubic metre . . . .	$35\frac{1}{4}$ cubic feet (.05 per cent. less).
1 litre . . . . .	$1\frac{1}{8}$ pints fully.
1 gallon . . . . .	$4\frac{1}{2}$ litres fully.
1 cubic foot . . . . .	28.3 litres.
1 cubic metre of water .	1 ton nearly.
1 gramme . . . . .	$15\frac{1}{2}$ grains nearly.
1 kilogramme . . . . .	2.2 pounds fully.
1000 kilogrammes } .	1 ton nearly.
1 metric ton } .	
1 hundredweight . . . .	51 kilogrammes nearly.

TABLE 67.—FRENCH AND ENGLISH COMPOUND  
EQUIVALENTS.

1 kilogramme per lineal metre . . . . .	{ .672 pound per lineal foot. 2.016 pounds per yard.
1000 kilogrammes (1 tonne) per metre . . . . .	{ .300 ton per foot.
1 kilogramme per kilometre .	3.548 pounds per mile.
1000 kilogrammes (1 tonne) per kilometre . . . . .	{ 1.584 tons per mile.
1 kilogramme per square millimetre . . . . .	{ 1422.32 pounds per square inch. .635 ton per square inch.
1 kilogramme per square centimetre . . . . .	{ 14.2232 pounds per square inch.
1 kilogramme per square decimetre . . . . .	{ 20.4776 pounds per square foot.
1 kilogramme per square metre . . . . .	{ 1.8430 pounds per square yard.
1000 kilogrammes (1 tonne) per square metre . . . . .	{ .8229 ton per square yard.
1 kilogramme per tonne . . .	2.240 pounds per ton.
1 kilogramme per tonne per kilometre . . . . .	{ 3.6042 pounds per ton per mile.
1 litre of water at 4° C. per tonne per kilometre . . . .	{ 3.6042 pounds per ton per mile. .3599 gallon at 62° F. per ton per mile.
1 gramme per square milli- metre . . . . .	{ 1.422 pounds per square inch.
1 gramme per square centi- metre . . . . .	{ .01422 pound per square inch.
1 kilogramme per cubic metre	{ 1.686 pounds per cubic yard. .0624 pound per cubic foot.
1000 kilogrammes (1 tonne) per cubic metre . . . . .	{ .984 ton per cubic metre. .752 ton per cubic yard.

1 cubic metre per kilogramme	16·019 cubic feet per pound.
1 cubic metre per tonne	{ 1·329 cubic yards per ton. 35·882 cubic feet per ton.
1 cubic metre per kilometre	2·105 cubic yards per mile.
1 gramme per litre	73·09 grains per gallon.
1 kilogramme per litre	10·4382 pounds per gallon.
1 cubic metre per lineal metre	{ 1·196 cubic yards per lineal yard.
1 cubic metre per square metre	3·281 cubic feet per square foot.
1 litre per square metre	·0204 gallon per square foot.
1 cubic metre per hectare	{ ·405 cubic metre per acre. ·529 cubic yard per acre. 89·065 gallons per acre.
1 kilogramme	7·233 foot-pounds.
1 tonne-metre	3 foot-tons.
1 cheval vapeur, or cheval (75k × m per second)	{ ·9863 horse-power.
1 kilogramme per cheval	2·235 pounds per horse-power.
1 square metre per cheval	{ 10·913 square feet per horse- power.
1 cubic metre per cheval	{ 35·806 cubic feet per horse- power.
1 calorie or French unit of heat	{ 3·968 English heat-units.
French mechanical equivalent of heat (425 kilogram- metres)	{ 3074 foot-pounds per unit.
1 calorie per square metre	·369 heat-unit per square foot.
1 calorie per kilogramme	1·800 heat-units per pound.
1 franc per kilogramme	{ ·360 shillings per pound. £40·32 per ton.
1 franc per quintal	·403 shillings per cwt.
1 franc per tonne	{ ·484 penny per cwt. ·806 shilling per ton.
1 franc per metre	{ ·726 shilling per yard. 8·709 pence per yard.
1 franc per kilometre	{ £0·6386 per mile. 15·326 pence per mile.
1 franc per square metre	{ 7·963 pence per square yard. ·6636 shilling per square yard.
1 franc per cubic metre	7·281 pence per cubic yard.
1 franc per litre	3·606 shillings per gallon.
1 franc per hectolitre	1·893 shillings per hogshead.

TABLE 68.—ENGLISH AND FRENCH COMPOUND  
EQUIVALENTS.

1 pound per lineal foot . . .	{ 1·488 kilogrammes per lineal metre.
1 pound per yard . . .	{ ·496 kilogramme per metre.
1 ton per foot . . .	{ 3333·333 kilogrammes (3½ tons) per metre.
1 ton per yard . . .	{ 1111·111 kilogrammes (1½ tons) per metre.
1 pound per mile . . .	{ ·2818 kilogrammes per kilometre.
1 ton per mile . . .	{ ·6313 tonne per kilometre.
1 pound per ton . . .	{ ·4464 kilogramme per tonne.
1 pound per ton per mile . . .	{ ·2774 kilogramme per tonne per kilometre.
	{ ·0703077 kilogramme persquare centimetre.
1 pound per square inch . . .	{ ·7031 gramme per square millimetre.
	{ 5·170 centimetres of mercury at 0° C.
1 atmosphere (14·7 pounds per square inch) . . .	{ 1·0335 kilogrammes per square centimetre.
1000 pounds per square inch . . .	{ ·703077 kilogramme per square millimetre.
2000 pounds per square inch . . .	{ 1·406154 kilogrammes per square millimetre.
1 ton per square inch . . .	{ 1·575 kilogrammes per square millimetre.
1 pound per square foot . . .	{ 4·883 kilogrammes per square metre.
1000 pounds per square foot . . .	{ 4882·517 kilogrammes per square metre.
1 ton per square foot . . .	{ 10·936 tonnes per square metre.
1000 pounds per square yard . . .	{ 542·500 kilogrammes per square metre.
1 ton per square yard . . .	{ 1·215 tonnes per square metre.
1 pound per cubic yard . . .	{ ·5933 kilogramme per cubic metre.
1 pound per cubic foot . . .	{ 16·020 kilogrammes per cubic metre.
1 ton per cubic yard . . .	{ 1·329 tonnes per cubic metre.
1 cubic yard per pound . . .	{ 1·6855 cubic metres per kilogramme.
1 cubic yard per ton . . .	{ ·7525 cubic metre per tonne.
1 cubic yard per mile . . .	{ ·4750 cubic metre per kilometre.



1 grain per gallon . . . .	·01426 gramme per litre.
1 pound per gallon . . . .	·09983 kilogramme per litre.
1 cubic yard per lineal yard .	{ ·836 cubic metre per lineal metre.
1 cubic foot per square foot .	{ 3·048 cubic metres per square metre.
1 gallon per square foot . . .	48·905 litres per square metre.
1 cubic metre per acre . . . .	2·471 cubic metres per hectare.
1 cubic yard per acre . . . .	1·902 cubic metres per hectare.
1000 gallons per acre . . . .	11·226 cubic metres per hectare.
1 foot-pound . . . . .	·1382 kilogrammetre.
1 foot-ton . . . . .	·3333 tonne-metre.
1 horse-power . . . . .	1·0139 cheval.
1 pound per horse-power . . .	·447 kilogramme per cheval.
1 square foot per horse-power .	·0196 square metre per cheval.
1 cubic foot per horse-power .	·0279 cubic metre per cheval.
1 English unit of heat, or heat-unit . . . . .	{ ·252 calorie.
English mechanical equivalent to one heat-unit (772 foot-pounds) . . . . .	{ 10·67 kilogrammetres.
1 English heat-unit per square foot . . . . .	{ 2·713 calories per square metre.
1 English heat-unit per pound .	$\frac{5}{9}$ calorie per kilogramme.
1 penny per pound . . . . .	·231 franc per kilogramme.
1 shilling per pound . . . . .	2·772 franc per kilogramme.
1 shilling per cent., or . . . .	{ 24·802 francs per tonne.
£1 per ton . . . . .	{ 2·48 francs per quintal.
1 shilling per yard . . . . .	1·378 francs per metre.
1 penny per mile . . . . .	·0652 franc per kilometre.
£1 per mile . . . . .	15·660 francs per kilometre.
1 shilling per square yard . . .	1·510 francs per square metre.
£1 per square yard . . . . .	30·194 francs per square metre.
1 penny per cubic foot . . . .	3·708 francs per cubic metre.
1 penny per cubic yard . . . .	·137 franc per cubic metre.
1 shilling per cubic yard . . . .	1·648 francs per cubic metre.
£1 per cubic yard . . . . .	32·962 francs per cubic metre.
1 shilling per hogshead . . . .	·528 franc per hectolitre.
1 penny per gallon . . . . .	·0231 franc per litre.

## EUROPE.

**Austria-Hungary.**

*Length.* 1 Fuss = 1·0371 feet ; 2 Fuss = 1 Elle = 2·0742 feet ;  
 6 Fuss = 1 Klafter = 6·2226 feet ; 4000 Klafter = 1 Meile =  
 4 714 miles.

*Surface.* 1 square Klafter=38·7225 square feet=4·3025 square yards; 1600 square Klafter=1 Joch=1·4223 acres.

*Volume.* 1 cubic Klafter=240·94 cubic feet=8·924 cubic yards.

*Capacity, dry.* 1 Achtel = 1·6920 gallons; 2 Achtel = 1 Viertel = 3·3840 gallons = 4230 bushel; 4 Viertel = 1 Metze = 1·6918 bushels.

*Capacity, liquid.* 1 Kanne = 1·2457 pints; 2 Kannen = 1 Mass = 1·2457 quarts; 10 Mass = 1 Viertel = 3·1143 gallons; 4 Viertel = 1 Eimer = 12·4572 gallons.

*Weight.* 1 Pfund = 1·2347 pounds; 100 Pfund = 1 Centner = 123·47 pounds = 1·1024 hundredweights.

The French metric system of weights and measures is legal in Austria-Hungary.

### Belgium.

The French metric system is in force in Belgium. The name *aune* is substituted for metre, *litron* for litre, *livre* for kilogramme.

### Denmark.

*Length.* 1 Fod = 1·0297 feet; 6 Fod = 1 Favn = 6·1783 feet; 1 Mil = 4·68055 miles.

*Surface.* 1 square Fod = 1·0603 square feet; 144 square Fod = 1 square Rode = 16·966 square yards.

*Volume.* 1 cubic Fod = 1·0918 cubic feet. The Favn of firewood = 6 Fod × 6 Fod × 2 Fod = 72 cubic Fod = 78·60 cubic feet.

*Capacity, liquid.* 38 Potter = 1 Anker = 8·0709 gallons; 136 Potter = 1 Tönde = 28·885 gallons.

*Capacity, dry.* 1 Tönde or barrel of grain or salt = 3·8231 bushels; barrel of coal = 4·7 bushels.

*Weight.* 100 Kvinten = 1 Pund = 1·1023 pounds; 100 Pund = 1 Centner = 110·23 pounds; 40 Centner = 1 Last = 1·9684 tons; 1 Skip-last = 2·5590 tons.

### Germany.

The French metrical system of weights and measures came into force in Germany, on January 1, 1872.

*Length.* The metre is known as the *Stab*; the centimetre, the *Neu-Zoll*; the kilometre is the same; 7 kilometres = 1 mile = 4·35 English miles.

*Surface.* The square metre is the *Quadrat-stab*; the are is the *Ar*; the hectare is the *Hectar*. The square kilometre is the *Quadrat* = 247·11 acres.

*Volume.* 2 Schoppens = 1 Kanne = 1 litre; 50 kannes = 1 scheffel = 50 litres = 1·376 bushels; 2 scheffels = 1 Fass (cask) = 1 hectolitre = 22·01 gallons.

*Weight.* The milligramme, centigramme, and decigramme

are respectively the *Milligram*, *Centigramm*, and *Dezigramm*.  
 100 dezigramms = 1 Neu-loth = 10 grammes =  $\cdot 35273$  ounce;  
 50 neu-loths = 1 Pfund =  $\frac{1}{2}$  kilogramme = 1.1023 pounds; 100  
 pfunds = 1 Centner = 50 kilogrammes = 110.23 pounds; 20  
 centners = 1 tonne = 2204.6 pounds or .9842 ton.

### Greece.

The French metric system is employed in Greece. The metre is the *pecheus*, the kilometre the *stadion*, the are the *stremma*; the litre the *litra*, the gramme the *drachmé*.  
 $1\frac{1}{2}$  kilogrammes = 1 Mnâ;  $1\frac{1}{2}$  quintals = 1 tolanton;  $1\frac{1}{2}$  tonneaux = 1 Tono = 29.526 hundredwt.

### Italy.

The French metric system is in force. The metre is known as the *metro*; the kilometre, *chilometro*; the are, *aro*; the hectare, *ettaro*; the litre, *litro*; the gramme, *gramo*; the tonne, *tonnellata*.

### Netherlands.

The French metric system is in force in the Netherlands. The French nomenclature is followed, with but trifling variations.

### Portugal.

The French metric system is the legal standard. The old measures principally still in use are: the libra = 1.012 pounds; the almude of Lisbon = 3.7 gallons; the almude of Oporto = 5.6 gallons; the alquiere = .36 bushel; the moio = 2.78 quarters.

### Roumania.

The French metric system is in force in Roumania. Turkish weights and measures are largely in use by the people.

### Russia.

*Length.* 1 Vershok = 1.75 inches; 16 Vershoks = 1 Arschine = 28 inches; 3 Arschines = 1 Sajene = 7 feet; 500 Sajenes = 1 Verst = 3,500 feet or .6629 mile. The English foot decimally divided is the ordinary standard of length. The Rhein Fuss (= 1.03 English feet) is used in calculating export duties on timber.

*Surface.* 1 square Arschine = 5.444 square feet; 9 square arschines = 1 square sajeen = 49 square feet; 2,400 square sajeens = 1 Desatine = 2.70 acres. For earthworks, masonry, &c., the sajene is divided into tenths (*dessiatka*), hundredths (*Sotka*), and thousandths (*tisiatchka*). These are squared and cubed, for superficial and cubic measurements.

*Capacity, liquid.* 1 Tsharkey = 2164 pint ; 10 tsharkeys = 1 Krushka = 1.0820 quarts ; 100 tsharkeys = 1 Vedro = 2.7049 gallons ; 3 vedros = 1 anker = 8.1147 gallons ; 40 Vedros = 1 Sarokowaja Boshka = 108.196 gallons.

*Capacity, dry.* (Grain.) 1 Tschetwert = 5.7704 bushels (usually reckoned at  $5\frac{3}{4}$  bushels) ; 16 Tschetwerts = 1 Last = 11.5408 quarters. 100 Tschetwerts are usually reckoned equal to 72 quarters ; they are exactly 72.1308 quarters.

*Weight.* 12 lanas = 32 lottis = 96 Zolotnicks = 1 Funt or pound = .90285 English pound = 14.446 ounces ; 40 pounds = 1 Pood = 36.114 English pounds ; 62.0257 Poods = 1 English ton ; 1 ship-last = 1.89 English tons.

### Servia.

The French metric system has been in use in Servia since 1883. The old Turkish and Austrian weights and measures still linger in outlying districts.

### Spain.

The French metric system has been established in Spain since 1859. The metre is the *metro* ; the litre, the *litro* ; the gramme the *gramo* ; the are, the *area*. The old system continues largely in use.

*Length.* 12 lineas = 1 pulgada = .927 inch ; 12 pulgadas = 1 Pies de Burgos = .9273 foot ; 3 Pies = 1 Vara = 2.782 feet ; 5,000 Varas = 1 Legua (Castilian) = 2.6345 miles ; 8,000 Varas = 1 Legua (Spanish) = 4.2151 miles.

*Surface.* 1 square Vara = .860 square yard ; 16 square Varas = 1 square Estadal = 13.759 square yards ; 576 square Estadals = 1 Fanegada = 1.6374 acres.

*Capacity, liquid.* 4 Cuartillas = 1 Arroba Mayor (for wine) = 3.552 gallons ; 1 Arroba Menor (for oil), 2.7652 gallons.

*Capacity, dry.* 12 Amuerzas = 1 Fanega = 1.5077 bushels.

*Weight.* 8 Octavos = 1 Onza = 1.0144 ounces ; 16 Onzas = 1 Libra = 1.0144 pounds ; 100 Libras = 1 Quintal = 101.442 pounds ; 10 Quintals = 1 Tonelada = 1014.42 pounds.

### Sweden.

The French metric system became obligatory in Sweden in 1889. The following are measures according to the system formerly in use.

*Length.* 10 Tumer = 1 Fot = 11.6892 inches ; 10 Fot = 1 Stang = 9.7411 feet ; 10 Stanger = 1 Ref = 32.4703 yards ; 360 Ref = 1 Meile = 6.6417 miles.

*Surface.* 100 square Tumer = 1 square Fot = .9489 square

foot ; 1 square Ref =  $\cdot 2178$  acre ;  $5\cdot 6$  square Ref = 1 Tunnland =  $1\cdot 2198$  acres.

### Switzerland.

The French metric system has been generally adopted in Switzerland, with some changes of names, and of subdivisions.

*Length.* 10 Zoll = 1 Fuss (3 decimetres) =  $11\cdot 811$  inches ; 6 Fuss = 1 Klafter =  $5\cdot 9056$  feet ; 10 Fuss = 1 Ruthe =  $9\cdot 8427$  feet ; 1600 Ruthen = 1 Lien =  $2\cdot 9826$  miles.

*Surface.* 100 square Fuss = 1 square Ruthe =  $10\cdot 7643$  square yards ; 400 square Ruthen = 1 Juchart =  $\cdot 8694$  acre ; 6400 Jucharten = 1 square Stunde =  $5693\cdot 52$  acres.

*Volume.* 1000 cubic Zoll = 1 cubic Fuss =  $\cdot 9535$  cubic foot ; 1000 cubic Fuss = 1 cubic Ruthe =  $35\cdot 3166$  cubic yards.

*Weight.* 16 Unzen = 1 Pfund ( $\frac{1}{2}$  kilogramme) =  $1\cdot 1023$  pounds ; 100 Pfund = 1 Centner =  $110\cdot 233$  pounds =  $\cdot 9842$  hundred-weight. The Pfund is legally divided into 500 grammes ; but the people generally prefer the divisions into halves, quarters, and eighths.

### Turkey.

*Length.* 1 pike, or drâ, or Andazé (cloth measure) = 27 inches, divided in 24 Kerâts. The Archin (land measure) = 30 inches ; 1 Forsang =  $3\cdot 116$  miles divided into 3 Berri ; Surveyor's Pik, or the Halebi =  $27\cdot 9$  inches ;  $5\frac{1}{2}$  Halebis = 1 reed.

*Surface.* The squares of the Kerât, the Pike, and the Reed. The Feddan is an area of land equal to as much as a yoke of oxen can plough in a day.

*Capacity, dry.* 900 Dirhems = 1 Rottol =  $1\cdot 411$  quarts ; 22 Rottols = 1 Kileh =  $7\cdot 762$  gallons, or  $\cdot 97$  bushels ; the chief measure for grain, 100 Kilehs =  $12\cdot 128$  imperial quarters.

*Capacity, liquid.* 1 Almud =  $1\cdot 152$  gallons ; 1 Rottol =  $2\cdot 5134$  pints ; 100 Rottols = 1 Cantar =  $31\cdot 417$  gallons.

*Weight.* The Oke =  $2\cdot 8342$  pounds ; 100 Rottolos = 1 Cantar =  $124\cdot 704$  pounds.

### Malta.

*Length.*  $3\frac{1}{2}$  palmi = 1 yard ; 1 Canna =  $2\frac{2}{3}$  yards.

*Surface.* 1 Salma =  $4\cdot 964$  acres. Approximately, 543 square palmi = 400 square feet ; 16 Salmi = 71 acres.

*Volume.* 1 cubic Tratto = 8 cubic feet ; 1 cubic Canna = 343 cubic feet.

*Weight.* 15 Oncie = 14 ounces ; 1 Rotolo =  $1\frac{1}{2}$  pounds ; 64 Rotoli = 1 hundredwt. ; 1 Cantaro = 175 pounds ; 1 Quintal = 199 pounds ; 64 Cantari = 5 tons.

The weights and measures of Turkey, England, and France, are all in use. The principal units are :—

1 Cantaro = 44 oche = 121·0 pounds (English).

1 Oca = 400 dramme = 2·75 pounds.

1 Dramma = 48·15 grains.

1 Picco = 2·296 feet.

1 Scala = 1914·4 square yards.

### Candia.

The Pic = 25·11 inches ; the Carga (corn) = 4·19 bushels ; the Rotolo = 1·165 pounds ; 100 Rotolos = 1 Cantaro = 116·5 pounds ; the Okka = 2·65 pounds.

## ASIA.

### Burmah.

The British yard, foot, and inch are in use in Burmah ; also the British measures of capacity.

The tounge or cubit of 3 maik or span =  $19\frac{1}{2}$  inches ; 4 tounge = 1 lan (fathom) ; 7 tounge = 1 ta ; 1000 ta = 1 taing, nearly two English miles.

Measures of capacity depend upon the teng or basket, the value of which varies for different localities : holding from 23 pounds to 50 pounds of rice. An endeavour has been made to introduce a standard basket, containing 2218·19 cubic inches, not as yet successfully.

1 Kyat = 252 grains ; 100 Kyats = 1 Piet-tha = 3·652 pounds avoirdupois.

### Ceylon.

The weights and measures of Ceylon are the same as those of the United Kingdom. There are also the Seer = 1·86 pints ; 10 parrahs = 1 Amomam = 5·6 bushels.

### China.

The Chih of 14·10 English inches is the legal standard in the tariff settled by treaty between Great Britain and China. It is the only authorised measure of length at all the ports of trade. The Fên = ·141 inch ; the Tsun = 1·41 inches ; 10 Chih = 1 Cháng = 11·75 feet ; 10 Cháng = 1 Yin = 39·17 yards. At Canton there are four different values of the chih ; at Pekin, there are thirteen different chih.

*Surface.* 25 square Chih = 1 Kung = 3·36 square yards ; 240 Kung = 1 Mou =  $806\frac{2}{3}$  square yards ; 100 Mou = 1 King =  $16\frac{2}{3}$  acres. The Mou is the chief land measure.

*Capacity.* The Tou =  $2\frac{1}{2}$  gallons.

*Weight.* The Tael =  $1\frac{1}{2}$  ounces ; the Katty =  $1\frac{1}{2}$  pounds ; the Picul =  $133\frac{1}{2}$  pounds.

### Cochin China.

The Thuoe, or Cubit, 19·2 inches, is the principal unit of length ; but it varies for different places. The Li is 486 yards ; 10 Li = 1 league = 2·761 miles. 9 square Ngu = 1 square Saö = 64 square yards ; 100 square Saö = 1 square Maö = 1·32 acres. 1 Ai = ·0000006 grain ; 1 Nen = ·8594 pound ; 1 Quan =  $687\frac{1}{2}$  pounds ; 1 Hao (grain) =  $6\frac{1}{2}$  gallons.

### Dutch East Indies—Java.

The legal weights and measures of Dutch India are those of the Netherlands. In Java, other measures are in common use. The Duim = 1·3 inches ; the Ell = 27·08 inches. The Djong of 4 Bahu = 7·015 acres. Measures of capacity are taken by definite weight : 1 Sack = 61·034 pounds ; 2 Sacks = 1 Pecul = 122·068 pounds. For liquids, the Kan = ·328 gallon ; the Leager = 127·34 gallons. For weights, the Tael = 1·36 ounces ; the Pecul = 135·63 pounds.

### Hong Kong.

The British weights and measures are in general use in Hong Hong. There are also the Tael =  $1\frac{1}{2}$  ounces ; the Picul = 133 pounds ; the Catty =  $1\frac{3}{4}$  pounds ; the Chek =  $14\frac{1}{2}$  inches ; the Cheung =  $12\frac{1}{16}$  feet.

### India—Bengal.

*Length.* 1 Jow, or Jaub =  $\frac{1}{2}$  inch ; 1 Guz = 1 yard ; 1 Coss = 2000 yards, or 1·1364 miles. But the Coss varies from 1 mile to 2 miles in different districts. In the Punjab it is generally 2 miles.

*Surface.* 4 square Hât'hs = 1 Cowrie = 1 square yard ; 1 Beegah = 1600 square yards, or ·3306 acre. For Government surveys, the following table is used :—

1 Guz . . . . .	33 lineal inches.
3 Guz . . . . .	1 Baus, or Rod . . . . . $8\frac{1}{4}$ lineal feet.
9 Square Guz . . . . .	1 Square Baus . . . . . $68\frac{1}{16}$ square feet.
400 Square Baus . . . . .	1 Beegah . . . . . $\left\{ \begin{array}{l} 3025 \text{ square yards,} \\ \cdot 625 \text{ acre.} \end{array} \right.$

*Capacity.* The Seer is taken at 68 cubic inches, or 1·962 pints. But it varies. 5 Seer = 1 Palli ; 40 Seer = 1 Maund = 9·81 gallons. The Sooli = 3·065 bushels.

*Weight.* The Tola = 180 grains, the weight of a rupee, is the unit of weight ; 5 Tolas = 1 Chittāk ; 80 Tolas = 1 Seer = 2·057 pounds ; 40 Seers = 1 Maund = 82·286 pounds.

**India—Bombay.**

The Tussoo =  $1\frac{1}{4}$  inches ; 16 Tussoos = 1 Hat'h = 18 inches ; 24 Tussoos = 1 Guz = 27 inches. The Builder's Tussoo = 2.3625 inches in Bombay ; and 1 inch in Surat.

*Surface.* The Kutty = 9.8175 square yards ; 20 Kutty = 1 Pund = 196.35 square yards ; 20 Pund = 1 Beegah = .8114 acre. In the Revenue Field Survey the English acre is used.

*Capacity.* The Seer = .56 pint ; 4 Seers = 1 Pylee = 2.2401 pints ; 16 Pylees = 1 Parah = 4.4802 gallons ; 8 Parahs = 1 Candy = 35.8415 gallons ; 25 Parahs = 112.0045 gallons. In timber measurement in Bombay Dockyards, a Covit or Candy = 12.704 cubic feet.

*Weight.* 1 Seer = 11.2 ounces, 1 Maund = 28 pounds ; 1 Candy = 5 cwt.

According to an Act passed in 1871, the primary standard of weight is a *Ser*, equal in weight to one kilogramme = 2.205 pounds avoirdupois. For capacity, the litre is the Standard. The divisions to be decimal.

**India—Madras.**

The British foot and yard are in use. The Guz = 33 inches ; the Baum or Fathom is about  $6\frac{1}{2}$  feet. The Nalli-Valli is a little less than  $1\frac{1}{2}$  miles ; 7 Nalli-Valli = 1 Kâdam, or about 10 miles.

1 Span = 8 inches ; 1 Cubit = 18 inches : 8000 Cubits = 1 Cos = 2.27 miles.

*Surface.* 1 Coolie = 64 square yards ; 100 Coolies = 1 Cawnie = 1.3223 acres.

*Capacity.* 8 Ollucks = 1 Puddee = 1.442 quarts ; 8 Puddees = 1 Mercâl = 2.885 gallons ; 5 Mercâls = 1 Parah = 14.426 gallons ; 80 Parahs = 1 Garec = 18.033 quarters. These measures of capacity, though legal, are not commonly used. The "Customary" Puddee, in general use, has, when slightly heaped, a capacity of 1.504 quarts. The Seer measure is the most common, measuring from  $66\frac{1}{2}$  to 67 cubic inches.

*Weight.* The Tola = 180 grains ; 3 Tolas = 1 Pollum = 1.234 ounces ; 8 Pollums = 1 Seer = 9.874 ounces ; 5 Seers = 1 Viss = 3.086 pounds ; 8 Viss = 1 Maund = 24.686 pounds ; 20 Maunds = 1 Candy = 4.480 hundredwts. The Vis is usually reckoned as  $3\frac{1}{4}$  pounds ; the Maund as 25 pounds ; the Candy as 500 pounds.

**Japan.**

*Length.* The Sun = 1.20 inches ; 10 Sun = 1 Shiaku = 1 foot nearly ; 10 Shiaku = 1 Jô = 9 feet  $11\frac{1}{4}$  inches ; 60 Ken = 1 Chô = 119.4 yards ; 36 Chô = 1 Ri = 2.442 miles. Cloth is measured by the Shiaku of 15 inches, divided decimally.



*Surface.* 30 Tsubo=1 Se=118·615 square yards; 100 Se=1 Chō=2·451 acres.

*Capacity.* 10 Gō=1 Shō=·3973 gallon; 10 Shō=1 To=3·970 gallons; 10 To=1 Koku=39·703 gallons.

*Weight.* 10 Fun=1 Momme=57·97 grains; 100 Momme=1 Hiyaku-me=·828 pound; 1000 Momme=1 Kwam-me=8·282 pounds; 160 Momme=1 Kiu=1½ pounds; 100 Kiu=1 Hiyak-Kin=132½ pounds.

### Java. (*See Dutch East Indies.*)

### Persia.

The unit of length is the Zer, of various lengths; the most common length is 40·95 inches. 16 Gerehs=1 Zer. A Farsakh varies from 3·87 miles to 4½ miles in length.

*Surface.* The measure of surface is the Jerib=from 1000 to 1066 square Zer of 40·95 inches=from 1294 to 1379 square yards.

*Capacity.* (Dry Goods.) 1 Sextario = ·07236 gallon; 1 Artata=1·809 bushels. Liquids are sold by weight.

*Weight.* The unit of weight is the Miskâl = 71 grains; 100 Miskâls=1 Rotel=1·014 pounds. 640 Miskâls=1 Batman (of Tabreez)=6·49 pounds; 100 Batman (of Tabreez)=1 Karwâr=649·142 pounds.

The Batman or Mau is the weight by which most articles are sold. It has very various values in different districts. Corn, straw, coal, &c., are sold by the Karwâr.

### Siam.

1 Niu = ·9875 inch; 1 Sen=131 feet 8 inches; 1 Yot=9 miles, 1715 yards, 1 foot, 8 inches. 1 Chang=2½ pounds; 50 Chang=133½ pounds.

### Straits Settlements.

The unit measure of length is the yard; land is measured by the acre.

The Chupak or quart, of 4 paus=8 imperial gills; 4 quarts=1 gantang or gallon=32 gills.

16 Tahil = 1 Kati = 1½ pound; 100 Kati = 1 Picul = 133½ pounds; 40 Picul = 1 Koyan=533½ pounds.

### AUSTRALASIA.

In Fiji, New South Wales, New Zealand, Queensland, South Australia, Tasmania, Victoria, Western Australia, the legal

weights and measures are those of the United Kingdom. But the old British measures of capacity are still in use.

In land measurement, a "section" is an area equal to 80 acres.

## AFRICA.

### Algeria.

The French metrical system only is in use.

### Arabia.

The Egyptian weights and measures are used in Arabia.

### Cape Colony.

The British system of weights and measures is in use ; excepting for land measure, for which the unit is the old Amsterdam Morgen, equal to 2.11654 acres ; but it is usually reckoned as 2 acres.

1 Cape foot is equal to 1.033 British foot.

### Egypt.

The French metric system was legally established in Egypt in 1876.

*Length.* In the old system in general use the Pik is the unit of length. The Pik or cubit of the Nile = 20.65 inches ; the indigenous Pik = 22.37 inches ; the Pik of merchandise = 25.51 inches ; the Pik of construction = 29.53 inches ; 4.73 Piks of construction = 1 Kassaba, in surveying = 11.65 feet.

*Surface.* 1 square Pik = 6.055 square feet ; 22.41 square Piks = 1 square Kassaba = 15.07 square yards ; 333.33 square Kassaba = 1 Feddan = .9342 acre.

*Capacity.* 1 Kelah = 3.367 gallons ; 2 Kelahs = 1 Webek = 6.734 gallons ; 6 Webeks = 1 Ardeb = 40.404 gallons = 6.48 cubic feet. The Guirbah of water is  $\frac{1}{16}$  cubic metre = 2.354 cubic feet.

*Weight.* 16 Kerats = 1 Dirhem = 1.792 drachms ; 12 Okiehs or 144 Dirhems = 1 Rottol = .9821 pound ; 100 Rottols = 1 Kantar = 98.207 pounds. 1 Oke = 2.728 pounds.

### Liberia.

The weights and measures of Liberia are mostly British.

### Mauritius.

The metric system, decreed by the Government of India in 1871, came into force in Mauritius in 1878.

**Morocco.**

*Length.* 8 Tomins = 1 Drah = 22·482 inches.

*Capacity.* 4 Muhds = 1 Saâ = 12·3254 gallons.

*Weight.* 20 Uekieh = 1 Rotal or Artal = 1·12 pounds; 100 Rotals = 1 Kintar = 112 pounds; for imported articles. There is also the Kintar of 168 pounds (100 Rotals) for internal produce.

Oil is sold by the Kula; the Tangier Kula weighs 28 Rotals = 47 pounds English = 5·29 gallons.

**South African Republic.**

The weights and measures are the same as those of Cape Colony.

**Tunis.**

*Length.* The Dhraâ or Pike is the unit of length. The Arabian Dhraâ, for cotton goods, is 19·224 inches long; the Turkish Dhraâ, for lace and silk; the Dhraâ Endaseh for cloth, 26·4888 inches. The Mil Sahâri = 9149 mile.

*Capacity.* The Kaffis = 16 Huebas, each of 12 Sabs = 16 bushels.

*Weight.* 100 Rottolos = 1 Cantar = 109·15 pounds.

**AMERICA.****Argentine Republic.**

The French metric system was, in 1887, legally and compulsorily established. The old weights and measures comprised the Quintal of 101·40 pounds; the Arroba, 25·35 pounds; the Fanega, 1½ bushels.

**Bolivia.**

The Vara = ·927 yard; the square Vara = ·859 square yard.

The gallon = ·74 imperial gallon; the Arroba, of 25 pounds, = 25·36 pounds avoirdupois; the Arroba for wines and spirits = 6·70 imperial gallons.

The ounce = 1·014 ounce avoirdupois; 16 ounces = 1 Libra = 1·014 pound; 100 Libras = 1 Quintal = 101·44 pounds.

**Brazil.**

The French metric system is legally established. The old weights and measures are still partly in use.

*Length.* The Pollegada = 1·0936 inches; the Pé = 13·1236 inches, or ¼ metre; the Vara = 1·215 yards; the Milha = 1·2965 miles; 3 Milhas = 1 Legoa = 3·8896 miles; 5 Varas are reckoned equal to 6 yards.

*Surface.* 64 square Polegadas=1 square Palmo=.5315 square foot; 25 square Palmos=1 square Vara; 4 square Varas=1 square Braça=5.9063 square yards; 4840 square Varas=1 Geira=1.4766 acres.

*Weight.* The Arratel=1.0119 pounds; 32 Arratels=1 Arroba=32.38 pounds; 4 Arrobas=1 Quintal=129.518 pounds; 13½ Quintals=1 Tonelada=15.6116 hundredwts. Ship's freight is reckoned by the English ton taken as equal to 70 Arrobas.

### Canada.

The legal weights and measures are the Imperial yard, the Imperial pound avoirdupois, the Imperial gallon, and the Imperial bushel. The Imperial system is practised, with the exception that the hundredweight=100 pounds, and the ton=2000 pounds. The French metric system is permissive, concurrently with the Standard System.

For sale and delivery of the undermentioned articles, the bushel is to be determined by weighing, unless a bushel by measure be specially agreed upon. The weights equivalent to a bushel are added:—

	lbs.		lbs.
Wheat . . . . .	60	Potatoes } . . . . .	60
Indian corn . . . . .	56	Turnips } . . . . .	60
Rye . . . . .	56	Carrots } . . . . .	60
Peas . . . . .	60	Parsnips } . . . . .	60
Barley . . . . .	48	Beets } . . . . .	60
Malt . . . . .	36	Onions } . . . . .	60
Oats . . . . .	34	Bituminous coal . . . . .	70
Beans . . . . .	60	Clover seed . . . . .	60
Flax seed . . . . .	50	Timothy . . . . .	48
Hemp . . . . .	44	Buck wheat . . . . .	48
Blue grass seed . . . . .	14		
Castor beans . . . . .	40		

### Chili.

The French metric system has been legally established in Chili; but the ancient weights and measures are still in use. These are the same as those of Bolivia.

### Colombia.

The French metric system is legally established in Colombia. In Custom House business, the kilogramme is the standard of weight. The old weights and measures continue in use in ordinary commerce. The Arroba, of 25 Spanish pounds or 12½ kilogrammes; the Quintal, of 100 Spanish pounds, or 50 kilogrammes; and the Carga, of 250 Spanish pounds, or 125 kilogrammes, are generally used. The libra, or pound

is equal to 1·102 pounds avoirdupois. The yard is the usual measure of length. The Colombian Vara, 80 centimetres, is also used. In liquid measure, the French litre is the legal standard.

#### **Costa Rica.**

The French metric system is in use, and its legal establishment is contemplated. The old weights and measures of Spain are in general use.

#### **Cuba.**

The old weights and measures of Spain are in general use. In engineering and carpentry, English and French measures also are in use. The French metric system is legalised, and is used in the Customs departments.

#### **Ecuador.**

The French metric system is the legal standard of this republic.

#### **Guatemala.**

The old weights and measures of Spain are in general use in Guatemala.

#### **Haiti.**

The French metric weights and measures are in use in Haiti.

#### **Honduras.**

The old weights and measures of Spain are in general use in Honduras.

#### **British Honduras.**

The British weights and measures are in use in British Honduras.

#### **Mexico.**

The weights and measures of the French metric system are legally established in Mexico. But the old Spanish measures are still in use.

#### **Nicaragua.**

The system of weights and measures in Nicaragua is that of the old weights and measures of Spain.

#### **Paraguay.**

The old weights and measures of Spain are in general use in Paraguay.

**Peru.**

The old weights and measures are the same as those of Bolivia and Chili. The French metric system was established in 1860, but is not yet in common use, except for the Customs tariff.

**Salvador.**

The weights and measures in common use in Salvador are the same as in the old Spanish system. The French metric system was introduced in 1885.

**St. Domingo.**

The old Spanish weights and measures are in general use. The French metric system also is in use.

**United States of America.**

The British Imperial system of weights and measures is employed in the United States, with the exception of the measures of capacity for dry goods and for liquids, which are the same as the old English measures. The standard U.S. gallon is the same as the old English wine gallon, or 231 cubic inches, capable of holding 8.33888 pounds of pure water of maximum density, at  $39.1^{\circ}$  F.; or  $8\frac{1}{4}$  pounds at  $62^{\circ}$  F. The U.S. gallon is thus  $83\frac{1}{3}$  per cent. or  $\frac{5}{6}$ ths of the Imperial standard gallon.

The chain for land measurement is 100 feet long, and each foot is divided into tenths.

In City measurements the inch is the unit, divided into tenths.

In mechanical measurements, the inch is the unit, divided into 100 parts.

1 cord of wood is (4 feet  $\times$  4 feet  $\times$  8 feet) = 128 cubic feet.

In addition to the legalised scale of weights, the same as that of Great Britain and Ireland, there are the Quintal or Centner of 100 pounds; and the New York ton of 2,000 pounds, which is also used in the other States of the Union. These, the Centner and the New York ton, have practically superseded the British hundredweight and ton.

The French metric system of weights and measures has been legalised concurrently with the existing system.

TABLE 69.—AMERICAN STANDARD WIRE-GAUGE.  
(Brown and Sharpe's.)  
For Sheets and Wire.

Mark.	Size.	Mark.	Size.	Mark.	Size.	Mark.	Size.
	Inch.		Inch.		Inch.		Inch.
4/0	·4600	8	·1285	19	·0359	30	·01003
3/0	·4096	9	·1144	20	·0320	31	·00893
2/0	·3648	10	·1019	21	·0285	32	·00795
0	·3249	11	·0907	22	·0253	33	·00708
1	·2893	12	·0808	23	·0226	34	·00603
2	·2576	13	·0720	24	·0201	35	·00561
3	·2294	14	·0641	25	·0179	36	·00500
4	·2043	15	·0571	26	·0159	37	·00445
5	·1819	16	·0508	27	·0142	38	·00397
6	·1620	17	·0453	28	·0126	39	·00353
7	·1443	18	·0403	29	·0113	40	·00314

TABLE 70.—LIQUID MEASURE (AMERICAN).

Imperial Gallons.

4 gills . . . . .	1 pint		
2 pints . . . . .	1 quart		
4 quarts (231 cubic inches)	1 gallon . . . . .	·8333	
31½ gallons . . . . .	1 barrel . . . . .	26·250	
63 gallons . . . . .	1 hogshead . . . . .	52·50	
2 hogsheads . . . . .	1 pipe, or butt . . . . .	105·00	
2 pipes . . . . .	1 tun . . . . .	210·00	

TABLE 71.—DRY MEASURE (AMERICAN).

2 pints . . . . .	1 quart		
4 quarts (268·8025 cubic inches)	1 gallon . . . . .	·96945	Imperial gallon.
2 gallons . . . . .	1 peck . . . . .	1·9388	do. peck
4 pecks . . . . .	1 struck bushel . . . . .	·96945	do. bushel

**Uruguay.**

The French metrical system has been officially adopted ; but it is not in general use. The old weights and measures are the same as those of the Argentine Republic. The weights and measures of Brazil are in general use.

**Venezuela.**

The French metrical system has been legally established. The system in general use is the same as that of Colombia.

**West Indies.**

The weights and measures are the same as those of the United Kingdom.

## MONEY.

## Great Britain and Ireland.

		WEIGHT. Grains.
4 farthings . . . }	1 penny . . .	145·833 bronze.
2 halfpence . . . }	1 threepenny piece . . .	21·818 silver.
3 pence . . .	1 sixpence . . .	43·636 "
6 pence . . .	1 shilling . . .	87·273 "
12 pence . . .	1 florin . . .	174·545 "
2 shillings . . .	1 half-crown . . .	218·182 "
2½ shillings . . .	1 half-sovereign . . .	61·6372 gold.
10 shillings . . .	1 sovereign, or pound } sterling . . . }	123·2745 "
20 shillings . . .		

*Approximate Diameters and Weights.*

	Diameter.	Weight.
1 farthing . . .	·80 inch . . .	$\frac{1}{16}$ ounce.
1 halfpenny . . .	1·0 " . . .	$\frac{1}{8}$ "
1 penny . . .	1·2 " . . .	$\frac{1}{4}$ "
1 threepenny piece	$\frac{5}{8}$ " . . .	$\frac{1}{20}$ "
1 sixpence . . .	$\frac{3}{4}$ " . . .	$\frac{1}{16}$ "
1 shilling . . .	$\frac{29}{32}$ " or ·90 inch . . .	$\frac{1}{8}$ "
1 florin . . .	$1\frac{5}{32}$ " or 1·16 " . . .	$\frac{1}{4}$ "
1 half-crown . . .	$1\frac{1}{4}$ " . . .	$\frac{1}{2}$ "
1 half-sovereign . . .	$\frac{5}{4}$ " . . .	$\frac{1}{2}$ " fully.
1 sovereign . . .	$2\frac{7}{32}$ " or ·84 inch . . .	$\frac{1}{2}$ " fully.

*Composition.*

Bronze :—Copper, tin, and zinc.

Silver :—Fine silver, 92½ per cent. ; alloy, 7½ per cent.

Gold :—Fine gold, 91½ per cent. ; alloy, 8½ per cent.

*Intrinsic Value.*

480 pence equal to £1 sterling.

22 shillings equal to £1 sterling.

Mint price of Standard Gold, £3 17s. 10½d. per ounce.

France.		EQUIVALENT VALUE. Penny.	
Bronze.	Weight.	Diameter.	
1 centime . . . $\frac{1}{100}$ franc	1 gramme	15 millimetres	·10
2 centimes . . . $\frac{1}{50}$ "	2 "	20 "	·20
5 centimes } (sou) . . . $\frac{1}{20}$ "	5 "	25 "	·50
10 centimes } (gros sou) } $\frac{1}{10}$ "	10 "	30 "	1·00



				EQUIVALENT VALUE.	
<i>Silver.</i>		Weight.	Diameter.	Pence.	
20 centimes	$\frac{1}{5}$ franc	1 gramme	16 millimetres	2	
50 centimes	$\frac{1}{2}$ „	2.5 „	18 „	4 $\frac{3}{4}$	
100 centimes	1 „	5 „	23 „	9 $\frac{1}{2}$	
				more )	9.524
				exactly }	
2 francs	2 „	10 „	27 „	1s. 7d.	
5 francs	5 „	25 „	37 „	3s. 11 $\frac{5}{8}$ d.	
<i>Gold.</i>				£	s. d.
5 francs	1.61290 grammes	17 millimetres		3	11 $\frac{5}{8}$
10 francs	3.22580 „	19 „		7	11 $\frac{1}{4}$
20 francs	6.45161 „	21 „		15	10 $\frac{1}{2}$
(napoleon)	= 99.56 grains				
50 francs	16.12903 grammes	28 „		1	19 8 $\frac{1}{2}$
100 francs	32.25806 „	35 „		3	19 4 $\frac{1}{10}$

The above English values of French coins are calculated at the rate of 25 francs 20 centimes to £1 sterling. The standard fineness of the gold pieces is 90 per cent., with 10 per cent. of copper.

A Monetary Convention exists between France, Belgium, Italy, Switzerland, and Spain, adopting the gold and silver coins above noted.

### Germany.

The mark, of 100 pfennigs, is a silver coin of the value of 11 $\frac{3}{4}$  pence. The 10-mark gold piece is of the value of 9s. 9 $\frac{1}{2}$ d. English money. The 20-mark gold piece is equivalent to 19s. 7d.; it weighs 122.92 grains. One thaler is nearly equal to 3 marks; it is equal to 3 shillings.

### Other Countries in Europe.

*Belgium.*—The monetary system is the same as that of France.

*Denmark.*—There is a decimal system of currency. 1 krone = 100 öre. 18 kronen = £1.

*Greece.*—The drachma = 1 franc; and 100 lepta = 1 drachma.

*Italy.*—The monetary system is the same as that of France. The lira, of 100 centesimi, = 1 franc.

*The Netherlands.*—The guilder or florin, of 100 cents, = 1s. 8d. English; or 12 guilders = £1.

*Portugal.*—The milreis, or 1,000 reis, = 4s. 5 $\frac{1}{2}$ d.; about 4 $\frac{1}{2}$  milreis = £1; 18 $\frac{3}{4}$  reis = 1 penny. One corda (gold coin) = 10,000 reis = £2 4s. 5 $\frac{1}{2}$ d.; and weighs 17.735 grammes.

*Roumania.*—The French decimal monetary system is practised, of which the unit is the lei = 1 franc.

*Russia*.—The silver rouble=100 kopecks, is the legal unit of money=3*s.* 2·054*d.* English. There are three gold coins; the three-rouble, five-rouble, and ten-rouble pieces. The marc of Finland=1 franc.

*Servia*.—The French monetary system is adopted. The dinar=1 franc. The gold milan=20 francs.

*Spain*.—The peseta, of 100 centimos, =1 franc. It is equal to 4 reals, of which there are about 100 to the £1. The 25-peseta piece is 19*s.* 9½*d.* English value.

*Sweden, Norway*.—The Swedish krona, of 100 öre, =1*s.* 1½*d.*; or 18 to £1. Norway.—The krone is of the same value as the Swedish krona.

*Switzerland*.—The French monetary system is legalised. The franc=10 batzen=100 rappen.

*Turkey*.—The lira or gold medjidieh, of 100 piastres, =18*s.* 064*d.* The piastre=2·16*d.*

### Malta.

1 scudo of 12 tari=1*s.* 8*d.* British money is in general circulation. The English sovereign is equal to 12 scudi; the shilling is equal to 7 tari 4 grani (20 grani=1 taro).

### Cyprus.

1 piastra, of 40 para, =1·4*d.* English. Turkish, English, and French moneys also are in circulation.

### Asia.

*Ceylon*.—The rupee of British India, with cents. The exchange value in 1887 was 1*s.* 6*d.*

*China*.—The haikwan tael=10 mace=100 candereens=1,000 cash. Rate of exchange in 1887, 5*s.* 0½*d.*

*Dutch East Indies, Java*.—The guilder, or florin = 100 centen = 1*s.* 8*d.*

*Hong Kong*.—The Mexican dollar=100 cents; average rate of exchange, 3*s.* 2*d.* The Chinese tael=4*s.* 5*d.*

*India*.—The pie=½ farthing; 3 pie=1 pice=1½ farthing; 4 pice=1 anna=1½*d.*; 16 annas=16 rupee=2*s.* 15 rupees=1 gold mohur=30*s.* 100,000 rupees is a lac of rupees; 10 millions are a crore of rupees.

*Japan*.—The yen, or dollar, of 100 sens; nominal value, 4*s.*; real value (1887), 3*s.* 4*d.*

*Persia*.—The krân is 7½*d.*=20 shâhîs; 1 shabi=·3582*d.*

*Siam*.—1 tical or bat=64 atts; rate of exchange, 2*s.* 1*d.*

*Straits Settlements*.—The legal tenders are, the dollar issued from Her Majesty's Mint at Hong Kong, the silver dollar of

Spain, Mexico, Peru, Bolivia, the American trade dollar, and the Japanese dollar, or yen.

*Australasia*.—The moneys are the same as those of the United Kingdom.

### Africa.

*Algeria*.—The French monetary system is practised.

*Cape Colony*.—The English monetary system is practised.

*Egypt*.—1 piastre (tariff) of 10 dimes or 40 paras = 2·461 pence ; 97½ piastres = £1 sterling ; 100 piastres = £1 Egyptian = £1 0s. 6d. 1 piastre (tariff) = 2 piastres (current).

*Liberia*.—Chiefly British money current.

*Madagascar*.—The only legalised coin is the silver five-franc piece. The Italian five-lire piece is accepted.

*Mauritius*.—The Indian rupee is the standard coin.

*Morocco*.—6 flocs = 1 blankeel or muzoona = ·09 penny.

4 blankeels = 1 ounce, or okia = ·38 „

10 ounces = 1 mitkal = 3·08 „

Spanish and French money are current in Morocco.

*Tunis*.—The piastre, of 16 karubs ; average value, 6d. Spanish and French money are current in Tunis.

*Zanzibar*.—The Indian rupee is the coin universally current ; though there is a special coinage issued under the authority of the Sultan, of which the dollar is the unit, of equal value with the American coins.

### America.

*Argentine Republic*.—The silver dollar of 100 centesimos ; average rate of exchange, 4s.

*Bolivia*.—The boliviano, or dollar of 100 centesimos, struck on the basis of the five-franc piece. Present value (1887), 3s. 4d.

*Brazil*.—The milreis of 1,000 reis. Par value, 2s. 3d.

*Canada*.—The dollar, of 100 cents ; rate of exchange, 4s. The value of the English sovereign is by law equal to 4 dollars and 86½ cents.

*Chili*.—The silver peso, of 100 centavos ; nominally 1 dollar, but actually coined on the basis of the five-franc piece ; value, 3s. 4d.

*Colombia*.—The peso or dollar, of 10 reales ; actual value, 3s. 4d. ; nominally, 4s.

*Costa Rica*.—The dollar of 100 centavos ; nominal value, 4s. ; present value, 3s. 6d.

*Equador*.—The monetary unit is the sueré, equal to a five-franc piece. Average rate of exchange, 36½ pence.

*Guatemala.*—The dollar, or piaster, of 100 centavas ; approximate value, 4*s*.

*Haiti.*—The dollar, or piastre ; nominal value, 4*s*. ; real value, 3*s*. 4*d*.

*Honduras.*—The dollar of 100 cents ; nominal value, 4*s*. ; real value, 3*s*. 4*d*.

*Mexico.*—The silver peso of 100 cents ; nominal value, 4*s*. ; real value, 3*s*. 1½*d*.

*Nicaragua.*—The same as for Honduras.

*Paraguay.*—The peso, or dollar=100 centavos ; nominal value, 4*s*. ; real value, 3*s*.

*Peru.*—The sole=100 centesimos ; nominal value, 4*s*. ; real value, 3*s*. 4*d*.

*Salvador.*—The peso, or piastre, of 8 reals ; approximate value, 4*s*. 3½*d*. The dollar of 100 centavos, 4*s*.

*San Domingo.*—The same as for Spain.

*United States.*—The dollar of 100 cents. Par value, 49·32*d*. ; or £1=4·866 dollars.

*Uruguay.*—The peso, or dollar, of 100 centavas ; approximate value, 4*s*. 3*d*. ; or £1=4·70 dollars.

*Venezuela.*—The venezolano of 100 centavas ; approximate value, 3*s*. 4*d*. The bolivar=1 franc.

## SPECIFIC GRAVITY, WEIGHT, AND VOLUME.

### Density of Alloys and Amalgams.

Messrs. F. Crace-Calvert and Richard Johnson investigated the conductivity of heat, tenacity, hardness, and expansion of alloys and amalgams formed with pure metals, according to the law of equivalents, and that of multiple preparations, the results of which are recorded in Table 72. It was discovered that all alloys of copper, in course of formation, make a contraction of volume ; whilst all the amalgams dilate and have less than the mean density calculated in terms of the densities and proportions of the elements. Also that the maximum contraction or dilation of an alloy or an amalgam takes place generally when an equivalent of each metal is taken, except in the case of tin and zinc. These general results are attributable, no doubt, to the fact of all the alloys, except these last-named, being combinations, not mixtures. Some alloys have exceptionally great contraction or dilation. Thus, the alloy of 3 equivalents of copper to 1 of tin, has 8·954 density ; calculated as a mixture, its density would only be 8·208. The amalgam of one equivalent of tin

with one of mercury dilates by one-tenth of the elementary volumes.

TABLE 72.—METALS: SPECIFIC GRAVITY, WEIGHT, AND VOLUME.

METALS.	Specific Gravity.	Weight of One Cubic Foot.	Weight of One Cubic Inch.	Cubic Feet per Ton.
	Water = 1.	Lbs.	Ozs.	Cubic Feet.
Aluminium, wrought . . . . .	2·67	167	1·55	13·44
"    cast . . . . .	2·56	160	1·48	14·02
Antimony . . . . .	6·71	418	3·87	5·35
Arsenic . . . . .	5·80	361·5	3·35	6·19
Bismuth . . . . .	9·90	617	6·03	3·63
Brass, cast :—	8·10	505	4·71	4·43
75 copper, 25 zinc, sheet . . . . .	8·45	527	4·87	4·25
66 "    34 "    yellow . . . . .	8·30	518	4·80	4·32
60 "    40 "    { Muntz's } { metal } . . . . .	8·20	511	4·73	4·38
Brass wire . . . . .	8·55	533	4·93	4·20
Bronze :—				
84 copper, 16 tin, gun metal . . . . .	8·56	534	4·93	4·19
83 "    17 "    " . . . . .	8·46	528	4·89	4·24
81 "    19 "    " . . . . .	8·46	528	4·89	4·24
79 "    21 "    mill bearings . . . . .	8·73	544	5·04	4·11
35 "    65 "    small bells . . . . .	8·06	503	4·66	4·45
21 "    79 "    " . . . . .	7·39	461	4·27	4·86
15 "    85 "    { speculum } { metal } . . . . .	7·45	465	4·31	4·82
Calcium . . . . .	1·58	98·5	0·91	22·72
Cobalt . . . . .	8·50	530	4·91	4·22
Chromium . . . . .	6·00	374	3·46	5·98
Copper, sheet . . . . .	8·81	549	5·08	4·08
"    hammered . . . . .	8·92	556	5·19	4·02
"    wire . . . . .	8·88	554	5·13	4·04
Gold . . . . .	19·24	1200	11·11	1·87
Iron, cast :—				
white . . . . .	7·50	468	4·33	4·79
grey . . . . .	7·20	449	4·16	4·99
hot blast . . . . .	6·97	435	4·03	5·15
"    14th melting . . . . .	7·53	470	4·35	4·77
mean, for ordinary calculations . . . . .	7·22	450	4·17	5·00

TABLE 72.—METALS: SPECIFIC GRAVITY, WEIGHT, AND VOLUME (*continued.*)

METALS.	Specific Gravity.	Weight of One Cubic Foot.	Weight of One Cubic Inch.	Cubic Feet per Ton.
	Water=1.	Pounds.	Ozs.	Cubic Ft.
Iron, wrought :—				
common bar, rails . . . . .	7.55	471	4.36	4.76
puddled slab . . . . .	7.53 to 7.60	469.5 to 474	4.35 to 4.39	4.77 to 4.72
various (Kirkaldy), } mean . . . . . }	7.65	477	4.42	4.69
Yorkshire bar . . . . .	7.76	484	4.48	4.63
Low Moor plates, thick . . . . .	7.81	487	4.51	4.60
pure iron, by electro- } deposit . . . . . }	8.14	508	4.70	4.41
mean, for ordinary } calculations . . . . . }	7.70	480	4.44	4.63
Lead, milled sheet . . . . .	11.42	712	6.59	3.14
" wire . . . . .	11.28	704	6.52	3.18
Lithium . . . . .	.59	37	.34	6.08
Magnesium . . . . .	1.74	108.5	10.00	20.63
Manganese . . . . .	8.00	499	4.51	4.49
Mercury . . . . .	13.60	849	7.86	2.64
Nickel, hammered . . . . .	8.67	541	5.09	4.14
" cast . . . . .	8.28	516	4.78	4.34
Platinum . . . . .	21.52	1342	12.42	1.67
Potassium . . . . .	.86	53.6	.41	41.65
Silver . . . . .	10.50	655	6.06	3.42
Sodium . . . . .	.97	60.5	.56	37.01
Steel :—				
blistered . . . . .	7.82	488	4.52	4.59
crucible . . . . .	7.84	489	4.53	4.58
cast . . . . .	7.85	489.3	4.53	4.57
Bessemer . . . . .	7.85	489.6	4.53	4.57
for ordinary calcula- } tions . . . . . }	7.86	490	4.54	4.57
Tin . . . . .	7.41	462	4.29	4.84
Zinc, sheet . . . . .	7.20	449	4.16	4.99
" cast . . . . .	6.86	428	4.02	5.23

TABLE 73.—DENSITY OF ALLOYS AND AMALGAMS.

(F. Crace-Calvert and R. Johnson.)

## I. ALLOYS OF GREATER THAN CALCULATED MEAN DENSITY : WITH CONTRACTION.

ALLOY.	Proportions per cent. by Weight.	Density ob- tained.	Density calcu- lated.	Diffe- rence.
1. <i>Copper and Tin</i> (bronze)				
Cu Sn <sup>5</sup> . . . .	{ C 9.73 } { T 90.27 }	7.517	7.431	.086
Cu Sn <sup>4</sup> . . . .	{ C 11.86 } { T 88.14 }	7.558	7.462	.096
Cu Sn <sup>3</sup> . . . .	{ C 15.21 } { T 84.79 }	7.606	7.514	.092
Cu Sn <sup>2</sup> . . . .	{ C 21.21 } { T 78.79 }	7.738	7.580	.158
Cu Sn . . . .	{ C 34.98 } { T 65.02 }	7.992	7.805	.187
Sn Cu <sup>2</sup> . . . .	{ T 51.83 } { C 48.17 }	8.533	8.059	.474
Sn Cu <sup>3</sup> . . . .	{ T 38.21 } { C 61.79 }	8.954	8.208	.746
Sn Cu <sup>4</sup> . . . .	{ T 31.73 } { C 68.27 }	8.948	8.306	.642
Sn Cu <sup>5</sup> . . . .	{ T 27.10 } { C 72.90 }	8.965	8.374	.591
Sn Cu <sup>10</sup> . . . .	{ T 15.68 } { C 84.32 }	8.832	8.545	.287
Sn Cu <sup>15</sup> . . . .	{ T 11.03 } { C 88.97 }	8.825	8.615	.210
Sn Cu <sup>20</sup> . . . .	{ T 8.51 } { C 91.49 }	8.793	8.634	.159
Sn Cu <sup>25</sup> . . . .	{ T 6.83 } { C 93.17 }	8.820	8.677	.143
2. <i>Copper and Zinc</i> (brass)				
Zn Cu <sup>5</sup> . . . .	{ C 82.95 } { Z 17.05 }	8.673	8.453	.220
Zn Cu <sup>4</sup> . . . .	{ C 79.56 } { Z 20.44 }	8.650	8.387	.263
Zn Cu <sup>3</sup> . . . .	{ C 74.48 } { Z 25.52 }	8.576	8.290	.286

TABLE 73.—DENSITY OF ALLOYS AND AMALGAMS  
(continued).

ALLOY.	Proportions per cent. by Weight.	Density ob- tained.	Density calcu- lated.	Diffe- rence.
2. <i>Copper and Zinc</i> (brass) (continued.)				
Zn Cu <sup>2</sup> . . . . .	{ C 66.06 } { Z 33.94 }	8.488	8.129	.359
Zn Cu . . . . .	{ C 49.32 } { Z 50.58 }	7.808	8.319	.511
Cu Zn <sup>2</sup> . . . . .	{ C 32.74 } { Z 67.26 }	7.859	7.489	.370
Cu Zn <sup>3</sup> . . . . .	{ C 24.64 } { Z 75.36 }	7.736	7.334	.401
Cu Zn <sup>4</sup> . . . . .	{ C 19.57 } { Z 80.43 }	7.445	7.237	.208
Cu Zn <sup>5</sup> . . . . .	{ C 16.30 } { Z 83.70 }	7.442	7.174	.208
3. <i>Copper and Bismuth.</i>				
Cu Bi . . . . .		9.634	9.566	.068
4. <i>Copper and Antimony.</i>				
Cu Sb . . . . .		7.990	7.386	.604
5. <i>Tin and Zinc.</i>				
Zn Sn <sup>2</sup> . . . . .	{ Z 21.65 } { T 78.35 }	7.274	7.193	.081
Zn Sn . . . . .	{ Z 35.60 } { T 64.40 }	7.262	7.134	.128
Sn Zn <sup>2</sup> . . . . .	{ T 47.49 } { Z 52.51 }	7.188	7.060	.128
Sn Zn <sup>3</sup> . . . . .	{ T 37.57 } { Z 62.43 }	7.180	7.021	.159
Sn Zn <sup>4</sup> . . . . .	{ T 31.14 } { Z 68.86 }	7.155	6.993	.162
Sn Zn <sup>5</sup> . . . . .	{ T 26.57 } { Z 73.43 }	7.140	6.974	.161
Sn Zn <sup>10</sup> . . . . .	{ T 15.32 } { Z 84.68 }	7.135	6.927	.208



TABLE 73.—DENSITY OF ALLOYS AND AMALGAMS  
(continued).II. ALLOYS AND AMALGAMS OF LESS THAN CALCULATED  
MEAN DENSITY : WITH DILATATION.

ALLOY.	Proportions per cent. by Weight.	Density ob- tained.	Density calcu- lated.	Diffe- rence.
6. <i>Mercury and Tin.</i>				
Hg Sn . . . . .	{ M 62·97 } { T 37·03 }	10·255	11·259	1·004
Hg Sn <sup>2</sup> . . . . .	{ M 45·88 } { T 54·12 }	9·314	10·180	·866
Hg Sn <sup>3</sup> . . . . .	{ M 36·18 } { T 63·82 }	8·805	9·568	·763
Hg Sn <sup>4</sup> . . . . .	{ M 29·84 } { T 70·16 }	8·510	9·168	·658
Hg Sn <sup>5</sup> . . . . .	{ M 25·38 } { T 74·62 }	8·312	8·885	·573
Hg Sn <sup>6</sup> . . . . .	{ M 22·08 } { T 77·92 }	8·151	8·678	·527
7. <i>Mercury and Bismuth.</i>				
Hg Bi . . . . .	{ M 48·44 } { B 51·56 }	11·208	11·638	·430
Hg Bi <sup>2</sup> . . . . .	{ M 31·82 } { B 68·18 }	10·693	11·007	·314
Hg Bi <sup>3</sup> . . . . .	{ M 23·86 } { B 76·14 }	10·474	10·704	·230
Hg Bi <sup>4</sup> . . . . .	{ M 19·03 } { B 80·97 }	10·350	10·522	·172
Hg Bi <sup>5</sup> . . . . .	{ M 15·82 } { B 84·18 }	10·240	10·410	·170
8. <i>Mercury and Zinc</i> .				
		11·304	11·944	·640
9. <i>Antimony and Bismuth</i>				
Bi Sb <sup>5</sup> . . . . .	{ B 24·81 } { A 75·19 }	7·271	7·470	·201
Bi Sb <sup>4</sup> . . . . .	{ B 29·20 } { A 70·80 }	7·370	7·606	·235
Bi Sb <sup>3</sup> . . . . .	{ B 35·48 } { A 64·52 }	7·561	7·801	·240
Bi Sb <sup>2</sup> . . . . .	{ B 45·21 } { A 54·79 }	7·829	8·102	·273
Bi Sb . . . . .	{ B 62·26 } { A 37·94 }	8·364	8·630	·268

TABLE 73.—DENSITY OF ALLOYS AND AMALGAMS  
(continued).

ALLOY.	Proportions per cent. by Weight.	Density ob- tained.	Density calcu- lated.	Diffe- rence.
9. <i>Antimony and Bismuth</i> (continued).				
Sb Bi <sup>2</sup> . . . .	{ A 23·26 } { B 76·74 }	8·859	9·077	·218
Sb Bi <sup>3</sup> . . . .	{ A 16·81 } { B 83·19 }	9·095	9·277	·182
Sb Bi <sup>4</sup> . . . .	{ A 13·17 } { B 86·83 }	9·276	9·391	·119
Sb Bi <sup>5</sup> . . . .	{ A 10·82 } { B 89·18 }	9·369	9·464	·095
10. <i>Bismuth and Zinc.</i>				
Bi Zn . . . .		9·046	9·132	·086
11. <i>Tin and Lead.</i>				
Pb Sn <sup>5</sup> . . . .	{ L 26·03 } { T 73·97 }	8·093	8·367	·254
Pb Sn <sup>4</sup> . . . .	{ L 30·57 } { T 69·43 }	8·196	8·548	·352
Pb Sn <sup>3</sup> . . . .	{ L 36·99 } { T 63·01 }	8·418	8·823	·405
Pb Sn <sup>2</sup> . . . .	{ L 46·82 } { T 53·18 }	8·774	9·232	·458
Pb Sn . . . .	{ L 63·78 } { T 36·22 }	9·458	9·938	·480
Sn Pb <sup>2</sup> . . . .	{ T 22·11 } { L 77·89 }	10·105	10·525	·420
Sn Pb <sup>3</sup> . . . .	{ T 15·91 } { L 84·09 }	10·421	10·783	·362
Sn Pb <sup>4</sup> . . . .	{ T 12·43 } { L 87·57 }	10·587	10·927	·340
Sn Pb <sup>5</sup> . . . .	{ T 10·20 } { L 89·80 }	10·751	11·017	·266
12. <i>Lead and Antimony.</i>				
Sb Pb <sup>5</sup> . . . .	{ A 11·08 } { L 88·92 }	10·556	10·919	·363
Sb Pb <sup>4</sup> . . . .	{ A 13·48 } { L 86·52 }	10·387	10·805	·418
Sb Pb <sup>3</sup> . . . .	{ A 17·20 } { L 82·80 }	10·136	10·629	·493

TABLE 73.—DENSITY OF ALLOYS AND AMALGAMS  
(continued).

ALLOY.	Proportions per cent. by Weight.	Density ob- tained.	Density calcu- lated.	Diffe- rence.
12. <i>Lead and Antimony</i> (continued).				
Sb Pb <sup>2</sup> . . . . .	{ A 23·68 L 76·32 }	9·723	10·321	·598
Sb Pb . . . . .	{ A 38·39 L 61·61 }	8·953	9·624	·671
Pb Sb <sup>2</sup> . . . . .	{ L 44·53 A 55·47 }	8·330	8·959	·629
Pb Sb <sup>3</sup> . . . . .	{ L 34·86 A 65·14 }	7·830	8·355	·525
Pb Sb <sup>4</sup> . . . . .	{ L 28·64 A 71·36 }	7·525	8·059	·534
Pb Sb <sup>5</sup> . . . . .	{ L 24·31 A 75·69 }	7·432	7·854	·422

TABLE 74.—STONES: SPECIFIC GRAVITY, WEIGHT  
AND VOLUME.

STONES.	Specific Gravity.	Weight of one Cubic Foot.	Cubic Feet per Ton.
	Water = 1.	Pounds.	Cubic Ft.
Alabaster, calcareous . . . . .	2·76	172·1	13·0
„ gypseous . . . . .	2·31	144·0	15·6
Barytes . . . . .	4·45	277·5	8·07
Basalt . . . . .	2·45 to	152·8 to	14·7 to
	3·00	187·1	12·0
Chalk, air-dried . . . . .	2·50	155	14·5
Diamond . . . . .	3·50	...	...
Flint . . . . .	2·63	164	13·7
Felspar . . . . .	2·60	162·1	13·8
Gneiss . . . . .	2·69	168	13·3
Granite . . . . .	2·50 to	156 to	14·4 to
	2·74	171	13·1
Graphite . . . . .	2·20	137·2	16·3
Jasper . . . . .	2·72	169·7	13·2
Lias . . . . .	2·25 to	140·3 to	16·0 to
	2·45	152·8	14·7
Limestone . . . . .	1·86 to	116 to	19·3 to
	2·53	158	14·2

TABLE 74.—STONES : SPECIFIC GRAVITY, WEIGHT  
AND VOLUME (*continued*).

STONES.	Specific Gravity.	Weight of one Cubic Foot.	Cubic Feet per Ton.
	Water=1.	Pounds.	Cubic Ft.
Marble :—			
African . . . . .	2·80	174·6	12·8
British . . . . .	2·71	169·0	13·3
Carrara . . . . .	2·72	169·6	13·2
Egyptian green . . . . .	2·67	166·5	13·5
Florentine . . . . .	2·52	157·1	14·3
French . . . . .	2·65	165·2	13·6
Mica . . . . .	2·93	183	12·2
Oolitic stones . . . . .	1·89 to 2·60	118 to 162	19·0 to 13·8
Ores :—			
Spicular or red iron ore . . . . .	5·21	327·4	6·84
Magnetic iron ore . . . . .	5·09	317·6	7·05
Brown iron ore . . . . .	3·92	244·6	9·16
Spathic iron ore . . . . .	3·83	238·8	9·38
Clydesdale iron ore . . . . .	3·05	190·5	11·76
Potter's stone . . . . .	2·80	174·6	12·8
Quartz . . . . .	2·61 to 2·71	162·8 to 169	13·8 to 13·3
„ broken up and heaped . . . . .	1·96	122	20
„ quarry debris . . . . .	1·47	91·4	24·5
Rock crystal . . . . .	2·65	165·4	13·6
Sandstone . . . . .	2·04 to 2·70	127 to 168	17·6 to 13·3
Serpentine . . . . .	2·81	175·2	12·8
Slate . . . . .	2·60 to 2·85	162·1 to 177·7	13·8 to 12·6
Talc, steatite . . . . .	2·70	168·4	13·3
Trap, touchstone . . . . .	2·72	169·6	13·2
ARTIFICIAL STONES.			
Apoenite :—Ransom's silicious stone (silica, soda, water) . . . . .	1·60	99·7	22·5
Concrete :—			
Portland cement 1, and shingle 10 . . . . .	2·23	139	16·1
Portland cement, rubble, and sand . . . . .	2·17 to 2·25	135 to 140	16·6 to 16·0

TABLE 74.—STONES: ARTIFICIAL STONES (*continued*).

Concrete :—( <i>continued</i> ).			
Portland cement 1, and sand 2 . . . . .	2.04	127	17.6
Roman cement 1, and sand 2 . . . . .	1.92	120	18.7
Victoriastone (crushed granite, Portland cement, silica) . .	2.31	144	15.6

TABLE 75.—WEIGHT AND COMPOSITION OF BUILDING  
STONES.  
(Gwilt.)

STONES.	Weight of One Cubic Foot.
<b>1. GRANITES.</b>	
	Pounds.
Stirling Hill, Stirling . . . . .	165.9
High Rock, Breadalbane . . . . .	166.0
Black Hill, Stirling . . . . .	166.6
Dalkey, Dublin . . . . .	169.6
Bars, Breadalbane . . . . .	169.7
Haytor, Devonshire . . . . .	165.2
Blue Penmaenmaur, Carnarvonshire . . . . .	160.1
Aberdeen Grey, Aberdeenshire . . . . .	166.5
"    Red . . . . .	165.3
Cornish Grey, Cornwall . . . . .	166.7
"    Red . . . . .	164.0
Average . . . . .	166.0
<b>2. LIMESTONES.</b>	
Beer, Devonshire . . . . .	131.7
Chilmark, Wiltshire . . . . .	153.4
Hopton Wood, Derbyshire . . . . .	158.4
Sea Combe, Dorsetshire . . . . .	151.0
Sutton, Glamorganshire . . . . .	136.0
Tottenhoe, Bedfordshire . . . . .	116.5
Average . . . . .	141.2
<b>3. MAGNESIAN LIMESTONES.</b>	
Bolsover, Denbigh . . . . .	151.7
Broadsworth, Yorkshire . . . . .	133.6
Cadeby . . . . .	126.6

TABLE 75.—WEIGHT AND COMPOSITION OF BUILDING STONES (*continued*).

STONES.	Weight of One Cubic Foot.
<b>3. MAGNESIAN LIMESTONES (<i>continued</i>).</b>	
Huddleston . . . . .	137·8
Roche Abbey . . . . .	139·1
Smawes . . . . .	127·5
Average . . . . .	
	136·0
<b>4. OOLITIC STONES.</b>	
Ancaster, Lincolnshire . . . . .	139·2
Barnack Mill, Northamptonshire . . . . .	136·7
Bath Lodge Hill, Somersetshire . . . . .	116·0
Bath Baynton . . . . .	123·0
Bath (Drew's Quarry) . . . . .	122·6
Cranmore, Wiltshire . . . . .	134·2
Haydon, Lincolnshire . . . . .	133·5
Ketton, Rutlandshire . . . . .	128·3
Portland . . . . .	126·8 to 147·6
Taynton, Oxon. . . . .	135·9
Wass, Yorkshire . . . . .	soft, 141·7
	hard, 162·5
Windrush, Gloucestershire . . . . .	soft, 118·1
	hard, 135·9
Average . . . . .	
	133·5
<b>5. SANDSTONES.</b>	
Abercarne, Monmouth . . . . .	167·9
Barbadoes, Tintern, Monmouth . . . . .	146·7
Binnie, Linlithgowshire . . . . .	140·1
Bolton's Quarry, Yorkshire . . . . .	126·7
Bramley Fall . . . . .	142·2
Calverley, Kent . . . . .	118·1
Craigleith, Edinburgh . . . . .	145·9
Craw Bank, Linlithgowshire . . . . .	129·1
Duffield, Derbyshire . . . . .	132·9
Duke's Quarries, Derbyshire . . . . .	144·5
Elland Edge, Yorkshire . . . . .	153·2
Gatherley Moor . . . . .	135·8
Gatton, Surrey . . . . .	103·1
Glamis, Forfarshire . . . . .	161·1
Heddon, Northumberland . . . . .	130·7
Hollington, Staffordshire . . . . .	133·1
Humbie, Linlithgow . . . . .	white, 140·2
	grey, 135·8

TABLE 75.—WEIGHT AND COMPOSITION OF BUILDING STONES (*continued.*)

STONES.		Weight of One Cubic Foot.
5. SANDSTONES ( <i>continued</i> ).		
Longannet, Perthshire		131·7
Munlochy, Ross-shire		160·6
Mylnefield, Perthshire		160·0
Park Spring, Yorkshire		151·1
Pensher, Durham		134·3
Pyot Dykes, Forfarshire		162·5
Scotgate, Yorkshire		158·0
Stancliff, Derbyshire		148·2
Stenton, Durham		142·5
Whitby Company's, Aislaby, Yorkshire		126·7
"	Egton "	127·9
"	Sneaton "	134·8
"	Newton Dale "	131·7
Average		140·5
6. MARBLES.		
Black, Kilkenny		171·4
Tirree, Hebrides		172·3
Carrara (Statuary), Tuscany		168·6
" Ravaccione		169·1
Ipplepen, Devonshire		163·4
Average		169·0

<i>General Composition of the above Stones.</i>					
STONES.	Carbonate of Lime.	Magne- sia.	Silica.	Iron, Alumina, Water, and Loss.	Total.
	Per cent.	Pr.cent.	Pr.cent.	Per cent.	
Limestones	81·0	4·2	5	9·8	100·0
Do. Magnesian	54·6	40·6	2	2·8	100·0
Oolitic Stones	94·0	2·7	...	3·3	100·0
Sandstones	1·1	...	95·5	3·4	100·0
Marbles	lime	...	...	water ·5	100·0
	56·5				
	carbonic acid				
	43·0				

TABLE 76.—BRICKS: DIMENSIONS AND WEIGHT.  
(Hawkes.)

BRICKS.	Dimensions.			Weight of one brick.	Weight per 1000 bricks.
	In. × In. × In.			Pounds.	Cwts.
London Stocks . . .	8 $\frac{3}{4}$ × 4 $\frac{1}{4}$ × 2 $\frac{3}{4}$			6·81	60·75
Red Kiln . . .	8 $\frac{3}{4}$ × 4 $\frac{1}{4}$ × 2 $\frac{3}{4}$			7·00	63
Welsh Fire . . .	9 × 4 $\frac{1}{2}$ × 2 $\frac{3}{4}$			7·84	65 to 75
Paving . . .	9 × 4 $\frac{1}{2}$ × 1 $\frac{3}{4}$			5·00	45
Dutch Clinkers . . .	6 $\frac{1}{4}$ × 3 × 1 $\frac{1}{2}$			1·55	14
Irish Fire . . .	8 $\frac{3}{4}$ × 4 $\frac{1}{4}$ × 2 $\frac{3}{8}$			7·50	67
Worcester, solid, machine made . . .	...			8·75	78
Do. perforated . . .	...			6·00	53·5
Staffordshire, solid, hand made . . .	...			9·50	85
London stock, hand made . . .	...			5·75	51

TABLE 77.—MINERAL SUBSTANCES, VARIOUS: SPECIFIC GRAVITY, WEIGHT, AND VOLUME.

SUBSTANCE.	Specific Gravity.	Weight of one Cubic Foot.	Cubic Feet per Ton.
	Water=1.	Pounds.	Cubic Ft.
Alum . . . . .	1·72	107·2	20·9
Asphalte . . . . .	1·40	87·3	25·6
Ballast (brick rubbish and gravel) . . . . .	1·80	112	20·0
Brick . . . . .	2·00 to	124·7 to	18·1 to
	2·17	135·3	16·0
Brickwork . . . . .	1·76 to		20·4 to
	1·84	110	18
Camphor . . . . .	·99	61·7	36·3
Clay . . . . .	1·92	119·7	18·7
Coal :—			
Anthracite . . . . .	1·37 to	85·4 to	26·2 to
	1·59	99·1	22·6
Bituminous . . . . .	1·20 to	74·8 to	30 to
	1·31	81·7	28·1
Boghead (Cannel) . . . . .	1·20	78·4	30



TABLE 77.—MINERAL SUBSTANCES, VARIOUS: SPECIFIC GRAVITY, WEIGHT, AND VOLUME (*continued*).

SUBSTANCE.	Specific Gravity.	Weight of One Cubic Foot.	Cubic Feet per Ton.
	Water=1.	Pounds.	Cubic Ft.
Earth, argillaceous :—			
Dry, loose . . . . .	1.15 to 1.29	72 to 80	31.1 to 28
Dry, shaken . . . . .	1.32 to 1.48	82 to 92	27.3 to 24.3
Moist, loose . . . . .	1.06 to 1.22	66 to 76	34.0 to 29.5
Packed . . . . .	1.44 to 1.60	90 to 100	24.8 to 22.4
Light vegetable . . . . .	1.40	87.3	25.7
Glass :—			
Flint . . . . .	3.00	187.0	12.0
Green . . . . .	2.70	168.4	13.3
Plate . . . . .	2.70	168.4	13.3
Thick flooring . . . . .	2.53	158.0	14.2
Crown . . . . .	2.50	155.9	14.4
St. Gobain . . . . .	2.49	155.3	14.4
Common, with base of potash . . . . .	2.46	153.4	14.6
Fine, with base of potash . . . . .	2.45	152.8	14.6
Common, with base of soda . . . . .	2.45	152.8	14.6
Fine, with base of soda . . . . .	2.44	152.1	14.8
Gunpowder, heaped . . . . .	1.75 to 1.84	109.1 to 114.7	20.5 to 19.5
Ice, melting . . . . .	.922	57.5	39
Marl . . . . .	1.60 to 1.90	99.8 to 118.5	22.4 to 18.9
Masonry :—			
Ashlar granite . . . . .	2.37	147.5	15.2
„ Limestone, hard . . . . .	2.70	168.5	11.4
„ „ semi-hard . . . . .	2.42	151.9	14.8
„ „ soft . . . . .	2.34	145.6	15.4
„ Millstone . . . . .	2.01 to 2.51	125 to 156.2	18.0 to 14.3
„ Sandstone . . . . .	2.61	162.5	13.2
Rubble, dry . . . . .	2.21	138	16.2
„ mortar . . . . .	2.47	154	14.6
Mortar, hardened . . . . .	1.65	103	21.7

TABLE 77.—MINERAL SUBSTANCES, VARIOUS: SPECIFIC GRAVITY, WEIGHT, AND VOLUME (*continued*).

SUBSTANCE.	Specific Gravity.	Weight of One Cubic Foot.	Cubic Foot per Ton.
	Water=1.	Pounds.	Cubic Ft.
Mud :—			
Dry, close . . . . .	1·28 to 1·93	80 to 110	28·0 to 20·4
Wet, moderately pressed . . . . .	1·93 to 2·09	110 to 130	20·4 to 17·2
Wet, fluid . . . . .	1·67 to 1·92	104 to 120	21·5 to 18·7
Phosphorus . . . . .	1·77	110·4	20·3
Plaster . . . . .	1·57	98	22·9
Portland cement . . . . .	1·25 to 1·51	78 to 94	28·7 to 23·8
Potash . . . . .	2·10	131	17·1
Sand . . . . .	1·44 to 1·87	90 to 117	24·9 to 19·1
„ saturated with water . . . . .	1·89 to 2·07	118 to 129	19 to 17·4
Salt, common . . . . .	1·92	119·7	18·7
„ rock . . . . .	2·10 to 2·26	131 to 140·7	17·1 to 15·9
Sulphur . . . . .	2·00	124·7	18·0
Tiles . . . . .	2·00	124·7	18·0

TABLE 77a.—FUELS IN FRANCE.

	Weight of one Cub. Ft.	Specific Gravity.
	Pounds.	Water=1.
Pure graphite . . . . .	145·3	2·88
Anthracite . . . . .	83·5 to 91·0	1·34 to 1·46
Rich coal with a long flame . . . . .	79·8 to 84·8	1·28 to 1·36
Dry coal with a long flame . . . . .	84·8	1·36
Rich and hard coal . . . . .	82·3	1·32
Smithy coal . . . . .	79·8 to 81·1	1·28 to 1·30
Lignite . . . . .	77·9 to 84·2	1·25 to 1·35
„ bituminous . . . . .	72·3 to 74·8	1·16 to 1·20
„ imperfect . . . . .	81·7	1·31
Bitumen, red . . . . .	72·3	1·16
„ black . . . . .	66·7	1·07
„ brown . . . . .	51·7	0·83
„ . . . . .	66·1	1·06

TABLE 78.—WEIGHT AND VOLUME IN BULK OF VARIOUS SOLIDS.  
(Tredgold.)

SUBSTANCE.	Weight of One Cubic Foot in bulk.	Volume of One Ton in bulk.
	Pounds.	Cubic Feet.
Lead, cast in pigs . . . . .	567	4
Iron, cast in pigs . . . . .	360	6.25
Limestone or Marble, in blocks . . . . .	172	13
Granite, Aberdeen, in blocks . . . . .	166	13.5
"    Cornish,    "    . . . . .	164	14
Sandstone, in blocks . . . . .	141	16
Portland Stone, in blocks . . . . .	132	17
Potter's Clay . . . . .	130	17
Loam or Strong Soil . . . . .	126	18
Bath Stone, in blocks . . . . .	123.5	18
Gravel . . . . .	109	21
Sand . . . . .	95	23.5
Bricks, Common Stock, dry . . . . .	93	24
Culm . . . . .	63	36
Water, River . . . . .	62.5	36
Splint Coal . . . . .	57	39.5
Oak, Seasoned . . . . .	52	43
Coal (Newcastle) coking . . . . .	50	45
Wheat . . . . .	48	47
Barley . . . . .	38	59
Red Fir . . . . .	38	59
Hay, compact, old . . . . .	8	280

TABLE 79.—MEASURES OF ORES, EARTH, &C.  
(Rand Drill Company.)

	Weight.
14.5 Cubic Feet of ordinary Gold or Silver Ore, in mine	1 ton
22 " of Broken Quartz . . . . .	1 "
20 " Gravel, in bank . . . . .	1 "
30 " Gravel, when dry . . . . .	1 "
28 " Sand . . . . .	1 "
20 " Earth, in bank . . . . .	1 "
30 " " " when dry . . . . .	1 "
19 " Clay . . . . .	1 "
45 " Bituminous Coal, heaped . . . . .	1 "
42 " Anthracite " . . . . .	1 "
123 " Charcoal " . . . . .	1 "
71 " Coke " . . . . .	1 "

		Weight.
1	Cubic Foot Anthracite, heaped . . .	50 lb. to 55 lb.
1	„ Bituminous Coal „ . . .	45 lb. to 55 lb.
1	„ Cumberland Coal . . .	53 lb.
1	„ Cannel Coal . . .	50½ lb.
1	„ Hardwood Charcoal . . .	18½ lb.
1	„ Pine Charcoal . . .	18 lb.

	Weight.	Equivalent as Fuel to
1 Cord of Wood, 4 feet × 4 feet × 8 feet . .	= 128 cubic feet	
1 Cord of air-dried Hickory or Hard Maple . . .	4,500 lb.	2,000 lb. coal.
1 „ „ White Oak . . .	3,850 „	1,715 „
1 „ „ Beech, Red Oak or Black Oak . . .	3,250 „	1,450 „
1 „ „ Poplar (white wood), Chestnut, or Elm . . .	2,350 „	1,050 „
1 „ „ Average Pine . . .	2,000 „	925 „

TABLE 80.—FUELS: SPECIFIC GRAVITY, WEIGHT, AND BULK.

FUELS.	Specific Gravity.	Weight of One Cubic Foot.		Volume of One Ton, heaped	
		Solid.	Heaped.		
COALS.		Water = 1.	Lbs.	Lbs.	Cub. Ft.
Anthracite . . . . .	1.37	85.4	58.3	38.4	
„ American . . . . .	1.30 to 1.84	93.5	54.0	...	
Welsh . . . . .	1.32	82.3	53.1	42.7	
Newcastle . . . . .	1.25	78.3	49.8	45.3	
Derbyshire and Yorkshire . . . . .	1.29	79.6	45.9	47.4	
Lancashire . . . . .	1.27	79.4	49.7	45.2	
Scotch . . . . .	1.26	78.6	50.0	42.0	
Irish: Slievardagh anthra- cite . . . . .	1.59	99.6	62.8	35.7	
Bituminous coal, American	1.35	84.0	50.0	...	
Boghead (Scotland) . . . . .	1.18	...	...	...	
COKE.					
Coke, generally . . . . .	...	40 to 50	30.0	70 to 80	
Soft . . . . .	.74	46	30.0	74.7	

TABLE 80.—FUELS: SPECIFIC GRAVITY, WEIGHT, AND BULK (*continued*).

FUELS.	Specific Gravity.	Weight of One Cubic Foot.		Volume of One Ton, heaped.
		Solid.	Heaped.	
	Water=1.	Lbs.	Lbs.	Cub. Ft.
<b>COKE (<i>continued</i>).</b>				
Gas coke . . . . .	...	...	23·8 to 28·6	...
American . . . . .	...	...	32·1	69·8
Seraing (France) . . . . .	...	...	31·0	72·0
Graphite . . . . .	2·33	145·3	...	...
<b>LIGNITE AND ASPHALTE.</b>				
Perfect lignite . . . . .	1·29	...	...	...
Imperfect lignite . . . . .	1·15	...	...	...
Bituminous lignite . . . . .	1·18	...	...	...
Asphalte . . . . .	1·06	...	...	...
<b>WOOD.—See Table 81.</b>				
<b>WOOD CHARCOAL.</b>				
<i>As made, heaped.</i>				
Oak and beech . . . . .	Heaped.			
	24 to 25	...	15 to 15·6	...
Birch . . . . .	22 to 23	...	13·7 to 14·3	...
Pine . . . . .	20 to 21	...	12·5 to 13·1	...
Average . . . . .	22·5	...	14	...
<i>In small pieces, heaped.</i>				
Walnut . . . . .	463	...	39·3	...
Ash . . . . .	53	...	34·3	...
Beech . . . . .	52	...	32·5	...
Yoke-Elm . . . . .	46	...	28·7	...
Appleton . . . . .	46	...	28·7	...
White oak . . . . .	42	...	26·2	...
Cherry tree . . . . .	41	...	25·6	...
Birch . . . . .	36	...	22·5	...
Elm . . . . .	36	...	22·5	...
Yellow pine . . . . .	33	...	20·6	...
Chestnut tree . . . . .	28	...	17·5	...
Poplar . . . . .	25	...	15·6	...
Cedar . . . . .	24	...	15·0	...
Average . . . . .	405	...	25·3	...

TABLE 80.—FUELS: SPECIFIC GRAVITY, WEIGHT, AND BULK (*continued*).

FUELS.	Specific Gravity.	Weight of One Cubic Foot.		Volume of One Ton, heaped.
		Solid.	Heaped.	
	Water=1.	Lbs.	Lbs.	Cub. Ft.
<i>As Powder.</i>				
Willow . . . . .	1.55	...	96.7	...
Oak . . . . .	1.53	...	95.4	...
Alder . . . . .	1.49	...	92.9	...
Lime tree . . . . .	1.46	...	91.0	...
Poplar . . . . .	1.45	...	90.4	...
Average . . . . .	1.50	...	93.5	...
Gunpowder, loose . . . . .	.90	...	...	...
"    shaken . . . . .	1.00	...	...	...
"    solid . . . . .	1.55 to 1.80	...	...	...
<i>Irish Peat.</i>				
Very light, spongy, surface peat . . . . .	.22 to .34	13.7 to 21.0	...	...
Light surface peat . . . . .	.34 to .41	20.9 to 25.3	...	...
Rather dense . . . . .	.48 to .67	29.7 to 41.7	...	...
Very dense, dark brown . . . . .	.65 to .71	40.5 to 44.5	...	...
Very dense, blackish brown, compact . . . . .	.72 to .98	45.1 to 61.3	...	...
Exceedingly dense, jet black . . . . .	.73 to .99	53.2 to 61.8	...	...
Exceedingly dense, dark blackish brown . . . . .	1.05	66.0	...	...
Upper moss . . . . .	...	...	6.06 to 8.81	369.6 to 254.2
Brown . . . . .	...	...	15.13	147.0
Compact black . . . . .	...	...	17.06	131.3
Densest black . . . . .	...	...	22.54	99.4
Condensed peat . . . . .	1.0 to 1.3	62.5 to 81.1	43.7 to 56.8	51.2 to 40.0

TABLE 81.—WOODS : SPECIFIC GRAVITY AND WEIGHT.

Wood.	Specific Gravity.	Weight of One Cubic Foot.
	Water = 1.	Pounds.
Acacia . . . . .	·82	51·1
„ with 20 per cent. moisture	·72	44·9
Alder tree . . . . .	·56	34·9
„ with 20 per cent. moisture	·60	37·4
Ash . . . . .	·84	52·4
„ with 20 per cent. moisture.	·70	43·7
Aspen tree . . . . .	·60	37·4
Apple tree . . . . .	·73	45·5
Bamboo . . . . .	·31 to ·40	19·5 to 24·9
Beech . . . . .	·75 to ·85	46·8 to 50·3
„ with 20 per cent. moisture	·82	51·1
„ cut one year . . . . .	·66	41·2
Birch . . . . .	·72 to ·74	44·9 to 46·1
Boxwood . . . . .	1·04	64·8
Cedar of Lebanon . . . . .	·49 to ·57	30·6 to 35·5
Cork . . . . .	·24	15·0
Cypress, cut one year . . . . .	·66	41·2
Ebony . . . . .	1·13	70·5
„ Green . . . . .	1·21	75·5
„ Black . . . . .	1·19	74·2
Elder pith . . . . .	·076	4·74
Elm . . . . .	·55	34·3
„ Green . . . . .	·76	47·5
„ with 20 per cent. moisture	·72	44·9
Fir, Norway Pine . . . . .	·74	46·1
„ Red Pine . . . . .	·48 to ·70	29·9 to 43·7
„ Spruce . . . . .	·48 to ·70	29·9 to 43·7
„ Larch . . . . .	·50 to ·64	31·2 to 39·9
„ White Pine, English . . . . .	·55	34·3
„ „ Scotch . . . . .	·53	34·3
„ „ „ with ) 20 per cent. moisture . . . . .	·49	30·6
„ Yellow Pine . . . . .	·66	41·2
„ „ American . . . . .	·46	28·7
Hawthorn . . . . .	·91	56·7
Holly . . . . .	·76	47·5
Hornbeam . . . . .	·76	47·5
Laburnum . . . . .	·92	57·4
Lance Wood . . . . .	·67 to 1·01	41·8 to 63·0
Lignum-Vitæ . . . . .	·65 to 1·33	40·5 to 82·9

TABLE 81.—WOODS : SPECIFIC GRAVITY AND WEIGHT  
(continued).

Wood.	Specific Gravity.	Weight of One Cubic Foot.
	Water=1.	Pounds.
Mahogany, Spanish . . . . .	.85	53.0
„ St. Domingo . . . . .	.75	46.8
„ Cuba . . . . .	.56	34.9
„ Honduras . . . . .	.56	34.9
Maple . . . . .	.65	40.5
„ 20 per cent. moisture . . . . .	.67	41.8
Mulberry . . . . .	.89	55.5
Oak, Heart of . . . . .	1.17	73.0
„ English . . . . .	.93	58.0
„ European . . . . .	.69 to .99	43.0 to 61.7
„ American Red . . . . .	.87	54.2
Olive tree . . . . .	.68	42.4
Orange tree . . . . .	.71	44.3
Pear tree . . . . .	.73	45.5
Plane tree . . . . .	.65	40.5
Plum tree . . . . .	.87	54.2
Pomegranate . . . . .	1.35	84.2
Poplar . . . . .	.39	24.3
„ White . . . . .	.32 to .51	20.0 to 31.8
„ 20 per cent. moisture . . . . .	.48	29.9
Rosewood . . . . .	1.03	64.2
Rock-Elm . . . . .	.80	50.0
Satin-wood . . . . .	.96	59.9
Service tree . . . . .	.67	41.8
Sycamore . . . . .	.59	36.8
Teak, African . . . . .	.98	61.0
Vine tree . . . . .	.60	37.4
Walnut, Green . . . . .	.92	57.4
„ Brown . . . . .	.68	42.4
Willow . . . . .	.49	30.6
Yew . . . . .	.74 to .81	46.1 to 50.5
Yoke Elm, with 20 per cent. moisture . . . . .	.76	47.5
INDIAN WOODS (Berkley).		
Khair . . . . .	1.17	73
Red Eyne . . . . .	1.09	68
Erroul . . . . .	1.01	63
„ . . . . .	.90	56



TABLE 81.—WOODS: SPECIFIC GRAVITY AND WEIGHT  
(continued).

Wood.	Specific Gravity.	Weight of One Cubic Foot.
	Water = 1.	Pounds.
<b>INDIAN WOODS (continued).</b>		
Blackwood . . . . .	.90	56
Northern Teak . . . . .	.88	55
Southern Teak . . . . .	.77	48
Jungle Teak . . . . .	.66	41
Kullum . . . . .	.66	41
Hedoo . . . . .	.63	39
Poon . . . . .	.63	39
<b>BRITISH GUIANA (Fowke).</b>		
Sipiri, or Green Heart . . . . .	1.05 to 1.09	65.5 to 68.0
Wallaba . . . . .	1.04	64.8
Brown Ebony . . . . .	1.03	64.2
Letter Wood . . . . .	1.00	62.4
Cuamara, or Tonka . . . . .	.99	61.7
Monkey Pot . . . . .	.94	58.6
Mora . . . . .	.92	57.4
Ducaballi . . . . .	.91	56.7
Cabacalli . . . . .	.89	55.5
Kaieeballi . . . . .	.87	54.2
Sirabuliballi . . . . .	.84	52.4
Buhuradda . . . . .	.81	50.5
Buckati . . . . .	.81	50.5
Houbaballi . . . . .	.81	50.5
Baracara . . . . .	.81	50.5
White Cedar . . . . .	.77	48.0
Locust tree . . . . .	.71	44.3
Cartan . . . . .	.70	43.7
Purple Heart . . . . .	.68	42.4
Bartaballi . . . . .	.64	39.4
Crabwood . . . . .	.60	37.4
Silverballi . . . . .	.55	34.3
<b>JAMAICA (Fowke).</b>		
Black Heart Ebony . . . . .	1.19	74.2
Lignum-Vitæ . . . . .	.65 to 1.17	40.5 to 73.0
Small Leaf . . . . .	1.17	73.0
Neesberry Bullet tree . . . . .	1.05	65.5
Red Bully tree . . . . .	1.00	62.4
Iron Wood . . . . .	.99	61.7
Sweet Wood . . . . .	.97	60.5

TABLE 81.—WOODS: SPECIFIC GRAVITY AND WEIGHT  
(continued).

WOOD.	Specific Gravity.	Weight of One Cubic Foot.
	Water=1.	Pounds.
<b>JAMAICA (continued).</b>		
Fustic . . . . .	·97	60·5
Satin Candlewood . . . . .	·96	59·9
Bastard Cabbage Bark . . . . .	·94	58·6
White Dogwood . . . . .	·94	58·6
Black " . . . . .	·93	58·0
Gynip . . . . .	·93	58·0
Wild Mahogany . . . . .	·92	57·4
Cashaw . . . . .	·92	57·4
Wild Orange . . . . .	·85 to ·91	53·0 to 56·7
Sweet Orange . . . . .	·79	49·3
Bullet tree (bastard) . . . . .	·90	56·1
Tamarind . . . . .	·87	54·2
" wild . . . . .	·75	46·8
Prune . . . . .	·86	53·6
Yellow Sanders . . . . .	·86	53·6
Beech . . . . .	·84	52·4
French Oak . . . . .	·77	48·0
Broad Leaf . . . . .	·77	48·0
Fiddlewood . . . . .	·71	44·3
Prickle Yellow . . . . .	·69	43·0
Boxwood . . . . .	·69	43·0
Locust tree . . . . .	·68	42·4
Lance Wood . . . . .	·68	42·4
Green Mahogany . . . . .	·66	41·2
Yacca . . . . .	·63	39·3
Cedar . . . . .	·58	36·2
Calabash . . . . .	·56	34·9
Bitter Wood . . . . .	·55	34·3
Blue Mahoe . . . . .	·54	33·7
<b>NEW SOUTH WALES.</b>		
Box of Ilwarra . . . . .	1·17	73·0
" Bastard . . . . .	1·12	69·8
" True, of Camden . . . . .	·97	60·5
Mountain Ash . . . . .	1·11	69·2
Kakaralli . . . . .	1·10	68·6
Iron Bark . . . . .	1·03	64·2
" broad leaved . . . . .	1·02	63·6
"olly Butt . . . . .	1·01	63·0
" . . . . .	·89	55·5

TABLE 81.—WOODS: SPECIFIC GRAVITY AND WEIGHT  
(continued).

WOOD.	Specific Gravity.	Weight of One Cubic Foot.
	Water=1.	Pounds.
NEW SOUTH WALES (continued).		
Water Gum . . . . .	1.00	62.4
Blue Gum . . . . .	.84	52.4
Cog Wood . . . . .	.95	59.9
Mahogany . . . . .	.95	59.2
" Swamp . . . . .	.86	53.6
Gray Gum . . . . .	.93	58.0
Stringy Bark . . . . .	.86	53.6
Hickory . . . . .	.75	46.8
Forest Swamp Oak . . . . .	.66	41.2

TABLE 82.—ANIMAL SUBSTANCES: SPECIFIC GRAVITY AND WEIGHT.  
(Clausel.)

SUBSTANCE.	Specific Gravity.	Weight of One Cubic Foot.
	Water=1.	Pounds.
Pearls . . . . .	2.72	169.6
Coral . . . . .	2.69	167.7
Ivory . . . . .	1.82 to 1.92	114 to 119.7
Bone . . . . .	1.80 to 2.00	112.2 to 124.7
Wool . . . . .	1.61	100.4
Tendon . . . . .	1.12	69.8
Cartilage . . . . .	1.09	68.0
Crystalline humour . . . . .	1.08	67.3
Human Body . . . . .	1.07	66.7
Nerve . . . . .	1.04	64.9
Bees Wax . . . . .	.96	59.9
Lard . . . . .	.95	59.3
Spermaceti . . . . .	.94	58.8
White of Whalebone . . . . .	.94	58.7
Butter . . . . .	.94	58.7
Pork Fat . . . . .	.94	58.7
Tallow . . . . .	.92	57.5
Beef Fat . . . . .	.92	57.5
Mutton Fat . . . . .	.92	57.4
Animal Charcoal, in heaps . . . . .	.80 to .83	50 to 52

TABLE 83.—VEGETABLE SUBSTANCES: SPECIFIC GRAVITY AND WEIGHT.

SUBSTANCE.	Specific Gravity.	Weight of One Cubic Foot.
	Water=1.	Pounds.
Cotton . . . . .	1.95	121.6
Flax . . . . .	1.79	111.6
Starch . . . . .	1.53	95.4
Fecula . . . . .	1.50	93.5
Gum, Arabic . . . . .	1.45	...
„ Mastic . . . . .	1.07	66.7
Resin, Guayacum . . . . .	1.20	74.8
„ Benzoin . . . . .	1.09	68.0
Indigo . . . . .	1.009	...
Sugar . . . . .	1.005	...
Amber . . . . .	1.09	68.0
Gutta-percha . . . . .	.97	60.5
India-rubber . . . . .	.93	58.0
	Weight of One Cubic Foot, loosely filled.	Weight of One Cubic Foot, closely filled.
Grain :—		
Wheat, Red Winter . . . . .	49	53½
„ Bombay . . . . .	49	53
„ California . . . . .	49	53
„ Walla-Walla . . . . .	46	50½
„ Bessarabia . . . . .	49	53
Peas, American . . . . .	50	54
Indian Corn, White American . . . . .	43½	47
„ Mixed . . . . .	44	47
Oats, Russian . . . . .	28	33
Beans, Egyptian . . . . .	46	50
Barley, English . . . . .	39	44

*Note.*—Under the Corn Returns Act, 1882, the bushel of the following grains is, for statistical purposes, to be taken respectively :—

For Wheat as . . . . .	60 lb.
For Barley as . . . . .	50 lb.
For Oats as . . . . .	39 lb.

TABLE 84.—LIQUIDS:—SPECIFIC GRAVITY AND WEIGHT,

LIQUIDS AT 32° F.	Specific Gravity.	Weight of One Cubic Foot.	Weight of One Gallon.
	Water=1.	Pounds.	Pounds.
Mercury . . . . .	13.596	848.7	136.0
Sulphuric Acid, maximum (concentration . . . . .)	1.84	114.9	18.4
Nitrous Acid . . . . .	1.55	96.8	15.5
Chloroform . . . . .	1.53	95.5	15.3
Nitric acid, of commerce . . . . .	1.22	76.2	12.2
Acetic acid, maximum concentration . . . . .	1.08	67.4	10.8
Milk . . . . .	1.03	64.3	10.3
Sea Water, ordinary . . . . .	1.026	64.05	10.3
Pure Water, at 39.0° F. . . . .	1.000	62.425	10.0112
Wine, Red . . . . .	.99	62.0	9.9
Oil, Linseed . . . . .	.94	58.7	9.4
„ Rapeseed . . . . .	.92	57.4	9.2
„ Whale . . . . .	.92	57.4	9.2
„ Olive . . . . .	.915	57.1	9.15
„ Turpentine . . . . .	.87	54.3	8.7
Tar . . . . .	1.00	62.4	10.0
Petroleum . . . . .	.88	54.9	8.8
Naphtha . . . . .	.85	53.1	8.5
Ether, Nitric . . . . .	1.11	69.3	11.1
„ Sulphurous . . . . .	1.08	67.4	10.8
„ Nitrous . . . . .	.89	55.6	8.9
„ Acetic . . . . .	.89	55.6	8.9
„ Hydrochloric . . . . .	.87	54.3	8.7
„ Sulphuric . . . . .	.72	44.9	7.2
Alcohol, proof spirit . . . . .	.92	57.4	9.2
„ pure . . . . .	.79	49.3	7.9
Benzine . . . . .	.85	53.1	8.5
Proof Spirit . . . . .	.80	49.9	8.0

TABLE 85.—WEIGHT AND SPECIFIC GRAVITY OF OILS.  
(Stilwell.)

OILS AT 39° F.	Weight of One Gallon.	Specific Gravity.
	Pounds.	Water=1.
Sperm, bleached, winter . . . . .	8·81	·881
„ natural, winter . . . . .	8·81	·881
Elaine . . . . .	9·01	·901
Red. saponified . . . . .	9·02	·902
Palm . . . . .	9·05	·905
Tallow . . . . .	9·14	·914
Neatsfoot . . . . .	9·14	·914
Rape-seed, white, winter . . . . .	9·14	·914
Olive, light greenish yellow . . . . .	9·14	·914
„ dark green . . . . .	9·14	·914
Peanut . . . . .	9·15	·915
Olive, virgin, very light yellow . . . . .	9·16	·916
Rape-seed, dark yellow . . . . .	9·17	·917
Olive, virgin, dark clear yellow . . . . .	9·17	·917
Lard, winter . . . . .	9·17	·917
Sea Elephant . . . . .	9·20	·920
Tanner's Cod . . . . .	9·20	·920
Cotton-seed, raw . . . . .	9·22	·922
„ refined, yellow . . . . .	9·23	·923
Salad (cotton-seed) . . . . .	9·23	·923
Labrador (cod) . . . . .	9·24	·924
Poppy . . . . .	9·24	·924
Seal, natural . . . . .	9·25	·925
Cocoonut . . . . .	9·25	·925
Whale, natural, winter . . . . .	9·25	·925
„ bleached, winter . . . . .	9·25	·925
Codliver, pure . . . . .	9·27	·927
Seal, racked . . . . .	9·29	·929
Cotton-seed, white, winter . . . . .	9·29	·929
Straits (cod) . . . . .	9·29	·929
Menhaden, dark . . . . .	9·29	·929
Linseed (raw) . . . . .	9·30	·930
Bank (cod) . . . . .	9·32	·932
Menhaden, light . . . . .	9·32	·932
Porgy . . . . .	9·33	·933
Linseed, boiled . . . . .	9·41	·941
Castor, pure cold pressed . . . . .	9·67	·967
Rosin, third run . . . . .	9·89	·989

TABLE 86.—GASES AND VAPOURS.—SPECIFIC GRAVITY, WEIGHT, AND VOLUME.

GASES at 32° F., and under one Atmosphere of Pressure.	Specific Gravity.	Weight of One Cubic Foot.		Volume of One Pound Weight
		Pounds.	Ounces.	
Mercury . . . . .	Air = 1. 6·9740	563	9·008	1·776
Chloroform . . . . .	5·3000	428	6·846	2·337
Turpentine . . . . .	4·6978	378	6·042	2·637
Acetic Ether . . . . .	3·0400	245	3·927	4·075
Benzine . . . . .	2·6943	217	3·480	4·598
Sulphuric Ether . . . . .	2·5860	209	3·340	4·790
Chlorine . . . . .	2·4400	197	3·152	5·077
Sulphurous Acid . . . . .	2·2470	1814	2·902	5·513
Alcohol . . . . .	1·6130	1302	2·083	7·679
Carbonic Acid . . . . .	1·5290	12344	1·975	8·101
Oxygen . . . . .	1·1056	·089253	1·428	11·205
Air . . . . .	1·0000	·080728	1·29165	12·387
Nitrogen . . . . .	·9736	·078596	1·258	12·723
Carbonic Oxide . . . . .	·9674	·0781	1·250	12·804
Olefiant Gas . . . . .	·9847	·0795	1·272	12·580
Ammoniacal Gas . . . . .	·5894	·04758	7·613	21·017
Light Carburetted Hydrogen . . . . .	·5527	·04462	·7139	22·412
Coal Gas . . . . .	·4381	·03536	·5658	28·279
Hydrogen . . . . .	·0692	·005592	·0895	178·83

TABLE 87.—WEIGHT AND VOLUME OF BODIES.

(Tol)

BODIES.	Weight of One Cubic Foot.		Weight of One Cubic Inch.	Cubic Inches in One Pound.
	Oz.	Lb.		
METALS.				
Antimony, cast . . . . .	6,702	418·8750	3·8748	3·8866
Zinc, cast . . . . .	7,190	449·3750	4·1608	3·8431
Iron, cast . . . . .	7,207	450·4375	4·1707	3·8364
Tin, cast . . . . .	7,291	455·6875	4·2193	3·7920
„ hardened . . . . .	7,299	456·1875	4·2239	3·7878
Pewter . . . . .	7,471	466·9375	4·3234	3·7007

TABLE 87.—WEIGHT AND VOLUME OF BODIES (*continued*).

BODIES.	Weight of One Cubic Foot.		Weight of One Cubic Inch.	Cubic Inches in One Pound.
	Oz.	Lb.	Oz.	Cub. In.
<b>METALS (<i>continued</i>).</b>				
Iron, bar . . . . .	7,788	486.7500	4.5069	3.5500
Cobalt, cast . . . . .	7,811	488.1875	4.5202	3.5396
Steel, hard . . . . .	7,816	488.5000	4.5231	3.5373
" soft meteoric . . . . .	7,833	489.5625	4.5329	3.5296
Iron, hammered . . . . .	7,965	497.8125	4.6093	3.4792
Nickel, cast . . . . .	8,279	517.4375	4.7910	3.3395
Brass, cast . . . . .	8,395	524.6875	4.8582	3.2933
" wire . . . . .	8,544	534.0000	4.9444	3.2359
Nickel, hammered . . . . .	8,666	541.6250	5.0150	3.1903
Gun-metal . . . . .	8,784	549.0000	5.0833	3.1476
Copper, cast . . . . .	8,788	549.2500	5.0856	3.1461
" wire . . . . .	8,878	554.8750	5.1377	3.1140
" coin . . . . .	8,915	557.1875	5.1591	3.0959
Bismuth, cast . . . . .	9,822	613.8750	5.6840	2.8149
Silver, hammered . . . . .	10,510	656.8750	6.0821	2.6306
" coin . . . . .	10,534	658.3750	6.0960	2.6246
" pure, cast . . . . .	10,744	671.5000	6.2175	2.5733
Rhodium . . . . .	11,000	687.5000	6.3657	2.5134
Lead, cast . . . . .	11,352	709.5000	6.3694	2.4355
Palladium . . . . .	11,800	737.5000	6.8287	2.5134
Mercury (quicksilver) } common }	13,568	848.0000	7.8518	2.0377
" pure . . . . .	14,000	875.0000	8.1018	1.9748
Gold, trinket . . . . .	15,709	981.8125	9.0908	1.7600
" coin . . . . .	17,647	1102.9375	10.2123	1.6124
" pure, cast . . . . .	19,258	1203.6250	11.1446	1.4356
" hammered . . . . .	19,316	1210.0625	11.2042	1.4280
Platinum, pure . . . . .	19,500	1218.7500	11.2847	1.4178
" hammered . . . . .	20,336	1271.0000	11.7685	1.3595
" wire . . . . .	21,041	1315.0625	12.1765	1.3140
" laminated . . . . .	22,069	1379.3125	12.7714	1.2528
Iridium, hammered . . . . .	23,000	1437.5000	13.3101	1.2021
<b>EARTH, STONES, &amp;c.</b>				
Amber . . . . .	1,078	67.3750	0.62384	25.6474
Coal . . . . .	1,250	78.7500	0.72337	21.9428
Sand . . . . .	1,500	93.7500	0.86803	18.4320
Bricks . . . . .	2,000	125.0000	1.15740	13.8240



TABLE 87.—WEIGHT AND VOLUME OF BODIES (*continued*).

BODIES.	Weight of One Cubic Foot.		Weight of One Cubic Inch.	Cubic Inches in One Pound.
	Oz.	Lb.	Oz.	Cub. In.
EARTH, STONES, &c. ( <i>continued</i> ).				
Sulphur, native . . . . .	2,033	127·0625	1·17650	13·5996
Opal . . . . .	2,114	132·1250	1·22337	13·0785
Clay . . . . .	2,160	135·0000	1·25000	12·8000
Gypsum . . . . .	2,280	142·5000	1·31944	12·1263
Porcelain, Limoges . . . . .	2,341	146·3125	1·35474	11·8103
„ China . . . . .	2,385	147·2500	1·38020	11·7351
Stone, paving . . . . .	2,416	151·4000	1·39814	11·4437
„ common . . . . .	2,520	157·5000	1·45833	10·9714
Flint . . . . .	2,594	162·1250	1·50115	10·6584
Spar . . . . .	2,594	162·1250	1·50115	10·6584
Pebble, English . . . . .	2,619	163·6875	1·51562	10·5566
Granite, Aberdeen . . . . .	2,625	164·0625	1·51909	10·5325
Quartz . . . . .	2,640	165·0000	1·52777	10·4727
Glass, green . . . . .	2,642	165·1250	1·52893	10·4648
Crystal, rock . . . . .	2,653	165·8125	1·53530	10·4214
Granite, red Egyptian . . . . .	2,654	165·8750	1·53587	10·4175
„ Cornish . . . . .	2,662	166·3750	1·53935	10·3861
Marble, Egyptian . . . . .	2,668	166·7500	1·54976	10·3628
Slate . . . . .	2,672	167·0000	1·54629	10·3473
Coral . . . . .	2,680	167·5000	1·55092	10·3164
Pearl, Oriental . . . . .	2,684	167·7500	1·55324	10·3010
Glass, bottle . . . . .	2,733	170·8125	1·58159	10·1163
Marble, green Cam- panian . . . . .	2,742	171·3750	1·58735	10·0831
Emerald of Peru . . . . .	2,775	173·4375	1·60590	9·8632
Chalk, British . . . . .	2,784	174·0000	1·61111	9·9310
Marble, Parian . . . . .	2,837	177·3125	1·64178	9·7455
Basalt, Giants' Cause- way . . . . .	2,864	179·0000	1·65740	9·6536
Glass, white . . . . .	2,892	180·7500	1·67361	9·5601
Limestone . . . . .	2,950	184·3750	1·70717	9·3721
Asbestos . . . . .	2,996	187·2500	1·73379	9·2283
Hornblende . . . . .	3,000	187·5000	1·73611	9·2160
White Lead . . . . .	3,160	197·5000	1·82870	8·7493
Glass, British flint . . . . .	3,329	208·0625	1·92650	8·3052
Diamond, average . . . . .	3,536	221·0000	2·04629	7·8190
Beryl, Oriental . . . . .	3,549	221·3125	2·05381	7·7903

TABLE 87.—WEIGHT AND VOLUME OF BODIES (*continued*).

BODIES.	Weight of One Cubic Foot.		Weight of One Cubic Inch.	Cubic Inches in One Pound.
	Oz.	Lb.	Oz.	Cub. In.
<b>EARTH, STONES, &amp;c.</b>				
<i>(continued).</i>				
Garnet, common . . . . .	3,576	223·5000	2·06944	7·7315
Topaz, average . . . . .	3,800	237·5000	2·19907	7·2800
Sapphire, Oriental . . . . .	3,994	243·3750	2·25347	7·1001
Garnet, precious . . . . .	4,230	264·3750	2·44791	6·5361
Ruby, Oriental . . . . .	4,283	267·6875	2·47858	6·4590
Jargon of Ceylon . . . . .	4,416	276·0000	2·55555	6·2608
Spar, heavy . . . . .	4,430	276·8750	2·56365	6·2410
Loadstone . . . . .	4,930	308·1250	2·85300	5·6081
The earth (mean of the globe) . . . . .	5,210	325·6250	3·01504	5·3067
<b>RESINS, GUMS, &amp;c.</b>				
Gunpowder, loose heap . . . . .	836	52·2500	0·48379	33·0717
Living men . . . . .	891	55·6875	0·51562	31·0303
Wax . . . . .	897	56·0625	0·51909	30·8227
Ice . . . . .	930	58·1250	0·53819	29·7293
Gunp'wder, close shaken . . . . .	937	58·5625	0·54224	29·5069
Tallow . . . . .	942	58·8750	0·54513	29·3503
Butter . . . . .	942	58·8750	0·54513	29·2993
Beeswax . . . . .	956	59·7500	0·55324	28·9205
Sodium . . . . .	972	60·7500	0·56250	28·4444
Camphor . . . . .	989	61·8125	0·56655	27·9555
Rosin . . . . .	1,100	68·7000	0·63657	25·0909
Pitch . . . . .	1,150	71·8750	0·66550	24·0417
Opium . . . . .	1,337	83·5625	0·77372	20·6791
Gum Arabic . . . . .	1,452	90·7500	0·84027	19·0413
Honey . . . . .	1,456	91·0000	0·84259	18·9890
Bone, of an ox . . . . .	1,659	103·6875	0·96006	16·6654
„ dry . . . . .	1,660	103·7500	0·96064	16·6554
Phosphorus . . . . .	1,714	107·1250	0·99184	16·1307
Alum . . . . .	1,714	107·1250	0·99184	16·1307
Gunpowder, solid . . . . .	1,745	109·0625	1·00983	15·8441
Nitre (saltpetre) . . . . .	1,900	118·7500	1·09953	14·5515
Ivory . . . . .	1,917	119·8125	1·10937	14·4422
<b>WOODS.</b>				
Cork . . . . .	240	15·0000	0·13888	115·2000

TABLE 87.—WEIGHT AND VOLUME OF BODIES (*continued*).

BODIES.	Weight of One Cubic Foot.		Weight of One Cubic Inch.	Cubic Inches in One Pound.
	Oz.	Lb.	Oz.	Cub. In.
WOODS ( <i>continued</i> ).				
Poplar . . . . .	383	23·9375	0·22164	71·7660
Larch . . . . .	544	34·0000	0·31481	50·8235
Fir, North of England	556	34·7500	0·32175	49·7266
Mahogany, Honduras .	560	35·0000	0·32407	49·3714
Cedar, American . . .	561	35·0625	0·32465	49·2833
Poon . . . . .	579	36·1875	0·33506	47·7512
Willow . . . . .	585	36·5625	0·35858	47·2615
Cedar . . . . .	596	37·2500	0·34490	46·3892
Cypress . . . . .	598	37·3750	0·34664	46·2341
Elm . . . . .	600	37·5000	0·34722	46·0800
Pitch-pine . . . . .	660	41·2500	0·38194	41·8909
Pear-tree . . . . .	661	41·3125	0·38252	41·8275
Walnut . . . . .	681	42·5625	0·39467	40·5991
Fir, Mar Forest . . . .	694	43·3750	0·40162	39·8386
Elder-tree . . . . .	695	43·4375	0·40219	39·7812
Orange-tree . . . . .	705	44·0625	0·40798	39·2170
Cherry-tree . . . . .	715	44·6875	0·41377	38·6685
Teak . . . . .	745	46·5625	0·43113	37·1114
Fir, Riga . . . . .	750	46·8750	0·43402	36·8640
Maple . . . . .	755	47·1857	0·43692	36·6198
Oak, Dantzic . . . . .	760	47·5000	0·43981	36·3789
Yew, Dutch . . . . .	788	49·2500	0·45590	35·0862
Apple-tree . . . . .	793	49·5625	0·45891	34·8656
Yew, Spanish . . . . .	807	50·4375	0·46701	34·2602
Ash . . . . .	845	52·8125	0·48900	32·7195
Beech . . . . .	852	53·2500	0·49305	32·4507
Oak, Canadian . . . . .	872	54·5000	0·50694	31·7064
Logwood . . . . .	913	57·0625	0·53125	30·2825
Oak, English . . . . .	970	60·6250	0·56134	28·5030
Box, French . . . . .	1,030	64·3750	0·59606	26·8427
Brazil-wood, red . . . .	1,031	64·3125	0·59664	26·8680
Mahogany, Spanish . . .	1,063	66·4250	0·61516	26·0143
Oak, English, 60 yrs old	1,170	73·1250	0·67708	23·6307
Ebony, American . . . .	1,331	83·1875	0·77025	20·7723
Lignum-vitæ . . . . .	1,333	83·3125	0·77141	20·7411
LIQUIDS.				
Ether, sulphuric . . . .	720	45·0000	0·41666	38·4000

TABLE 87.—WEIGHT AND VOLUME OF BODIES (*continued*).

BODIES.	Weight of One Cubic Foot.		Weight of One Cubic Inch.	Cubic Inches in One Pound.
	Oz.	Lb.	Oz.	Cub. In.
<i>LIQUIDS (continued).</i>				
Alcohol, absolute . . .	796	49·7500	0·46064	34·7487
Brandy . . . . .	837	52·3125	0·48437	33·0322
Bitumen, liquid . . .	848	53·0000	0·49074	32·6037
Turpentine, oil of . .	870	54·3750	0·50347	31·9632
Ether, muriatic . . .	874	54·6250	0·50578	31·6338
Olive oil . . . . .	915	57·1875	0·52951	30·2163
Moselle wine . . . .	916	57·2500	0·53009	30·1834
Whale oil . . . . .	923	57·6875	0·53414	29·9544
Proof spirit . . . . .	930	58·1250	0·53819	29·7290
Linseed oil . . . . .	940	58·7500	0·54398	29·4127
Castor oil . . . . .	970	60·6250	0·56134	28·5030
Wine, red port . . . .	990	61·8750	0·57291	27·9272
„ of Burgundy . . . .	991	61·9375	0·57349	27·8990
„ of Bordeaux . . . .	994	62·1250	0·57523	27·8148
„ white Champagne . .	997	62·3125	0·57696	27·7311
Water, distilled . . . .	1,000	62·5000	0·57870	27·6480
Tar . . . . .	1,015	63·4375	0·58738	27·2396
Vinegar . . . . .	1,026	64·1250	0·59375	26·9473
Sea-water . . . . .	1,028	64·2500	0·59490	26·8949
Milk . . . . .	1,030	64·3750	0·59606	26·8427
Ale (average) . . . . .	1,035	64·6875	0·59895	26·7130
Blood, human . . . . .	1,045	65·3125	0·60474	26·4574
Muriatic acid of com- } merce . . . . . }	1,218	76·1250	0·70486	22·6995
Aqua regia . . . . .	1,234	77·1250	0·71412	22·4051
Water of Dead Sea . .	1,240	77·5000	0·71759	22·2580
Nitrous acid . . . . .	1,452	90·7500	0·84024	19·0082
Nitric acid, or aquafortis	1,500	93·7500	0·86805	18·4000
Boracic acid . . . . .	1,830	114·3750	1·05902	15·1081
Sulphuric acid . . . .	1,848	128·0000	1·06944	13·5000
Quicksilver . . . . .	(See Metals.)			

TABLE 88.—SPECIFIC GRAVITIES OF BODIES.

*(Adapted by the Standards Department of the Board of Trade.)*

	Specific Gravity.
Agate . . . . .	2·6
Aluminium (rolled) . . . . .	2·67
„ bronze, copper 9, aluminium 1 . . . . .	8·0
Antimony . . . . .	6·72
Arsenic . . . . .	5·67
Barium . . . . .	4·0
Beech . . . . .	0·8
Bismuth . . . . .	9·82
Bone . . . . .	1·8 to 2·0
Boron . . . . .	2·69
Brass . . . . .	8·0
Brick, ordinary . . . . .	2·17
Bromine . . . . .	2·966
Bronze, copper 86·3, zinc 4·0, tin 9·7 . . . . .	8·45
Bronze, copper 32, zinc 2, tin 5 (Baily's) . . . . .	8·4
Bronze coins, copper 95, zinc 1, tin 4 . . . . .	8·66
Calcium . . . . .	1·58
Carbonic acid gas . . . . .	1·529
Chalk . . . . .	2·1
Cobalt . . . . .	7·81
Copper (rolled) . . . . .	8·94
Cork . . . . .	0·24
Ebony . . . . .	1·18
Ether, $C_2H_5O_2$ . . . . .	0·73
Glass, ordinary crown . . . . .	2·45
„ French . . . . .	2·65
„ flint . . . . .	3·59
„ crystal . . . . .	3·33
Glycerine . . . . .	1·27
Gold . . . . .	19·32
„ alloy (18 carat) . . . . .	14·88
„ „ gold 983, copper 17 . . . . .	18·92
„ „ 11 „ 1 . . . . .	17·49
„ „ 9 „ 1 . . . . .	17·17
Granite . . . . .	2·64 to 2·76
Hydrogen . . . . .	0·06926
Iodine . . . . .	4·95
Iridium . . . . .	22·38
Iron : . . . . .	
„ wrought . . . . .	7·79

TABLE 88.—SPECIFIC GRAVITIES OF BODIES (*continued*).

	Specific Gravity.
Iron, cast . . . . .	7.20
Lead . . . . .	11.35
Magnesium . . . . .	1.74
Mahogany . . . . .	0.56
Manganese . . . . .	8.01
Marble . . . . .	2.52 to 2.84
Mercury . . . . .	13.59593
Nickel (rolled) . . . . .	8.67
Nitric acid (fuming) . . . . .	1.451
Nitrogen . . . . .	0.97137
Oak . . . . .	0.93
Oil, olive . . . . .	0.91
„ sperm . . . . .	0.93
„ colza . . . . .	0.91
Osmium . . . . .	21.40
Oxygen . . . . .	1.10563
Palladium (rolled) . . . . .	11.78
Palladium alloy, Matthey's Standard, silver (	
60% palladium, 40% . . . . .)	11.00
Petroleum . . . . .	0.84
Pine wood . . . . .	0.56
Phosphorus . . . . .	1.77
Porcelain . . . . .	2.5
Platinum . . . . .	21.45
„ alloy, platinum 90, iridium 10 . . . . .	21.57
„ „ „ 85, „ 15 . . . . .	21.58
„ „ „ 2, „ 1 . . . . .	21.62
„ „ „ 5, „ 95 . . . . .	22.35
Potassium . . . . .	0.86
Quartz . . . . .	2.65122
Rhodium . . . . .	12.1
Rock crystal, <i>see</i> Quartz.	
Ruthenium . . . . .	12.29
Selenium . . . . .	4.30
Silver . . . . .	10.51
„ alloy, silver 37, copper 3 . . . . .	10.38
„ „ 9 „ 1 . . . . .	10.31
„ „ 835 „ 165 . . . . .	10.20
„ „ 80 „ 20 . . . . .	10.06
„ „ 60 „ 40 . . . . .	9.80
„ „ 13 $\frac{1}{4}$ „ 2 $\frac{3}{4}$ . . . . .	10.17
Slate . . . . .	2.11
Sodium . . . . .	0.97

TABLE 88.—SPECIFIC GRAVITIES OF BODIES (*continued*).

	Specific Gravity.
Steel (Whitworth's compressed) . . . . .	7.796
Strontium . . . . .	2.54
Sulphur . . . . .	2.0
Sulphuric acid . . . . .	1.848
Teak . . . . .	0.86
Thallium . . . . .	11.88
Tin . . . . .	7.29
Water { pure at 0°C. } { $D_{40} = 1$ . . } . . . . .	0.9998635
Wax . . . . .	0.93
Zinc, sheet . . . . .	7.19

## MANUFACTURED METALS.

## Tables of Weights of Manufactured Metals.

The following tables are for the most part calculated for the ordinary dimensions manufactured by the trades.

The units of specific gravity and weights adopted in the calculations of these tables, excepting where otherwise stated, are as follows:—

METALS.	Specific Gravity.	Weight of One Cubic Foot.	Weight of One Cubic Inch.
	Water = 1.000.	Pounds.	Pound.
Wrought Iron . . . . .	7.698	480	2778
Steel . . . . .	7.858	490	2836
Cast Iron . . . . .	7.217	450	2604
Lead . . . . .	11.355	708	4097
Copper . . . . .	8.917	554.4	3208
Brass (70 copper, 30 zinc) . . . . .	8.558	533.6	3088
" (2 " 1 " ) . . . . .	8.508	530.5	3070

The values above given for copper and brass are the results of very careful investigations made by the Broughton Copper Company.

The weights of other metals may be calculated by means of suitable multipliers from the weights of any given metal. Taking the weights of wrought-iron, copper, and the brasses successively as 1, the respective multipliers for the weights of the other metals are as follows :—

METAL.	Wrought Iron = 1.	Copper = 1.	Brass (70 C. and 30 Z.) = 1.
Wrought Iron . . . . .	1·000	·8558	·8995
Steel . . . . .	1·0208	·8837	·9182
Cast Iron . . . . .	·9375	·8117	·8433
Lead . . . . .	1·4750	1·2771	1·3269
Copper . . . . .	1·1550	1·0000	1·0388
Brass (70 copper, 30 zinc) .	1·1117	·9625	1·0000
„ (2 „ 1 „ ) .	1·1052	·9568	·9941

### Bars or Rods, and Wire.

Bars or rods are rolled to dimensions in inches and fractions of an inch, as exhibited in following Tables. Wire generally is rolled to the Imperial Gauge.

### Tubes.

Boiler tubes, of iron, steel, or brass, are manufactured to given external diameters. Iron or steel tubes for gas, steam, or water, are manufactured to given internal diameters. Copper tubes also are ordinarily manufactured to internal diameters. The thicknesses of tubes are, for the most part, regulated on the basis of the Imperial Wire-Gauge. But the old Birmingham Wire-Gauge is also, to some extent, followed.

### Joists and Girders.

The dimensions, weights, and calculated loads of joists and girders, of iron and steel are given in following Tables. The calculated strengths have been verified by numerous actual tests. The factor of safety, 4, applies to the uniformly loaded joists and girders of Messrs. Measures Brothers & Co.; the factor, 3, is applied for the distributed loads of the steel joists and girders of Messrs. Dorman, Long & Co.; and the breaking weight, applied at the centre, is given with the co-efficients of strength in the joists of the Butterley Company.

Joists fail under loads by the breaking of the flange in compression; never by tensile stress.

The normal length of joists is 30 feet.



TABLE 89.—METALS: WEIGHTS FOR VARIOUS DIMENSIONS.

METAL.	Specific Weight.	Weight of One Cubic Foot.	Weight of One Square Foot.			Weight of One Lineal Ft. 1 In. Sq.	Weight of One Cubic Inch.
			1 Inch Thick.	$\frac{1}{8}$ th Inch Thick.	$\frac{1}{16}$ th Inch Thick.		
	Wrought Iron = 1.	Lb.	Lb.	Lb.	Lb.	Lb.	Lb.
Aluminium, wrought	·348	167	13·92	1·74	1·39	1·160	·097
„ cast . . .	·333	160	13·33	1·67	1·33	1·111	·092
Antimony . . .	·879	418	34·83	4·35	3·48	2·902	·242
Bismuth . . .	1·285	617	51·42	6·42	5·14	4·283	·357
Brass, cast . . .	1·052	505	42·08	5·26	4·21	3·507	·292
„ sheet . . .	1·098	527	43·92	5·49	4·39	3·652	·304
„ yellow . . .	1·079	518	43·17	5·40	4·32	3·597	·298
„ Muntz metal.	1·062	511	42·58	5·32	4·26	3·549	·296
„ wire . . .	1·110	533	44·42	5·55	4·44	3·701	·308
Bronze, gun-metal .	1·106	531	44·25	5·54	4·43	3·688	·307
„ mill bearings .	1·133	544	45·33	5·66	4·53	3·780	·315
„ small bells .	1·004	482	40·17	5·04	4·02	3·347	·279
„ speculum metal	·969	465	38·75	4·84	3·88	3·299	·269
Copper, sheet . . .	1·114	549	45·75	5·72	4·58	3·813	·318
„ hammered .	1·158	556	46·33	5·79	4·63	3·861	·322
„ wire . . .	1·154	554	46·17	5·77	4·62	3·778	·315
Gold . . .	2·500	1200	100·00	12·50	10·00	8·333	·694
Iron, cast . . .	·937	450	37·50	4·69	3·75	3·125	·260
„ wrought . . .	1·000	480	40·00	5·00	4·00	3·333	·278
Lead, sheet . . .	1·483	712	59·33	7·41	5·93	4·944	·412
Manganese . . .	1·040	499	41·58	5·20	4·16	3·465	·289
Mercury . . .	1·769	849	70·75	8·84	7·07	5·896	·491
Nickel, hammered .	1·127	541	45·08	5·64	4·51	3·757	·313
„ cast . . .	1·075	516	43·00	5·37	4·30	3·583	·299
Platinum . . .	2·796	1342	111·83	13·97	11·18	9·320	·777
Silver . . .	1·365	655	54·58	6·82	5·46	4·549	·379
Steel . . .	1·020	490	40·83	5·12	4·10	3·403	·284
Tin . . .	·962	462	38·50	4·81	3·85	3·208	·268
Zinc, sheet . . .	·935	449	37·42	4·67	3·74	3·118	·260
„ cast . . .	·892	428	35·67	4·46	3·57	2·972	·248

TABLE 90.—WEIGHTS OF FLAT BAR IRON

Length 1 Foot.

Thick- ness.	Width in Inches.								
	$\frac{1}{2}$	$\frac{3}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	$1\frac{1}{8}$	$1\frac{1}{4}$	$1\frac{3}{8}$	$1\frac{1}{2}$
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{1}{8}$	·208	·260	·312	·365	·417	·469	·521	·573	·625
$\frac{3}{16}$	·312	·391	·469	·547	·625	·703	·781	·859	·937
$\frac{1}{4}$	·417	·521	·625	·729	·833	·938	1·04	1·15	1·25
$\frac{5}{16}$	·521	·651	·781	·911	1·04	1·17	1·30	1·43	1·56
$\frac{3}{8}$	·625	·781	·937	1·09	1·25	1·41	1·56	1·72	1·88
$\frac{7}{16}$	·729	·911	1·09	1·28	1·46	1·64	1·82	2·01	2·19
$\frac{1}{2}$	·833	1·04	1·25	1·46	1·67	1·88	2·08	2·29	2·50
$\frac{9}{16}$	·937	1·17	1·41	1·64	1·88	2·11	2·34	2·58	2·81
$\frac{5}{8}$	1·04	1·30	1·56	1·82	2·08	2·34	2·60	2·86	3·13
$\frac{11}{16}$	1·15	1·43	1·72	2·01	2·29	2·58	2·86	3·15	3·44
$\frac{3}{4}$	1·25	1·56	1·87	2·19	2·50	2·81	3·13	3·44	3·75
$\frac{13}{16}$	1·35	1·69	2·03	2·37	2·71	3·05	3·39	3·72	4·06
$\frac{7}{8}$	1·46	1·82	2·19	2·55	2·92	3·28	3·65	4·01	4·38
$\frac{15}{16}$	1·56	1·95	2·34	2·73	3·13	3·52	3·91	4·30	4·69
1	1·67	2·08	2·50	2·92	3·33	3·75	4·17	4·58	5·00

Thick- ness.	Width in Inches.									
	$1\frac{5}{8}$	$1\frac{3}{4}$	$1\frac{7}{8}$	2	$2\frac{1}{8}$	$2\frac{1}{4}$	$2\frac{3}{8}$	$2\frac{1}{2}$	$2\frac{5}{8}$	$2\frac{3}{4}$
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{1}{8}$	·677	·729	·781	·833	...	...	...	...	...	...
$\frac{3}{16}$	1·02	1·09	1·17	1·25	1·33	1·41	1·48	1·56	1·64	1·72
$\frac{1}{4}$	1·35	1·46	1·56	1·67	1·77	1·88	1·98	2·08	2·19	2·29
$\frac{5}{16}$	1·69	1·82	1·95	2·08	2·21	2·34	2·47	2·60	2·73	2·86
$\frac{3}{8}$	2·03	2·19	2·34	2·50	2·66	2·81	2·97	3·13	3·28	3·44
$\frac{7}{16}$	2·37	2·55	2·73	2·92	3·10	3·28	3·46	3·65	3·83	4·01
$\frac{1}{2}$	2·71	2·92	3·13	3·33	3·54	3·75	3·96	4·17	4·38	4·58
$\frac{9}{16}$	3·05	3·28	3·52	3·75	3·98	4·22	4·45	4·69	4·92	5·16
$\frac{5}{8}$	3·39	3·65	3·91	4·17	4·43	4·69	4·95	5·21	5·47	5·73
$\frac{11}{16}$	3·72	4·01	4·30	4·58	4·87	5·16	5·44	5·73	6·02	6·30
$\frac{3}{4}$	4·06	4·38	4·69	5·00	5·31	5·63	5·94	6·25	6·56	6·88
$\frac{13}{16}$	4·40	4·74	5·08	5·42	5·76	6·09	6·43	6·77	7·11	7·45
$\frac{7}{8}$	4·74	5·10	5·47	5·83	6·20	6·56	6·93	7·29	7·66	8·02
$\frac{15}{16}$	5·08	5·47	5·86	6·25	6·64	7·03	7·42	7·81	8·20	8·59
1	5·42	5·83	6·25	6·67	7·08	7·50	7·92	8·33	8·75	9·17

TABLE 90.—WEIGHTS OF FLAT BAR IRON (*continued*).

Thick- ness.	Width in Inches.									
	2½	3	3½	3½	3½	4	4½	4½	4½	5
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
⅜	1.80	1.88	2.03	...	...	...	...	...	...	...
¼	2.40	2.50	2.71	2.92	3.13	3.33	3.54	3.75	3.96	4.17
⅓	3.00	3.13	3.39	3.65	3.91	4.17	4.43	4.69	4.95	5.21
⅔	3.59	3.75	4.06	4.38	4.69	5.00	5.31	5.63	5.94	6.25
7/16	4.19	4.38	4.74	5.10	5.47	5.83	6.20	6.56	6.93	7.29
½	4.79	5.00	5.42	5.83	6.25	6.67	7.08	7.50	7.92	8.33
9/16	5.39	5.63	6.09	6.56	7.03	7.50	7.97	8.44	8.91	9.38
5/8	6.00	6.25	6.77	7.29	7.81	8.33	8.85	9.38	9.90	10.4
11/16	6.59	6.88	7.45	8.02	8.59	9.17	9.74	10.3	10.9	11.5
¾	7.19	7.50	8.13	8.75	9.38	10.0	10.6	11.3	11.9	12.5
13/16	7.79	8.13	8.80	9.48	10.2	10.8	11.5	12.2	12.9	13.5
7/8	8.39	8.75	9.48	10.2	10.9	11.7	12.4	13.1	13.9	14.6
15/16	8.98	9.38	10.2	10.9	11.7	12.5	13.3	14.1	14.8	15.6
1	9.58	10.0	10.8	11.7	12.5	13.3	14.2	15.0	15.8	16.7

Thick- ness.	Width in Inches.								
	5½	6	6½	7	8	9	10	11	12
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
¼	4.58	5.00	5.42	5.83	6.67	7.50	8.33	9.17	10.0
⅓	5.73	6.25	6.77	7.29	8.33	9.38	10.4	11.5	12.5
⅔	6.88	7.50	8.13	8.75	10.0	11.3	12.5	13.8	15.0
7/16	8.02	8.75	9.47	10.2	11.7	13.1	14.6	16.0	17.5
½	9.17	10.0	10.8	11.7	13.3	15.0	16.7	18.3	20.0
9/16	10.3	11.3	12.2	13.1	15.0	16.9	18.8	20.6	22.5
5/8	11.5	12.5	13.5	14.6	16.7	18.8	20.8	22.9	25.0
11/16	12.6	13.8	14.9	16.0	18.3	20.6	22.9	25.2	27.5
¾	13.8	15.0	16.3	17.5	20.0	22.5	25.0	27.5	30.0
13/16	14.9	16.3	17.6	19.0	21.7	24.4	27.1	29.8	32.5
7/8	16.0	17.5	19.0	20.4	23.3	26.3	29.2	32.1	35.0
15/16	17.2	18.8	20.3	21.9	25.0	28.1	31.3	34.4	37.5
1	18.3	20.0	21.7	23.3	26.7	30.0	33.3	36.7	40.0

TABLE 91.—WEIGHTS OF ROUND IRON.

Length, 1 Foot.

Diam.	Weight.	Diam.	Weight.	Diam.	W. ight.	Diam.	Weight.
Inches.	Lbs.	Inches.	Lbs.	Inches.	Lbs.	Inches.	Cwts.
$\frac{1}{8}$	·041	1	2·62	$2\frac{3}{8}$	14·8	8	1·496
$\frac{5}{32}$	·064	$1\frac{1}{32}$	2·78	$2\frac{7}{16}$	15·6	$8\frac{1}{2}$	1·689
$\frac{3}{16}$	·092	$1\frac{1}{16}$	2·96	$2\frac{1}{2}$	16·4	9	1·893
$\frac{7}{32}$	·125	$1\frac{3}{32}$	3·14	$2\frac{5}{8}$	18·0	$9\frac{1}{2}$	2·110
$\frac{1}{4}$	·164	$1\frac{1}{8}$	3·31	$2\frac{3}{4}$	19·8	10	2·338
$\frac{9}{32}$	·207	$1\frac{5}{32}$	3·50	$2\frac{7}{8}$	21·6	$10\frac{1}{2}$	2·577
$\frac{5}{16}$	·256	$1\frac{3}{16}$	3·69	3	23·6	11	2·828
$\frac{11}{32}$	·310	$1\frac{7}{32}$	3·90	$3\frac{1}{8}$	25·6	$11\frac{1}{2}$	3·088
$\frac{3}{8}$	·368	$1\frac{1}{4}$	4·09	$3\frac{1}{4}$	27·7	12	3·366
$\frac{13}{32}$	·432	$1\frac{9}{32}$	4·29	$3\frac{3}{8}$	29·8	$12\frac{1}{2}$	3·656
$\frac{7}{16}$	·501	$1\frac{5}{16}$	4·51	$3\frac{1}{2}$	32·1	13	3·950
$\frac{15}{32}$	·575	$1\frac{11}{32}$	4·70	$3\frac{5}{8}$	34·4	$13\frac{1}{2}$	4·260
$\frac{1}{2}$	·654	$1\frac{3}{8}$	4·95	$3\frac{3}{4}$	36·8	14	4·581
$\frac{17}{32}$	·740	$1\frac{7}{16}$	5·08	$3\frac{7}{8}$	39·3	$14\frac{1}{2}$	4·915
$\frac{9}{16}$	·828	$1\frac{1}{2}$	5·89	4	41·9	15	5·259
$\frac{19}{32}$	·922	$1\frac{9}{16}$	6·29	$4\frac{1}{4}$	47·3	$15\frac{1}{2}$	5·616
$\frac{5}{8}$	1·02	$1\frac{5}{8}$	6·91	$4\frac{1}{2}$	53·0	16	5·984
$\frac{21}{32}$	1·13	$1\frac{11}{16}$	7·46	$4\frac{3}{4}$	59·1	$16\frac{1}{2}$	6·364
$\frac{11}{16}$	1·24	$1\frac{3}{4}$	8·02	5	65·5	17	6·755
$\frac{23}{32}$	1·27	$1\frac{13}{16}$	8·60	$5\frac{1}{4}$	72·2	$17\frac{1}{2}$	7·159
$\frac{3}{4}$	1·47	$1\frac{7}{8}$	9·20	$5\frac{1}{2}$	79·2	18	7·573
$\frac{25}{32}$	1·60	$1\frac{15}{16}$	9·83	$5\frac{3}{4}$	86·6	19	8·438
$\frac{13}{16}$	1·73	2	10·5	6	94·2	20	9·350
$\frac{27}{32}$	1·86	$2\frac{1}{16}$	11·1	Inches.	Cwts.	21	10·31
$\frac{7}{8}$	2·00	$2\frac{1}{8}$	11·8			22	11·31
$\frac{29}{32}$	2·15	$2\frac{3}{16}$	12·6			23	12·37
$\frac{15}{16}$	2·30	$2\frac{1}{4}$	13·3			24	13·46
$\frac{31}{32}$	2·46	$2\frac{5}{16}$	14·0	$7\frac{1}{2}$	1·315		

TABLE 92.—WEIGHTS OF SQUARE IRON.

Length, 1 Foot.

Side of Square.	Weight.	Side of Square.	Weight.	Side of Square.	Weight.	Side of Square.	Weight.
Inches.	Lbs.	Inches.	Lbs.	Inches.	Lbs.	Inches.	Lbs.
$\frac{1}{8}$	·052	$\frac{11}{16}$	1·58	$1\frac{7}{32}$	4·96	$2\frac{1}{2}$	20·8
$\frac{5}{32}$	·081	$\frac{23}{32}$	1·72	$1\frac{1}{4}$	5·21	$2\frac{5}{8}$	23·0
$\frac{3}{16}$	·117	$\frac{3}{4}$	1·88	$1\frac{5}{16}$	5·74	$2\frac{3}{4}$	25·2
$\frac{7}{32}$	·159	$\frac{25}{32}$	2·03	$1\frac{3}{8}$	6·30	$2\frac{7}{8}$	27·6
$\frac{1}{4}$	·208	$\frac{13}{16}$	2·20	$1\frac{7}{16}$	6·89	3	30·0
$\frac{9}{32}$	·265	$\frac{27}{32}$	2·40	$1\frac{1}{2}$	7·50	$3\frac{1}{4}$	35·2
$\frac{5}{16}$	·326	$\frac{27}{16}$	2·55	$1\frac{9}{16}$	8·14	$3\frac{1}{2}$	40·8
$\frac{11}{32}$	·395	$\frac{29}{16}$	2·75	$1\frac{5}{8}$	8·80	$3\frac{3}{4}$	46·9
$\frac{3}{8}$	·469	$\frac{15}{8}$	2·93	$1\frac{11}{16}$	9·60	4	53·3
$\frac{13}{32}$	·550	$\frac{31}{32}$	3·12	$1\frac{3}{4}$	10·2	$4\frac{1}{4}$	60·2
$\frac{7}{16}$	·638	1	3·33	$1\frac{13}{16}$	11·0	$4\frac{1}{2}$	67·5
$\frac{15}{32}$	·732	$1\frac{1}{32}$	3·54	$1\frac{7}{8}$	11·7	$4\frac{3}{4}$	75·2
$\frac{1}{2}$	·833	$1\frac{1}{16}$	3·76	$1\frac{15}{16}$	12·5	5	83·3
$\frac{17}{32}$	·940	$1\frac{3}{32}$	4·03	2	13·3	$5\frac{1}{4}$	91·9
$\frac{9}{16}$	1·06	$1\frac{1}{8}$	4·22	$2\frac{1}{8}$	15·1	$5\frac{1}{2}$	100·8
$\frac{19}{32}$	1·17	$1\frac{5}{16}$	4·48	$2\frac{1}{4}$	16·9	$5\frac{3}{4}$	110·2
$\frac{5}{8}$	1·30	$1\frac{3}{8}$	4·70	$2\frac{3}{8}$	18·8	6	120·0
$\frac{21}{32}$	1·43						

## French Bar Iron.

The length of bars varies. In general, it is 4 metres for the larger bars, and 6 metres for the smaller bars; with a tolerance of  $\frac{1}{2}$  metre, more or less. Square iron advances in size by 1 millimetre from 6 to 86 millimetres. Round iron advances by 1 millimetre from 6 to 28 millimetres; and by 2 millimetres from 28 to 130 millimetres, with a few exceptions. Flat bar iron:—

16, 18, 20, 22, 24, 26, 28, 30, 32, 34, 36 millimetres, by 1 to 3 millimetres thick.

18, 20, 22, 24, 26, 28, 30, 32 millimetres, by 4 to 14 millimetres thick.

34, 40, 42, 46, 48 millimetres, by  $1\frac{1}{2}$  to 30 millimetres thick.

48, 50, 52, 54, 58, 60, 62, 64, 66, 68, 70, 72 millimetres, by 2 to 40 millimetres thick.

75 by 2 to 40, 80 by 2 to 45, 85 by 2 to 50, 90 by 2 to 45, 95 by 2 to 50, 100 by 2 to 50, 110 by 2 to 40, 115 by 2 to 40

135 by 3 to 45, 140 by 3 to 40, 150 by 3 to 45, 160 by 3 to 45, 165 by 3 to 45, 180 by 3 to 45, 210 by 8 to 45, 250 by 7 to 40, 300 by 8 to 40, 355 by 8 to 40, 400 by 8 to 40, 450 by 8 to 40 millimetres thick.

TABLE 93.—WROUGHT IRON : WEIGHT OF ONE SQUARE FOOT FOR ALL THICKNESSES OF THE IMPERIAL WIRE GAUGE (Standards Department).

Specific Gravity, 7·80.

I. W. G. Gauge Number.	Thickness.	Weight per Square Foot.	I. W. G. Gauge Number.	Thickness.	Weight per Square Foot.
No.	Inch.	Pounds.	No.	Inch.	Pounds.
7/0	·500	20·254	23	·024	·972
6/0	·464	18·796	24	·022	·891
5/0	·432	17·500	25	·020	·810
4/0	·400	16·203	26	·018	·729
3/0	·372	15·069	27	·0164	·664
2/0	·348	14·097	28	·0148	·600
0	·324	13·125	29	·0136	·551
1	·300	12·153	30	·0124	·502
2	·276	11·180	31	·0116	·470
3	·252	10·208	32	·0108	·437
4	·232	9·398	33	·0100	·405
5	·212	8·588	34	·0092	·373
6	·192	7·778	35	·0084	·340
7	·176	7·130	36	·0076	·308
8	·160	6·481	37	·0068	·275
9	·144	5·833	38	·0060	·243
10	·128	5·185	39	·0052	·211
11	·116	4·699	40	·0048	·194
12	·104	4·213	41	·0044	·178
13	·092	3·727	42	·0040	·162
14	·080	3·241	43	·0036	·146
15	·072	2·917	44	·0032	·130
16	·064	2·593	45	·0028	·113
17	·056	2·268	46	·0024	·097
18	·048	1·944	47	·0020	·081
19	·040	1·620	48	·0016	·065
20	·036	1·458	49	·0012	·049
21	·032	1·296	50	·0010	·041
22	·028	1·134			

TABLE 94.—ANGLE IRONS AND TEE IRONS: WEIGHT.  
Length, 1 Foot.

Average Thickness.	Sum of the Width and Depth in Inches.							
	2	2 $\frac{1}{4}$	2 $\frac{1}{2}$	2 $\frac{3}{4}$	3	3 $\frac{1}{4}$	3 $\frac{1}{2}$	3 $\frac{3}{4}$
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{1}{8}$	·78	·88	·99	1·09	1·20	1·30	1·41	1·51
$\frac{3}{16}$	1·13	1·29	1·45	1·60	1·76	1·91	2·07	2·23
$\frac{1}{4}$	1·46	1·67	1·88	2·08	2·29	2·50	2·71	2·92
$\frac{5}{16}$	1·76	2·02	2·28	2·54	2·80	3·06	3·32	3·58
$\frac{3}{8}$	...	...	...	...	3·28	3·59	3·91	4·22
$\frac{7}{16}$	...	...	...	...	...	...	4·48	4·84
Average Thickness.	Sum of the Width and Depth in Inches.							
	4	4 $\frac{1}{4}$	4 $\frac{1}{2}$	4 $\frac{3}{4}$	5	5 $\frac{1}{4}$	5 $\frac{1}{2}$	5 $\frac{3}{4}$
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{3}{16}$	2·38	2·54	2·70	2·85	3·01	3·16	3·32	3·48
$\frac{1}{4}$	3·13	3·33	3·54	3·75	3·96	4·17	4·38	4·58
$\frac{5}{16}$	3·84	4·10	4·36	4·62	4·88	5·14	5·40	5·66
$\frac{3}{8}$	4·53	4·84	5·16	5·47	5·78	6·09	6·41	6·72
$\frac{7}{16}$	5·20	5·56	5·92	6·29	6·65	7·02	7·38	7·75
$\frac{1}{2}$	...	...	6·67	7·08	7·50	7·92	8·33	8·75
$\frac{9}{16}$	...	...	7·38	7·85	8·32	8·79	9·26	9·73
$\frac{5}{8}$	...	...	...	8·59	9·11	9·63	10·16	10·68
$\frac{11}{16}$	...	...	...	...	10·03	10·62	11·20	11·78
$\frac{3}{4}$	...	...	...	...	...	...	...	12·50
Average Thickness.	Sum of the Width and Depth in Inches.							
	6	6 $\frac{1}{2}$	7	7 $\frac{1}{2}$	8	8 $\frac{1}{2}$	9	9 $\frac{1}{2}$
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{1}{4}$	4·79	5·21	5·63	6·04	6·46	6·88	7·29	7·71
$\frac{5}{16}$	5·92	6·45	6·97	7·49	8·01	8·53	9·05	9·57
$\frac{3}{8}$	7·03	7·66	8·28	8·91	9·53	10·16	10·78	11·41
$\frac{7}{16}$	8·11	8·84	9·57	10·30	11·03	11·76	12·49	13·22
$\frac{1}{2}$	9·17	10·00	10·83	11·67	12·50	13·33	14·17	15·00
$\frac{9}{16}$	10·20	11·13	12·07	13·01	13·94	14·88	15·82	16·76
$\frac{5}{8}$	11·19	12·24	13·28	14·32	15·36	16·41	17·45	18·49
$\frac{11}{16}$	12·37	13·54	14·70	15·87	17·03	18·20	19·36	20·53
$\frac{3}{4}$	13·13	14·38	15·63	16·88	18·13	19·38	20·63	21·88
$\frac{7}{8}$	14·95	16·41	17·86	19·32	20·78	22·24	23·70	25·16
1	...	...	...	21·67	23·33	25·00	26·67	28·33

TABLE 94.—ANGLE IRONS AND TEE IRONS : WEIGHT  
(continued).

Average Thick- ness.	Sum of the Width and Depth in Inches.							
	10	10½	11	12	13	14	15	16
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{3}{8}$	12·03	12·66	13·28	14·53	...	...	...	...
$\frac{7}{16}$	13·95	14·67	15·40	16·86	18·31	19·77	21·22	22·67
$\frac{1}{2}$	15·83	16·67	17·50	19·17	20·84	22·50	24·17	25·84
$\frac{9}{16}$	17·70	18·63	19·57	21·44	23·31	25·19	27·06	28·93
$\frac{5}{8}$	19·53	20·57	21·61	23·70	25·78	27·87	29·95	32·03
$\frac{11}{16}$	21·69	22·86	24·03	26·36	28·70	31·03	33·36	35·70
$\frac{3}{4}$	23·13	24·38	25·63	28·13	30·63	33·13	35·63	38·13
$\frac{7}{8}$	26·61	28·07	29·53	32·45	35·36	38·28	41·19	44·12
1	30·00	31·67	33·333	36·67	40·00	43·30	46·67	50·00

TABLE 95.—WEIGHT OF FLAT BAR STEEL.

Length, 1 Foot.

Thick- ness.	Width.								
	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	1½	1¼	1⅝	1½
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{1}{8}$	·213	·266	·319	·372	·425	·478	·532	·584	·638
$\frac{3}{16}$	·320	·399	·478	·558	·638	·717	·797	·877	·957
$\frac{1}{4}$	·425	·532	·638	·744	·851	·960	1·06	1·17	1·28
$\frac{5}{16}$	·532	·665	·797	·930	1·06	1·20	1·33	1·46	1·59
$\frac{3}{8}$	·638	·797	·957	1·11	1·28	1·43	1·59	1·75	1·91
$\frac{7}{16}$	·744	·930	1·12	1·30	1·49	1·67	1·86	2·05	2·23
$\frac{1}{2}$	·851	1·06	1·28	1·49	1·70	1·91	2·13	2·34	2·55
$\frac{9}{16}$	·957	1·20	1·43	1·67	1·91	2·15	2·39	2·63	2·87
$\frac{5}{8}$	1·06	1·33	1·59	1·86	2·13	2·39	2·66	2·92	3·19
$\frac{11}{16}$	1·17	1·46	1·75	2·05	2·34	2·63	2·92	3·21	3·51
$\frac{3}{4}$	1·28	1·59	1·91	2·23	2·55	2·87	3·19	3·51	3·83
$\frac{13}{16}$	1·38	1·73	2·07	2·42	2·76	3·11	3·45	3·70	4·15
$\frac{7}{8}$	1·49	1·86	2·23	2·60	2·98	3·35	3·72	4·09	4·47
$\frac{15}{16}$	1·59	1·99	2·39	2·79	3·19	3·59	3·99	4·39	4·78
1	1·70	2·13	2·55	2·98	3·40	3·83	4·25	4·68	5·10



TABLE 95.—WEIGHT OF FLAT BAR STEEL (*continued*).

Thick- ness.	Width.									
	1½	1¾	1⅞	2	2⅛	2¼	2⅝	2½	2¾	2⅞
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
⅛	·691	·744	·797	·851	·904	·958	1·01	1·06	1·11	1·16
3/16	1·04	1·11	1·196	1·28	1·36	1·43	1·51	1·59	1·67	1·75
¼	1·38	1·49	1·59	1·70	1·81	1·91	2·02	2·13	2·23	2·34
5/16	1·73	1·86	1·99	2·13	2·26	2·39	2·52	2·66	2·79	2·92
¾	2·07	2·23	2·39	2·55	2·71	2·87	3·03	3·19	3·35	3·51
7/16	2·42	2·60	2·79	2·98	3·16	3·35	3·53	3·72	3·91	4·09
½	2·76	2·98	3·19	3·40	3·61	3·83	4·04	4·25	4·46	4·68
9/16	3·11	3·35	3·59	3·83	4·07	4·31	4·54	4·78	5·02	5·26
5/8	3·45	3·72	3·99	4·25	4·52	4·78	5·05	5·31	5·58	5·84
11/16	3·80	4·09	4·39	4·68	4·97	5·26	5·56	5·86	6·14	6·43
¾	4·14	4·46	4·78	5·10	5·42	5·74	6·06	6·38	6·69	7·01
13/16	4·49	4·84	5·18	5·53	5·87	6·22	6·57	6·92	7·26	7·60
7/8	4·83	5·21	5·58	5·96	6·32	6·79	7·07	7·44	7·81	8·18
15/16	5·18	5·58	5·98	6·38	6·78	7·18	7·58	7·98	8·37	8·77
1	5·53	5·96	6·38	6·81	7·23	7·66	8·08	8·51	8·93	9·36

Thick- ness.	Width.									
	2⅞	3	3¼	3½	3¾	4	4¼	4½	4¾	5
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
⅛	1·22	1·28	1·38	1·49	1·59	1·70	...	...	...	...
3/16	1·83	1·91	2·07	2·23	2·39	2·55	...	...	...	...
¼	2·44	2·55	2·76	2·98	3·19	3·40	3·61	3·83	4·04	4·25
5/16	3·06	3·19	3·45	3·72	3·98	4·25	4·51	4·78	5·05	5·32
¾	3·67	3·83	4·14	4·46	4·78	5·10	5·44	5·74	6·06	6·38
7/16	4·28	4·46	4·83	5·21	5·58	5·95	6·32	6·70	7·07	7·44
½	4·89	5·10	5·53	5·95	6·38	6·80	7·23	7·66	8·08	8·50
9/16	5·50	5·74	6·22	6·70	7·18	7·66	8·13	8·61	9·09	9·57
5/8	6·11	6·38	6·91	7·44	7·97	8·50	9·04	9·57	10·10	10·63
11/16	6·72	7·02	7·60	8·19	8·78	9·36	9·94	10·52	11·11	11·70
¾	7·33	7·65	8·29	8·93	9·56	10·20	10·85	11·48	12·12	12·76
13/16	7·95	8·29	8·98	9·68	10·37	11·06	11·75	12·44	13·13	13·82
7/8	8·55	8·93	9·67	10·41	11·16	11·90	12·65	13·40	14·14	14·89
15/16	9·17	9·57	10·37	11·16	11·96	12·76	13·56	14·35	15·15	15·95
1	9·78	10·21	11·06	11·91	12·76	13·68	14·46	15·31	16·16	17·01

TABLE 95.—WEIGHT OF FLAT BAR STEEL (*continued*).

Thick- ness.	Width.								
	5½	6	6½	7	8	9	10	11	12
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$\frac{1}{8}$	4·68	5·10	5·53	5·95	6·80	7·66	8·51	9·36	10·21
$\frac{5}{16}$	5·84	6·38	6·91	7·44	8·50	9·57	10·63	11·70	12·76
$\frac{3}{8}$	7·02	7·66	8·29	8·93	10·20	11·48	12·76	14·04	15·31
$\frac{7}{16}$	8·19	8·93	9·68	10·42	11·90	13·39	14·89	16·37	17·86
$\frac{1}{2}$	9·36	10·21	11·06	11·91	13·60	15·31	17·01	18·71	20·42
$\frac{9}{16}$	10·53	11·48	12·44	13·40	15·30	17·23	19·14	21·05	22·97
$\frac{5}{8}$	11·70	12·76	13·82	14·89	17·00	19·14	21·27	23·39	25·52
$\frac{11}{16}$	12·87	14·04	15·20	16·37	18·70	21·05	23·39	25·73	28·07
$\frac{3}{4}$	14·04	15·31	16·59	17·86	20·40	22·97	25·32	28·07	30·62
$\frac{13}{16}$	15·21	16·59	17·97	19·35	22·10	24·88	27·65	30·41	33·18
$\frac{7}{8}$	16·37	17·86	19·35	20·84	23·80	26·80	29·77	32·75	35·73
$\frac{15}{16}$	17·54	19·14	20·73	21·33	25·50	28·71	31·90	35·09	38·28
1	18·71	20·41	22·12	23·82	27·20	30·60	34·03	37·43	40·80

TABLE 96.—WEIGHT OF SQUARE STEEL.  
Length, 1 Foot.

Side of Square.	Weight.	Side of Square.	Weight.	Side of Square.	Weight.	Side of Square.	Weight.
Inches.	Lbs.	Inches.	Lbs.	Inches.	Lbs.	Inches.	Lbs.
$\frac{1}{8}$	·053	$\frac{11}{16}$	1·61	$1\frac{7}{32}$	5·06	$2\frac{1}{2}$	21·3
$\frac{5}{32}$	·083	$\frac{23}{32}$	1·76	$1\frac{1}{4}$	5·32	$2\frac{5}{8}$	23·5
$\frac{3}{16}$	·120	$\frac{3}{4}$	1·91	$1\frac{5}{16}$	5·86	$2\frac{3}{4}$	25·7
$\frac{7}{32}$	·163	$\frac{25}{32}$	2·08	$1\frac{3}{8}$	6·43	$2\frac{7}{8}$	28·1
$\frac{1}{4}$	·213	$\frac{13}{16}$	2·25	$1\frac{7}{16}$	7·03	3	30·6
$\frac{9}{32}$	·269	$\frac{27}{32}$	2·45	$1\frac{1}{2}$	7·71	$3\frac{1}{4}$	35·9
$\frac{5}{16}$	·332	$\frac{7}{8}$	2·61	$1\frac{9}{16}$	8·31	$3\frac{1}{2}$	41·7
$\frac{11}{32}$	·402	$\frac{29}{32}$	2·81	$1\frac{5}{8}$	8·99	$3\frac{3}{4}$	47·8
$\frac{3}{8}$	·479	$\frac{15}{16}$	2·99	$1\frac{11}{16}$	9·80	4	54·4
$\frac{13}{32}$	·562	$\frac{31}{32}$	3·19	$1\frac{3}{4}$	10·4	$4\frac{1}{4}$	61·5
$\frac{7}{16}$	·651	1	3·40	$1\frac{13}{16}$	11·2	$4\frac{1}{2}$	68·9
$\frac{9}{16}$	·748	$1\frac{1}{32}$	3·61	$1\frac{1}{2}$	12·0	$4\frac{3}{4}$	76·8
$\frac{5}{8}$	·851	$1\frac{1}{16}$	3·84	$1\frac{13}{16}$	12·8	5	85·1
$\frac{17}{32}$	·960	$1\frac{3}{32}$	4·11	2	13·6	$5\frac{1}{4}$	93·8
$\frac{9}{16}$	1·08	$1\frac{1}{8}$	4·31	$2\frac{1}{8}$	15·4	$5\frac{1}{2}$	102·9
$\frac{19}{32}$	1·20	$1\frac{5}{16}$	4·57	$2\frac{1}{4}$	17·2	$5\frac{3}{4}$	112·4
$\frac{5}{8}$	1·33	$1\frac{3}{8}$	4·80	$2\frac{3}{8}$	19·2	6	122·5
$\frac{21}{32}$	1·47						

TABLE 97.—WEIGHT OF ROUND STEEL.  
Length, 1 Foot.

Diam.	Weight.	Diam.	Weight.	Diam.	Weight.	Diam.	Weight.
Inches.	Lbs.	Inches.	Lbs.	Inches.	Lbs.	Inches.	Cwts.
$\frac{1}{8}$	·042	1	2·68	$2\frac{3}{8}$	15·1	8	1·527
$\frac{5}{32}$	·065	$1\frac{1}{32}$	2·84	$2\frac{7}{16}$	15·9	$8\frac{1}{2}$	1·725
$\frac{3}{16}$	·094	$1\frac{1}{16}$	3·02	$2\frac{1}{2}$	16·8	9	1·932
$\frac{7}{32}$	·128	$1\frac{3}{32}$	3·21	$2\frac{5}{8}$	18·4	$9\frac{1}{2}$	2·154
$\frac{1}{4}$	·167	$1\frac{1}{8}$	3·38	$2\frac{3}{4}$	20·2	10	2·387
$\frac{9}{32}$	·211	$1\frac{5}{32}$	3·57	$2\frac{7}{8}$	22·1	$10\frac{1}{2}$	2·631
$\frac{5}{16}$	·261	$1\frac{3}{16}$	3·77	3	24·1	11	2·887
$\frac{11}{32}$	·317	$1\frac{7}{32}$	3·98	$3\frac{1}{8}$	26·1	$11\frac{1}{2}$	3·152
$\frac{3}{8}$	·376	$1\frac{1}{4}$	4·17	$3\frac{1}{4}$	28·3	12	3·436
$\frac{13}{32}$	·441	$1\frac{9}{32}$	4·38	$3\frac{3}{8}$	30·4	$12\frac{1}{2}$	3·732
$\frac{7}{16}$	·511	$1\frac{5}{16}$	4·61	$3\frac{1}{2}$	32·8	13	4·032
$\frac{15}{32}$	·587	$1\frac{11}{32}$	4·80	$3\frac{5}{8}$	35·1	$13\frac{1}{2}$	4·349
$\frac{1}{2}$	·658	$1\frac{3}{8}$	5·05	$3\frac{3}{4}$	37·6	14	4·676
$\frac{17}{32}$	·755	$1\frac{7}{16}$	5·19	$3\frac{7}{8}$	40·1	$14\frac{1}{2}$	5·317
$\frac{9}{16}$	·845	$1\frac{1}{2}$	6·01	4	42·8	15	5·668
$\frac{19}{32}$	·941	$1\frac{9}{16}$	6·52	$4\frac{1}{4}$	46·3	$15\frac{1}{2}$	5·733
$\frac{5}{8}$	1·04	$1\frac{5}{8}$	7·05	$4\frac{1}{2}$	54·1	16	6·108
$\frac{21}{32}$	1·15	$1\frac{11}{16}$	7·62	$4\frac{3}{4}$	60·3	$16\frac{1}{2}$	6·496
$\frac{11}{16}$	1·29	$1\frac{3}{4}$	8·19	5	66·9	17	6·896
$\frac{23}{32}$	1·30	$1\frac{13}{16}$	8·78	$5\frac{1}{4}$	73·7	$17\frac{1}{2}$	7·308
$\frac{3}{4}$	1·50	$1\frac{7}{8}$	9·39	$5\frac{1}{2}$	80·9	18	7·731
$\frac{25}{32}$	1·63	$1\frac{15}{16}$	10·0	$5\frac{3}{4}$	88·4	19	8·614
$\frac{13}{16}$	1·77	2	10·7	6	96·2	20	9·545
$\frac{27}{32}$	1·90	$2\frac{1}{16}$	11·3	Inches.	Cwts.	21	10·53
$\frac{7}{8}$	2·04	$2\frac{1}{8}$	12·0			22	11·55
$\frac{29}{32}$	2·20	$2\frac{3}{16}$	12·9			23	12·63
$\frac{15}{16}$	2·35	$2\frac{1}{4}$	13·6			24	13·74
$\frac{31}{32}$	2·51	$2\frac{5}{16}$	14·3				

TABLE 98.—STEEL PLATES: ORDINARY SIZES.

Thick- ness.	Maxi- mum Area.	Maxi- mum Length.	Maxi- mum Width.	Thick- ness.	Maxi- mum Area.	Maxi- mum Length.	Maxi- mum Width.
Inch.	Sq. Ft.	Feet.	Feet.	Inch.	Sq. Ft.	Feet.	Feet.
$\frac{1}{16}$	28	14	4	$\frac{7}{16}$	98	40	7
$\frac{3}{32}$	31	18	$4\frac{1}{2}$	$\frac{1}{2}$	105	40	$7\frac{1}{2}$
$\frac{1}{8}$	40	22	5	$\frac{3}{8}$	115	40	$8\frac{1}{4}$
$\frac{5}{32}$	50	25	$5\frac{1}{4}$	$\frac{3}{4}$	125	37	$8\frac{3}{4}$
$\frac{3}{16}$	65	30	$5\frac{1}{2}$	$\frac{7}{8}$	125	34	$8\frac{3}{4}$
$\frac{1}{4}$	72	33	6	1	125	31	$8\frac{3}{4}$
$\frac{5}{16}$	75	35	$6\frac{1}{4}$	$1\frac{1}{8}$	110	28	$8\frac{3}{4}$
$\frac{3}{8}$	85	38	$6\frac{1}{2}$	$1\frac{1}{4}$	110	25	$8\frac{3}{4}$

TABLE 99.—WEIGHT PER SQUARE FOOT OF STEEL SHEETS AND PLATES.

(The Steel Pipe Company.)

Thickness.			Weight per Square Foot. Pounds.	Thickness.			Weight per Square Foot. Pounds.
Inch.	Inch.	Imperial Standard Gauge.		Inch.	Inch.	Imperial Standard Gauge.	
·0625	$\frac{1}{16}$	...	2·55	·21875	$\frac{7}{32}$	...	8·97
·064	...	16	2·61	·232	...	4	9·46
·072	...	15	2·94	·25	$\frac{1}{4}$	...	10·20
·080	...	14	3·26	·252	...	3	10·28
·092	...	13	3·75	·276	...	2	11·26
·09375	$\frac{3}{32}$	...	3·87	·300	...	1	12·24
·104	...	12	4·24	·3125	$\frac{5}{16}$	...	12·75
·116	...	11	4·73	·375	$\frac{3}{8}$	...	15·30
·125	$\frac{1}{8}$	...	5·10	·4375	$\frac{7}{16}$	...	17·85
·128	...	10	5·22	·500	$\frac{1}{2}$	...	20·40
·144	...	9	5·87	·5625	$\frac{9}{16}$	...	22·95
·15625	$\frac{5}{32}$	...	6·37	·625	$\frac{5}{8}$	...	25·50
·160	...	8	6·53	·6875	$\frac{11}{16}$	...	28·05
·176	...	7	7·18	·75	$\frac{3}{4}$	...	30·60
·1875	$\frac{3}{16}$	...	7·65	·875	$\frac{7}{8}$	...	35·70
·192	...	6	7·83	1·00	1	...	40·80
·212	...	5	8·65				

TABLE 100.—CHISEL STEEL : WEIGHT.  
Length, 1 Foot.

Diameter across the Sides.	Weight.		Diameter across the Sides.	Weight.	
	Hexagonal Section.	Octagonal Section.		Hexagonal Section.	Octagonal Section.
Inches.	Pounds.	Pounds.	Inches.	Pounds.	Pounds.
$\frac{3}{8}$	·414	·396	1	2·94	2·82
$\frac{1}{2}$	·736	·704	$1\frac{1}{8}$	3·73	3·56
$\frac{5}{8}$	1·15	1·10	$1\frac{1}{4}$	4·60	4·40
$\frac{3}{4}$	1·66	1·58	$1\frac{3}{8}$	5·57	5·32
$\frac{7}{8}$	2·25	2·16	$1\frac{1}{2}$	6·63	6·34
OVAL FLAT SECTION.					
Width × Thickness.			Weight.		
Inches.			Pounds.		
$\frac{3}{4} \times \frac{3}{8}$			·853		
$1 \times \frac{1}{2}$			1·52		
$1\frac{1}{4} \times \frac{5}{8}$			2·37		

TABLE 101.—SIZES, WEIGHTS, LENGTHS, AND BREAKING STRESS OF IRON WIRE.

Issued by the Iron and Steel Wire Manufacturers' Association,  
January 15, 1884.

(Imperial Standard Wire-Gauge.)

Size on Wire Gauge.	Diameter.		Sectional Area.	Weight of		Length of Cwt.	Breaking Stress.	
	Inch.	Millimetres.		100 Yards.	Mile.		Annealed.	Bright.
			Sq. Ins.	Lbs.	Lbs.	Yards.	Lbs.	Lbs.
7/0	·500	12·7	·1963	193·4	3404	58	10470	15700
6/0	·464	11·8	·1691	166·5	2930	67	9017	13525
5/0	·432	11	·1466	144·4	2541	78	7814	11725
4/0	·400	10·2	·1257	123·8	2179	91	6702	10052
3/0	·372	9·4	·1087	107·1	1885	105	5796	8694
2/0	·348	8·8	·0951	93·7	1649	120	5072	7608
1/0	·324	8·2	·0824	81·2	1429	138	4397	6595
1	·300	7·6	·0707	69·6	1225	161	3770	5655
2	·276	7	·0598	58·9	1037	190	3190	4785
3	·252	6·4	·0499	49·1	864	228	2660	3990
4	·232	5·9	·0423	41·6	732	269	2254	3381
5	·212	5·4	·0353	34·8	612	322	1883	2824
6	·192	4·9	·0290	28·5	502	393	1544	2316
7	·176	4·5	·0243	24	422	467	1298	1946
8	·160	4·1	·0201	19·8	348	566	1072	1608
9	·144	3·7	·0163	16	282	700	869	1303
10	·128	3·3	·0129	12·7	223	882	687	1030
11	·116	3	·0106	10·4	183	1077	564	845
12	·104	2·6	·0085	8·4	148	1333	454	680
13	·092	2·3	·0066	6·5	114	1723	355	532
14	·080	2	·0050	5	88	2240	268	402
15	·072	1·8	·0041	4	70	2800	218	326
16	·064	1·6	·0032	3·2	56	3500	172	257
17	·056	1·4	·0025	2·4	42	4667	131	197
18	·048	1·2	·0018	1·8	32	6222	97	145
19	·040	1	·0013	1·2	21	9333	67	100
20	·036	0·9	·0010	1	18	11200	55	82

## Indian Government Telegraphs.

## TELEGRAPH WIRES FOR LINES AND CABLES.

The data for inspection as to size, weight, tensile strength, and ductility, for all sizes of telegraph wires in use by the Indian Government, are given in the Tables 102 and 103, for line wire and cable wire. The wires are of iron, galvanised. In testing the wire for tensile strength, it is loaded by direct weight vertically, and is required at first to lift a weight equal to  $\frac{1}{10}$ ths of the maximum proof load. If the wire supports the load without failure, the load is gradually augmented by four successive advances, until the wire fails or the maximum load is reached. Testing for ductility, the piece of wire, after failure by load, or after supporting the maximum load, is gripped by two vices and twisted. The vices are 6 inches apart for sizes above 150 pounds per mile; and 3 inches apart for sizes of 150 pounds or less. The number of twists applied is reduced as the proportional resistance to load is greater, according to the scale of loads and relative twists given in the Tables.

A margin of  $1\frac{1}{2}$  per cent. deviation either way from the required weight of wire, weighing 600 pounds per mile and upwards is allowed; and for wires of less weight, 2 per cent. is allowed.

Weld joints are not allowed in cable-wire, except in the case of cable-wire weighing 900 pounds per mile, sent to Calcutta, in which, if in coils of from 400 to 500 pounds weight, one weld may be introduced.

The maximum resistances per inch of wires, at 60° F.—not to be exceeded—are as follows:—

No.	Units.	No.	Units.
1 . . . . .	4.5	9 $\frac{1}{2}$ . . . . .	18
3 $\frac{1}{2}$ . . . . .	6.5	12 $\frac{1}{2}$ . . . . .	36
4 $\frac{1}{2}$ . . . . .	7.25	15 $\frac{1}{2}$ . . . . .	72
5 . . . . .	8	16 . . . . .	90
5 $\frac{1}{2}$ . . . . .	9	16 . . . . .	108
7 . . . . .	12		

The wires are to bear winding round bars of different diameters, without cracking, as follows:—

Nos.	Bars.
3 $\frac{1}{2}$ and 4 $\frac{1}{2}$ . . . . .	4 inches in diameter.
5 " 5 $\frac{1}{2}$ . . . . .	2 $\frac{1}{2}$ " "
7 " 9 $\frac{1}{2}$ . . . . .	2 " "
12 $\frac{1}{2}$ " 15 $\frac{1}{2}$ . . . . .	1 " "
16 " 17 . . . . .	$\frac{1}{2}$ " "

TABLE 102.—GALVANISED IRON TELEGRAPH WIRES : STANDARD SIZES, WEIGHTS AND TESTS.  
(India Stores Department.)

## LINE WIRE.

Nominal Size.	Diameter.	Weight per Mile.	Weight of Ten Feet.	Tests for Strength and Ductility.								Weight of each Coil.	
				Load.	Twists.	Load.	Twists.	Load.	Twists.	Load.	Twists.	Mini- mum.	Maxi- mum.
Nos.	Inch.	Lbs.	Lbs.	Lbs.	Twists.	Lbs.	Twists.	Lbs.	Twists.	Lbs.	Twists.	Lbs.	Lbs.
1	.2960	1200	2-272	3700	11	3800	10	3900	9	4000	8	100	120
3½	.2547	900	1-704	2775	14	2850	13	2925	12	3000	11	95	105
4½	.2325	750	1-420	2312	15	2375	14	2437	13	2500	12	95	105
5	.2205	675	1-278	2081	16	2137	15	2193	14	2250	13	95	105
5½	.2079	600	1-136	1850	17	1900	16	1950	15	2000	14	95	105
7	.1801	450	.852	1388	19	1425	18	1460	17	1500	16	80	105
9½	.1470	300	.568	925	24	950	22	975	21	1000	19	70	80
12½	.1039	150	.284	462	17	475	16	487	15	500	14	35	40
15½	.0735	75	.142	208	24	214	23	219	21	225	19	35	40
16	.0657	60	.113	167	26	171	25	176	23	180	22	35	40
17	.0600	50	.095	152	30	157	28	162	26	167	24	35	40

TABLE 103.—GALVANISED TELEGRAPH WIRES: STANDARD SIZES, WEIGHTS AND TESTS.  
(India Stores Department.)

## CABLE WIRE.

Nominal Size.	Weight per Mile.	Tests for Strength and Ductility.										Weight of each Coil.	
		Load.	Twists.	Load.	Twists.	Load.	Twists.	Load.	Twists.	Load.	Twists.	Mini- mum.	Maxi- mum.
No.	Lbs.	Lbs.		Lbs.		Lbs.		Lbs.		Lbs.		Lbs.	Lbs.
3	925	3090	10	3165	9	3240	8	3315	7	3390	6	210	230
3½	900	3000	10	3075	9	3150	8	3225	7	3300	6	210	230
4½	750	2500	11	2562	10	2625	9	2687	8	2750	7	150	160
5½	600	2000	12	2050	11	2100	10	2150	9	2200	8	150	160
7	450	1500	14	1540	13	1580	12	1620	11	1660	10	120	130
9½	300	1000	17	1025	16	1050	15	1075	14	1100	13	120	130



TABLE 104.—SHEET AND HOOP-IRON GAUGE.

Issued by the South Staffordshire Iron Masters' Association,  
March 1, 1884.

Parts of Inch.	No. on Gauge.	Thick- ness.	Weight of One Square Foot.		Parts of Inch.	No. on Gauge.	Thick- ness.	Weight of One Square Foot.	
			Iron.	Steel.				Iron.	Steel.
Inch.		Inch.	Lbs.		Inch.		Inch.	Lbs.	
1	15°	1.000	40	40.83		20	.0392	1.57	1.60
	14°	0.9583	38.33	39.13		21	.0349	1.40	1.43
	13°	.9167	36.67	37.44	$\frac{1}{32}$	22	.0312	1.25	1.28
$\frac{7}{8}$	12°	.8750	35.00	35.73		23	.0278	1.11	1.13
	11°	.8333	33.33	34.03		24	.0247	.992	1.01
	10°	.7917	31.67	32.33		25	.0220	.883	.901
$\frac{3}{4}$	9°	.750	30.00	30.63		26	.0196	.784	.800
	8°	.7083	28.33	28.92		27	.0174	.696	.710
	7°	.6666	26.67	27.23	$\frac{1}{64}$	28	.015625	.625	.638
$\frac{5}{8}$	6°	.625	25.00	25.52		29	.0139	.556	.568
	5°	.5883	23.33	23.82		30	.0123	.492	.502
	4°	.5416	21.67	22.12		31	.0110	.440	.449
$\frac{1}{2}$	3°	.500	20.00	20.42		32	.0098	.392	.400
	2°	.4452	18.33	18.69		33	.0087	.349	.356
	1°	.3964	16.67	17.02		34	.0077	.308	.314
	1	.3532	15.00	15.31		35	.0069	.276	.282
	2	.3147	13.33	13.61		36	.0061	.244	.249
	3	.2804	11.67	12.01		37	.0054	.216	.221
$\frac{1}{4}$	4	.250	10.00	10.21		38	.0048	.192	.196
	5	.2225	8.90	9.08		39	.0043	.172	.176
	6	.1981	7.92	8.09		40	.00386	.154	.157
	7	.1764	7.06	7.20		41	.00343	.138	.140
	8	.1570	6.38	6.52		42	.00306	.123	.126
	9	.1398	6.51	6.65		43	.00272	.109	.111
$\frac{1}{8}$	10	.1250	5.00	5.10		44	.00242	.097	.099
	11	.1113	4.45	4.54		45	.00215	.086	.088
	12	.0991	3.97	4.05		46	.00192	.077	.079
	13	.0882	3.53	3.55		47	.00170	.068	.069
	14	.0785	3.14	3.21		48	.00152	.061	.062
	15	.0699	2.80	2.86		49	.00135	.054	.055
$\frac{1}{16}$	16	.0625	2.50	2.55		50	.00120	.048	.049
	17	.0556	2.23	2.27		51	.00107	.043	.044
	18	.0495	1.98	2.02		52	.00095	.038	.039
	19	.0440	1.76	1.80					

TABLE 105.—LAP-WELDED  
(Andrew and  
WEIGHT OF ONE

Thickness by Imperial Wire Gauge.			External			
Wire Gauge.	Inches.	Millimetres.	1	1½	1¾	1⅞
			Lbs.	Lbs.	Lbs.	Lbs.
16	·064	1·626	0·627	0·711	...	...
15	·072	1·829	0·700	0·794	0·888	0·982
14	·080	2·032	0·771	0·875	0·980	1·085
13	·092	2·337	0·875	0·995	<b>1·116</b>	<b>1·236</b>
12	·104	2·642	0·976	1·112	1·248	1·384
11	·116	2·946	1·074	1·226	1·377	1·529
10	·128	3·251	1·169	1·336	1·504	1·671
9	·144	3·658	1·291	1·479	1·668	1·856
8	·160	4·064	1·407	1·617	1·826	2·036
7	·176	4·470	1·519	1·749	1·979	2·210
6	·192	4·877	1·624	1·876	2·127	2·378
5	·212	5·385	1·749	2·027	2·304	2·582
4	·232	5·893	1·866	2·169	2·473	2·777
3	·252	6·401	1·974	2·304	2·634	2·963
2	·276	7·010	2·092	2·454	2·815	3·176
1	·300	7·620	2·199	2·592	2·984	3·377
⅛ in.	·125	3·175	1·145	1·309	1·473	1·636
⅜ "	·187	4·762	1·595	1·841	2·086	2·332
¼ "	·250	6·350	1·963	2·291	2·618	2·945
⅝ "	·313	7·937	2·250	2·659	3·068	3·477
⅞ "	·375	9·525	2·454	2·945	3·436	3·927
7/8 "	·437	11·112	2·577	3·150	3·723	4·295
½ "	·500	12·700	2·618	3·272	3·927	4·581

*Note.*—The most common thick-  
\* The weight per lineal foot of a steel tube is given by multiply-

**IRON BOILER TUBES.\***

James Stewart.)

FOOT IN LENGTH.

Diameter in Inches.							
<b>1½</b>	<b>1⅝</b>	<b>1¾</b>	<b>1⅞</b>	<b>2</b>	<b>2⅛</b>	<b>2¼</b>	<b>2⅜</b>
Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
...	...	...	...	...	...	...	...
1·077	1·171	1·265	1·359	...	...	...	...
1·190	1·294	1·399	1·504	1·608	1·713	1·818	...
<b>1·356</b>	<b>1·477</b>	<b>1·597</b>	<b>1·718</b>	1·838	1·959	2·079	2·199
1·520	1·656	1·793	1·929	<b>2·065</b>	<b>2·201</b>	<b>2·337</b>	2·473
1·681	1·833	1·985	2·137	2·288	2·440	2·592	<b>2·744</b>
1·839	2·007	2·174	2·342	2·509	2·677	2·844	3·012
2·045	2·233	2·422	2·610	2·799	2·987	3·176	3·364
2·245	2·455	2·664	2·873	3·083	3·292	3·502	3·711
2·440	2·671	2·901	3·131	3·362	3·592	3·822	4·053
2·630	2·881	3·132	3·384	3·635	3·886	4·138	4·389
2·859	3·137	3·414	3·692	3·969	4·247	4·524	4·802
3·081	3·384	3·688	3·992	4·295	4·599	4·903	5·206
3·293	3·623	3·953	4·283	4·613	4·943	5·273	5·602
3·538	3·899	4·260	4·621	4·983	5·344	5·705	6·067
3·770	4·163	4·555	4·948	5·341	5·733	6·126	6·519
1·800	1·963	2·127	2·291	2·454	2·618	2·782	2·945
2·577	2·822	3·068	3·313	3·559	3·804	4·050	4·295
3·272	3·600	3·927	4·254	4·581	4·909	5·236	5·563
3·886	4·295	4·704	5·113	5·522	5·931	6·340	6·749
4·418	4·909	5·400	5·890	6·381	6·872	7·363	7·854
4·868	5·440	6·013	6·586	7·159	7·731	8·304	8·877
5·236	5·890	6·545	7·199	7·854	8·508	9·163	9·817

nesses are printed in dark figures.

ing the tabular weight of a like wrought-iron tube by 1·021.

TABLE 105.—LAP-WELDED IRON  
(Andrew and  
WEIGHT OF ONE

Thickness by Imperial Wire Gauge.	External						
	2½	2⅝	2¾	2⅞	3	3⅛	3¼
Wire Gauge.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
16	...	...	...	...	...	...	...
15	...	...	...	...	...	...	...
14	...	...	...	...	...	...	...
13	2·320	2·440	2·561	2·681	2·802	...	...
12	2·609	2·745	2·882	3·018	3·154	3·290	3·426
11	<b>2·896</b>	<b>3·048</b>	<b>3·200</b>	<b>3·351</b>	<b>3·503</b>	3·655	3·807
10	3·179	3·347	3·514	3·682	3·850	<b>4·017</b>	<b>4·185</b>
9	3·553	3·741	3·930	4·118	4·307	4·495	4·684
8	3·921	4·130	4·339	4·549	4·758	4·968	5·177
7	4·283	4·514	4·744	4·974	5·205	5·435	5·665
6	4·640	4·892	5·143	5·394	5·646	5·897	6·148
5	5·079	5·357	5·634	5·912	6·189	6·467	6·744
4	5·510	5·814	6·117	6·421	6·725	7·028	7·332
3	5·932	6·262	6·592	6·922	7·252	7·582	7·911
2	6·428	6·789	7·150	7·512	7·873	8·234	8·596
1	6·911	7·304	7·697	8·090	8·482	8·875	9·268
⅛ in.	3·109	3·272	3·436	3·600	3·763	3·927	4·091
$\frac{3}{16}$ "	4·541	4·786	5·031	5·277	5·522	5·768	6·013
$\frac{1}{4}$ "	5·890	6·218	6·545	6·872	7·200	7·527	7·854
$\frac{5}{16}$ "	7·159	7·568	7·977	8·386	8·795	9·204	9·613
$\frac{3}{8}$ "	8·345	8·836	9·327	9·818	10·308	10·799	11·290
$\frac{7}{16}$ "	9·449	10·022	10·595	11·167	11·740	12·313	12·885
$\frac{1}{2}$ "	10·472	11·126	11·781	12·435	13·090	13·744	14·399

*Note.*—The most common thick-  
\* The weight per lineal foot of a steel tube is given by multi-

BOILER TUBES\*—*continued.*

James Stewart.)

FOOT IN LENGTH.

Diameter in Inches.								
3 $\frac{3}{8}$	3 $\frac{1}{2}$	3 $\frac{5}{8}$	3 $\frac{3}{4}$	3 $\frac{7}{8}$	4	4 $\frac{1}{4}$	4 $\frac{1}{2}$	4 $\frac{3}{4}$
Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
3.562	3.698	3.835	3.971	4.107	...	...	...	...
3.959	4.111	4.262	4.414	4.566	4.718	5.022	5.325	...
<b>4.352</b>	<b>4.520</b>	<b>4.687</b>	<b>4.855</b>	5.022	5.190	5.525	5.860	6.195
4.872	5.061	5.249	5.438	<b>5.626</b>	<b>5.815</b>	<b>6.192</b>	<b>6.569</b>	6.946
5.387	5.596	5.806	6.015	6.224	6.434	6.853	7.272	<b>7.690</b>
5.896	6.126	6.357	6.587	6.817	7.048	7.509	7.969	8.430
6.400	6.651	6.902	7.154	7.405	7.656	8.159	8.662	9.164
7.022	7.299	7.577	7.854	8.132	8.410	8.965	9.520	10.075
7.636	7.940	8.243	8.547	8.851	9.154	9.762	10.369	10.976
8.241	8.571	8.901	9.231	9.561	9.891	10.550	11.210	11.870
8.957	9.318	9.679	10.041	10.402	10.763	11.486	12.208	12.931
9.660	10.053	10.446	10.838	11.231	11.624	12.409	13.195	13.980
4.254	4.418	4.581	4.745	4.908	5.072	5.400	5.727	6.054
6.259	6.504	6.750	6.995	7.240	7.486	7.977	8.468	8.959
8.181	8.508	8.836	9.163	9.490	9.817	10.472	11.126	11.781
10.022	10.431	10.840	11.249	11.658	12.067	12.885	13.704	14.522
11.781	12.272	12.763	13.254	13.745	14.235	15.217	16.199	17.181
13.458	14.031	14.604	15.176	15.749	16.322	17.467	18.612	19.758
15.053	15.708	16.362	17.017	17.671	18.326	19.635	20.944	22.253

nesses are printed in dark figures.

plying the tabular weight of a like wrought-iron tube by 1.021.

TABLE 105.—LAP-WELDED IRON  
(Andrew and  
WEIGHT OF ONE

Thickness by Imperial Wire Gauge.	External						
	5	5½	5½	5¾	6	6½	6½
Wire Gauge.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
16	...	...	...	...	...	...	...
15	...	...	...	...	...	...	...
14	...	...	...	...	...	...	...
13	...	...	...	...	...	...	...
12	...	...	...	...	...	...	...
11	...	...	...	...	...	...	...
10	6·530	6·866	...	...	...	...	...
9	7·323	7·700	8·077	8·454	8·831	9·208	9·585
8	<b>8·109</b>	<b>8·528</b>	8·947	9·366	9·785	10·204	10·623
7	8·891	9·352	<b>9·812</b>	<b>10·273</b>	<b>10·734</b>	<b>11·195</b>	<b>11·655</b>
6	9·667	10·170	10·672	11·175	11·678	12·180	12·683
5	10·630	11·185	11·740	12·295	12·850	13·405	13·960
4	11·584	12·191	12·798	13·406	14·013	14·621	15·228
3	12·530	13·189	13·849	14·509	15·169	15·828	16·488
2	13·654	14·376	15·099	15·821	16·544	17·266	17·989
1	14·765	15·551	16·336	17·122	17·907	18·692	19·478
$\frac{1}{8}$ in.	6·381	6·709	7·036	7·363	7·690	8·017	8·345
$\frac{3}{16}$ "	9·450	9·940	10·431	10·922	11·413	11·904	12·395
$\frac{1}{4}$ "	12·435	13·090	13·744	14·399	15·053	15·708	16·362
$\frac{5}{16}$ "	15·340	16·158	16·976	17·794	18·612	19·430	20·249
$\frac{3}{8}$ "	18·162	19·144	20·126	21·108	22·090	23·071	24·053
$\frac{7}{16}$ "	20·903	22·048	23·194	24·339	25·485	26·630	27·775
$\frac{1}{2}$ "	23·562	24·871	26·180	27·489	28·798	30·107	31·416

*Note.*—The most common thick-  
\* The weight per lineal foot of a steel tube is given by multi-

BOILER TUBES \*—*continued.*

James Stewart.)

FOOT IN LENGTH.

Diameter in Inches.								
6 $\frac{3}{4}$	7	7 $\frac{1}{4}$	7 $\frac{1}{2}$	7 $\frac{3}{4}$	8	8 $\frac{1}{4}$	8 $\frac{1}{2}$	8 $\frac{3}{4}$
Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
...	...	...	...	...	...	...	...	...
9.962	10.339	...	...	...	...	...	...	...
11.042	11.460	...	...	...	...	...	...	...
<b>12.116</b>	<b>12.577</b>	13.038	13.499	13.959	14.420	14.880	15.345	15.815
13.186	13.688	14.191	14.694	15.196	15.699	16.204	16.710	17.216
14.515	15.070	<b>15.625</b>	<b>16.180</b>	<b>16.735</b>	<b>17.290</b>	17.845	18.400	18.955
15.835	16.443	17.050	17.658	18.265	18.872	19.480	20.087	20.694
17.148	17.807	18.467	19.127	19.787	20.446	<b>21.106</b>	<b>21.766</b>	<b>22.426</b>
18.712	19.434	20.157	20.879	21.602	22.324	23.047	23.769	24.492
20.263	21.048	21.834	22.619	23.405	24.190	24.976	25.761	26.546
8.672	8.999	9.327	9.654	9.981	10.308	10.636	10.963	11.290
12.886	13.376	13.867	14.358	14.849	15.340	15.831	16.322	16.813
17.017	17.671	18.326	18.980	19.635	20.289	20.944	21.598	22.253
21.067	21.885	22.703	23.521	24.339	25.157	25.975	26.794	27.612
25.035	26.017	26.998	27.980	28.962	29.944	30.925	31.907	32.889
28.921	30.066	31.212	32.357	33.502	34.648	35.793	36.938	38.084
32.725	34.034	35.343	36.652	37.961	39.270	40.579	41.888	43.197

nesses are printed in dark figures.

plying the tabular weight of a like wrought-iron tube by 1.021.

TABLE 105.—LAP-WELDED IRON  
(Andrew and  
WEIGHT OF ONE

Thickness by Imperial Wire Gauge.			External		
Wire Gauge.	Inches.	Millimetres.	9	9½	9½
			Lbs.	Lbs.	Lbs.
16	·064	1·626	...	...	...
15	·072	1·829	...	...	...
14	·080	2·032	...	...	...
13	·092	2·337	...	...	...
12	·104	2·642	...	...	...
11	·116	2·946	...	...	...
10	·128	3·251	...	...	...
9	·144	3·658	...	...	...
8	·160	4·064	...	...	...
7	·176	4·470	16·290	16·770	17·255
6	·192	4·877	17·722	18·230	18·738
5	·212	5·385	19·510	20·065	20·620
4	·232	5·893	21·302	21·909	22·517
3	·252	6·401	<b>23·085</b>	<b>23·745</b>	<b>24·405</b>
2	·276	7·010	25·215	25·937	26·660
1	·300	7·620	27·332	28·117	28·903
⅛ in.	·125	3·175	11·617	11·945	12·272
⅜ "	·187	4·762	17·303	17·794	18·285
¼ "	·250	6·350	22·907	23·562	24·216
⅝ "	·313	7·937	28·430	29·248	30·066
⅞ "	·375	9·525	33·871	34·852	35·834
7/16 "	·437	11·112	39·229	40·375	41·520
½ "	·500	12·700	44·506	45·815	47·124

*Note.*—The most common thick-  
The weight per lineal foot of a steel tube is given by multi-





TABLE 106.—FERRULES FOR BOILER TUBES, IRON AND STEEL.

(Howell &amp; Co.)

External Diameter at Larger End.	Thickness by B. W. G.		Length.	External Diameter at Larger End.	Thickness by B. W. G.		Length.
	Iron.	Steel.			Iron.	Steel.	
Inches.	No.	No.	Inches.	Inches.	No.	No.	Inches.
1½	14	15	1	2⅞	10	11	1¼
1⅝	13	14	1⅛	3	10	11	1¼
1¾	12	13	1⅜	3½	10	11	1⅝
1⅞	12	13	1⅝	3¼	10	11	1⅝
2	12	13	1⅞	3⅜	9	10	1⅝
2⅛	11	12	1⅞	3½	9	10	1⅝
2¼	11	12	1⅞	3⅝	9	10	1⅝
2⅜	11	12	1⅞	3¾	8	9	1⅝
2½	11	12	1¾	3⅞	8	9	1⅝
2⅝	11	12	1¼	4	8	9	1⅝
2¾	11	12	1¼				

TABLE 107.—LAP-WELDED SEMI-STEEL LOCOMOTIVE TUBES: SIZES AND WEIGHT. Standard Dimensions. (National Tube Works Company, U.S.A.).

(Haswell.)

Diameter.		Thickness.	Wire Gauge.	Circumference.		Transverse Areas.			Length per Sq. Foot of Surface.		Weight per Foot.
Ex-ternal.	In-ternal.			Ex-ternal.	In-ternal.	Ex-ternal.	In-ternal.	Metal.	Ex-ternal.	In-ternal.	
Ins.	Ins.	Ins.	No.	Ins.	Ins.	Sq. Ins.	Sq. Ins.	Sq. Ins.	Feet.	Feet.	Lbs.
1	·834	·083	14	3·142	2·62	·785	·546	·239	3·82	4·58	·81
1·25	1·084	·083	14	3·927	3·405	1·227	·923	·304	3·056	3·524	1·03
1·5	1·31	·095	13	4·712	4·115	1·767	1·348	·419	2·546	2·916	1·42
1·75	1·532	·109	12	5·498	4·813	2·405	1·843	·562	2·183	2·493	1·91
2	1·782	·109	12	6·283	5·598	3·142	2·494	·648	1·91	2·144	2·2
2·25	2·032	·109	12	7·069	6·384	3·976	3·243	·733	1·698	1·88	2·49
2·5	2·26	·12	11	7·854	7·1	4·909	4·011	·898	1·528	1·69	3·05
2·75	2·51	·12	11	8·639	7·885	5·94	4·948	·992	1·389	1·522	3·37
3	2·76	·12	11	9·425	8·67	7·069	5·983	1·086	1·273	1·384	3·68

TABLE 108.—LAP-WELDED CHARCOAL IRON BOILER TUBES  
(National Tube Works Company, U.S.A.). Standard  
Dimensions.

(Haswell.)

Diameter.		Thick- ness.	Wire Gauge.	Circum- ference.		Transverse Areas.			Length per Sq. Foot of Surface.		Weight per Foot.
Ex- ternal.	In- ternal.			Ex- ternal.	Inter- nal.	Ex- ternal.	In- ternal.	Metal	Ex- ternal.	In- ternal.	
Ins.	Ins.	Ins.	No.	Ins.	Ins.	Sq. Ins.	Sq. Ins.	S. Ins.	Feet.	Feet.	Lbs.
1	.86	.072	15	3.14	2.69	.78	.57	.21	3.82	4.46	.71
1.125	.98	.072	15	3.53	3.08	.99	.76	.24	3.39	3.89	.8
1.25	1.11	.072	15	3.93	3.47	1.23	.96	.27	3.06	3.45	.89
1.32	1.15	.083	14	4.12	3.6	1.35	1.03	.32	2.91	3.33	1.08
1.375	1.21	.083	14	4.32	3.8	1.48	1.15	.34	2.78	3.16	1.13
1.5	1.33	.083	14	4.71	4.19	1.77	1.4	.37	2.55	2.86	1.24
1.625	1.43	.095	13	5.1	4.51	2.07	1.62	.46	2.35	2.66	1.53
1.75	1.56	.095	13	5.5	4.9	2.4	1.91	.49	2.18	2.45	1.66
1.875	1.68	.095	13	5.89	5.29	2.76	2.23	.53	2.04	2.27	1.78
2	1.81	.095	13	6.28	5.69	3.14	2.57	.57	1.91	2.11	1.91
2.125	1.93	.095	13	6.68	6.08	3.55	2.94	.61	1.8	1.97	2.04
2.25	2.06	.095	13	7.07	6.47	3.98	3.33	.64	1.7	1.85	2.16
2.375	2.16	.109	12	7.46	6.78	4.43	3.65	.78	1.61	1.77	2.61
2.5	2.28	.109	12	7.85	7.17	4.91	4.09	.82	1.53	1.67	2.75
2.75	2.53	.109	12	8.64	7.95	5.94	5.03	.9	1.39	1.51	3.04
2.875	2.66	.109	12	9.03	8.35	6.49	5.54	.95	1.33	1.44	3.18
3	2.78	.109	12	9.42	8.74	7.07	6.08	.99	1.27	1.37	3.33
3.25	3.01	.12	11	10.21	9.46	8.3	7.12	1.18	1.17	1.26	3.96
3.5	3.26	.12	11	11	10.24	9.62	8.35	1.27	1.09	1.17	4.28
3.75	3.51	.12	11	11.78	11.03	11.04	9.68	1.37	1.02	1.09	4.6
4	3.73	.134	10	12.57	11.72	12.57	10.94	1.63	.95	1.02	5.47
4.25	3.98	.134	10	13.35	12.51	14.19	12.45	1.73	.9	.96	5.82
4.5	4.23	.134	10	14.14	13.29	15.9	14.07	1.84	.85	.9	6.17
4.75	4.48	.134	10	14.92	14.08	17.72	15.78	1.94	.8	.85	6.53
5	4.7	.148	9	15.71	14.78	19.63	17.38	2.26	.76	.81	7.58
5.25	4.95	.148	9	16.49	15.56	21.65	19.27	2.37	.73	.77	7.97
5.5	5.2	.148	9	17.28	16.35	23.76	21.27	2.49	.7	.73	8.36
6	5.67	.165	8	18.85	17.81	28.27	25.25	3.02	.64	.67	10.16
7	6.67	.165	8	21.99	20.95	38.48	34.94	3.54	.55	.57	11.9
8	7.64	.165	8	25.13	24.1	50.27	46.2	4.06	.48	.50	13.65
9	8.59	.18	7	28.27	27.14	63.62	58.63	4.99	.42	.44	16.76
10	9.59	.203	6	31.42	30.14	78.54	72.29	6.25	.38	.4	20.99
11	10.56	.22	5	34.56	33.17	95.03	87.58	7.45	.35	.36	25.03
12	11.54	.229	4.5	37.7	36.26	113.1	104.63	8.47	.32	.33	28.46
13	12.52	.238	4	40.84	39.34	132.73	123.19	9.54	.29	.3	32.06
14	13.5	.248	3.5	43.98	42.42	153.94	143.22	10.71	.27	.28	36
15	14.48	.259	3	47.12	45.5	176.71	164.72	11.99	.25	.26	40.3
16	15.43	.284	2	50.26	48.48	201.06	187.04	14.02	.24	.25	47.11
17	16.4	.3	1	53.41	51.52	226.98	211.24	15.74	.22	.23	52.89
18	17.32	.34	0	56.55	54.41	254.47	235.61	18.86	.21	.22	63.32

NOTE.—In estimating effective heating or evaporating surface of Tubes, as heating liquids by steam, superheating steam, or transferring heat from one liquid or one gas to another, mean surface of Tubes is to be computed.

TABLE 109.—LAP-WELDED WROUGHT-IRON TUBES FOR ARTESIAN WELLS: WEIGHT PER LINEAL FOOT.  
(Lloyd and Lloyd.)

SWELLED JOINTS: Screwed together, External and Internal Screws.													
External Diameter, inches	2	2 $\frac{1}{4}$	2 $\frac{1}{2}$	2 $\frac{3}{4}$	3	3 $\frac{1}{4}$	3 $\frac{1}{2}$	3 $\frac{3}{4}$	4	4 $\frac{1}{4}$	Inches. Thickness.	Weight.	
Thickness, I. W. G., No.	11	11	11	11	11	10	10	10	9	9			
Weight per lineal foot, lbs.	2·347	2·659	2·971	3·283	3·596	4·344	4·693	5·041	5·932	6·316			
External Diameter, inches	4 $\frac{1}{2}$	4 $\frac{3}{4}$	5	5 $\frac{1}{4}$	5 $\frac{1}{2}$	5 $\frac{3}{4}$	6	6 $\frac{1}{4}$	6 $\frac{1}{2}$	7	Inches. Thickness.	Weight.	
Thickness, I. W. G., No.	9	8	8	8	7	7	7	7	7	7			
Weight per lineal foot, lbs.	6·701	7·871	8·300	8·729	9·933	10·480	10·900	11·836	12·773				
FLUSH JOINTS: Screwed together, External and Internal Screws.													
External Diameter, inches	2	2 $\frac{1}{4}$	2 $\frac{1}{2}$	2 $\frac{3}{4}$	3	3 $\frac{1}{4}$	3 $\frac{1}{2}$	3 $\frac{3}{4}$	4	4 $\frac{1}{4}$	Inches.	Weight.	
Weight in { 4 inch thick	4·552	5·202	5·852	6·503	7·153	7·803	8·453	9·104	9·754	10·404			
pounds per { 1 $\frac{5}{8}$ " "	5·480	6·291	7·103	7·914	8·726	9·537	10·349	11·160	11·972	12·784			
lineal foot { 1 $\frac{3}{4}$ " "	6·340	7·315	8·291	9·266	10·242	11·217	12·193	13·168	14·144	15·119			
External Diameter, inches	4 $\frac{1}{2}$	4 $\frac{3}{4}$	5	5 $\frac{1}{4}$	5 $\frac{1}{2}$	5 $\frac{3}{4}$	6	6 $\frac{1}{4}$	6 $\frac{1}{2}$	7	Inches.	Weight.	
Weight in { 4 inch thick	11·054	11·705	12·355	13·006	13·656	14·306	14·957	16·533	17·558				
pounds per { 1 $\frac{5}{8}$ " "	13·598	14·407	15·219	16·030	16·843	17·653	18·465	20·088	21·711				
lineal foot { 1 $\frac{3}{4}$ " "	16·096	17·070	18·046	19·021	19·997	20·972	21·948	23·898	25·850				

TABLE 110.—LAP-WELDED IRON PIPES OR TUBES OF LARGE DIAMETER: WEIGHT OF  
1 LINEAL FOOT.  
(Lloyd and Lloyd.)

Internal Diameter, inches	8	9	10	11	12	13	14	15	16	17	18
Weight in pounds per lineal foot . $\left\{ \begin{array}{l} \frac{1}{4} \text{ inch thick} \\ \frac{3}{8} \text{ " } \\ \frac{1}{2} \text{ " } \end{array} \right.$	22 35 47	25 38 52	28 42 58	30 46 63	33 50 68	35 54 73	38 58 78	41 62 84	43 66 89	46 70 94	48 74 100
Internal Diameter, inches	19	20	21	22	23	24	25	26	27	28	
Weight in pounds per lineal foot . $\left\{ \begin{array}{l} \frac{1}{4} \text{ inch thick} \\ \frac{3}{8} \text{ " } \\ \frac{1}{2} \text{ " } \end{array} \right.$	51 78 105	54 82 110	56 86 115	59 90 120	62 93 126	64 97 131	67 101 136	69 105 141	72 109 147	75 113 152	
Internal Diameter, inches	29	30	31	32	33	34	35	36	37	38	
Weight in pounds per lineal foot . $\left\{ \begin{array}{l} \frac{1}{4} \text{ inch thick} \\ \frac{3}{8} \text{ " } \\ \frac{1}{2} \text{ " } \end{array} \right.$	77 117 157	80 121 162	83 125 168	85 129 173	88 133 178	90 137 183	93 140 188	96 144 194	98 148 199	101 152 204	
Internal Diameter, inches	39	40	41	42	43	44	45	46	47	48	
Weight in pounds per lineal foot . $\left\{ \begin{array}{l} \frac{1}{4} \text{ inch thick} \\ \frac{3}{8} \text{ " } \\ \frac{1}{2} \text{ " } \end{array} \right.$	104 156 210	106 160 215	109 164 220	111 168 225	114 172 230	117 176 236	119 180 241	122 184 246	124 188 251	127 192 257	

Steam-tubes, gas-tubes, and water-tubes, are made to weight, according to the "size" or bore; butt-welded. The weight of tubes of any given size varies very much with different manufacturers. Table 111 gives the average weights of gas-tubes, as made by seven leading manufacturers. "Steam-tubes" and "water-tubes" are made to the same sizes as the gas-tubes, but of different weights. The tubes are proved by hydrostatic pressure, usually according to the following scale:—

Gas-tubes . . . . .	50 lbs. per square inch.
Water-tubes . . . . .	300 lbs.       "       "
Steam-tubes . . . . .	500 lbs.       "       "

To find the thickness of a pipe, when the inside or the outside diameter, and the weight per lineal foot, are given.

Let  $d$  be the internal diameter, inches,  $D$  the external diameter,  $w$  the weight of pipe in pounds per lineal foot. Let, also,  $c$  be a constant of weight for the same material, say, the weight of a straight bar 1 inch square, 1 foot long, in pounds. Then,

1st. *When the internal diameter is given,*

$$\text{The external diameter, } D = \sqrt{\frac{w}{.7854 c} + d^2} . \quad (1)$$

2nd. *When the external diameter is given,*

$$\text{The internal diameter, } d = \sqrt{D^2 - \frac{w}{.7854 c}} . \quad (2)$$

The other diameter having been ascertained by one or other of these formulas, half the difference of the external and internal diameters, is the thickness of the pipe.

For example, a lead pipe of 1 inch bore, weighs 70 pounds for a 15-feet length. What is the thickness? The weight  $w$ , per lineal foot is  $\left(\frac{70}{15} =\right)$  4.666 pounds; the weight  $c$  of a 1-inch square bar, 1 foot long, is 4.944 pounds; and by formula (1), the external diameter  $D$  is equal to  $\sqrt{\frac{4.666}{.7854 \times 4.944} + 1^2} = \sqrt{1.202 + 1} = \sqrt{2.202} = 1.484$  inches. Then  $1.484 - 1 = .484$  inch, one half of which is .242 inch, nearly  $\frac{1}{4}$  inch, the thickness of the lead pipe.

Conversely, taking the same pipe for example, let the external diameter, 1.484, be given, to find the internal diameter. By formula (2), the internal diameter,  $d$ , is equal to

$$\sqrt{1.484^2 - \frac{4.666}{.7854 \times 4.944}} = \sqrt{2.202 - 1.202} = \sqrt{1} = 1 \text{ inch bore.}$$

The constants for other metals are given in TABLE 89, page 221.

TABLE 111.—BUTT-WELDED GAS TUBES AND FITTINGS:  
AVERAGE WEIGHT.

Tubes.			Fittings.		
Bore.	Weight per 100 Feet.	Length to weigh One Ton.	Weight of Ten Elbows.	Weight of Ten Tees.	Weight of Ten Crosses.
Inches.	Pounds.	Feet.	Lb. Oz.	Lb. Oz.	Lb. Oz.
$\frac{1}{8}$	26.3	8502	1 1	1 0	1 8
$\frac{1}{4}$	40.5	5532	1 7	1 8	1 14
$\frac{3}{8}$	57.5	3892	1 13	2 4	2 3
$\frac{1}{2}$	82.9	2700	2 15	3 0	3 4
$\frac{3}{4}$	122.0	1836	4 6	5 4	5 11
1	174.9	1281	6 4	7 10	9 2
$1\frac{1}{4}$	244.3	917	10 10	12 15	14 11
$1\frac{1}{2}$	310.2	722	15 8	16 7	18 10
$1\frac{3}{4}$	359.5	623	15 12	20 0	21 4
2	421.0	532	22 6	27 0	31 4
$2\frac{1}{4}$	515.0	435	30 2	32 8	41 4
$2\frac{1}{2}$	610.4	367	46 2	50 15	51 4
$2\frac{3}{4}$	658.8	340	55 10	68 8	80 10
3	759.3	295	73 8	85 5	88 12
$3\frac{1}{2}$	878.4	255	101 0	121 0	129 0
4	1032.3	217	126 0	144 0	158 0

Note 1.—Normal length, 14 feet.

Note 2.—Steam tubes and water tubes also are manufactured of the same bores.

TABLE 112.—STANDARD SIZES OF CONNECTING PIPES OR  
UNIONS OF GAS METERS.  
(Board of Trade, Standards Department.)

Size of Meter.	Boss.			Cap.			Lining.
	Mean Diameter of External Screw.	Number of Threads per Inch.	Internal Diameter.	Mean Diameter of Internal Screw.	Number of Threads per Inch.	Height of Cap.	External Diameter to enter Boss.
Lights.	Inches.	Threads.	Inches.	Inches.	Threads.	Inches.	Inches.
150	3·68	9	3·05	3·65	9	1·20	3·03
100 }	3·00	11	2·30	2·95	11	1·00	2·28
80 }	2·45	11	2·00	2·40	11	·80	1·98
60	2·25	11	1·80	2·25	11	·70	1·75
50	2·05	11	1·55	2·00	11	·70	1·53
30	1·80	11	1·42	1·75	11	·60	1·40
20	1·45	11	1·05	1·40	11	·60	1·03
10	1·15	14	·83	1·10	14	·50	·81
5	·98	19	·67	·94	19	·50	·65
3	·88	19	·57	·84	19	·40	·55
2 }	·70	19	·50	·66	19	·40	·50
1 }							
0							

TABLE 113.—IRON WELDED STEAM, GAS, AND WATER  
PIPES (National Tube Works Company).  
(Haswell.)

Internal Diameter.	Thickness.	Weight per Lineal Foot.	Internal Diameter.	Thickness.	Weight per Lineal Foot.
Inches.	Inch.	Pounds.	Inches.	Inch.	Pounds.
$\frac{1}{4}$	·07	·24	5	·26	14·50
$\frac{1}{2}$	·09	·42	6	·28	18·76
$\frac{3}{8}$	·09	·56	7	·30	23·27
$\frac{1}{2}$	·11	·84	8	·32	28·18
$\frac{3}{4}$	·11	1·11	9	·34	33·70
1	·13	1·67	10	·37	40·06
$1\frac{1}{4}$	·14	2·24	11	·37	45·02
$1\frac{1}{2}$	·14	2·68	12	·37	48·98
2	·15	3·61	13	·37	53·92
$2\frac{1}{2}$	·20	5·74	14	·37	57·89
3	·22	7·50	15	·28	47·11
$3\frac{1}{2}$	·23	9·00	16	·30	52·89
4	·24	10·66	17	·34	63·32
$4\frac{1}{2}$	·25	12·34			





**STEEL PIPES.****Mild Steel Pipes.**

The Steel Pipe Company show, in the annexed Tables, the relative thickness and weight of pipes of cast-iron, wrought-iron, and steel, for equal strengths :—

**TABLE 115.—RELATIVE THICKNESS OF RIVETED PIPES FOR EQUAL STRENGTH.**

Metal.	Cast-Iron.	Wrought-Iron.	Steel.
Weight of 1 square foot, 1 inch thick	37·5 lbs.	40 lbs.	40·8 lbs.
Tenacity per square inch	18,000 lbs.	48,600 lbs.	72,000 lbs.
Relative strength for equal thicknesses	1	2·7	4
Factor of safety	10	6	5
Relative strength due to factor of safety	1	4·5	8
Reduction in strength due to riveted joints	...	30 per cent.	30 per cent.
Relative strength after reduction for riveted joints	1	3·15	5·6
Relative thickness for plates of equal strength	1	·3174	·1786

**TABLE 116.—RELATIVE WEIGHT OF PIPES FOR EQUAL STRENGTH.**

Metal.	Cast-Iron.	Wrought-Iron.	Steel.
Thickness of plates, weighing 40 lb. per square foot	1·066 inches.	1·00 inch.	·9804 inch.
Relative strength for equal weight	1	2·533	3·678
Relative strength due to factor of safety	1	4·22	7·356
Relative strength after reduction for riveted joints	1	2·955	5·149
Relative weight of plain cylinders of equal strength	1	·3384	·1942
Increase in weight of pipes due to socket and spigot joints	5·8 per cent.	15 per cent.	15 per cent.
Relative weight of pipes of equal strength	1	·3678	·2111

From the first Table it appears that the resistance of riveted steel pipes to bursting is 5·6 times that of cast-iron pipes of equal thickness. The longitudinal seams of the

riveted pipes are double-riveted and are estimated to have 70 per cent. of the strength of the solid undrilled plates. The pipes are united in lengths of from 4 feet to 6 feet, with circular seams of single riveting.

The minimum thickness of welded plates is  $\frac{1}{8}$  inch.

The weight of steel pipes, complete with sockets, spigots, rivets, lap-joints, and asphalt coating  $\frac{1}{32}$  inch thick, is one-fourth of that of cast-iron pipes of equal strength. The coating effectually prevents corrosion. The weight of steel pipes complete as above specified, is given by the formula (1).

*Weight of Steel Pipes per Lineal Foot.*

$$W = \cdot 33 d w \quad . \quad . \quad . \quad . \quad . \quad . \quad . \quad (1)$$

W = weight per lineal foot.

d = diameter in inches.

w = weight of plate or sheet in pounds per square foot.

t = thickness of pipe in inches.

H = working head in feet of water.

*Thickness of Pipes and Working Head of Pressure.*

$$\text{Cast-iron pipes} \quad \left\{ \begin{array}{l} t = \cdot 00012 d H \quad . \quad . \quad . \quad . \quad (2) \\ H = \frac{t}{\cdot 00012 d} \quad . \quad . \quad . \quad . \quad (3) \end{array} \right.$$

$$\text{Steel pipes} \quad . \quad \left\{ \begin{array}{l} t = \cdot 000025 d H \quad . \quad . \quad . \quad . \quad (4) \\ H = \frac{t}{\cdot 000025 d} \quad . \quad . \quad . \quad . \quad (5) \end{array} \right.$$

A 12-inch riveted steel pipe, 8 feet 7 inches long,  $\frac{1}{8}$  inch thick, was tested under a bursting pressure of 760 lbs. per square inch. It leaked slightly at one of the rivets, and a portion of the caulking slightly yielded. No other sign of damage was visible. The longitudinal lap-joints had  $1\frac{1}{8}$  inches of lap, with  $\frac{1}{4}$ -inch rivets at  $1\frac{1}{8}$  inches of pitch. It was fitted at each end with a circular flange  $2\frac{1}{2}$  inches by  $2\frac{1}{2}$  inches by  $\frac{1}{4}$ -inch thick. The ultimate tensile strength of the metal was 24 tons per square inch. The stress on the metal was at the rate of  $760 \times 12 = 9120$  lbs. per lineal inch, or  $(9120 \times 4 = )$  36480 lbs., or 16.3 tons per square inch of section of both sides together. This is about equal to 70 per cent. of the ultimate resistance, or 16.8 tons per square inch, the strength at the joint; showing that the calculated ultimate resistance is corroborated by the results of the test.

TABLE 117.—WEIGHT OF RIVETED STEEL PIPES, WITH PLAIN ENDS.

(The Steel Pipe Company).

Thickness. Inches.	.064	.072	.080	.092	.104	.116	.125	.128	.144	.160	.176	.1875
Imperial Gauge.	16	15	14	13	12	11	$\frac{1}{8}$	10	9	8	7	$\frac{3}{16}$
Diam.	WEIGHT PER LINEAL FOOT.											
Ins.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
3	2.75	3.20	3.50	4.05								
4	3.54	4.04	4.44	5.13								
5	4.33	4.89	5.38	6.21								
6	5.12	5.73	6.32	7.29	8.35	9.42						
7	5.91	6.58	7.26	8.37	9.57	10.78						
8	6.70	7.43	8.20	9.45	10.79	12.14						
9	7.49	8.29	9.14	10.53	12.91	13.50	14.48					
10	8.28	9.12	10.08	11.61	14.13	14.86	15.95					
11	...	9.96	11.02	12.69	15.35	16.22	17.42					
12	...	10.86	11.96	13.77	16.57	17.58	18.89	19.41	22.42	24.94	27.71	29.83
13	...	...	12.90	14.85	17.79	18.94	20.36	20.91	24.10	26.80	29.76	32.01
14	...	...	13.84	15.93	19.01	20.30	21.83	22.42	25.77	28.67	31.81	34.20
15	...	...	...	17.01	20.23	21.67	23.30	23.92	27.44	30.53	33.86	36.37
16	...	...	...	18.10	21.45	23.03	24.77	25.43	29.12	32.40	35.91	38.56
17	...	...	...	...	22.67	24.40	26.24	26.94	30.80	34.26	37.96	40.74
18	...	...	...	...	23.89	25.75	27.71	28.44	32.47	36.13	40.01	42.93
19	...	...	...	...	...	27.11	29.18	29.95	34.15	38.00	42.06	45.11
20	...	...	...	...	...	28.47	30.65	31.45	35.82	39.85	44.11	47.30
21	...	...	...	...	...	...	32.12	32.96	37.50	41.71	46.16	49.48
22	...	...	...	...	...	...	33.59	34.47	39.18	43.58	48.21	51.67
23	...	...	...	...	...	...	35.06	35.97	40.85	45.44	50.26	53.85
24	...	...	...	...	...	...	36.53	37.48	42.53	47.31	52.31	56.04
25	...	...	...	...	...	...	...	38.98	44.20	49.17	54.36	58.22
26	...	...	...	...	...	...	...	40.50	45.88	51.04	56.41	60.41
27	...	...	...	...	...	...	...	42.00	47.56	52.90	58.46	62.60
28	...	...	...	...	...	...	...	43.50	49.23	54.77	60.51	64.78
29	...	...	...	...	...	...	...	45.00	50.91	56.63	62.56	66.96
30	...	...	...	...	...	...	...	46.50	52.58	58.50	64.61	69.15

Note.—Usual lengths, 18 feet to 40 feet.

TABLE 118.—WEIGHT OF RIVETED STEEL PIPES, WITH PLAIN ENDS: TO 36 INCHES IN DIAMETER.

(The Steel Pipe Company.)

Thickness, Inches.											
	$\frac{1}{8}$	$\frac{3}{16}$	$\frac{1}{4}$	$\frac{5}{16}$	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{9}{16}$	$\frac{5}{8}$	$\frac{11}{16}$	$\frac{3}{4}$
Diam.	WEIGHT PER LINEAL FOOT.										
Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
12	18.9	20.8	40.5								
13	20.3	32.0	43.3								
14	21.8	34.2	46.2								
15	23.3	36.4	49.0	60.3							
16	24.7	38.5	51.8	63.9							
17	26.2	40.7	54.7	67.5							
18	27.7	42.9	57.5	71.0	85.7						
19	29.2	45.1	60.4	74.6	90.0						
20	30.6	47.3	63.2	78.3	94.3						
21	32.1	49.5	66.1	81.8	98.6	112.5					
22	33.6	51.6	68.9	85.4	102.9	117.6					
23	35.0	53.8	71.8	89.0	107.2	122.8					
24	36.5	56.0	74.6	92.6	111.5	127.9	149.0	167.8	186.7	205.9	225.6
25	...	58.2	77.5	96.2	115.8	133.1	154.7	174.2	193.8	213.6	234.0
26	...	60.4	80.3	99.8	120.1	138.2	160.4	180.6	200.9	221.4	242.4
27	...	62.6	83.1	103.4	124.4	143.4	166.1	187.0	208.0	229.2	250.8
28	...	64.8	86.0	107.0	128.7	148.5	171.8	193.4	215.1	237.0	259.3
29	...	66.9	88.8	110.6	133.0	153.7	177.5	199.8	222.2	244.8	267.7
30	...	69.1	91.7	114.2	137.3	158.8	183.2	206.2	229.3	252.5	276.1
31	...	...	94.5	117.8	141.6	164.0	188.9	212.7	236.4	260.3	284.5
32	...	...	97.4	121.4	145.9	169.2	194.6	219.1	243.5	268.1	293.0
33	...	...	100.2	125.0	150.2	174.3	200.3	225.5	250.6	275.9	301.4
34	...	...	103.0	128.6	154.5	179.5	206.0	232.0	257.8	283.7	309.8
35	...	...	105.9	132.2	158.8	184.6	211.7	238.3	264.9	291.4	318.2
36	...	...	108.7	135.8	163.1	189.8	217.4	244.7	272.0	299.2	326.7

The usual lengths to which the riveted steel pipes are constructed, are from 18 feet to 40 feet.

The longitudinal seams of riveted steel pipes, double-riveted, are proved to have a bursting strength equal to 70 per cent. of that of the solid undrilled plates.

TABLE 119.—WEIGHT OF RIVETED STEEL PIPES, WITH PLAIN ENDS : TO 60 INCHES IN DIAMETER.

(The Steel Pipe Company.)

Thicknss. Inches.											
	$\frac{1}{4}$	$\frac{5}{16}$	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{9}{16}$	$\frac{5}{8}$	$\frac{11}{16}$	$\frac{3}{4}$	$\frac{7}{8}$	1
Diam.	WEIGHT PER LINEAL FOOT.										
	Ins.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
37	111.5	139.0	167.0	195.0	223.0	251.0	279.0	307.0	343.5		
38	114.0	143.0	171.5	200.0	229.0	257.5	286.0	315.0	352.0		
39	117.0	146.5	176.0	205.0	234.5	264.0	293.0	322.5	360.0		
40	120.0	150.0	180.0	210.0	240.0	270.0	300.0	330.0	370.0		
41	122.5	153.5	184.0	215.0	246.0	277.0	308.0	339.0	380.0		
42	125.0	157.0	188.5	220.0	252.0	284.0	316.0	348.0	390.0		
43	127.5	160.5	193.0	225.5	258.0	291.0	324.0	356.5	399.5		
44	130.0	164.0	197.0	230.5	264.0	298.0	332.0	365.5	409.5	460.0	
45	132.5	167.5	201.5	236.0	270.5	305.0	340.0	374.5	419.0	472.0	
46	135.0	171.0	205.5	241.0	276.5	312.0	348.0	383.0	429.0	484.5	
47	137.5	174.5	210.0	246.0	282.5	319.0	356.0	392.0	439.0	496.5	
48	140.0	178.0	214.5	251.5	289.0	326.0	364.0	401.0	449.0	509.0	576.0
49	...	181.5	218.5	256.5	295.0	333.0	372.0	410.0	459.0	521.0	591.0
50	...	185.0	223.0	262.0	301.0	340.0	380.0	419.0	469.0	533.5	606.0
51	...	188.5	227.0	267.0	307.0	347.0	388.0	428.0	479.0	545.5	621.0
52	...	192.0	231.5	272.0	313.0	354.0	396.0	437.0	489.0	558.0	636.0
53	...	195.5	236.0	277.5	319.0	361.0	404.0	446.0	498.5	570.0	651.0
54	...	199.0	240.0	282.5	325.0	368.0	412.0	454.5	508.5	582.5	666.0
55	...	...	244.5	288.0	331.5	375.0	420.0	463.5	518.0	594.5	681.0
56	...	...	248.5	293.0	337.5	382.0	428.0	472.0	528.0	607.0	696.0
57	...	...	253.0	298.0	343.5	389.0	436.0	481.0	538.0	619.0	711.0
58	...	...	257.5	303.5	350.0	396.0	444.0	490.0	548.0	631.5	726.0
59	...	...	261.5	308.5	356.0	403.0	452.0	499.0	558.0	643.5	741.0
60	...	...	266.0	314.0	362.0	410.0	460.0	508.0	568.0	656.0	756.0

The usual lengths to which the riveted steel pipes are constructed, are from 18 feet to 40 feet.

The longitudinal seams, double-riveted, have 70 per cent. of the strength of the solid plate.

TABLE 120.—WEIGHT OF LAP-WELDED PIPES WITH PLAIN ENDS.

(The Steel Pipe Company.)

Imperial Gauge.	Thickness, Inches.											
	7	6	5	4	3	2	1	$\frac{1}{4}$	$\frac{5}{15}$	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$
Diam.	WEIGHT PER LINEAL FOOT.											
Ins.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
3	5.97	6.54	7.27	8.00	8.75	9.65	10.57	8.69	11.04	13.53	15.19	18.70
4	7.85	8.59	9.54	10.48	11.44	12.60	13.78	11.36	14.38	17.53	20.76	24.04
5	9.73	10.64	11.80	12.95	14.13	15.55	16.98	14.03	17.70	21.53	25.43	29.38
6	11.61	12.69	14.07	15.43	16.82	18.50	20.18	16.70	21.06	25.54	30.10	34.72
7	13.49	14.78	16.33	17.91	19.51	21.44	23.40	19.37	24.40	29.54	34.77	40.06
8	15.37	16.79	18.60	20.38	22.20	24.40	26.60	22.04	27.74	33.55	39.44	45.40
9	17.25	18.83	20.87	22.86	24.90	27.34	29.80	24.71	31.08	37.55	44.11	50.74
10	19.13	20.89	23.13	25.33	27.40	30.28	33.00	27.38	34.42	41.56	48.78	56.08
11	21.01	22.94	25.40	27.81	30.28	33.23	36.21	30.05	37.76	45.56	53.45	61.42
12	22.89	24.98	27.66	30.29	32.97	36.18	39.41	32.72	41.10	49.57	58.12	66.76
13	24.77	27.03	29.92	32.76	35.66	39.13	42.62	35.39	44.43	53.57	62.79	72.10
14	26.65	29.08	32.19	35.24	38.33	42.07	45.82	38.06	47.77	57.58	67.46	77.43
15	28.53	31.12	34.45	37.72	41.04	45.02	49.03	40.73	51.11	61.58	72.13	82.77
16	30.41	33.18	36.72	40.19	43.74	47.97	52.23	43.40	54.45	65.59	76.80	88.11
17	32.29	35.23	38.98	42.67	46.43	50.92	55.44	46.07	57.78	69.59	81.47	93.45
18	34.17	37.28	41.24	45.15	49.12	53.86	58.64	48.74	61.12	73.60	86.14	98.80
19	36.05	39.33	43.51	47.62	51.81	56.81	61.84	51.40	64.46	77.60	90.81	104.13
20	37.93	41.38	45.77	50.10	54.50	59.76	65.05	54.07	67.80	81.60	95.48	109.47
21	39.81	43.43	48.04	52.58	57.20	62.70	68.25	56.74	71.13	85.61	100.15	114.81
22	41.69	45.47	50.30	55.05	59.88	65.65	71.46	59.41	74.47	89.62	104.82	120.15
23	43.57	47.52	52.57	57.53	62.57	68.60	74.66	62.08	77.81	93.62	109.49	125.45
24	45.45	49.57	54.83	60.01	65.27	71.55	77.87	64.75	81.15	97.63	114.16	130.82
25	47.33	51.62	57.09	62.48	67.96	74.50	81.08	67.42	84.48	101.63	118.83	136.16
26	49.21	53.67	59.36	64.96	70.65	77.44	84.28	70.10	87.82	105.64	123.50	141.50
27	51.09	55.72	61.63	67.43	73.34	80.39	87.49	72.76	91.16	109.64	128.17	146.81
28	52.97	57.77	63.89	69.91	76.03	83.34	90.72	75.44	94.50	113.65	132.84	152.18
29	54.85	59.82	66.16	72.39	78.72	86.28	93.92	78.11	97.83	117.65	137.51	157.52
30	56.73	61.87	68.42	74.86	81.42	89.23	97.13	80.78	101.17	121.66	142.18	162.86

Usual length, 14 feet to 18 feet.

TABLE 121.—ROLLED IRON JOISTS : ESTIMATED

(Measures

Factor of

Reference Number.	Clear Span in Feet, or							
	6	8	10	12	14	16	18	20
No.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
1	90.0	67.4	54.0	45.0	38.6	33.7	30.0	27.0
2	66.6	50.0	40.0	33.3	28.7	25.0	22.2	20.0
3	61.8	46.2	36.6	30.9	26.5	23.1	20.6	18.3
4	50.8	37.9	30.4	25.4	21.7	19.0	16.9	15.2
5	...	43.6	35.0	29.0	25.0	21.8	19.2	17.3
6	45.5	32.8	26.8	21.9	18.7	16.4	14.8	13.1
7	36.2	27.2	21.7	18.1	15.5	13.6	12.1	10.9
8	33.3	25.0	20.0	16.6	14.2	12.5	11.1	10.0
9	24.7	18.5	14.8	12.4	10.6	9.3	8.2	7.4
10	21.6	16.2	13.0	10.8	9.3	8.1	7.2	6.5
11	...	...	...	...	...	...	...	...
12	19.2	14.5	11.6	9.6	8.3	7.2	6.4	5.8
13	...	15.6	12.5	10.4	8.9	7.8	7.0	6.2
14	18.6	14.0	11.2	9.3	8.0	7.0	6.2	5.6
15	13.9	10.5	8.0	7.0	6.0	5.2	4.5	4.2
16	15.4	11.5	9.2	7.7	6.6	5.8	5.1	4.6
17	13.1	9.8	7.8	6.5	5.6	4.9	4.3	4.0
18	9.3	7.0	5.3	4.7	4.0	3.5	3.1	2.8
19	6.4	4.8	3.9	3.2	2.8	2.4	2.1	1.9
20	11.5	8.5	6.8	5.7	4.9	4.3	3.8	3.4
21	7.6	5.7	4.4	3.8	3.2	2.8	2.5	2.3
22	4.1	3.8	2.5	2.1	1.8	1.5	1.4	1.2
23	3.1	2.3	1.9	1.6	1.3	1.2	1.0	0.9
24	1.9	1.3	1.1	0.9	0.8	0.7	0.6	0.5
25	5.5	4.2	3.3	2.8	2.4	2.1	1.8	1.6
26	4.1	3.0	2.4	2.1	1.7	1.5	1.4	1.2
27	2.3	1.7	1.4	1.1	0.9	0.8	0.7	0.67
28	1.7	1.3	1.0	0.9	0.7	0.6	0.57	0.50
29	0.8	0.6	0.5	0.4 $\frac{1}{2}$	0.3 $\frac{1}{2}$	0.3	0.28	0.25

Note.—For Dimensions and



## SAFE PERMANENT DISTRIBUTED LOADS.

Brothers &amp; Co.).

Safety, 1-4th.

Distance between Supports.								Reference Number.
22	24	26	28	30	32	34	36	No.
Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	
24.5	22.5	20.8	19.3	18.0	16.8	15.9	15.0	1
18.0	16.7	15.6	14.4	13.3	12.5	11.8	11.1	2
16.8	15.4	14.2	13.2	12.3	11.6	10.9	10.3	3
13.8	12.7	11.7	10.9	10.1	9.5	9.0	8.4	4
15.7	14.2	13.2	12.2	11.0	10.2	9.8	...	5
11.9	10.9	10.1	9.4	8.7	8.5	7.7	7.2	6
9.9	9.0	8.4	7.8	7.2	6.8	6.4	6.0	7
9.0	8.3	7.7	7.0	6.7	6.2	5.8	5.5	8
6.7	6.2	5.7	5.3	4.9	4.6	4.3	4.1	9
5.9	5.4	5.0	4.6	4.3	4.0	3.8	3.6	10
...	...	...	...	...	...	...	...	11
5.3	4.8	4.4	4.1	3.9	...	...	...	12
5.6	5.0	4.6	4.2	...	...	...	...	13
5.1	4.6	4.3	4.0	3.7	...	...	...	14
3.8	3.5	3.2	3.0	2.8	...	...	...	15
4.2	3.8	3.6	3.3	3.1	2.9	2.7	...	16
3.6	3.3	3.0	2.8	2.6	...	...	...	17
2.5	2.3	2.2	2.0	1.9	...	...	...	18
1.8	1.6	1.5	1.4	1.2	...	...	...	19
3.1	2.8	2.6	2.4	2.1	...	...	...	20
2.0	1.9	1.7	1.5	1.3	...	...	...	21
1.1	1.0	0.9	0.8	0.7	...	...	...	22
...	...	...	...	...	...	...	...	23
...	...	...	...	...	...	...	...	24
1.5	1.4	1.3	1.2	1.1	...	...	...	25
1.1	1.0	0.9	0.8	0.7	...	...	...	26
0.60	0.58	0.52	...	...	...	...	...	27
0.41½	0.40	0.38	...	...	...	...	...	28
0.22	0.20	0.18	...	...	...	...	...	29

Weights of Joists, see Table 122.

TABLE 122.—ROLLED IRON JOISTS.  
(Measures Brothers & Co.)

Reference Number.	Sectional Dimensions. Depth × Width.	Thickness of		Weight per Lineal Foot.	Stock Lengths.
		Web.	Flanges (average).		
	Inches.	Inch.	Inch.	Pounds.	Feet.
1	$19\frac{3}{4} \times 7\frac{1}{8}$	$\frac{13}{16} b$	$1\frac{1}{16}$	100	16 to 40
2	$17\frac{3}{4} \times 6\frac{3}{4}$	$\frac{11}{16}$	$\frac{15}{16}$	82	16 to 40
3	$16 \times 6$	$\frac{9}{16}$	$\frac{13}{16}$	62	8 to 40
4	$14 \times 6$	$\frac{9}{16} \frac{1}{32}$	$\frac{13}{16}$	60	8 to 40
5	$12 \times 7\frac{1}{4}$	...	...	72	16 to 35
6	$12 \times 6$	$\frac{5}{8} \frac{1}{32}$	$\frac{3}{4}$	56	6 to 40
7	$12 \times 5$	$\frac{1}{2} \frac{1}{32}$	$\frac{5}{8} \frac{1}{32}$	42	6 to 40
8	$10 \times 6$	$\frac{1}{2}$	$\frac{7}{8}$	56	7 to 36
9	$10 \times 5$	$\frac{7}{16}$	$\frac{11}{16}$	36	6 to 40
10	$10 \times 4\frac{1}{2}$	$\frac{7}{16}$	$\frac{9}{16}$	32	6 to 30
11	$8\frac{7}{8} \times 6$	...	...	42	10 to 30
12	$9\frac{1}{2} \times 4\frac{1}{2}$	$\frac{3}{8} \frac{1}{32}$	$\frac{9}{16}$	29	6 to 40
13	$9\frac{1}{4} \times 3\frac{3}{4}$	$\frac{3}{8} \frac{1}{32}$	$\frac{3}{8} \frac{1}{32}$	24	6 to 40
14	$8 \times 6$	$\frac{1}{2} \frac{1}{32}$	$\frac{1}{2}$	34	6 to 30
15	$8 \times 5$	$\frac{3}{8} \frac{1}{32}$	$\frac{1}{2} \frac{1}{32}$	29	5 to 40
16	$8 \times 4$	$\frac{1}{2}$	$\frac{7}{16}$	22	5 to 30
17	$7 \times 3\frac{3}{4}$	$\frac{5}{16}$	$\frac{7}{16}$	20	5 to 40
18	$6 \times 5$	$\frac{1}{2}$	$\frac{1}{2}$	29	5 to 36
19	$6\frac{1}{4} \times 3\frac{1}{8}$	$\frac{5}{16}$	$\frac{7}{16}$	16	5 to 40
20	$5 \times 4\frac{1}{2}$	$\frac{5}{16} \frac{1}{32}$	$\frac{1}{2}$	23	5 to 36
21	$4\frac{3}{4} \times 3$	$\frac{5}{16}$	$\frac{5}{16}$	13	5 to 36
22	$4 \times 3$	$\frac{1}{4} \frac{1}{32}$	$\frac{5}{16}$	12	5 to 30
23	$3 \times 3$	$\frac{3}{16} \frac{1}{32}$	$\frac{5}{16} b$	10	5 to 30
24	$8 \times 2\frac{1}{2}$	$\frac{5}{16} \frac{1}{32}$	$\frac{3}{8} \frac{1}{32}$	15	6 to 30
25	$7 \times 2\frac{1}{4}$	$\frac{5}{16}$	$\frac{3}{8} \frac{1}{32}$	14	6 to 30
26	$6\frac{1}{4} \times 2$	$\frac{1}{4} f$	$\frac{3}{8}$	11	5 to 30
27	$4\frac{3}{4} \times 1\frac{3}{4}$	$\frac{3}{16} f$	$\frac{5}{16}$	8	5 to 26
28	$4 \times 1\frac{3}{4}$	$\frac{3}{16} f$	$\frac{5}{16}$	7	5 to 26
29	$3 \times 1\frac{1}{2}$	$\frac{3}{16}$	$\frac{3}{16} \frac{1}{32}$	5	5 to 26

$b$  = bare ;  $f$  = full.

Note.—For Safe Loads, see Table 121.

TABLE 123.—ROLLED IRON JOISTS: CALCULATED BREAKING LOAD AT THE CENTRE.

(Butterley Iron Company.)

Sectional Dimensions. Depth × Width.	Minimum Thickness of Web.	Average Thickness of Flanges.	Weight per Lineal Foot.	Coefficient of Transverse Strength : Loaded at the Middle.
Inches	Inch.	Inch.	Pounds.	
20 × 10	$\frac{13}{16}$	$1\frac{1}{4}$	140 to 144	20,312
19 $\frac{3}{4}$ × 6 $\frac{1}{4}$	$\frac{9}{8}$	$\frac{3}{4}$	69 to 70	8,700
18 × 6 $\frac{1}{4}$	$\frac{9}{8}$	$\frac{3}{4}$	67 to 70	7,704
16 × 6 $\frac{1}{4}$	$\frac{9}{8}$	$\frac{3}{4}$	63 to 66	6,696
16 × 5 $\frac{1}{2}$	$\frac{11}{16}$	1	69 to 72	7,644
15 × 5 $\frac{1}{2}$	$\frac{9}{8}$	$\frac{7}{8}$	57 to 60	6,704
14 × 6 $\frac{1}{4}$	$\frac{9}{8}$	$\frac{3}{4}$	59 to 62	5,544
12 × 6 $\frac{1}{4}$	$\frac{9}{8}$	$\frac{3}{4}$	59 to 62	5,064
12 × 6	$\frac{3}{4}$	1	67 to 77	6,048
12 × 5	$\frac{1}{2}$	$\frac{13}{16}$	46 to 50	4,069
10 $\frac{1}{2}$ × 5 $\frac{1}{2}$	$\frac{1}{2}$	$\frac{9}{8}$	38 to 41	2,700
10 × 5	$\frac{1}{2}$	$\frac{9}{8}$	36 to 40	2,564
9 × 5 $\frac{1}{2}$	$\frac{1}{2}$	$\frac{3}{4}$	42 to 45	2,902
9 × 4 $\frac{1}{2}$	$\frac{1}{2}$	$\frac{9}{8}$	33 to 37	2,144
8 $\frac{1}{2}$ × 4	$\frac{9}{16}$	$\frac{3}{4}$	33 to 36	2,100
8 × 4 $\frac{1}{2}$	$\frac{1}{2}$	$\frac{9}{16}$	28 to 30	1,748
8 × 4	$\frac{13}{16}$	$\frac{7}{8}$	40 to 42	2,340
8 × 2 $\frac{1}{2}$	$\frac{7}{16}$	$\frac{9}{8}$	19 to 21	1,194
7 $\frac{1}{4}$ × 2 $\frac{1}{4}$	$\frac{1}{2}$	$\frac{7}{16}$	19 to 21	807
7 × 3 $\frac{1}{2}$	$\frac{1}{2}$	$\frac{9}{16}$	23 to 25	1,144
6 $\frac{3}{8}$ × 3 $\frac{3}{8}$	$\frac{7}{16}$	$\frac{7}{16}$	18 to 20	846
6 $\frac{1}{4}$ × 2 $\frac{7}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	18 to 20	825
6 × 6	$\frac{1}{2}$	$\frac{9}{16}$	30 to 32	1,512
6 × 5	$\frac{7}{16}$	$\frac{9}{16}$	26 to 28	1,245
6 × 4	$\frac{1}{2}$	$\frac{9}{16}$	23 to 25	1,094
5 $\frac{7}{8}$ × 5	$\frac{1}{2}$	$\frac{1}{2}$	27 to 29	1,117
5 $\frac{1}{2}$ × 1 $\frac{3}{4}$	$\frac{3}{8}$	$\frac{1}{2}$	11 to 13	375
5 × 1 $\frac{3}{4}$	$\frac{5}{16}$	$\frac{1}{2}$	9 to 11	334
4 $\frac{1}{2}$ × 4	$\frac{3}{8}$	$\frac{3}{8}$	18 to 18	560
4 $\frac{1}{4}$ × 1 $\frac{1}{2}$	$\frac{1}{4}$	$\frac{7}{16}$	7 to 9	251
3 × 1 $\frac{1}{8}$	$\frac{5}{32}$	$\frac{1}{4}$	3 to 4	60

*Use of the Table.*—Divide the number in the last column by the span in inches; the quotient is the breaking load in tons at the centre.

\*TABLE 124.—ENGLISH  
(Dorman, Long)

Number of Section.	Weight per Foot in Pounds.	Normal Sizes - in Inches.	Dimensions in Inches.		
			Depth.	Width.	Web Thickness.
No.					Mean Th. of Flange.
G 1	89	20 × 7½	20 × 7.5	.6	1.0
G 2	75	18 × 7	18 × 7.	.55	.94
G 3	62	16 × 6	16 × 6.	.56	.85
G 3A	50	16 × 5	16 × 5.	.51	.73
G 4	59	15 × 6	15 × 6.	.54	.85
G 5	42	15 × 5	15 × 5.	.422	.625
G 6	57	14 × 6	14 × 6.	.51	.85
G 6A	46	14 × 6	14 × 6.	.435	.65
G 6B	41.5	13 × 5	13 × 5.	.51	.6
G 7	54	12 × 6	12 × 6.	.51	.87
G 7B	44	12 × 6	12 × 6.	.41	.72
G 7A	32	12 × 5	12 × 5.	.35	.56
G 8	39	12 × 5	12 × 5.	.44	.65
G 9	45	10 × 6	10 × 6.	.489	.74
G 10	35	10 × 5	10 × 5.	.48	.6
G 10A	29	10 × 5	10 × 5.	.35	.54
G 11	30	10 × 4½	10 × 4.5	.387	.6
G 11A	36	9½ × 4½	9½ × 4.5	.516	.69
G 12	58	9 × 7	9 × 7.	.777	.81
G 13	20	9 × 3¾	9 × 3.75	.3	.45
G 14	35	8 × 6	8 × 6.	.44	.61
G 15	30	8 × 5	8 × 5.	.4	.61
G 16	25	8 × 4	8 × 4.	.41	.56
G 16A	19	8 × 4	8 × 4.	.329	.4
G 17	18	7 × 3¾	7 × 3.75	.313	.46

\* For diagrams relating

ROLLED STEEL JOISTS.  
& Co., Limited.)

Square Inches. Area.	Distributed Loads in Tons that One Foot will Carry, being			Number of Section.
	$\frac{1}{2}$ rd	$\frac{1}{4}$ th	$\frac{1}{8}$ th	
	of the Breaking Strain.			
26·2	1170·91	878·18	702·54	No. G 1
22·06	909·06	631·8	545·43	G 2
18·23	642·09	481·57	385·25	G 3
14·7	494·67	371·01	296·80	G 3A
17·25	585·05	438·79	351·03	G 4
12·28	393·01	294·76	235·81	G 5
16·71	528·91	396·38	317·34	G 6
13·57	429·27	321·95	257·56	G 6A
12·24	328·91	246·68	197·35	G 6B
15·9	438·41	328·8	263·04	G 7
12·9	372·6	279·5	223·6	G 7B
9·41	261·86	196·4	157·12	G 7A
11·41	301·60	226·2	180·96	G 8
13·23	307·15	230·36	184·26	G 9
10·28	227·52	170·34	136·51	G 10
8·53	201·48	151·11	120·89	G 10A
8·83	201·12	150·84	120·67	G 11
10·58	224·97	168·73	134·98	G 11A
17·05	342·61	256·96	205·56	G 12
5·88	118·54	88·91	71·12	G 13
10·3	198·37	148·78	119·03	G 14
8·81	166·86	125·14	100·11	G 15
7·3	130·20	97·65	78·12	G 16
5·562	100·41	75·30	60·24	G 16A
5·28	85·31	63·98	51·18	G 17

to this Table, see p. 270.

TABLE 124.—ENGLISH ROLLED

Number of Section.	Weight per Foot in Pounds.	Normal Sizes in Inches.	Dimensions in Inches.		
			Depth.	Width.	Web Thick-ness. Mean Th. of Flange.
No.					
G 17A	16	$7 \times 3\frac{3}{4}$	$7 \times 3.75$	.25	.375
G 18	18	$6\frac{1}{4} \times 3\frac{1}{2}$	$6\frac{1}{4} \times 3.5$	.339	.5
G 19	25	$6 \times 5$	$6 \times 5$	.423	.52
G 19A	20	$6 \times 4\frac{1}{2}$	$6 \times 4.5$	.434	.4
G 20	16	$6 \times 3$	$6 \times 3$	.39	.45
G 20A	13	$6 \times 3$	$6 \times 3$	.322	.35
G 21	12	$6 \times 2$	$6 \times 2$	.381	.38
G 22	10.5	$5\frac{1}{2} \times 2$	$5\frac{1}{2} \times 2$	.329	.38
G 22A	9	$5\frac{1}{4} \times 1\frac{1}{2}$	$5\frac{1}{4} \times 1.5$	.368	.312
G 23	24	$5 \times 5$	$5 \times 5$	.371	.56
G 24	22	$5 \times 4\frac{1}{2}$	$5 \times 4.5$	.342	.57
G 24A	19	$5 \times 4\frac{3}{16}$	$5 \times 4.1875$	.44	.45
G 25	15	$5 \times 3$	$5 \times 3$	.4	.44
G 25A	11	$5 \times 3$	$5 \times 3$	.23	.38
G 26	10	$4\frac{3}{4} \times 1\frac{3}{4}$	$4\frac{3}{4} \times 1.75$	.4	.38
G 26A	6.5	$4\frac{3}{4} \times 1\frac{3}{4}$	$4\frac{3}{4} \times 1.75$	.1875	.3125
G 27	14	$4\frac{5}{8} \times 3$	$4\frac{5}{8} \times 3$	.4	.43
G 28	12	$4 \times 3$	$4 \times 3$	.299	.43
G 28A	9.5	$4 \times 3$	$4 \times 3$	.225	.34
G 29	8	$4 \times 1\frac{3}{4}$	$4 \times 1.75$	.331	.36
G 29A	5	$4 \times 1\frac{3}{4}$	$4 \times 1.75$	.18	.24
G 30	10.5	$3\frac{1}{2} \times 3$	$3\frac{1}{2} \times 3$	.35	.35
G 31	6	$3\frac{1}{2} \times 1\frac{1}{2}$	$3\frac{1}{2} \times 1.5$	.296	.3
G 32	10	$3 \times 3$	$3 \times 3$	.29	.38
G 33	4	$3 \times 1\frac{1}{4}$	$3 \times 1.25$	.218	.25

STEEL JOISTS (*continued*).

Square Inches. Area.	Distributed Loads in Tons that One Foot will Carry, being			Number of Section.
	$\frac{1}{3}$ rd	$\frac{1}{2}$ th	$\frac{1}{4}$ th	
	of the Breaking Strain.			
4.43	73.10	54.82	43.86	No. G 17A
5.28	75.29	56.47	45.17	G 18
7.3	103.01	77.26	61.81	G 19
5.86	79.05	59.28	47.42	G 19A
4.693	59.59	44.69	35.75	G 20
3.81	49.23	36.92	29.53	G 20A
3.52	39.3	29.47	23.58	G 21
3.08	33.35	25.01	20.01	G 22
2.64	23.75	17.81	14.25	G 22A
7.04	84.05	63.04	50.43	G 23
6.45	76.62	57.47	45.97	G 24
5.575	62.83	47.12	37.7	G 24A
4.40	45.76	34.32	27.46	G 25
3.25	38.82	29.12	23.29	G 25A
2.93	25.38	19.04	15.23	G 26
1.90	19.4	14.5	11.6	G 26A
4.10	40.49	30.37	24.29	G 27
3.52	32.10	24.08	19.26	G 28
2.79	26.8	20.1	16.06	G 28A
2.347	18.34	13.76	11.0	G 29
1.47	12.899	9.67	7.73	G 29A
3.08	23.85	17.88	14.31	G 30
1.76	11.82	8.86	7.09	G 31
2.93	19.95	14.96	11.97	G 32
1.17	6.96	5.22	4.18	G 33

TABLE 125.—ENGLISH ROLLED STEEL JOISTS:  
(Dorman, Long  
Factor of

Reference Number.	Clear Span in Feet							
	2	4	6	8	10	12	14	16
No.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
G 1	...	...	...	...	...	...	62	54
G 2	...	...	...	...	...	...	48	42
G 3	...	...	...	...	...	40	34	30
G 3A	...	...	...	...	...	30	26	23
G 4	...	...	...	...	43	36	31	27
G 5	...	...	...	...	29	24	21	18
G 6	...	...	...	...	39	33	28	24
G 6A	...	...	...	...	32	26	22	20
G 6B	...	...	...	...	24	20	17	15
G 7	...	...	...	...	32	27	23	20
G 7B	...	...	...	...	27	23	20	17
G 7A	...	...	...	...	19	16	14	12
G 8	...	...	...	...	22	18	16	14
G 9	...	...	...	28	23	19	16	14
G 10	...	...	...	21	17	14	12	10
G 10A	...	...	...	19	15	12	10	9
G 11	...	...	...	18	15	12	10	9
G 11A	...	...	...	21	16	14	12	10
G 12	...	...	...	32	25	21	18	16
G 13	...	...	...	11	8	7	6	5
G 14	...	...	24	18	14	12	10	...
G 15	...	...	20	15	12	10	9	...
G 16	...	...	16	12	9	8	7	...
G 16A	...	...	12	9	7	6	5	...
G 17	...	15	10	7	6	5	...	...
G 17A	...	13	9	6	5	4	...	...
G 18	...	14	9	7	5	...	...	...
G 19	...	19	13	9	7	...	...	...
G 19A	...	14	9	7	5	...	...	...
G 20	...	11	7	5	4	...	...	...
G 20A	...	9	6	4	3	...	...	...
G 21	...	7	4	3	2	...	...	...
G 22	...	6	4	3	2	...	...	...
G 22A	...	4	3	2	...	...	...	...
G 23	...	15	10	7	...	...	...	...
G 24	...	14	9	7	...	...	...	...
G 24A	...	11	7	5	...	...	...	...
G 25	...	8	5	4	...	...	...	...
G 25A	...	7	4	3	...	...	...	...
G 26	...	4	3	2	...	...	...	...
G 26A	...	3	2	1	...	...	...	...
G 27	...	7	5	3	...	...	...	...
G 28	12	6	4	...	...	...	...	...
G 29	6	3	2	...	...	...	...	...
G 29A	4	2	1	...	...	...	...	...
G 30	8	4	2	...	...	...	...	...
G 31	4	2	1	...	...	...	...	...
G 32	7	3	...	...	...	...	...	...
G 33	2	1	...	...	...	...	...	...

Note.—For Dimensions and



## CALCULATED SAFE PERMANENT DISTRIBUTED LOADS.

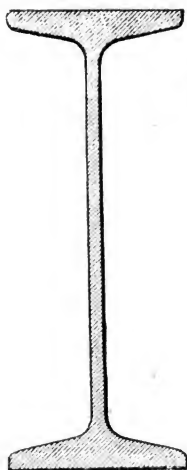
&amp; Co., Limited.)

Safety, 1-4th.

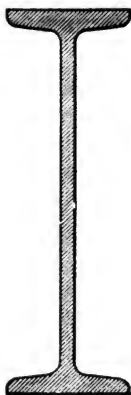
between Supports.

Reference  
Number.

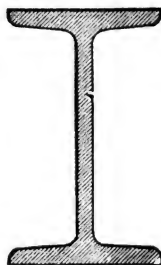
18	20	22	24	26	28	30	32	No.
Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	
48	43	39	36	33	21	29	27	G 1
37	34	30	28	26	24	22	...	G 2
26	24	21	20	18	17	...	...	G 3
20	18	16	15	14	13	...	...	G 3A
24	21	19	18	16	...	...	...	G 4
16	14	13	12	11	...	...	...	G 5
22	19	18	...	...	...	...	...	G 6
17	16	14	...	...	...	...	...	G 6A
13	12	11	...	...	...	...	...	G 6B
13	16	...	...	...	...	...	...	G 7
15	14	...	...	...	...	...	...	G 7B
10	9	...	...	...	...	...	...	G 7A
12	11	...	...	...	...	...	...	G 8
...	...	...	...	...	...	...	...	G 9
...	...	...	...	...	...	...	...	G 10
...	...	...	...	...	...	...	...	G 10A
...	...	...	...	...	...	...	...	G 11
...	...	...	...	...	...	...	...	G 11A
...	...	...	...	...	...	...	...	G 12
...	...	...	...	...	...	...	...	G 13
...	...	...	...	...	...	...	...	G 14
...	...	...	...	...	...	...	...	G 15
...	...	...	...	...	...	...	...	G 16
...	...	...	...	...	...	...	...	G 16A
...	...	...	...	...	...	...	...	G 17
...	...	...	...	...	...	...	...	G 17A
...	...	...	...	...	...	...	...	G 18
...	...	...	...	...	...	...	...	G 19
...	...	...	...	...	...	...	...	G 19A
...	...	...	...	...	...	...	...	G 20
...	...	...	...	...	...	...	...	G 20A
...	...	...	...	...	...	...	...	G 21
...	...	...	...	...	...	...	...	G 22
...	...	...	...	...	...	...	...	G 22A
...	...	...	...	...	...	...	...	G 23
...	...	...	...	...	...	...	...	G 24
...	...	...	...	...	...	...	...	G 24A
...	...	...	...	...	...	...	...	G 25
...	...	...	...	...	...	...	...	G 25A
...	...	...	...	...	...	...	...	G 26
...	...	...	...	...	...	...	...	G 26A
...	...	...	...	...	...	...	...	G 27
...	...	...	...	...	...	...	...	G 28
...	...	...	...	...	...	...	...	G 29
...	...	...	...	...	...	...	...	G 29A
...	...	...	...	...	...	...	...	G 30
...	...	...	...	...	...	...	...	G 31
...	...	...	...	...	...	...	...	G 32
...	...	...	...	...	...	...	...	G 33



G 2.



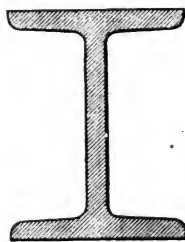
G 5.



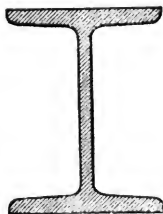
G 9.



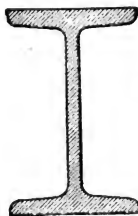
G 10.



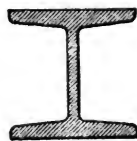
G 12.



G 14.



G 15.



G 23.



G 19.



G 20.



G 21.



G 31.



G 32.



G 33.

19, 19—32.—Rolled Steel Joists, Table 124 (Dorman, Long & Co.). Scale 1-8th.

TABLE 125A.—SAFE DISTRIBUTED LOADS IN TONS ON COMPOUND GIRDERS, OF VARYING SPANS.

(Dorman, Long &amp; Co.)

Factor of Safety = 4.

Number of Section.	Weight per Ft. in Lbs.	Clear Spans in Feet between Supports.															
		10	12	14	16	18	20	22	24	26	28	30	32	34	36	38	
G 1 C 1	144	...	...	...	...	...	76	69	63	59	54	51	48	45	42	40	
G 1 C 2	260	...	...	...	...	...	132	120	110	102	94	88	83	78	74	69	
G 1 C 3	377	...	...	...	...	...	188	170	157	145	134	125	118	111	104	99	
G 1 C 4	195	...	...	...	...	...	116	106	97	89	83	77	73	68	64	61	
G 1 C 5	335	...	...	...	...	...	191	174	159	147	136	127	119	112	106	100	
G 1 C 6	480	...	...	...	...	...	265	241	221	204	189	176	165	156	147	139	
G 1 C 7	248	...	...	...	...	...	159	144	132	122	113	106	99	93	88	83	
G 1 C 8	414	...	...	...	...	...	252	229	210	194	180	168	158	148	140	133	
G 1 C 9	582	...	...	...	...	...	346	314	288	266	247	230	216	203	195	182	
G 2 C 1	130	...	...	...	...	...	71	64	58	53	49	45	42	40	37	...	
G 2 C 2	227	...	...	...	...	...	114	103	93	86	79	73	68	64	60	...	
G 2 C 3	340	...	...	...	...	...	171	154	140	128	119	110	103	96	91	...	
G 2 C 4	180	...	...	...	...	...	111	100	91	83	77	71	67	62	58	...	
G 2 C 5	294	...	...	...	...	...	166	149	135	124	115	106	99	93	88	...	
G 2 C 6	440	...	...	...	...	...	249	224	203	186	172	160	149	140	131	...	
G 2 C 7	360	...	...	...	...	...	220	198	179	165	152	142	132	124	117	...	
G 2 C 8	540	...	...	...	...	...	331	298	271	248	229	213	198	186	175	...	
G 3 C 1	98	...	...	...	...	...	50	44	40	36	33	31	28	27	25	...	
G 3 C 2	178½	...	...	...	...	...	84	75	67	61	56	52	48	45	42	...	
G 3 C 3	266	...	...	...	...	...	124	110	99	90	83	76	70	66	62	...	
G 3 C 4	132	...	...	...	...	...	76	69	61	55	51	47	43	41	38	...	
G 3 C 5	271	...	...	...	...	...	156	139	125	113	104	96	89	83	78	...	
G 3 C 6	394	...	...	...	...	...	226	201	181	164	150	139	129	120	113	...	
G 5 C 1	77	...	...	...	...	...	44	38	34	30	28	25	23	22	20	...	
G 5 C 2	127	...	...	...	...	...	64	56	50	45	41	37	34	32	30	...	
G 5 C 3	191	...	...	...	...	...	97	85	75	68	62	56	52	48	45	...	
G 5 C 4	111½	...	...	...	...	...	72	63	56	50	46	42	39	36	33	...	
G 5 C 5	210	...	...	...	...	...	129	113	100	90	82	75	69	64	60	...	
G 5 C 6	315	...	...	...	...	...	193	172	151	136	123	113	104	96	90	...	
G 6 C 1	142	...	...	...	...	...	64	56	49	45	40	37	34	32	...	...	
G 6 C 2	93	...	...	...	...	...	48	42	38	34	31	28	26	24	...	...	
G 6 C 3	164	...	...	...	...	...	81	71	63	56	51	47	43	40	...	...	
G 6 C 4	245	...	...	...	...	...	119	104	92	83	75	69	64	59	...	...	
G 6 C 5	127	...	...	...	...	...	75	66	58	52	48	44	40	37	...	...	
G 6 C 6	212	...	...	...	...	...	116	102	90	81	74	68	62	58	...	...	
G 6 C 7	326	...	...	...	...	...	169	148	131	118	107	99	92	85	...	...	
G 8 C 1	50½	...	...	...	...	...	21	18	16	14	12	11	10	...	...	...	
G 8 C 2	96	...	...	...	...	...	40	34	30	27	24	22	20	...	...	...	
G 8 C 3	141	...	...	...	...	...	59	51	44	39	35	32	29	...	...	...	
G 8 C 4	75	...	...	...	...	...	41	35	31	27	25	23	20	...	...	...	
G 8 C 5	121	...	...	...	...	...	61	52	45	40	36	33	30	...	...	...	
G 8 C 6	182	...	...	...	...	...	91	78	68	61	55	50	45	...	...	...	
G 8 C 7	108	...	...	...	...	...	69	59	52	46	41	37	34	...	...	...	
G 8 C 8	162	...	...	...	...	...	92	79	69	61	55	50	46	...	...	...	
G 8 C 9	244	...	...	...	...	...	138	118	103	92	83	75	69	...	...	...	
G 10 C 1	46½	18	15	13	11	10	9	...	...	...	...	...	...	...	...	...	
G 10 C 2	87	36	30	26	23	20	18	...	...	...	...	...	...	...	...	...	
G 10 C 3	56½	29	24	21	18	16	15	...	...	...	...	...	...	...	...	...	
G 10 C 4	103	50	42	36	31	28	25	...	...	...	...	...	...	...	...	...	
G 10 C 5	170	87	73	62	54	48	43	...	...	...	...	...	...	...	...	...	
G 10 C 6	76½	45	38	32	28	25	22	...	...	...	...	...	...	...	...	...	
G 10 C 7	134	73	61	52	46	41	37	...	...	...	...	...	...	...	...	...	
G 10 C 8	231	135	112	96	85	75	67	...	...	...	...	...	...	...	...	...	

TABLE 126.—IRON JOIST GIRDERS: ESTIMATED

(Measures

Factor of

Reference Number.	Sectional Dimensions, Depth × Width.	Weight per Lineal Foot.	Clear Span in Feet, or				
			10	12	14	16	18
No.	Inches.	Pounds.	Tons.	Tons.	Tons.	Tons.	Tons.
1	22½ × 12	245	170·6	142·8	122·0	106·8	94·8
2	20½ × 12	160	112·0	93·2	80·0	70·0	62·1
3	13½ × 8	100	39·6	33·6	29·4	25·2	22·5
4	17 × 14	175	112·0	102·7	79·5	69·3	61·8
5	16 × 14	216	110·0	91·7	78·6	69·0	61·1
6	14 × 12	172	96·0	80·0	68·5	59·8	53·2
7	11½ × 12	130	66·0	55·0	47·0	40·6	36·2
8	12½ × 12	110	72·0	56·0	48·0	41·0	37·0
9	10½ × 12	80	39·0	32·4	27·9	24·3	21·6
10	10½ × 16	130	59·0	49·1	41·9	36·5	32·5
11	9¾ × 8	65	25·2	21·0	18·2	15·6	13·5
12	7½ × 9	56	19·7	16·6	14·4	12·1	10·3
13	13 × 12	99	44·0	38·0	31·8	28·2	24·6
14	11 × 9	63	25·0	21·6	18·6	16·7	14·4
15	12½ × 8	57	30·0	24·0	21·7	18·7	16·9
16	10½ × 6	44	18·8	15·2	14·8	12·7	10·0
17	9¾ × 6	35	13·4	12·1	8·8	8·4	7·8
18	8½ × 6	34	10·7	9·1	7·8	6·8	6·1
19	16½ × 5	78	36·8	30·6	26·2	23·0	20·4
20	18½ × 3¾	50	29·4	24·5	21·0	18·2	16·3
21	20 × 5	70	45·4	37·8	32·4	28·4	25·2
22	20½ × 9	84	53·2	43·2	37·2	32·4	28·0
23	24 × 5	88	75·8	63·1	54·1	47·6	42·5
24	16 × 4	46	28·0	23·3	20·0	17·2	15·1
25	16 × 5	67	38·0	31·2	27·1	23·5	21·1
26	14½ × 4½	54	28·4	23·4	20·2	17·8	15·8
27	14 × 3¾	42	19·6	16·5	14·4	12·3	11·1
28	12 × 5	60	23·6	20·0	17·5	15·1	13·4

## SAFE PERMANENT DISTRIBUTED LOADS.

Brothers &amp; Co.).

Safety, 1-4th.

Distances between Supports.									Reference Number.
20	22	24	26	28	30	32	34	36	
Tons	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.	No.
85.4	77.2	71.2	65.7	60.1	56.9	53.4	50.2	47.4	1
55.8	50.6	46.3	42.8	38.8	36.5	35.0	32.8	31.1	2
19.8	18.3	16.8	15.6	14.7	13.5	...	...	...	3
56.0	50.4	46.2	42.6	39.0	36.9	34.0	32.4	30.9	4
55.0	50.0	45.8	42.5	39.3	36.7	34.5	32.5	30.5	5
48.0	42.9	39.6	37.8	34.3	33.1	29.9	28.1	26.6	6
33.0	29.7	27.6	25.4	23.5	21.7	20.3	19.0	18.0	7
34.0	30.0	28.0	26.0	24.0	22.0	20.0	19.0	18.0	8
19.5	17.7	16.2	15.0	13.8	12.9	12.1	11.4	10.8	9
29.5	26.5	24.3	22.5	20.9	19.0	18.4	17.3	16.3	10
12.6	11.4	10.5	9.6	9.0	8.4	7.8	7.5	6.7	11
9.8	7.5	6.8	6.3	5.8	5.5	...	...	...	12
22.4	20.0	18.6	17.1	15.9	14.7	13.1	14.0	12.4	13
13.0	11.8	10.8	10.0	9.0	8.6	8.1	7.6	7.2	14
15.0	13.7	12.0	11.3	10.4	9.8	9.3	...	...	15
9.4	8.3	7.6	7.2	7.0	6.5	...	...	...	16
6.8	6.2	4.6	4.3	4.0	3.2	...	...	...	17
5.5	5.0	4.5	4.2	3.9	3.0	...	...	...	18
18.4	16.7	15.2	14.1	13.2	12.2	11.6	10.8	10.2	19
14.7	13.3	12.3	11.3	10.5	9.8	...	...	...	20
22.7	20.6	18.9	17.5	16.1	15.0	14.1	13.3	12.6	21
26.6	23.6	21.6	20.0	18.4	17.2	...	...	...	22
37.6	34.1	31.5	29.6	27.4	25.2	3.8	22.4	21.0	23
14.0	12.3	11.6	10.5	9.8	8.9	...	...	...	24
19.0	17.2	15.7	14.6	13.5	12.6	11.8	11.1	10.5	25
14.2	12.9	11.7	10.8	10.1	9.5	8.9	...	7.9	26
9.8	8.7	8.0	7.5	7.0	6.6	...	...	...	27
11.9	10.7	10.0	9.3	8.6	8.0	...	...	...	28

FIGS. 33—44.—SECTIONS OF GIRDERS IN TABLE 126.

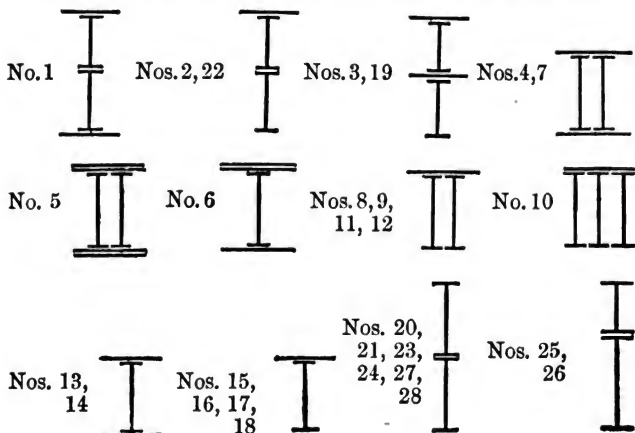


TABLE 127.—ANGLE RIVETED IRON GIRDERS: ESTIMATED  
SAFE PERMANENT DISTRIBUTED LOAD.  
(Measures Brothers & Co.)

Reference Number.	Sectional Dimensions, Depth × Width.	Weight per Lineal Foot.	Clear Span, or Distance between Supports, in Feet.					
			10	12	14	16	18	20
No.	Inches.	Pounds.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
1	9 × 6 $\frac{3}{8}$	46	13	11	9	8	7	6.5
2	12 × 9	112	...	39	...	29	26	23
3	13 × 16	154	...	59	...	44	...	35
4	20 × 18	224	...	...	...	...	...	88

Reference Number.	Sectional Dimensions, Depth × Width.	Weight per Lineal Foot.	Clear Span, or Distance between Supports, in Feet.					
			22	24	26	30	32	34
No.	Inches.	Pounds.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
1	9 × 6 $\frac{3}{8}$	46	...	...	...	...	...	...
2	12 × 9	112	21	19	...	...	...	...
3	13 × 16	154	...	29	27	...	...	...
4	20 × 18	224	...	...	67	58	54	51
							49	

FIGS. 45—48.—SECTIONS OF GIRDERS IN TABLE 127.

TABLE 128.—ANGLES (IRON).  
(The Butterley Company.)

Reference Number.	Sum of the Sides.	Sectional Dimensions.	Thickness.	Weight per Lineal Foot.
No.	Inches.	Inches.	Inch.	Pounds.
1	14	7 × 7	$\frac{3}{4}$ to $1\frac{1}{4}$	26 to 28
2	$13\frac{1}{2}$	10 × $3\frac{1}{2}$	$\frac{7}{16}$ to $\frac{5}{8}$	20 to $21\frac{3}{4}$
3	$12\frac{1}{2}$	9 × $3\frac{1}{2}$	$\frac{7}{16}$ to $\frac{5}{8}$	$17\frac{1}{2}$ to 23
*4	$12\frac{1}{2}$	8 × $4\frac{1}{2}$	$\frac{7}{16}$ to $\frac{5}{8}$	$17\frac{3}{4}$ to $22\frac{1}{2}$
*5	$12\frac{1}{2}$	8 × $4\frac{1}{2}$	$\frac{3}{4}$ only.	...
*6	12	6 × 6	to 1	24 to 27
7	$11\frac{1}{2}$	8 × $3\frac{1}{2}$	$\frac{5}{8}$ to $\frac{5}{8}$	$16\frac{1}{2}$ to 19
*8	11	$5\frac{1}{2}$ × $5\frac{1}{2}$	$\frac{1}{2}$ to $\frac{3}{4}$	$19\frac{1}{2}$ to $25\frac{3}{4}$
*9	$10\frac{1}{2}$	7 × $3\frac{1}{2}$	$\frac{7}{16}$ to $\frac{5}{8}$	$14\frac{3}{4}$ to $18\frac{1}{2}$
*10	$10\frac{1}{2}$	$6\frac{1}{2}$ × 4	$\frac{1}{2}$ to $\frac{5}{8}$	17 to 23
*11	10	7 × 3	$\frac{5}{8}$ to $\frac{5}{8}$	13 to 16
*12	10	6 × 4	$\frac{1}{2}$ to $\frac{5}{8}$	16 to 23
*13	10	5 × 5	$\frac{1}{2}$ to $\frac{3}{4}$	17 to 24
*14	$9\frac{1}{2}$	6 × $3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{5}{8}$	$13\frac{1}{2}$ to 17
*15	9	6 × 3	$\frac{3}{8}$ to $\frac{5}{8}$	$12\frac{1}{2}$ to 17
*16	9	5 × 4	$\frac{3}{8}$ to $\frac{5}{8}$	...
*17	9	$4\frac{1}{2}$ × $4\frac{1}{2}$	$\frac{3}{8}$ to $\frac{5}{8}$	$14\frac{1}{2}$ to 21
*18	$8\frac{1}{2}$	$5\frac{1}{2}$ × 3	$\frac{3}{8}$ to $\frac{5}{8}$	$10\frac{1}{2}$ to $16\frac{1}{2}$
*19	$8\frac{1}{2}$	5 × $3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{5}{8}$	$10\frac{1}{4}$ to $16\frac{1}{2}$
*20	$8\frac{1}{2}$	$4\frac{1}{4}$ × $4\frac{1}{4}$	$\frac{3}{8}$ to $\frac{5}{8}$	$10\frac{1}{4}$ to $16\frac{1}{2}$
*21	$8\frac{1}{2}$	$4\frac{3}{4}$ × $3\frac{3}{4}$	$\frac{3}{8}$ to $\frac{5}{8}$	$13\frac{1}{2}$ to 18
*22	8	5 × 3	$\frac{3}{8}$ to $\frac{5}{8}$	$9\frac{1}{2}$ to $15\frac{1}{2}$
*23	8	$4\frac{1}{2}$ × $3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{5}{8}$	$9\frac{1}{2}$ to $18\frac{1}{2}$
*24	8	4 × 4	$\frac{3}{8}$ to $\frac{5}{8}$	$9\frac{1}{2}$ to 17
*25	$7\frac{1}{2}$	$4\frac{1}{2}$ × 3	$\frac{3}{8}$ to $\frac{5}{8}$	9 to 12
*26	$7\frac{1}{2}$	4 × $3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{5}{8}$	9 to $14\frac{1}{2}$
*27	7	4 × 3	$\frac{5}{16}$ to $\frac{5}{8}$	$8\frac{1}{2}$ to $13\frac{1}{2}$
*28	7	$3\frac{1}{2}$ × $3\frac{1}{2}$	$\frac{5}{16}$ to $\frac{5}{8}$	$8\frac{1}{4}$ to $13\frac{1}{4}$
*29	$6\frac{1}{2}$	4 × $2\frac{1}{2}$	$\frac{5}{16}$ to $\frac{5}{8}$	$6\frac{1}{2}$ to $11\frac{1}{2}$
*30	$6\frac{1}{2}$	$3\frac{1}{2}$ × 3	$\frac{5}{16}$ to $\frac{5}{8}$	$6\frac{1}{2}$ to $11\frac{1}{2}$
*31	$6\frac{1}{2}$	$3\frac{1}{4}$ × $3\frac{1}{4}$	$\frac{5}{16}$ to $\frac{5}{8}$	$6\frac{1}{2}$ to $12\frac{1}{4}$
*32	6	4 × 2	$\frac{5}{16}$ to $\frac{1}{2}$	6 to $10\frac{1}{2}$
*33	6	$3\frac{1}{2}$ × $2\frac{1}{2}$	$\frac{5}{16}$ to $\frac{1}{2}$	6 to $10\frac{1}{2}$
*34	6	3 × 3	$\frac{5}{16}$ to $\frac{1}{2}$	7 to $11\frac{1}{2}$
*35	$5\frac{1}{2}$	3 × $2\frac{1}{2}$	$\frac{1}{4}$ to $\frac{1}{2}$	$4\frac{1}{2}$ to $8\frac{1}{2}$

TABLE 128.—ANGLES (IRON) (*continued*).

Reference Number.	Sum of the Sides.	Sectional Dimensions.	Thickness.	Weight per Lineal Foot.
No.	Inches.	Inches.	Inch.	Pounds.
*36	5½	2¾ × 2¾	¼ to ½	5½ to 8½
*37	5¼	2¾ × 2½	¼ to ¾	...
*38	5	3 × 2	¼ to ¾	4 to 7½
*39	5	2½ × 2½	¼ to ¾	4 to 7½
*40	4¾	2¾ × 2	⅜ to ¾	...
*41	4½	3 × 1½	¾ only.	...
*42	4½	2½ × 2	⅜ to ¾	3½ to 6
*43	4½	2¼ × 2¼	⅜ to ¾	3½ to 6¾
*44	4	2 × 2	⅜ to ¾	2½ to 5¼
*45	3¾	2 × 1¾	⅜ to ¾	...
*46	3½	2 × 1½	⅜ to ¾	2¾ to 4
*47	3½	1¾ × 1¾	⅜ to ¾	2 to 4
*48	3¼	1¾ × 1½	⅜ to ¾	2¾ to 4
*49	3	1½ × 1½	⅜ to ¾	1¾ to 3¼
*50	2¾	1½ × 1¼	⅜ to ¾	...
*51	2½	1¼ × 1¼	⅜ to ¼	1½ to 2¾
*52	2	1 × 1	⅜ to ¼	1 to 1¼
*53	1¾	¾ × ¾	⅜ to ¼	13 oz.
*54	1⅝	⅝ × ⅝	⅜ to ¼	...
*55	1½	¾ × ¾	⅜ to ⅜	12 oz.
*56	1¼	¾ × ¾	⅜ to ⅜	...

\* In iron or steel, others in iron only.

TABLE 129.—CHANNELS (IRON).  
(The Butterley Company.)

Order Number.	Sectional Dimensions.	Thick-ness of Web.	Average Thick-ness of Flanges.	Weight per Lineal Foot.
No.	Inches.	Inch.	Inch.	Pounds.
1	12 × 3¾	11/16	⅝	40 to 42
2	10 × 3½	1/2	1/2	28 to 30
3	8 × 4	1/2	1/2	26 to 28
4	7 × 2¾	3/8	3/8	...
5	7 × 2	5/8	5/8	21 to 23
*6	6 × 2½	3/8	3/8	} 11 to 14
*7	6 × 2½	5/16	5/16	
8	5 × 3½	1/2	1/2	18 to 19
*9	4½ × 1½	1/2	1/2	11 to 12
*10	4½ × ¾	5/16	5/16	6 to 6½
*11	4 × ¾	5/16	5/16	5¾ to 6
12	3½ × 5 and 2½	1/2	1/2	17 to 18
*13	2½ × 1½	3/8	3/8	5 to 6

\* In iron or steel ; others in iron only.



TABLE 130.—TEES (IRON) (The Butterley Company).

Order Number.	Sum of the Flange and Web.	Sectional Dimensions.	Thickness.		Thickness.		Thickness.		Weight per Lineal Foot.
			Flange.	Web.	Flange.	Web.	Flange.	Web.	
No.	Inches.	Ins. (Flange). Ins. (Web).	Inch.	Inch.	Inch.	Inch.	Inch.	Inch.	Pounds.
1	20	10 × 10	1 1/8	1 3/8	1 1/8	7/8	...	...	69 to 70
2	16 1/4	6 1/2 × 8	1 1/8	1 3/8	1 1/8	...	...	...	57 to 60
3	14 1/4	6 1/4 × 6	1 1/8	1 3/8	1 1/8	...	...	...	32 to 34
4	12 1/4	6 1/4 × 6	1 1/8	1 3/8	1 1/8	...	...	...	28 to 30
5	12	6 × 6	1 1/8	1 3/8	1 1/8	...	...	...	23 to 25
6	10 1/2	7 × 4 1/2	1 1/8	1 3/8	1 1/8	...	...	...	17 to 18
7	*10	6 × 4	1 1/8	1 3/8	1 1/8	...	...	...	15 to 20
8	*10	5 × 5	1 1/8	1 3/8	1 1/8	...	...	...	16 to 18
9	*9 3/8	5 1/2 × 3 3/8	1 1/8	1 3/8	1 1/8	...	...	...	18
10	*9	5 × 4	1 1/8	1 3/8	1 1/8	...	...	...	14 1/2 to 16
11	*9	6 × 3	1 1/8	1 3/8	1 1/8	...	...	...	11 to 14 1/2
12	*8 1/2	5 1/2 × 3 1/2	1 1/8	1 3/8	1 1/8	...	...	...	13 1/4
13	*8 1/2	5 × 3 1/2	1 1/8	1 3/8	1 1/8	...	...	...	16
14	*8	5 × 4	1 1/8	1 3/8	1 1/8	...	...	...	12 1/4
15	*8	4 × 3	1 1/8	1 3/8	1 1/8	...	...	...	9 1/2 to 12 1/2
16	*7	4 × 3 1/2	1 1/8	1 3/8	1 1/8	...	...	...	11
17	*7	3 1/2 × 3 1/2	1 1/8	1 3/8	1 1/8	...	...	...	11
18	*6 1/2	3 1/2 × 3	1 1/8	1 3/8	1 1/8	...	...	...	7 3/4 to 10 1/4

\* In iron or steel; others in iron only.

TABLE 130.—TEES (IRON) (*continued*).

Order Number.	Sum of the Flange and Web.	Sectional Dimensions.	Thickness.		Thickness.		Thickness.		Weight per Lineal Foot.
			Flange.	Web.	Flange.	Web.	Flange.	Web.	
No.	Inches.	Ins. (Flange). Ins. (Web).	Inch.	Inch.	Inch.	Inch.	Inch.	Inch.	Pounds.
19	*6½	3 3½	½	1 ½	7/16	7/16	...	...	10
20	*6	4 2	½	1 ½	7/16	7/16	...	...	7
21	*6	3 3	½	1 ½	7/16	7/16	...	...	7
22	*5½	3 2½	½	1 ½	7/16	7/16	...	...	9
23	*5½	3 2½	½	1 ½	7/16	7/16	...	...	...
24	*5	3 2½	½	1 ½	7/16	7/16	...	...	6
25	*5	2½ 2½	½	1 ½	7/16	7/16	...	...	5½
26	*4½	2½ 2½	½	1 ½	7/16	7/16	...	...	...
27	*4½	2½ 2½	½	1 ½	7/16	7/16	...	...	...
28	*4½	2½ 2	½	1 ½	7/16	7/16	...	...	3½
29	*4	2 2	½	1 ½	7/16	7/16	...	...	3 to 4½
30	*3½	1½ 1½	½	1 ½	7/16	7/16	...	...	...
31	*3½	1½ 1½	½	1 ½	7/16	7/16	...	...	3
32	*3½	1½ 1½	½	1 ½	7/16	7/16	...	...	...
33	*3	1½ 1½	½	1 ½	7/16	7/16	...	...	2
34	*2½	1½ 1	½	1 ½	7/16	7/16	...	...	...
35	*2	1½ 1	½	1 ½	7/16	7/16	...	...	8 to 12
36	*1½	1 7/8	½	1 ½	7/16	7/16	...	...	...
37	*1½	1 7/8	½	1 ½	7/16	7/16	...	...	...

\* In iron or steel.

TABLE 131.—BULB BARS (IRON).  
(The Butterley Company.)

Order Number.	Width.	Thickness of Bulb.	Thickness of Web.	Weight per Lineal Foot.
	Inches.	Inches.	Inch.	Pounds.
1	10	2½ to 2⅝	½ to ⅝	23
2	6	3¼ to 3⅝	½ full to ⅝ full	21 to 24
3	6	2¼ to 2⅝	½ to ⅝	13½ to 18

Rolled in iron only.

TABLE 132.—BULB TEES OR DECK BEAMS (IRON).  
(The Butterley Company.)

Depth (Web).	Width of Flange.	Width of Bulb.	Minimum Thickness of Web.	Weight per Lineal Foot in Iron.
Inches.	Inches.	Inches.	Inch.	Pounds.
16	6¼	3¼	⅝ bare	58 to 62
16	6¼	2¼	⅝ bare	53 to 57
15	6¼	3¼	⅝ bare	56 to 60
15	6¼	2¼	⅝ bare	51 to 55
14	6¼	3¼	⅝ bare	54 to 58
14	6¼	2¼	⅝ bare	50 to 54
13	6¼	3¼	⅝ bare	52 to 56
13	6¼	2¼	⅝ bare	48 to 52
12	6¼	3¼	⅝ bare	50 to 54
12	6¼	2¼	⅝ bare	46 to 50
11	6½	2¼	½ bare	45 to 49
†11	6	2¼	½ bare	36 to 40
10	6	2⅝	½ bare	35 to 39
†10	6	2	½ bare	32 to 36
†9½	5½	1¾	½ bare	31 to 35
9	5½	2	⅞	32 to 36
9	6½	2	½ bare	35 to 39
9	5¼	1¾	15/32	29 to 29
8½	5¼	1¾	20/32	25 to 28
8	6¼	1¾	9/16 bare	31 to 33
8	5¼	1⅞	7/16	27 to 30
†8	5	1¾	3/8 full	22 to 24
7	5	1¾	3/8	23 to 26
†7	5	1⅝	3/8	19 to 22
6	5	1½	3/8	19 to 22
*6	4½	1⅞	3/8	16 to 18
*6	4	1½	7/16	18 to 20
*5	4	1½	3/8	14 to 16
4	3	1¼	5/16	9 to 10

\* In iron or steel; † in steel only; the others in iron only.

TABLE 133.—BULB ANGLES (IRON).  
(The Butterley Company.)

Order Number.	Depth (Web).	Width of Flange.	Width of Bulb.	Thickness of Web.	Weight per Lineal Foot.
No.	Inches.	Inches.	Inches.	Inch.	Pounds.
1	12	3½	2¼	½ to ⅝	33 to 38
*2	9	3½	2¼	⅞ to ⅝	24½ to 31
*3	8	2½	1	⅞ to ½	...
*4	7	3¾	1⅝	½ to ⅝	19 to 22
*5	6½	3½	1⅝	½ to ⅝	16 to 20
*6	6	2½	⅞	⅞ to ½	...
*7	5	2½	1⅝	⅝ to ½	11 to 13

\* In iron or steel; other in iron only.

TABLE 134.—SPACE OR Z ANGLES (IRON).  
(The Butterley Company.)

Order Number.	Depth of Web.	Width of Flanges.	Thickness.	Weight per Lineal Foot.
No.	Inches.	Inches.	Inch.	Pounds.
1	10	3½ and 3½	⅞ to ⅞	24 to 31
2	9	3 and 3	⅞ to ½	...
3	6	3½ and 3	⅞ to ½	15 to 20
4	5	3 and 2½	½ to ⅝	16 to 20
5	4	3½ and 3	⅞ to ⅞	12½ to 20
6	4	2½ and 2½	⅞ to ½	11 to 14
7	3	3 and 2½	⅞ to ⅞	11 to 15
8	3	2¼ and 2¼	⅞ to ½	9 to 12
9	2½	2½ and 2¼	⅞ to ⅞	10 to 14
10	2½	2½ and 2½	⅞ to ½	9 to 12

Can be rolled in iron or steel.

TABLE 135.—Z ANGLES (STEEL).  
(Dorman, Long & Co., Limited.)

Depth and Thickness (Web).		Width and Thickness of Flanges.		Depth and Thickness (Web).		Width and Thickness of Flanges.	
Ins.	In.	Ins.	In.	Ins.	In.	Ins.	In.
8 × 1	to ⅝	3½ and 3½ × 1	& ⅞	5½ × 1	to ⅝	3 and 3 × 1	to ⅝
7 × 1	to ⅝	3 and 3 × 1	to ⅞	5 × 1	to ⅝	3½ and 3½ × 1	to ⅝
6 × 1	to ⅝	3½ and 3½ × 1	to ⅞	5 × 1	to ⅝	3 and 3 × 1	to ⅝
6 × 1	to ⅝	3½ and 3 × 1	to ⅞	5 × 1	to ⅝	2½ and 3 × 1	to ⅝
5½ × 1	to ⅝	3 and 3 × 1	to ⅞	4 × 1	to ⅝	3 and 3 × 1	to ⅝

TABLE 136.—ANGLES (STEEL).

(Dorman, Long &amp; Co., Limited.)

Sectional Dimensions.	Thickness.	Sectional Dimensions.	Thickness.	Sectional Dimensions.	Thickness.
EQUAL SIDED.		UNEQUAL SIDED.			
Inches.	Inch.	Inches.	Inch.	Inches.	Inch.
8 × 8	$\frac{1}{2}$ to 1	7 × 4	$\frac{7}{16}$ to $\frac{7}{8}$	$4\frac{1}{2} \times 3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{7}{8}$
7 × 7	$\frac{1}{2}$ to 1	7 × 3	$\frac{3}{8}$ to $\frac{3}{4}$	$4\frac{1}{2} \times 3$	$\frac{5}{16}$ to $\frac{3}{4}$
6 × 6	$\frac{1}{2}$ to 1	$6\frac{1}{2} \times 4\frac{1}{2}$	$\frac{7}{16}$ to 1	$4\frac{1}{2} \times 2\frac{1}{2}$	$\frac{3}{8}$ to $\frac{3}{4}$
5 × 5	$\frac{7}{16}$ to $\frac{7}{8}$	$6\frac{1}{2} \times 4$	$\frac{7}{16}$ to $\frac{13}{16}$	$4 \times 3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{7}{8}$
$4\frac{1}{2} \times 4\frac{1}{2}$	$\frac{3}{8}$ to $\frac{7}{8}$	$6\frac{1}{2} \times 3$	$\frac{7}{16}$ to $\frac{3}{4}$	$4 \times 3$	$\frac{3}{8}$ to $\frac{3}{4}$
4 × 4	$\frac{5}{16}$ to $\frac{11}{16}$	6 × 5	$\frac{7}{16}$ to 1	$4 \times 2\frac{1}{2}$	$\frac{5}{16}$ to $\frac{3}{4}$
$3\frac{1}{2} \times 3\frac{1}{2}$	$\frac{5}{16}$ to $\frac{11}{16}$	6 × 4	$\frac{3}{8}$ to $\frac{7}{8}$	$3\frac{1}{2} \times 3$	$\frac{5}{16}$ to $\frac{11}{16}$
3 × 3	$\frac{1}{4}$ to $\frac{11}{16}$	$6 \times 3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{7}{8}$	$3\frac{1}{2} \times 2\frac{1}{2}$	$\frac{5}{16}$ to $\frac{3}{8}$
$2\frac{3}{4} \times 2\frac{3}{4}$	$\frac{1}{4}$ to $\frac{5}{8}$	6 × 3	$\frac{3}{8}$ to $\frac{3}{4}$	$3\frac{1}{2} \times 1\frac{3}{4}$	$\frac{7}{16}$ and $\frac{3}{8}$
$2\frac{1}{2} \times 2\frac{1}{2}$	$\frac{1}{4}$ to $\frac{5}{8}$	$5\frac{1}{2} \times 4$	$\frac{3}{8}$ to $\frac{7}{8}$	$3\frac{1}{2} \times 1\frac{3}{4}$	and $\frac{5}{16}$
$2\frac{1}{4} \times 2\frac{1}{4}$	$\frac{1}{4}$ to $\frac{1}{2}$	$5\frac{1}{2} \times 3\frac{1}{2}$	$\frac{3}{8}$ to $\frac{13}{16}$	$3\frac{1}{2} \times 1\frac{3}{4}$	and $\frac{5}{16}$
2 × 2	$\frac{3}{16}$ to $\frac{3}{8}$	$5\frac{1}{2} \times 3$	$\frac{3}{8}$ to $\frac{3}{4}$	$3 \times 2\frac{3}{4}$	$\frac{1}{4}$ to $\frac{11}{16}$
$1\frac{3}{4} \times 1\frac{3}{4}$	$\frac{3}{16}$ to $\frac{3}{8}$	5 × 4	$\frac{3}{8}$ to $\frac{13}{16}$	$3 \times 2\frac{1}{2}$	$\frac{1}{4}$ to $\frac{11}{16}$
$1\frac{1}{2} \times 1\frac{1}{2}$	$\frac{1}{8}$ to $\frac{5}{16}$	5 × $3\frac{1}{2}$	$\frac{5}{16}$ to $\frac{3}{4}$	3 × 2	$\frac{1}{4}$ to $\frac{9}{16}$
$1\frac{1}{4} \times 1\frac{1}{4}$	$\frac{1}{8}$ to $\frac{5}{16}$	5 × 3	$\frac{5}{16}$ to $\frac{3}{4}$	$2\frac{1}{2} \times 2$	$\frac{1}{4}$ to $\frac{1}{2}$
1 × 1	$\frac{3}{32}$ to $\frac{1}{4}$	$4\frac{1}{2} \times 4$	$\frac{3}{8}$ to $\frac{7}{8}$	3 × $1\frac{1}{2}$	$\frac{5}{16}$ to $\frac{3}{8}$
				2 × $1\frac{1}{2}$	$\frac{3}{16}$ to $\frac{3}{8}$

TABLE 137.—TEES (STEEL).

(Dorman, Long &amp; Co., Limited.)

Width of Flange.	Depth (Web).	Thickness.	Width of Flange.	Depth (Web).	Thickness.
Inches.	Inches.	Inch.	Inches.	Inches.	Inch.
6	3	$\frac{3}{8}$ and $\frac{1}{2}$	3	3	$\frac{3}{8}$
5	3	$\frac{3}{8}$ and $\frac{1}{2}$	3	$2\frac{1}{2}$	$\frac{3}{8}$
5	$2\frac{1}{2}$	$\frac{3}{8}$	$2\frac{1}{2}$	$2\frac{1}{2}$	$\frac{1}{4}$
$4\frac{1}{2}$	$3\frac{1}{2}$	$\frac{7}{16}$	$2\frac{1}{4}$	$2\frac{1}{4}$	$\frac{1}{4}$
4	5	$\frac{1}{2}$	2	2	$\frac{1}{4}$
4	4	$\frac{1}{2}$	2	$1\frac{1}{2}$	$\frac{1}{4}$
4	$3\frac{1}{2}$	$\frac{3}{8}$	2	$1\frac{1}{4}$	$\frac{1}{4}$
4	3	$\frac{3}{8}$	$1\frac{3}{4}$	$1\frac{3}{4}$	$\frac{3}{16}$
$3\frac{1}{2}$	$3\frac{1}{2}$	$\frac{3}{8}$	$1\frac{1}{2}$	2	$\frac{1}{4}$
$3\frac{1}{2}$	3	$\frac{3}{8}$	$1\frac{1}{2}$	$1\frac{1}{2}$	$\frac{1}{4}$

TABLE 138.—CHANNELS (STEEL).  
(Dorman, Long & Co., Limited.)

Refer- ence Num- ber.	Sectional Dimen- sions.	Web Thick- ness.	Flange Thick- ness.	Sec- tional Area.	Refer- ence Num- ber.	Sectional Dimen- sions.	Web Thick- ness.	Flange Thick- ness.	Sec- tional Area.
No.	Inches.	Inch.	Inch.	Sq. In.	No.	Inches.	Inch.	Inch.	Sq. In.
C 12A	12 × 3 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	9.37	C 7	6 × 4	$\frac{3}{16}$	$\frac{1}{4}$	7.81
C 12	12 × 3 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	9.0	C 6	6 × 3	$\frac{3}{16}$	$\frac{1}{4}$	4.54
C 11A	10 × 4	$\frac{3}{16}$	$\frac{1}{4}$	8.06	C 6A	6 × 2 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	4.42
C 11	10 × 3	$\frac{3}{16}$	$\frac{1}{4}$	6.61	C 6B	6 × 3 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	5.49
C 9	8 × 3 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	7.0	C 5	5 $\frac{1}{2}$ × 2 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	4.67
C 9A	7 $\frac{1}{2}$ × 3 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	7.18	C 4	4 $\frac{1}{2}$ × 2	$\frac{3}{16}$	$\frac{1}{4}$	3.33
C 8A	7 × 3 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	6.5	C 2	4 × 3	$\frac{3}{16}$	$\frac{1}{4}$	4.81
C 8	7 × 3	$\frac{3}{16}$	$\frac{1}{4}$	6.0	C 1	3 $\frac{1}{2}$ × 1 $\frac{1}{2}$	$\frac{3}{16}$	$\frac{1}{4}$	2.43

TABLE 139.—BULB BARS (STEEL).  
(Dorman, Long & Co., Limited.)

Length.	Thickness.	Length.	Thickness.	Length.	Thickness.
Inches.	Inch.	Inches.	Inch.	Inches.	Inch.
12	$\frac{10}{20}$ to $\frac{14}{20}$	9	$\frac{9}{20}$ to $\frac{11}{20}$	7 $\frac{1}{2}$	$\frac{7}{20}$ to $\frac{9}{20}$
11	$\frac{10}{20}$ to $\frac{13}{20}$	8 $\frac{1}{2}$	$\frac{8}{20}$ to $\frac{10}{20}$	7	$\frac{7}{20}$ to $\frac{9}{20}$
10 $\frac{1}{2}$	$\frac{10}{20}$ to $\frac{12}{20}$	8	$\frac{8}{20}$ to $\frac{10}{20}$	6 $\frac{1}{2}$	$\frac{6}{20}$ to $\frac{8}{20}$
10	$\frac{10}{20}$ to $\frac{12}{20}$	7 $\frac{1}{2}$	$\frac{11}{20}$ to $\frac{11}{20}$	6	$\frac{6}{20}$ to $\frac{8}{20}$
9 $\frac{1}{2}$	$\frac{9}{20}$ to $\frac{11}{20}$				

TABLE 140.—BULB ANGLES (STEEL).  
(Dorman, Long & Co., Limited.)

Depth (Web).	Width of Flange.	Web Thick- ness.	Flange Thick- ness.	Depth (Web).	Width of Flange.	Web Thickness.	Flange Thick- ness.
Inches.	Inches.	Inch.	Inch.	Inches.	Inches.	Inch.	Inch.
9	3 $\frac{1}{2}$	$\frac{10}{20}$ to $\frac{12}{20}$	$\frac{11}{20}$	6 $\frac{1}{2}$	3	$\frac{8}{20}$ to $\frac{11}{20}$	$\frac{8}{20}$
8	3	$\frac{10}{20}$ to $\frac{12}{20}$	$\frac{10}{20}$	6	3 $\frac{1}{2}$	$\frac{8}{20}$ to $\frac{12}{20}$	$\frac{8}{20}$
7 $\frac{1}{2}$	3	$\frac{9}{20}$ to $\frac{12}{20}$	$\frac{9}{20}$	6	3	$\frac{8}{20}$ to $\frac{11}{20}$	$\frac{8}{20}$
7	3	$\frac{8}{20}$ to $\frac{11}{20}$	$\frac{9}{20}$	5 $\frac{1}{2}$	3	$\frac{8}{20}$ to $\frac{11}{20}$	$\frac{8}{20}$
6 $\frac{1}{2}$	3 $\frac{1}{2}$	$\frac{9}{20}$ to $\frac{11}{20}$	$\frac{10}{20}$	3 $\frac{3}{4}$	2 $\frac{1}{2}$	$\frac{9}{20}$ & $\frac{11}{20}$	$\frac{9}{20}$
9	3	$\frac{10}{20}$ to $\frac{12}{20}$					

TABLE 141.—ENGLISH STEEL COMPOUND GIRDERS.  
(Dorman, Long & Co., Limited.)

No. of Section.	Weight per Foot in Pounds.	Sizes in Inches.	Compounded of	Distributed Loads in Tons that One Foot will Carry, being $\frac{1}{4}$ th of Breaking Strain.	
				$\frac{1}{4}$ th	$\frac{1}{2}$ th
G 1 C 1	144	21 $\frac{1}{2}$ × 12	1 G 1 and 2 $\frac{1}{4}$ -in. plates	1533·43	1226·72
G 1 C 2	260	21 $\frac{1}{2}$ × 18	2 G 1 " 2 " "	2654·36	2123·48
G 1 C 3	377	21 $\frac{1}{2}$ × 24	3 G 1 " 2 " "	3775·29	3020·23
G 1 C 4	195	22 $\frac{1}{2}$ × 12	1 G 1 " 4 " "	2335·51	1868·4
G 1 C 5	335	22 $\frac{1}{2}$ × 18	2 G 1 " 4 " "	3821·02	3056·81
G 1 C 6	480	22 $\frac{1}{2}$ × 24	3 G 1 " 4 " "	5306·54	4245·23
G 1 C 7	248	23 $\frac{1}{2}$ × 12	1 G 1 " 6 " "	3183·43	2546·74
G 1 C 8	414	23 $\frac{1}{2}$ × 18	2 G 1 " 6 " "	5054·36	4043·48
G 1 C 9	582	23 $\frac{1}{2}$ × 24	3 G 1 " 6 " "	6925·29	5540·23
G 2 C 1	130	19 $\frac{1}{2}$ × 12	1 G 2 " 2 " "	1279·19	1023·35
G 2 C 2	227	19 $\frac{1}{2}$ × 16	2 G 2 " 2 " "	2061·72	1649·37
G 2 C 3	340	19 $\frac{1}{2}$ × 24	3 G 2 " 2 " "	3092·59	2474·07
G 2 C 4	180	20 $\frac{1}{2}$ × 12	1 G 2 " 4 " "	2007·94	1606·35
G 2 C 5	294	20 $\frac{1}{2}$ × 16	2 G 2 " 4 " "	2989·22	2391·37
G 2 C 6	440	20 $\frac{1}{2}$ × 24	3 G 2 " 4 " "	4483·84	3587·07
G 2 C 7	360	21 $\frac{1}{2}$ × 16	2 G 2 " 6 " "	3975·06	3180·04
G 2 C 8	540	21 $\frac{1}{2}$ × 24	3 G 2 " 6 " "	5962·59	4770·07
G 3 C 1	98	17 × 10	1 G 3 and 2 $\frac{1}{2}$ -in. plates	808·89	647·11
G 3 C 2	178 $\frac{1}{2}$	17 × 14	2 G 3 " 2 " "	1353·78	1083·02
G 3 C 3	266	17 × 20	3 G 3 " 2 " "	1986·67	1589·33
G 3 C 4	132	18 × 10	1 G 3 " 4 " "	1228·89	983·11
G 3 C 5	271	19 × 14	2 G 3 " 6 " "	2505·78	2004·62
G 3 C 6	394	19 × 20	3 G 3 " 6 " "	3618·67	2894·83
G 5 C 1	77	16 × 10	1 G 5 " 2 " "	618·85	495·08
G 5 C 2	127	16 × 12	2 G 5 " 2 " "	907·03	725·62
G 5 C 3	191	16 × 18	3 G 5 " 2 " "	1360·55	1088·44
G 5 C 4	111 $\frac{1}{2}$	17 × 10	1 G 5 " 4 " "	1014·83	811·86
G 5 C 5	210	18 × 12	2 G 5 " 6 " "	1813·7	1450·96
G 5 C 6	315	18 × 18	3 G 5 " 6 " "	2720·55	2176·44
G 6 C 1	142	14 $\frac{1}{2}$ × 15	2 G 6 " 1 " "	898·33	718·66
G 6 C 2	93	15 × 10	1 G 6 " 2 " "	684·77	547·81
G 6 C 3	164	15 × 14	2 G 6 " 2 " "	1137·54	910·03
G 6 C 4	245	15 × 20	3 G 6 " 2 " "	1667·64	1334·11
G 6 C 5	127	16 × 10	1 G 6 " 4 " "	1056·77	845·41
G 6 C 6	212	16 × 14	2 G 6 " 4 " "	1633·54	1306·83
G 6 C 7	326	16 × 20	3 G 6 " 4 " "	2370·31	1896·24
G 8 C 1	50 $\frac{1}{2}$	12 $\frac{1}{2}$ × 8	1 G 8 and 1 $\frac{3}{8}$ -in. plates	257·83	206·26
G 8 C 2	96	12 $\frac{1}{2}$ × 12	2 G 8 " 1 " "	485·9	388·72
G 8 C 3	141	12 $\frac{1}{2}$ × 16	3 G 8 " 1 " "	713·78	571·02
G 8 C 4	75	13 × 10	1 G 8 and 2 $\frac{1}{4}$ -in. plates	500·49	400·39
G 8 C 5	121	13 × 12	2 G 8 " 2 " "	734·31	587·44
G 8 C 6	182	13 × 18	3 G 8 " 2 " "	1101·47	881·17
G 8 C 7	108	14 × 10	1 G 8 " 4 " "	831·24	664·99
G 8 C 8	162	14 × 12	2 G 8 " 4 " "	1107·81	886·24
G 8 C 9	244	14 × 18	3 G 8 " 4 " "	1661·72	1329·37
G 10 C 1	46 $\frac{1}{2}$	10 $\frac{1}{2}$ × 8	1 G 10 and 1 $\frac{3}{8}$ -in. plates	187·94	150·35
G 10 C 2	87	10 $\frac{1}{2}$ × 12	2 G 10 " 1 " "	367·66	294·15
G 10 C 3	56 $\frac{1}{2}$	10 $\frac{1}{2}$ × 8	1 G 10 " 2 " "	295·34	236·27
G 10 C 4	103	10 $\frac{1}{2}$ × 12	2 G 10 " 2 " "	507·64	406·11
G 10 C 5	170	11 × 18	3 G 10 " 2 $\frac{1}{4}$ -in. plates	874·35	699·48
G 10 C 6	76 $\frac{1}{2}$	11 $\frac{1}{2}$ × 8	1 G 10 " 4 $\frac{1}{8}$ -in. plates	455·26	364·21
G 10 C 7	134	11 $\frac{1}{2}$ × 12	2 G 10 " 4 " "	738·52	590·81
G 10 C 8	231	12 × 18	3 G 10 " 4 $\frac{1}{4}$ -in. plates	1351·6	1081·28

TABLE 142.—BULB TEES (STEEL).

(Dorman, Long &amp; Co., Limited.)

Depth (Web).	Width of Flange.	Web Thickness.	Flange Thick- ness.	Depth (Web).	Width of Flange.	Web Thickness.	Flange Thick- ness.
Inches.	Inches.	Inch.	Inch.	Inches.	Inches.	Inch.	Inch.
12	6½	$\frac{11}{20}$ to $\frac{14}{20}$	$\frac{11}{20}$	8½	5½	$\frac{8}{20}$ to $\frac{10}{20}$	$\frac{8}{20}$
11	6½	$\frac{10}{20}$ to $\frac{13}{20}$	$\frac{10}{20}$	8	5	$\frac{8}{20}$ & $\frac{9}{20}$	$\frac{8}{20}$
10	6	$\frac{10}{20}$ to $\frac{13}{20}$	$\frac{9}{20}$	7	5	$\frac{8}{20}$ & $\frac{10}{20}$	$\frac{8}{20}$
9	5½	$\frac{9}{20}$ & $\frac{11}{20}$	$\frac{9}{20}$	6	4½	$\frac{8}{20}$ & $\frac{10}{20}$	$\frac{8}{20}$

## BOLTS AND NUTS.

## Screw Bolts and Nuts.

According to the Whitworth system of standard sizes of bolts and nuts, the thickness of the bolt-head is  $\frac{1}{4}$ ths of the diameter, and that of the nut is equal to the diameter. The angle formed by the two sides of the triangular thread is 55 degrees. The top and the bottom of the thread are rounded, each to the extent of one-sixth of the nominal height of the thread, and the actual height of the thread is about 63 per cent. of the pitch. For screws with square threads, the number of threads per inch is one half of the number for triangular threads.

The dimensions of bolts and nuts for triangular threads are given in Table 143.

In the Sellers or Franklin Institute (U.S.A.) system of screw threads, the angle of the triangular thread is 60 degrees. The top of the thread is flattened, and there is a flat interspace at the base of the thread. The head and nuts are hexagonal. The thicknesses of heads and nuts are equal to 1 diameter minus  $\frac{1}{16}$ th inch. The breadth across the flats is equal to  $1\frac{1}{2}$  diameters plus  $\frac{1}{16}$  inch.

Dimensions are given in Table 144.



TABLE 143.—WHITWORTH STANDARD SCREW BOLTS AND NUTS.

*Threads triangular in section; Heads and Nuts hexagonal.*

Screw.			Head and Nut, Hexagonal.		
Diameter of Bolt and Screw.	Diameter at Bottom of Thread.	Threads per Inch.	Thickness of Head.	Thickness of Nut.	Breadth across the Flats.
Inches.	Inches.	Threads.	Inches.	Inches.	Inches.
$\frac{1}{16}$	...	60	...	...	...
$\frac{3}{32}$	...	48	...	...	...
$\frac{1}{8}$	·093	40	·109	$\frac{1}{8}$	·338
$\frac{5}{32}$	...	32	...	...	...
$\frac{3}{16}$	·134	24	·164	$\frac{3}{16}$	·448
$\frac{7}{32}$	...	24	...	...	...
$\frac{1}{4}$	·186	20	·219	$\frac{1}{4}$	·525
$\frac{5}{16}$	·241	18	·273	$\frac{5}{16}$	·601
$\frac{3}{8}$	·295	16	·328	$\frac{3}{8}$	·709
$\frac{7}{16}$	·346	14	·383	$\frac{7}{16}$	·820
$\frac{1}{2}$	·393	12	·437	$\frac{1}{2}$	·919
$\frac{9}{16}$	·456	12	·492	$\frac{9}{16}$	1·011
$\frac{5}{8}$	·508	11	·547	$\frac{5}{8}$	1·101
$\frac{11}{16}$	·571	11	·601	$\frac{11}{16}$	1·201
$\frac{3}{4}$	·622	10	·656	$\frac{3}{4}$	1·301
$\frac{13}{16}$	·684	10	·711	$\frac{13}{16}$	1·39
$\frac{7}{8}$	·733	9	·766	$\frac{7}{8}$	1·479
$\frac{15}{16}$	·795	9	·820	$\frac{15}{16}$	1·574
1	·840	8	·875	1	1·670
$1\frac{1}{8}$	·942	7	·984	$1\frac{1}{8}$	1·860
$1\frac{1}{4}$	1·067	7	1·094	$1\frac{1}{4}$	2·048
$1\frac{3}{8}$	1·161	6	1·203	$1\frac{3}{8}$	2·215
$1\frac{1}{2}$	1·286	6	1·312	$1\frac{1}{2}$	2·413
$1\frac{5}{8}$	1·369	5	1·422	$1\frac{5}{8}$	2·576
$1\frac{3}{4}$	1·494	5	1·531	$1\frac{3}{4}$	2·758
$1\frac{7}{8}$	1·590	$4\frac{1}{2}$	1·641	$1\frac{7}{8}$	3·018
2	1·715	$4\frac{1}{2}$	1·75	2	3·149
$2\frac{1}{8}$	1·840	$4\frac{1}{2}$	1·859	$2\frac{1}{8}$	3·337
$2\frac{1}{4}$	1·930	4	1·969	$2\frac{1}{4}$	3·546
$2\frac{3}{8}$	2·055	4	2·078	$2\frac{3}{8}$	3·75
$2\frac{1}{2}$	2·180	4	2·187	$2\frac{1}{2}$	3·894
$2\frac{5}{8}$	2·305	4	2·297	$2\frac{5}{8}$	4·049
$2\frac{3}{4}$	2·384	$3\frac{1}{2}$	2·406	$2\frac{3}{4}$	4·181
$2\frac{7}{8}$	2·509	$3\frac{1}{2}$	2·516	$2\frac{7}{8}$	4·346
3	2·634	$3\frac{1}{2}$	2·625	3	4·531
$3\frac{1}{4}$	...	$3\frac{1}{4}$	...	...	...
$3\frac{1}{2}$	...	$3\frac{1}{4}$	...	...	...
$3\frac{3}{4}$	...	3	...	...	...

TABLE 143.—WHITWORTH SCREW BOLTS, ETC. (*continued*).

Screw.			Head and Nut, Hexagonal.		
Diameter of Bolt and Screw.	Diameter at Bottom of Thread.	Threads per Inch.	Thickness of Head.	Thickness of Nut.	Breadth across the Flats.
Inches.	Inches.	Threads.	Inches.	Inches.	Inches.
4	...	3	...	...	...
4 $\frac{1}{4}$	...	2 $\frac{7}{8}$	...	...	...
4 $\frac{1}{2}$	...	2 $\frac{7}{8}$	...	...	...
4 $\frac{3}{4}$	...	2 $\frac{3}{4}$	...	...	...
5	...	2 $\frac{3}{4}$	...	...	...
5 $\frac{1}{4}$	...	2 $\frac{5}{8}$	...	...	...
5 $\frac{1}{2}$	...	2 $\frac{5}{8}$	...	...	...
5 $\frac{3}{4}$	...	2 $\frac{1}{2}$	...	...	...
6	...	2 $\frac{1}{2}$	...	...	...

TABLE 144.—SELLERS OR FRANKLIN INSTITUTE STANDARD SCREW BOLTS AND NUTS.

*Threads triangular in section; heads and nuts hexagonal.*

Dia- meter of Bolt and Screw.	Dia- meter at Bottom of Thread.	Width of Flat Sum- mits and Base of Thread.	Threads per Inch.	Dia- meter of Bolt and Screw.	Dia- meter at Bottom of Thread.	Width of Flat Sum- mits and Base of Thread.	Threads per Inch.
Inches.	Inches.	Inch.	Thre'ds.	Inches.	Inches.	Inch.	Thre'ds.
$\frac{1}{4}$	·185	·0062	20	2	1·712	·0277	4 $\frac{1}{2}$
$\frac{5}{16}$	·240	·0074	18	2 $\frac{1}{4}$	1·962	·0277	4 $\frac{1}{2}$
$\frac{3}{8}$	·294	·0078	16	2 $\frac{1}{2}$	2·176	·0312	4
$\frac{7}{16}$	·344	·0089	14	2 $\frac{3}{4}$	2·426	·0312	4
$\frac{1}{2}$	·400	·0096	13	3	2·629	·0357	3 $\frac{1}{2}$
$\frac{9}{16}$	·454	·0104	12	3 $\frac{1}{4}$	2·879	·0357	3 $\frac{1}{2}$
$\frac{5}{8}$	·507	·0113	11	3 $\frac{1}{2}$	3·100	·0384	3 $\frac{1}{4}$
$\frac{3}{4}$	·620	·0125	10	3 $\frac{3}{4}$	3·317	·0413	3
$\frac{7}{8}$	·731	·0138	9	4	3·567	·0413	3
1	·837	·0156	8	4 $\frac{1}{4}$	3·798	·0435	2 $\frac{7}{8}$
1 $\frac{1}{8}$	·940	·0178	7	4 $\frac{1}{2}$	4·028	·0454	2 $\frac{3}{4}$
1 $\frac{1}{4}$	1·065	·0178	7	4 $\frac{3}{4}$	4·256	·0476	2 $\frac{5}{8}$
1 $\frac{3}{8}$	1·160	·0208	6	5	4·480	·0500	2 $\frac{1}{2}$
1 $\frac{1}{2}$	1·284	·0208	6	5 $\frac{1}{4}$	4·730	·0500	2 $\frac{1}{2}$
1 $\frac{5}{8}$	1·389	·0227	5 $\frac{1}{2}$	5 $\frac{1}{2}$	4·953	·0526	2 $\frac{3}{8}$
1 $\frac{3}{4}$	1·491	·0250	5	5 $\frac{3}{4}$	5·203	·0526	2 $\frac{3}{8}$
1 $\frac{7}{8}$	1·616	·0250	5	6	5·423	·0555	2 $\frac{1}{4}$

*Note 1.*—The breadth of heads and nuts, across the flats, is equal to  $1\frac{1}{2}$  diameters +  $\frac{1}{16}$  inch.

*Note 2.*—The thicknesses of the head and the nut are equal diameter -  $\frac{1}{16}$  inch.

TABLE 145.—WHITWORTH'S STANDARD PITCHES OF  
THREAD FOR SCREWED IRON PIPING.

Diameter.	Threads per Inch.	Diameter.	Threads per Inch.	Diameter.	Threads per Inch.
Inches.	Threads.	Inches.	Threads.	Inches.	Threads.
$\frac{1}{8}$	28	$\frac{5}{8}$	14	$1\frac{1}{2}$	11
$\frac{1}{4}$	19	$\frac{3}{4}$	14	$1\frac{3}{4}$	11
$\frac{3}{8}$	19	1	11	2	11
$\frac{1}{2}$	14	$1\frac{1}{4}$	11	above 2	11

TABLE 146.—FRENCH STANDARD BOLTS AND NUTS WITH  
HEXAGONAL HEADS AND NUTS.

(Armengaud).

## 1. TRIANGULAR THREAD (Equilateral Triangle).

Screw.				Head and Nut.			Work- ing Tensile Stress.
Diameter of Bolt and Screw.		Dia- meter at Bottom of Thread.	Number of Threads per Inch.	Thick- ness of Head.	Thick- ness of Nut.	Breadth across the Flats.	
Millimetres.	Inches.	Inches.	Threads.	Inches.	Inches.	Inches.	Lbs.
5	.20	.13	18.1	.24	.20	.55	44
7.5	.30	.22	16	.30	.30	.68	99
10	.39	.31	14.1	.38	.39	.88	178
12.5	.49	.39	12.7	.44	.49	1.04	277
15	.59	.48	11.5	.52	.59	1.20	400
17.5	.69	.58	10.6	.58	.69	1.40	545
20	.79	.66	9.8	.66	.79	1.50	713
22.5	.89	.76	9.1	.72	.89	1.68	902
							Tons.
25	.98	.84	8.5	.80	.98	1.84	.50
30	1.18	1.02	7.5	.94	1.18	2.16	.73
35	1.38	1.20	6.7	1.08	1.38	2.48	.99
40	1.58	1.40	6.0	1.22	1.58	2.80	1.30
45	1.77	1.56	5.5	1.36	1.77	3.20	1.64
50	1.97	1.74	5.1	1.50	1.97	3.44	2.03
55	2.17	1.92	4.7	1.64	2.17	3.76	2.45
60	2.36	2.08	4.4	1.74	2.36	4.08	2.92
65	2.56	2.26	4.1	1.92	2.56	4.40	3.42
70	2.76	2.44	3.8	2.06	2.76	4.70	3.97
75	2.95	2.60	3.5	2.20	2.95	5.00	4.56
80	3.15	2.78	3.4	2.34	3.15	5.35	5.12

TABLE 146.—FRENCH STANDARD BOLTS AND NUTS (*cont.*).

## 2. SQUARE THREAD.

Screw.				Head and Nut.			Working Tensile Stress.
Diameter of Bolt and Screw.		Depth of Thread.	Number of Threads per Inch.	Thick- ness of Head.	Thick- ness of Nut.	Breadth across the Flats.	
Millimetres.	Inches.	Inches.	Threads.	Inches.	Inches.	Inches.	Tons.
20	·79	·072	6·57	...	1·82	...	·32
25	·98	·081	5·97	...	2·01	...	·51
30	1·18	·093	5·40	...	2·22	...	·73
35	1·38	·10	4·93	...	2·41	...	·99
40	1·57	·106	4·53	...	2·63	...	1·30
45	1·77	·114	4·20	...	2·85	...	1·64
50	1·97	·128	3·91	...	3·07	...	2·03
55	2·17	·13	3·65	...	3·30	...	2·45
60	2·36	·14	3·43	...	3·50	...	2·92
65	2·56	·15	3·23	...	3·70	...	3·42
70	2·76	·158	3·06	...	3·92	...	3·97
75	2·95	·166	2·92	...	4·13	...	4·56
80	3·15	·174	2·76	...	4·36	...	5·18
85	3·35	·183	2·63	...	4·58	...	5·85
90	3·54	·192	2·51	...	4·78	...	6·56
95	3·74	·200	2·41	...	5·00	...	7·30
100	3·94	·209	2·31	...	5·22	...	8·10
105	4·13	·220	2·22	...	5·43	...	8·93
110	4·33	·226	2·13	...	5·66	...	9·80
115	4·53	·230	2·06	...	5·87	...	10·71
120	4·72	·234	2·00	...	6·08	...	11·66

TABLE 147.—IRON WASHERS.

Diameters.		Thick- ness.	Number per Pound.	Diameters.		Thick- ness.	Number per Pound.
Washer.	Bolt Hole.			Washer.	Bolt Hole.		
Inches.	Inches.	B. W. G.	Washers.	Inches.	Inches.	B. W. G.	Washers.
$\frac{1}{2}$	$\frac{1}{4}$	18	543	$1\frac{3}{4}$	$\frac{11}{16}$	10	17·0
$\frac{5}{8}$	$\frac{5}{16}$	16	228	2	$\frac{13}{16}$	10	10·7
$\frac{3}{4}$	$\frac{5}{16}$	16	147	$2\frac{1}{4}$	$\frac{15}{16}$	9	8·7
$\frac{7}{8}$	$\frac{3}{8}$	16	123	$2\frac{1}{2}$	$1\frac{1}{16}$	9	6·3
1	$\frac{7}{16}$	14	70·0	$2\frac{3}{4}$	$1\frac{1}{4}$	9	4·7
$1\frac{1}{4}$	$\frac{1}{2}$	14	50·0	3	$1\frac{3}{8}$	9	3·7
$1\frac{3}{8}$	$\frac{9}{16}$	12	30·0	$3\frac{1}{2}$	$1\frac{1}{2}$	9	3·0
$1\frac{1}{2}$	$\frac{5}{8}$	12	25·7				

TABLE 148.—WEIGHTS OF 100 HEXAGONAL HEAD BOLTS AND NUTS.

Length under Head.	Diameter of Bolts.						
	$\frac{1}{4}$ in.	$\frac{3}{8}$ in.	$\frac{1}{2}$ in.	$\frac{5}{8}$ in.	$\frac{3}{4}$ in.	$\frac{7}{8}$ in.	1 in.
Inches.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
1	$3\frac{1}{4}$	$7\frac{3}{4}$	$16\frac{3}{8}$	$26\frac{3}{4}$	...	...	...
$1\frac{1}{4}$	$3\frac{1}{2}$	$8\frac{5}{8}$	$17\frac{3}{8}$	$29\frac{1}{4}$	...	...	...
$1\frac{1}{2}$	$3\frac{7}{8}$	$9\frac{1}{2}$	$18\frac{3}{8}$	$31\frac{3}{8}$	...	...	...
$1\frac{3}{4}$	$4\frac{1}{4}$	$10\frac{3}{8}$	$19\frac{3}{8}$	$34\frac{1}{4}$	...	...	...
2	$4\frac{5}{8}$	$11\frac{1}{4}$	$20\frac{3}{8}$	$36\frac{3}{4}$	58	115	159
$2\frac{1}{4}$	5	$12\frac{1}{4}$	$21\frac{7}{8}$	$39\frac{1}{4}$	$61\frac{1}{2}$	$117\frac{1}{2}$	164
$2\frac{1}{2}$	$5\frac{3}{8}$	$13\frac{1}{8}$	$23\frac{3}{8}$	$41\frac{3}{4}$	65	120	169
$2\frac{3}{4}$	$5\frac{3}{4}$	14	$24\frac{7}{8}$	$44\frac{1}{4}$	$68\frac{1}{2}$	$122\frac{1}{2}$	174
3	$6\frac{1}{8}$	15	$26\frac{3}{8}$	$46\frac{3}{4}$	72	125	179
$3\frac{1}{2}$	$6\frac{3}{4}$	$16\frac{7}{8}$	$29\frac{3}{8}$	$51\frac{1}{4}$	78	133	189
4	$7\frac{3}{8}$	$18\frac{7}{8}$	$32\frac{3}{8}$	$55\frac{3}{4}$	84	141	199
$4\frac{1}{2}$	8	$20\frac{3}{8}$	$35\frac{3}{8}$	$60\frac{1}{4}$	$89\frac{1}{2}$	149	209
5	$8\frac{5}{8}$	22	$38\frac{3}{8}$	$64\frac{3}{4}$	95	157	219
$5\frac{1}{2}$	$9\frac{3}{8}$	$23\frac{5}{8}$	$41\frac{3}{8}$	$68\frac{3}{4}$	$100\frac{1}{2}$	165	230
6	10	$25\frac{1}{4}$	$44\frac{3}{8}$	$72\frac{3}{4}$	106	173	241
7	$11\frac{3}{8}$	$28\frac{1}{4}$	$50\frac{3}{8}$	$80\frac{3}{4}$	118	189	263
8	$12\frac{3}{4}$	$31\frac{3}{4}$	$56\frac{3}{8}$	$88\frac{3}{4}$	131	205	285
9	$14\frac{1}{8}$	$34\frac{3}{4}$	$62\frac{3}{8}$	$96\frac{3}{4}$	144	221	307
10	$15\frac{5}{8}$	$38\frac{3}{4}$	$68\frac{3}{8}$	$104\frac{3}{4}$	158	237	329
11	$16\frac{7}{8}$	$41\frac{3}{8}$	$74\frac{3}{8}$	$112\frac{7}{8}$	173	253	351
12	$18\frac{1}{4}$	$44\frac{3}{4}$	$80\frac{3}{8}$	$121\frac{1}{2}$	188	269	372

TABLE 149.—WEIGHTS OF 100 SQUARE-HEAD BOLTS AND NUTS.

Length under Head.	Diameter of Bolts.						
	$\frac{1}{4}$ in.	$\frac{3}{8}$ in.	$\frac{1}{2}$ in.	$\frac{5}{8}$ in.	$\frac{3}{4}$ in.	$\frac{7}{8}$ in.	1 in.
Inches.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
1	$3\frac{1}{2}$	9	20	32	...	...	...
$1\frac{1}{4}$	$3\frac{7}{8}$	$9\frac{7}{8}$	21	$34\frac{1}{2}$	...	...	...
$1\frac{1}{2}$	$4\frac{1}{4}$	$10\frac{3}{4}$	22	37	...	...	...
$1\frac{3}{4}$	$4\frac{5}{8}$	$11\frac{5}{8}$	23	$39\frac{1}{2}$	...	...	...
2	5	$12\frac{1}{2}$	24	42	70	130	180
$2\frac{1}{4}$	$5\frac{3}{8}$	$13\frac{1}{2}$	$25\frac{1}{2}$	$44\frac{1}{2}$	$73\frac{1}{2}$	$132\frac{1}{2}$	185
$2\frac{1}{2}$	$5\frac{3}{4}$	$14\frac{3}{8}$	27	47	77	135	190

TABLE 149.—WEIGHT OF 100 SQUARE-HEAD BOLTS AND NUTS (*continued*).

Length under Head.	Diameter of Bolts.						
	$\frac{1}{4}$ in.	$\frac{3}{8}$ in.	$\frac{1}{2}$ in.	$\frac{5}{8}$ in.	$\frac{3}{4}$ in.	$\frac{7}{8}$ in.	1 in.
Inches.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
$2\frac{3}{4}$	$6\frac{1}{8}$	$15\frac{1}{2}$	$28\frac{1}{2}$	$49\frac{1}{2}$	$80\frac{1}{2}$	$137\frac{1}{2}$	195
3	$6\frac{1}{2}$	$16\frac{1}{4}$	30	52	84	140	200
$3\frac{1}{2}$	$7\frac{1}{8}$	$18\frac{1}{8}$	33	$56\frac{1}{2}$	90	148	210
4	$7\frac{3}{4}$	20	36	61	96	156	220
$4\frac{1}{2}$	$8\frac{3}{8}$	$21\frac{5}{8}$	39	$65\frac{1}{2}$	$101\frac{1}{2}$	164	230
5	9	$23\frac{1}{4}$	42	70	107	172	240
$5\frac{1}{2}$	$9\frac{3}{4}$	$24\frac{7}{8}$	45	74	$112\frac{1}{2}$	180	251
6	$10\frac{3}{8}$	$26\frac{1}{2}$	48	78	118	188	262
7	$11\frac{3}{4}$	$29\frac{1}{2}$	54	86	130	204	284
8	$13\frac{1}{8}$	33	60	94	143	220	306
9	$14\frac{1}{2}$	36	66	102	156	236	328
10	16	40	72	110	170	252	350
11	$17\frac{1}{4}$	43	78	118	185	268	372
12	$18\frac{5}{8}$	46	84	127	200	284	393

TABLE 150.—WEIGHT AND TENSILE STRENGTH OF ORDINARY IRON BOLTS.

(Chapman.)

Ends Enlarged, or Upset.				Ends not Enlarged.	
Diameter of Shank.	Weight per Lineal Foot.	Breaking Stress.	Breaking Stress.	Diameter of Shank.	Weight per Lineal Foot.
Inches.	Pounds.	Tons.	Pounds.	Inches.	Pounds.
$\frac{1}{8}$	·0414	·245	549	...	...
$\frac{3}{16}$	·093	·553	1,239	...	...
$\frac{1}{4}$	·165	·983	2,202	·35	·321
$\frac{5}{16}$	·258	1·53	3,427	·43	·452
$\frac{3}{8}$	·372	2·21	4,950	·50	·654
$\frac{7}{16}$	·506	3·00	6,720	·58	·897
$\frac{1}{2}$	·661	3·93	8,803	·66	1·14
$\frac{9}{16}$	·837	4·97	11,133	·73	1·41
$\frac{5}{8}$	1·03	6·14	13,754	·80	1·67
$\frac{11}{16}$	1·25	7·42	16,621	·88	2·03
$\frac{3}{4}$	1·49	8·83	19,779	·96	2·41
$\frac{13}{16}$	1·75	10·4	23,296	1·04	2·81

TABLE 150.—WEIGHT AND STRENGTH OF IRON BOLTS (*con.*).

Ends Enlarged, or Upset.				Ends not Enlarged.	
Diameter of Shank.	Weight per Lineal Foot.	Breaking Stress.	Breaking Stress.	Diameter of Shank.	Weight per Lineal Foot.
Inches.	Pounds.	Tons.	Pounds.	Inches.	Pounds.
$\frac{7}{8}$	2.03	12.0	26,880	1.12	3.26
$\frac{15}{16}$	2.33	13.8	30,012	1.20	3.77
1	2.65	15.7	35,168	1.27	4.27
$1\frac{1}{16}$	2.99	16.8	37,632	1.35	4.77
$1\frac{1}{8}$	3.35	18.9	42,336	1.42	5.28
$1\frac{3}{16}$	3.73	21.1	47,264	1.49	5.81
$1\frac{1}{4}$	4.13	23.3	52,192	1.55	6.39
$1\frac{5}{16}$	4.56	25.7	57,568	1.64	7.04
$1\frac{3}{8}$	5.00	28.2	63,168	1.72	7.74
$1\frac{7}{16}$	5.47	30.8	68,992	1.80	8.48
$1\frac{1}{2}$	5.95	33.6	75,264	1.87	9.20
$1\frac{9}{16}$	6.46	36.4	81,536	1.94	9.88
$1\frac{5}{8}$	6.99	39.4	88,256	2.00	10.6
$1\frac{11}{16}$	7.53	42.5	95,200	2.07	11.3
$1\frac{3}{4}$	8.10	45.7	102,368	2.14	12.0
$1\frac{13}{16}$	8.69	49.0	109,760	2.22	12.9
$1\frac{7}{8}$	9.30	52.5	117,600	2.30	13.8
$1\frac{15}{16}$	9.93	56.0	125,440	2.38	14.7
2	10.6	59.7	133,728	2.45	15.7
$2\frac{1}{8}$	12.0	63.8	142,912	2.59	17.5
$2\frac{1}{4}$	13.4	71.6	160,384	2.73	19.5
$2\frac{3}{8}$	14.9	79.7	178,528	2.88	21.6
$2\frac{1}{2}$	16.5	88.4	198,016	3.02	23.9
$2\frac{5}{8}$	18.2	97.4	218,176	3.16	26.1
$2\frac{3}{4}$	20.0	106.9	239,456	3.30	28.5
$2\frac{7}{8}$	21.9	116.8	261,632	3.45	31.1
3	23.8	127.2	284,928	3.60	33.9
$3\frac{1}{4}$	27.9	141.0	315,840	3.86	39.1
$3\frac{1}{2}$	32.4	163.6	366,464	4.12	44.4
$3\frac{3}{4}$	37.2	187.7	420,448	4.41	51.0
4	42.3	213.6	478,464	4.70	57.8
$4\frac{1}{4}$	47.8	227.0	508,480	4.98	65.2
$4\frac{1}{2}$	53.6	254.5	570,080	5.25	72.9
$4\frac{3}{4}$	59.7	283.5	635,040	5.53	80.5
5	66.1	314.2	703,808	5.80	88.1
$5\frac{1}{4}$	72.9	324.7	727,328	6.08	97.0
$5\frac{1}{2}$	80.0	356.4	798,336	6.36	106
$5\frac{3}{4}$	87.5	389.5	872,480	6.63	116
6	95.2	424.1	949,984	6.90	126

TABLE 151.—NAILS, IRON OR STEEL : SIZES AND WEIGHTS.

Description.	Length.	Weight per 1,000.		Description.	Length.	Weight per 1,000.	
		Lb.	Oz.			Lb.	Oz.
Spike, die heads, {	1½	4	0	Clasp, fine, wrought	1¾	11	0
flat points, {	2	7	4	"	4	...	
wrought . . {	2½	12	8	Clasp, fine, cut .	2	6	0
"	3	19	12	"	2½	10	0
"	3½	27	4	"	3	16	0
"	4	42	8	Clasp, strong .	1¾	7	0
"	5	89	8	"	2¼	10	0
"	6	153	12	"	2½	12	0
"	7	241	0	"	2¾	14	0
Spike, square {	6	263	0	"	3	20	0
head, flat {	7	361	12	"	3½	25	0
points, wrought {	8	478	12	"	3¾	32	0
"	9	596	0	"	4	40	0
"	10	707	8	Clout, counter-	1	4	12
"	12	998	0	sunk, fine, {	1½	9	0
Rose, sharp {	1	2	9	wrought . . {	2	19	0
points, wrought {	1¼	5	0	"	3	44	0
Rose, fine flat {	1½	4	0	Clout, counter-	1½	14	8
points, wrought {	2	7	12	sunk, strong, {	2	25	8
"	2½	18	8	wrought . . {	2½	43	8
Rose, fine flat {	3	28	12	Clout, " strong, {	3½	82	0
points, strong . {	3½	40	0	wrought . . {	4	2	0
"	4	54	4	"	1¼	3	0
"	4½	74	8	"	1½	5	0
"	5	92	8	"	1¾	7	0
Rose, fine flat {	1¼	4	0	"	2	13	0
points, stamped {	1½	5	0	Brads, fine, billed, {	½	0	4
"	2	7	0	wrought . . {	¾	0	10
"	2½	11	0	"	1	1	0
"	3	25	0	"	1¼	1	8
Clasp, bastard, {	2	7	0	"	1½	2	8
wrought . . {	2½	12	0	"	1¾	3	0
Clasp, fine, wrought	1	1	8	"	2	4	0
"	1¼	2	0	Brads, fine, billed, {	½	0	3¾
"	1½	3	0	cut . . . {	¾	0	7¾
"	1¾	4	0	"	1	1	0
"	2	5	0	"	1¼	1	8
"	2½	7	0	"	1½	2	0
"				"	2	3	4



TABLE 151.—NAILS, IRON OR STEEL : SIZES AND WEIGHTS (*continued*).

Description.	Length.	Weight per 1,000.	Description.	Length.	Weight per 1,000.
	In.	Lb. Oz.		In.	Lb. Oz.
Brads, flooring, cut	2½	10 0	Dog, counter-	2	21 4
"	2½	15 0	sunk, wrought	2½	27 12
"	3¼	20 0	"	3	39 8
Brads, moulder's, {	3½	10 8	Tenter hooks . .	1½	6 0
fine, cut . . . }	4	12 13	Mop, caulker's, {	4½	62 0
"	4½	15 4	wrought . . . }	7	125 0
"	5	17 10	Slating, wrought, {	2	...
Tacks, flat head, {	¾	0 5	galvanised . . }		
wrought . . . }	½	0 8	Scupper, wrought .	¾	4 0
"	¾	0 14	"	1	6 4
Tacks, round {	¾	1 4	Roofing " rivets, {	1¼	10 4
head, wrought }			wrought with {	½	...
Tacks, tinned, flat {	¾	0 5½	burrs, galvan-	¾	...
head, wrought . }	½	0 9	ised, ¼ in. diam. }		
"	¾	0 15½	Glaziers' sprigs . .	½	0 4
Tacks, moulding, {	2½	19 12	"	¾	0 14
wrought . . . }	3	32 4	Horse shoe . . .	2	5 8
"	4	54 0	" . . .	2½	7 0
Tacks, flat head, {	¾	0 5½	" . . .	2¼	8 8
cut . . . . }	½	0 8½	" . . .	2¾	10 0
"	¾	0 12	" . . .	2½	11 0
Cooper's flat, {	¾	1 8	" . . .	2¼	13 8
wrought . . . }	1	2 4	Cart wheel tyre .	3½	187 8
"	1¼	3 4	"	4	218 12

TABLE 152.—GALVANISED WROUGHT IRON CYLINDRICAL CISTERNs.  
(Gospel Oak Company.)

Capacity (about)	Diameter.	Height.	Capacity (about)	Diameter.	Height.
Gallons.	Inches.	Inches.	Gallons.	Inches.	Inches.
5	11	17½	40	21	33
10	14	21	50	23	35
15	16	22	60	25	36
20	18	24	80	27	42
30	19½	30	100	28	48

TABLE 153.—GALVANISED WROUGHT IRON RECTANGULAR  
CISTERNS AND TANKS.  
(Gospel Oak Company.)

Open Rectangular Cisterns.				Closed Hot Water Tanks.			
Capacity (about)	Length.	Width.	Depth.	Capacity (about)	Length.	Width.	Depth.
Gallons.	Ft. In.	Ft. In.	Ft. In.	Gallons.	Ft. In.	Ft. In.	Ft. In.
25	2 0	1 5	1 5	20	1 8	1 3	1 6
30	2 0	1 6	1 7	25	2 0	1 5	1 5
40	2 3	1 8	1 8	30	2 0	1 6	1 7
50	2 5	1 10	1 10	40	2 3	1 8	1 8
60	2 6	1 11	2 0	50	2 5	1 10	1 10
70	2 8	2 2	2 0	60	2 6	1 11	2 0
80	2 10	2 3	2 0	80	2 10	2 3	2 0
100	3 2	2 3	2 3	100	3 2	2 3	2 3
125	3 4	2 7	2 4	<p><i>Note 1.</i>—The cisterns are constructed of three thicknesses—light; medium, <math>\frac{1}{8}</math> inch bare; <math>\frac{1}{8}</math> inch full.</p> <p><i>Note 2.</i>—The tanks are constructed of four thicknesses—light, strong, <math>\frac{1}{8}</math> inch bare, <math>\frac{1}{8}</math> inch full.</p>			
150	3 6	2 7	2 8				
200	3 10	2 11	2 11				
250	4 2	3 3	3 0				
300	4 6	3 7	3 0				
400	5 10	3 9	3 0				
500	6 6	4 1	3 0				
600	7 6	4 1	3 2				
700	8 3	4 1	3 4				
800	8 3	4 5	3 6				
900	8 3	4 11	3 8				
1000	8 3	4 11	4 0				

TABLE 154.—CAST-IRON CYLINDERS :—WEIGHT, BY INTERNAL DIAMETER.  
Length, 1 Foot.

Inside Diam.	Thickness in Inches.							
	$\frac{3}{8}$	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	$1\frac{1}{8}$	$1\frac{1}{4}$
Ins.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
1	5.06	7.36	9.97	12.9	16.1	19.6	...	...
$1\frac{1}{4}$	6.90	9.82	13.1	16.6	20.4	24.5	...	...
2	8.74	12.3	16.1	20.3	24.7	29.5	...	...
$2\frac{1}{2}$	10.6	14.7	19.2	23.9	29.0	34.4	...	...
3	12.4	17.2	22.2	27.6	33.3	39.3	...	...
$3\frac{1}{2}$	14.3	19.6	25.3	31.3	37.6	44.2	...	...
4	16.1	22.1	28.4	35.0	41.9	49.1	...	...
$4\frac{1}{2}$	18.0	24.5	31.5	38.7	46.2	54.0	...	...
5	19.8	27.0	34.5	42.3	50.5	58.9	...	...
$5\frac{1}{2}$	21.6	29.5	37.6	46.0	54.8	63.8	...	...

TABLE 154.—CAST-IRON CYLINDERS (*continued*).

Inside Diam.	Thickness in Inches							
	$\frac{3}{8}$	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	$1\frac{1}{8}$	$1\frac{1}{4}$
Ins.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
6	23.5	32.0	40.7	49.7	59.1	68.7	78.7	89.0
6 $\frac{1}{2}$	25.3	34.4	43.7	53.4	63.4	73.6	84.2	95.1
7	27.2	36.8	46.8	57.1	67.7	78.5	89.7	101.2
7 $\frac{1}{2}$	29.0	39.3	49.9	60.8	71.9	83.5	95.3	107.4
8	30.8	41.7	52.9	64.4	76.2	88.4	100.8	113.5
9	34.5	46.6	59.0	71.8	84.8	98.2	111.8	125.8
10	38.2	51.5	65.1	79.2	93.4	108.0	122.9	138.1
11	41.9	56.5	71.2	86.5	102.0	117.8	133.9	150.3
12	45.6	61.4	77.5	93.9	110.6	127.6	145.0	162.6
13	49.2	66.3	83.6	101.2	119.2	137.5	156.0	174.9
14	52.9	71.2	89.7	108.6	127.8	147.3	167.1	187.2
15	56.6	76.1	95.9	116.0	136.4	157.1	178.1	199.4
16	60.3	81.0	102.0	123.3	145.0	166.9	189.1	211.7
17	64.0	85.9	108.2	130.7	153.6	176.7	200.2	224.0
18	67.7	90.8	114.3	138.1	162.2	186.5	211.2	236.2

Inside Diam.	Thickness in Inches.											
	$\frac{3}{8}$	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	$1\frac{1}{8}$	$1\frac{1}{4}$	$1\frac{1}{2}$	$1\frac{3}{4}$	2	
Inch.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	
18	604	811	102	123	145	167	189	211	256	286	329	
19	637	855	108	130	152	175	199	222	270	302	347	
20	670	898	113	136	160	184	208	233	283	318	365	
21	703	942	119	143	168	193	218	244	296	334	384	
22	736	986	124	149	176	202	228	255	309	350	402	
23	769	103	129	156	183	210	238	266	322	366	420	
24	802	107	135	163	191	219	248	277	335	382	439	
25	835	112	140	169	199	228	258	288	348	397	457	
26	868	116	146	176	206	237	268	299	362	413	475	
27	901	121	151	182	214	245	277	309	375	429	493	
28	934	125	157	189	222	254	287	320	388	445	511	
29	967	129	162	196	229	263	297	331	401	462	530	
30	998	134	168	202	237	272	307	342	414	477	548	
32	106	143	179	215	252	289	327	364	441	509	584	
34	113	151	190	229	267	307	346	386	467	541	621	
36	120	160	201	242	283	324	366	408	494	572	658	
38	126	169	212	255	298	342	386	430	520	604	694	
40	133	177	223	268	314	359	405	452	547	636	731	
42	139	186	234	281	329	377	425	474	573	668	767	
45	149	199	250	301	352	403	455	507	613	715	825	
48	159	212	266	321	375	430	485	540	652	763	877	

TABLE 154.—CAST IRON CYLINDERS (*continued*).

Inside Diam.	Thickness in Inches.										
	$\frac{3}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	$1\frac{1}{8}$	$1\frac{1}{4}$	$1\frac{3}{8}$	$1\frac{1}{2}$	$1\frac{3}{4}$	2	$2\frac{1}{4}$
Inch.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.
48	2·66	3·21	3·75	4·30	4·85	5·40	5·96	6·52	7·63	8·77	9·91
51	2·82	3·40	3·98	4·56	5·14	5·73	6·32	6·91	8·09	9·29	10·5
54	2·99	3·60	4·21	4·82	5·44	6·06	6·69	7·31	8·55	9·82	11·1
57	3·15	3·80	4·44	5·09	5·73	6·38	7·05	7·70	9·01	10·4	11·7
60	3·32	4·00	4·67	5·35	6·03	6·71	7·41	8·10	9·47	10·9	12·3
63	3·48	4·19	4·90	5·61	6·33	7·04	7·78	8·49	9·93	11·4	12·9
66	3·64	4·39	5·13	5·88	6·62	7·37	8·14	8·89	10·4	11·9	13·5
69	3·81	4·59	5·36	6·14	6·92	7·70	8·51	9·28	10·9	12·5	14·1
72	3·97	4·78	5·59	6·40	7·21	8·03	8·87	9·67	11·3	13·0	14·7
75	4·14	4·98	5·82	6·66	7·51	8·36	9·24	10·1	11·8	13·5	15·2
78	4·30	5·18	6·05	6·93	7·81	8·69	9·60	10·5	12·2	14·0	15·8
81	4·46	5·38	6·28	7·19	8·10	9·02	9·97	10·9	12·7	14·6	16·4
84	4·63	5·57	6·51	7·45	8·40	9·35	10·3	11·3	13·2	15·1	17·0
87	4·79	5·77	6·74	7·72	8·69	9·67	10·7	11·6	13·6	15·6	17·6
90	4·96	5·97	6·97	7·98	8·99	10·0	11·1	12·0	14·1	16·1	18·2
93	5·12	6·17	7·20	8·24	9·29	10·3	11·4	12·4	14·5	16·7	18·8
96	5·28	6·36	7·43	8·51	9·58	10·7	11·8	12·8	15·0	17·2	19·4
99	5·45	6·56	7·66	8·77	9·88	11·0	12·2	13·2	15·5	17·7	20·0
102	5·61	6·76	7·89	9·03	10·2	11·3	12·5	13·6	15·9	18·2	20·6
105	5·78	6·95	8·12	9·29	10·5	11·7	12·9	14·0	16·4	18·8	21·2
108	5·94	7·15	8·36	9·56	10·8	12·0	13·3	14·4	16·8	19·3	21·8
111	6·10	7·35	8·59	9·82	11·1	12·3	13·6	14·8	17·3	19·8	22·3
114	6·27	7·55	8·82	10·1	11·4	12·6	14·0	15·2	17·8	20·3	22·9
117	6·43	7·74	9·05	10·4	11·7	13·0	14·3	15·6	18·2	20·9	23·5
120	6·59	7·94	9·28	10·6	12·0	13·3	14·7	16·0	18·7	21·4	24·1

TABLE 156.—CAST-IRON CYLINDERS : WEIGHT BY EXTERNAL DIAMETER.  
Length, 1 Foot.

External Diameter.	Thickness in Inches.						
	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1
Inches.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
3	9·65	11·0	12·3	14·6	16·6	18·3	19·6
$3\frac{1}{2}$	11·5	13·2	14·7	17·6	20·3	22·6	24·5
4	13·3	15·3	17·2	20·7	24·0	26·9	29·5
$4\frac{1}{2}$	15·2	17·5	19·6	23·8	27·7	31·1	34·4
5	17·0	19·6	22·1	26·9	31·5	35·4	39·3
$5\frac{1}{2}$	18·9	21·8	24·5	29·9	35·2	39·7	44·2
6	20·7	23·9	27·0	33·0	38·9	44·0	49·1
$6\frac{1}{2}$	22·5	26·0	29·5	36·1	42·6	48·3	54·0

TABLE 156.—CAST-IRON CYLINDERS (*continued*).

External Diameter.	Thickness in Inches.						
	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1
Inches.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
7	24.4	28.2	31.9	39.1	46.4	52.6	58.9
7½	26.2	30.3	34.4	42.2	50.1	56.9	63.8
8	28.1	32.5	36.8	45.3	53.8	61.2	68.7
8½	29.9	34.6	39.3	48.3	57.5	65.5	73.6
9	31.8	36.8	41.7	51.4	61.3	69.8	78.5
9½	33.6	38.9	44.2	54.5	65.0	74.1	83.5
10	35.4	41.1	46.6	57.5	68.7	78.4	88.4
11	39.1	45.4	51.5	63.7	76.0	87.0	98.2
12	42.8	49.7	56.5	69.8	83.4	95.6	108.0
13	46.5	54.0	61.4	75.9	90.7	104.2	117.8
14	50.2	58.3	66.3	82.1	98.0	112.8	127.6
15	53.8	62.6	71.2	88.2	105.4	121.3	137.4
16	57.5	66.9	76.1	94.3	112.7	129.9	147.3
17	61.2	71.1	81.0	100.5	120.0	138.5	157.1
18	64.9	75.4	85.9	106.6	127.4	147.1	166.9
19	68.6	79.7	90.8	112.8	134.7	155.7	176.7
20	72.3	84.0	95.7	118.9	142.0	164.3	186.5
21	75.9	88.3	100.6	125.0	149.4	172.9	196.4
22	79.6	92.6	105.5	131.2	156.7	181.5	206.2
23	83.3	96.9	110.5	137.3	164.0	190.1	215.0
24	87.0	101.2	115.4	143.4	171.4	198.7	225.8
25	90.7	105.5	120.3	149.6	178.7	207.2	235.6
26	94.3	109.8	125.2	155.7	186.1	215.8	245.4
27	98.0	114.1	130.1	161.8	193.4	224.4	255.3
28	101.7	118.4	135.0	168.0	200.7	233.0	265.1
29	105.4	122.7	139.9	174.1	208.1	241.6	274.9
30	109.1	127.0	144.8	180.2	215.4	250.2	284.7
31	112.8	131.3	149.7	186.4	222.7	258.8	294.5
32	116.4	135.6	154.6	192.5	230.1	267.4	304.3
33	120.1	139.9	159.5	198.7	237.5	276.0	314.2
34	123.8	144.2	164.5	204.8	244.8	284.6	324.0
35	127.5	148.5	169.4	210.9	252.2	293.1	333.8
36	131.2	152.7	174.3	217.1	259.5	301.7	343.6
38	138.5	161.3	184.1	229.3	274.3	318.9	363.2
40	145.9	169.9	193.9	241.6	289.0	336.1	382.9
42	153.3	178.5	203.7	253.9	303.7	353.3	402.5
45	164.3	191.2	218.5	272.3	325.8	379.1	432.0
48	175.4	203.8	233.2	290.7	347.9	404.8	461.4
51	186.4	216.5	247.9	309.1	370.0	430.6	490.9
54	197.5	229.2	262.6	327.5	392.1	456.4	520.3
57	208.5	241.8	277.4	345.9	414.2	482.1	549.8
60	219.6	254.5	292.1	364.3	436.3	507.9	579.3

TABLE 156.—CAST-IRON CYLINDERS (*continued*).

External Diameter.	Thickness in Inches.						
	$\frac{3}{8}$	$\frac{7}{16}$	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1
Inches.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.
63	2.06	2.39	2.74	3.42	4.09	4.77	5.43
66	2.16	2.50	2.87	3.58	4.29	5.00	5.70
69	2.26	2.62	3.00	3.75	4.49	5.23	5.96
72	2.36	2.74	3.14	3.91	4.69	5.46	6.22
75	2.45	2.85	3.27	4.08	4.88	5.69	6.49
78	2.55	2.97	3.40	4.24	5.08	5.92	6.75
81	2.65	3.09	3.53	4.41	5.28	6.15	7.01
84	2.75	3.20	3.66	4.57	5.47	6.38	7.28
90	2.95	3.43	3.92	4.90	5.87	6.84	7.80
96	3.15	3.67	4.19	5.23	6.26	7.30	8.33

External Diameter.	Thickness in Inches.						
	$1\frac{1}{8}$	$1\frac{1}{4}$	$1\frac{3}{8}$	$1\frac{1}{2}$	$1\frac{3}{4}$	2	$2\frac{1}{4}$
Inches.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.
6	.481	.520	.557	.592	.652	.701	.740
6½	.530	.575	.618	.657	.729	.789	.838
7	.579	.630	.678	.723	.805	.876	.938
7½	.629	.685	.738	.789	.882	.964	1.04
8	.678	.740	.799	.855	.959	1.05	1.14
8½	.727	.794	.859	.921	1.04	1.14	1.23
9	.777	.849	.919	.986	1.11	1.23	1.33
9½	.826	.904	.980	1.05	1.19	1.31	1.43
10	.875	.959	1.04	1.12	1.27	1.40	1.53
11	.974	1.07	1.16	1.25	1.42	1.58	1.73
12	1.07	1.18	1.28	1.38	1.57	1.75	1.92
13	1.17	1.29	1.40	1.51	1.73	1.93	2.12
14	1.27	1.40	1.52	1.64	1.88	2.10	2.32
15	1.37	1.51	1.65	1.78	2.03	2.28	2.52
16	1.47	1.62	1.77	1.91	2.19	2.45	2.71
17	1.57	1.73	1.89	2.04	2.34	2.63	2.91
18	1.66	1.84	2.01	2.17	2.49	2.81	3.11
20	1.86	2.06	2.25	2.43	2.80	3.16	3.50
22	2.06	2.27	2.49	2.70	3.11	3.51	3.90
24	2.26	2.49	2.73	2.96	3.41	3.86	4.29
27	2.55	2.82	3.09	3.35	3.87	4.38	4.88
30	2.85	3.15	3.46	3.75	4.33	4.91	5.47
33	3.14	3.48	3.82	4.14	4.79	5.44	6.06
36	3.44	3.81	4.18	4.54	5.25	5.96	6.66
39	3.74	4.14	4.54	4.93	5.72	6.49	7.25

TABLE 156.—CAST-IRON CYLINDERS (*continued*).

External Diameter.	Thickness in Inches.						
	1 $\frac{1}{8}$	1 $\frac{1}{4}$	1 $\frac{3}{8}$	1 $\frac{1}{2}$	1 $\frac{3}{4}$	2	2 $\frac{1}{4}$
Inches.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.
42	4·03	4·47	4·90	5·33	6·18	7·01	7·84
45	4·33	4·79	5·26	5·72	6·64	7·54	8·43
48	4·62	5·12	5·62	6·12	7·10	8·07	9·02
51	4·92	5·45	5·98	6·51	7·56	8·59	9·61
54	5·22	5·78	6·35	6·91	8·02	9·12	10·2
57	5·51	6·11	6·71	7·30	8·48	9·64	10·8
60	5·81	6·44	7·07	7·70	8·94	10·2	11·4
Ft. In.							
5 3	6·10	6·77	7·43	8·09	9·40	10·7	12·0
5 6	6·40	7·09	7·79	8·48	9·86	11·2	12·6
5 9	6·70	7·42	8·15	8·88	10·3	11·8	13·2
6 0	7·00	7·75	8·51	9·27	10·8	12·3	13·8
6 3	7·29	8·08	8·88	9·67	11·2	12·8	14·4
6 6	7·58	8·41	9·24	10·1	11·7	13·3	14·9
6 9	7·88	8·74	9·60	10·5	12·2	13·9	15·5
7 0	8·17	9·07	9·96	10·9	12·6	14·4	16·1
7 6	8·77	9·72	10·7	11·6	13·5	15·4	17·3
8 0	9·36	10·4	11·4	12·4	14·5	16·5	18·5
8 6	9·95	11·0	12·1	13·2	15·4	17·5	19·7
9 0	10·5	11·7	12·9	14·0	16·3	18·6	20·8
9 6	11·1	12·3	13·6	14·8	17·2	19·6	22·0
10 0	11·7	13·0	14·3	15·6	18·1	20·7	23·2
10 6	12·3	13·7	15·0	16·4	19·1	21·7	24·4
11 0	12·9	14·3	15·7	17·2	20·0	22·8	25·6
11 6	13·5	15·0	16·5	17·9	20·9	23·8	26·7
12 0	14·1	15·6	17·2	18·7	21·8	24·9	27·9
13 0	15·3	16·9	18·6	20·3	23·7	27·0	30·3
14 0	16·5	18·3	20·1	21·9	25·5	29·1	32·7
15 0	17·7	19·6	21·5	23·5	27·3	31·2	35·0
16 0	18·8	20·9	23·0	25·0	29·2	33·3	37·4
17 0	20·0	22·2	24·4	26·6	31·0	35·4	39·8
18 0	21·2	23·5	25·9	28·2	32·9	37·5	42·2
19 0	22·4	24·8	27·3	29·8	34·7	39·6	44·5
20 0	23·6	26·1	28·8	31·4	36·5	41·7	46·9

TABLE 157.—CAST-IRON BALLS AND THEIR CIRCUMSCRIBING CYLINDERS: WEIGHTS.

Diameter.	Weight of Ball.	Weight of Circumscribing Cylinder.	Diameter.	Weight of Ball.	Weight of Circumscribing Cylinder.
Inches.	Pounds.	Pounds.	Inches.	Cwts.	Cwts.
2	1·09	1·64	10	1·22	1·83
2½	2·13	3·19	11	1·62	2·43
3	3·68	5·52	12	2·10	3·15
3½	5·85	8·77	14	3·34	5·01
4	8·73	13·1	16	4·99	7·48
4½	12·4	18·6	18	7·10	10·65
5	17·0	25·5	20	9·74	14·61
5½	22·7	34·0	22	12·97	19·45
6	29·5	44·2	24	16·83	25·25
6½	37·5	56·2	26	21·40	32·10
7	46·8	70·2	28	26·72	40·08
7½	57·5	86·2	30	32·87	49·31
8	69·8	104·7	Cylinder, one-half heavier than ball.		
9	99·4	149·1			

TABLE 158.—COPPER AND BRASS: WEIGHT OF ONE LINEAL FOOT OF ROUND BOLTS OR RODS.

(Elliott's Metal Company.)

On the basis of 558lb. per cubic foot of Copper; and 534lb. for Brass.

Diameter.	Copper.	Brass.	Diameter.	Copper.	Brass.
Inches.	Pounds.	Pounds.	Inches.	Pounds.	Pounds.
½	·76	·72	2¼	15·40	14·74
⅝	·96	·92	2⅜	17·16	16·42
⅞	1·19	1·13	2½	19·01	18·19
1⅛	1·43	1·37	2⅝	29·96	20·06
1¼	1·71	1·63	2¾	23·01	22·01
1⅜	2·01	1·92	2⅞	25·15	24·06
1½	2·33	2·23	3	27·38	26·20
1⅝	2·67	2·56	3¼	32·14	30·75
1⅞	3·04	2·91	3½	37·27	35·67
2	3·43	3·28	3¾	42·78	40·93
2⅛	3·85	3·68	4	48·67	46·57
2¼	4·29	4·10	4¼	54·94	52·58
2½	4·75	4·55	4½	61·61	58·95
2⅞	5·75	5·50	4¾	68·66	65·70
3	6·84	6·55	5	76·06	72·79
3⅛	8·03	7·68	5¼	83·86	80·24
3½	9·32	8·91	5½	92·03	88·06
3⅞	10·69	10·23	6	109·55	104·82
4	12·17	11·64	6½	128·57	123·03
4¼	13·73	13·14	7	149·10	142·68



TABLE 159.—COPPER AND BRASS : WEIGHT OF ONE SQUARE FOOT.

(Elliott's Metal Company.)

On the basis of 558lb. per cubic foot of Copper, and 534lb. for Brass.

Thick- ness.	Weight per Square Foot.		Thick- ness.	Weight per Square Foot.	
	Copper.	Brass.		Copper.	Brass.
I. W. G.	Pounds.	Pounds.	I. W. G.	Pounds.	Pounds.
1	13·950	13·350	22	1·302	1·246
2	12·834	12·282	23	1·116	1·068
3	11·718	11·214	24	1·023	·979
4	10·788	10·324	25	·930	·890
5	9·858	9·434	26	·837	·801
6	8·928	8·544	27	·762	·729
7	8·184	7·832	28	·688	·658
8	7·440	7·120	29	·632	·605
9	6·696	6·408	30	·576	·551
10	5·952	5·696	31	·539	·516
11	5·394	5·162	32	·502	·480
12	4·836	4·628	33	·465	·445
13	4·278	4·094	34	·427	·409
14	3·720	3·560	35	·390	·373
15	3·348	3·204	36	·353	·338
16	2·976	2·848	37	·316	·302
17	2·604	2·492	38	·279	·267
18	2·232	2·136	39	·241	·231
19	1·860	1·780	40	·223	·213
20	1·624	1·602	41	·204	·195
21	1·488	1·424	42	·186	·178

TABLE 160.—COPPER : APPROXIMATE WEIGHT OF ONE SQUARE FOOT.

(Elliott's Metal Company.)

Thick- ness, I. W. G.	Approximate Weight per Square Foot.		Thick- ness, I. W. G.	Approximate Weight per Square Foot.		Thick- ness, I. W. G.	Approximate Weight per Square Foot.	
	No.	Lbs. Oz.		No.	Lbs. Oz.		No.	Lbs. Oz.
	1	14 0		11	5 6		21	1 7½
	2	12 14		12	4 13		22	1 5
	3	11 12		13	4 4		23	1 2½
	4	10 12		14	3 12		24	1 0
	5	9 14		15	3 6		25	0 14¾
	6	9 0		16	3 0		26	0 13½
	7	8 2		17	2 10		27	0 12¼
	8	7 6		18	2 4		28	0 11
	9	6 11		19	1 14		29	0 10
	10	6 0		20	1 10		30	0 9

TABLE 161.—WEIGHT OF SEAMLESS COPPER TUBES: IMPERIAL  
Calculated on the basis of

1884.		THICKNESS											
I. W. G.		0000	000	00	0	1	2	3	4	5	6	7	
Inches.	{	0.400	0.372	0.348	0.324	0.300	0.276	0.252	0.232	0.212	0.192	0.176	
		$\frac{1\frac{1}{2}}{2} b$	$\frac{3}{8} b$	$\frac{1}{2} f$	$\frac{3}{4} b$	$\frac{1}{2} f$	$\frac{3}{8} b$	$\frac{1}{4} f$	$\frac{1}{8} b$	$\frac{3}{16} b$	$\frac{1}{4} f$	$\frac{1}{8} f$	
Millimetres.		10.160	9.449	8.839	8.229	7.620	7.010	6.401	5.893	5.385	4.877	4.470	

Internal Diameter.		WEIGHT OF A LINEAL											
Inches.	Millim.	3.2	2.54	2.24	1.99	1.76	1.54	1.34	1.15	1.00	0.86	0.74	0.64
1	6.3	3.14	2.80	2.52	2.25	2.00	1.76	1.53	1.35	1.18	1.03	0.91	
	9.5	3.75	3.36	3.04	2.74	2.45	2.17	1.91	1.70	1.50	1.32	1.17	
	12.7	4.35	3.92	3.57	3.23	2.90	2.59	2.29	2.05	1.83	1.61	1.44	
	15.9	4.96	4.49	4.10	3.72	3.36	3.01	2.67	2.40	2.15	1.90	1.70	
	19.0	5.56	5.05	4.62	4.21	3.81	3.43	3.05	2.76	2.47	2.19	1.97	
	22.2	6.17	5.61	5.15	4.70	4.26	3.84	3.44	3.11	2.79	2.48	2.24	
	25.4	6.77	6.17	5.67	5.19	4.72	4.26	3.82	3.46	3.11	2.77	2.50	
	28.6	7.38	6.74	6.20	5.68	5.17	4.68	4.20	3.81	3.43	3.06	2.77	
	31.7	7.98	7.30	6.73	6.17	5.62	5.09	4.58	4.16	3.75	3.35	3.04	
	34.9	8.59	7.86	7.25	6.66	6.08	5.51	4.96	4.51	4.07	3.64	3.30	
	38.1	9.19	8.42	7.78	7.15	6.53	5.93	5.34	4.86	4.39	3.93	3.57	
	41.3	9.80	8.99	8.31	7.64	6.99	6.35	5.72	5.21	4.71	4.22	3.83	
1	44.4	10.40	9.55	8.83	8.13	7.44	6.76	6.10	5.56	5.03	4.51	4.10	
	47.6	11.01	10.11	9.36	8.62	7.89	7.18	6.48	5.91	5.35	4.80	4.37	
	50.8	11.61	10.67	9.88	9.11	8.35	7.60	6.86	6.26	5.67	5.09	4.63	
	54.0	12.22	11.24	10.41	9.60	8.80	8.02	7.25	6.61	5.99	5.38	4.90	
	57.1	12.82	11.80	10.94	10.09	9.25	8.43	7.63	6.97	6.31	5.67	5.16	
	60.3	13.43	12.36	11.46	10.58	9.71	8.85	8.01	7.32	6.63	5.96	5.43	
	63.5	14.03	12.92	11.99	11.07	10.16	9.27	8.39	7.67	6.95	6.25	5.70	
	66.7	14.64	13.49	12.52	11.56	10.62	9.69	8.77	8.02	7.28	6.54	5.96	
	69.8	15.24	14.05	13.04	12.05	11.07	10.10	9.15	8.37	7.60	6.83	6.23	
	73.0	15.85	14.61	13.57	12.54	11.52	10.52	9.53	8.72	7.92	7.12	6.50	
	76.2	16.45	15.17	14.09	13.03	11.98	10.94	9.91	9.07	8.24	7.41	6.76	
	3	82.5	17.66	16.30	15.15	14.01	12.88	11.77	10.68	9.77	8.88	7.99	7.29
88.9		18.87	17.42	16.20	14.99	13.79	12.61	11.44	10.47	9.52	8.58	7.83	
95.2		20.08	18.55	17.25	15.97	14.70	13.44	12.20	11.18	10.16	9.16	8.36	
101.6		21.20	19.67	18.30	16.95	15.62	14.28	12.96	11.88	10.80	9.74	8.89	
107.9		22.50	20.80	19.36	17.93	16.51	15.11	13.72	12.58	11.44	10.32	9.42	
114.3		23.71	21.93	20.41	18.91	17.42	15.95	14.49	13.28	12.08	10.90	9.96	
120.6		24.92	23.05	21.46	19.89	18.33	16.78	15.25	13.98	12.73	11.48	10.49	
127.0		26.13	24.18	22.51	20.87	19.23	17.62	16.01	14.68	13.37	12.06	11.02	
133.3		27.34	25.30	23.57	21.85	20.14	18.45	16.77	15.39	14.01	12.64	11.55	
139.7		28.55	26.43	24.62	22.83	21.05	19.29	17.54	16.09	14.65	13.22	12.08	
146.0		29.76	27.55	25.67	23.81	21.96	20.12	18.30	16.79	15.29	13.80	12.62	
6		152.4	30.97	28.68	26.72	24.79	22.86	20.95	19.06	17.49	15.93	14.38	13.15
	158.7	32.18	29.80	27.78	25.77	23.77	21.79	19.82	18.19	16.57	14.96	13.68	
	165.1	33.39	30.93	28.83	26.75	24.68	22.62	20.58	18.89	17.21	15.54	14.21	

Note to Table.—If the External Diameter is given, subtract  
Weight per Lineal Foot of a Copper Tube 2 ins. external

WIRE GAUGE, 1884 (The Broughton Copper Company).  
the specific gravity, 8·8917.

## OF COPPER.

8	9	10	11	12	13	14	15	16	17	18	19	20
0·160 $\frac{1}{16} f$	0·144 $\frac{3}{16} f$	0·128 $\frac{1}{4} f$	0·116 $\frac{5}{16} f$	0·104 $\frac{3}{8} b$	0·092 $\frac{1}{2} f$	0·080 $\frac{1}{4} f$	0·072 $\frac{1}{4} b$	0·064 $\frac{1}{8} b$	0·056 $\frac{1}{8} b$	0·048 $\frac{1}{4} f$	0·040 $\frac{1}{8} b$	0·036 $\frac{1}{16} f$
4·064	3·658	3·251	2·946	2·642	2·337	2·032	1·829	1·626	1·422	1·219	1·016	0·914

## FOOT IN POUNDS.

0·55	0·47	0·39	0·34	0·29	0·24	0·20	0·17	0·15	0·12	0·10	0·08	0·07
0·79	0·69	0·58	0·51	0·44	0·38	0·32	0·28	0·24	0·21	0·17	0·14	0·12
1·04	0·90	0·78	0·69	0·60	0·52	0·44	0·39	0·34	0·29	0·25	0·20	0·18
1·28	1·12	0·97	0·86	0·76	0·66	0·56	0·50	0·44	0·38	0·32	0·26	0·23
1·52	1·34	1·17	1·04	0·92	0·80	0·68	0·61	0·53	0·46	0·39	0·32	0·29
1·76	1·56	1·36	1·21	1·07	0·94	0·80	0·72	0·63	0·55	0·46	0·38	0·34
2·00	1·77	1·55	1·39	1·23	1·08	0·92	0·82	0·73	0·63	0·54	0·44	0·40
2·24	1·99	1·75	1·57	1·39	1·21	1·04	0·93	0·82	0·71	0·61	0·50	0·45
2·49	2·21	1·94	1·74	1·55	1·35	1·17	1·04	0·92	0·80	0·68	0·56	0·51
2·73	2·43	2·13	1·92	1·70	1·49	1·29	1·15	1·02	0·88	0·75	0·62	0·56
2·97	2·65	2·33	2·09	1·86	1·63	1·41	1·26	1·11	0·97	0·83	0·68	0·61
3·21	2·86	2·52	2·27	2·02	1·77	1·53	1·37	1·21	1·05	0·90	0·74	0·67
3·45	3·08	2·71	2·44	2·17	1·91	1·65	1·48	1·31	1·14	0·97	0·81	0·72
3·70	3·30	2·91	2·62	2·33	2·05	1·77	1·59	1·40	1·22	1·04	0·87	0·78
3·94	3·52	3·10	2·79	2·49	2·19	1·89	1·70	1·50	1·31	1·12	0·93	0·83
4·18	3·73	3·29	2·97	2·65	2·33	2·01	1·80	1·60	1·39	1·19	0·99	0·89
4·42	3·95	3·49	3·14	2·80	2·47	2·13	1·91	1·69	1·48	1·26	1·05	0·94
4·66	4·17	3·68	3·32	2·96	2·61	2·25	2·02	1·79	1·56	1·33	1·11	1·00
4·91	4·39	3·88	3·50	3·12	2·75	2·38	2·13	1·89	1·65	1·41	1·17	1·05
5·15	4·61	4·07	3·67	3·28	2·88	2·50	2·24	1·98	1·73	1·48	1·23	1·10
5·39	4·82	4·26	3·85	3·43	3·02	2·62	2·35	2·08	1·82	1·55	1·29	1·16
5·63	5·04	4·46	4·02	3·59	3·16	2·74	2·46	2·18	1·90	1·62	1·35	1·21
5·87	5·26	4·65	4·20	3·75	3·30	2·86	2·57	2·27	1·99	1·70	1·41	1·27
6·12	5·48	4·84	4·37	3·90	3·44	2·98	2·68	2·37	2·07	1·77	1·47	1·32
6·36	5·91	5·23	4·72	4·22	3·72	3·22	2·89	2·57	2·24	1·91	1·59	1·43
7·08	6·35	5·62	5·07	4·53	4·00	3·46	3·11	2·76	2·41	2·06	1·71	1·54
7·57	6·78	6·00	5·42	4·85	4·28	3·71	3·33	2·95	2·58	2·20	1·83	1·65
8·06	7·22	6·30	5·77	5·16	4·55	3·95	3·55	3·15	2·75	2·35	1·95	1·76
8·54	7·65	6·78	6·13	5·48	4·83	4·19	3·76	3·34	2·92	2·50	2·08	1·87
9·02	8·09	7·17	6·48	5·79	5·11	4·43	3·98	3·53	3·09	2·64	2·20	1·97
9·50	8·53	7·55	6·83	6·11	5·39	4·67	4·20	3·73	3·26	2·79	2·32	2·08
9·99	8·96	7·94	7·18	6·42	5·67	4·92	4·42	3·92	3·42	2·93	2·44	2·19
10·47	9·40	8·33	7·53	6·74	5·95	5·16	4·64	4·11	3·59	3·08	2·56	...
10·96	9·83	8·71	7·88	7·05	6·22	5·40	4·85	4·31	3·76	3·22	2·68	...
11·44	10·27	9·10	8·23	7·36	6·50	5·64	5·07	4·50	3·93	3·37	2·80	...
11·92	10·70	9·49	8·58	7·68	6·78	5·88	5·29	4·69	4·10	3·51	2·92	...
12·41	11·14	9·88	8·93	7·99	7·06	6·13	5·51	4·89	4·27	3·66	...	...
12·89	11·57	10·26	9·28	8·31	7·34	6·37	5·72	5·08	4·44	3·80	...	...

number at bottom of column, pages 304, 305. For example—The diameter, 12 I. W. G., is  $2·65 - 0·26 = 2·39$  lbs.  $f$ , full;  $b$ , bare.

TABLE 161.—WEIGHT OF SEAMLESS COPPER TUBES : IMPERIAL  
Calculated on the basis of

1884.		THICKNESS										
I. W. G.	Inches. { Millimetres.	0000	000	00	0	1	2	3	4	5	6	7
		0·400 $\frac{1}{16} b$	0·372 $\frac{3}{8} b$	0·348 $\frac{1}{4} f$	0·324 $\frac{3}{16} b$	0·300 $\frac{1}{4} f$	0·276 $\frac{5}{16} b$	0·252 $\frac{1}{2} f$	0·232 $\frac{1}{4} b$	0·212 $\frac{3}{8} b$	0·192 $\frac{1}{4} f$	0·176 $\frac{1}{8} f$
		10·160	9·449	8·839	8·229	7·620	7·010	6·401	5·893	5·385	4·877	4·470
Internal Diameter.		WEIGHT OF A LINEAL										
Inches.	Millim.											
$\frac{5}{16}$	171·4	34·60	32·05	29·88	27·73	25·59	23·46	21·35	19·60	17·85	16·12	14·75
$\frac{7}{16}$	177·8	35·81	33·18	30·93	28·71	26·49	24·29	22·11	20·30	18·50	16·70	15·28
$\frac{1}{2}$	184·1	37·02	34·30	31·99	29·69	27·40	25·13	22·87	21·00	19·14	17·29	15·81
$\frac{5}{8}$	190·5	38·23	35·43	33·04	30·67	28·31	25·96	23·63	21·70	19·78	17·87	16·34
$\frac{3}{4}$	196·8	39·44	36·55	34·09	31·65	29·22	26·80	24·39	22·40	20·42	18·45	16·88
$\frac{7}{8}$	203·2	40·65	37·68	35·14	32·63	30·12	27·63	25·16	23·10	21·06	19·03	17·41
8	209·5	41·86	38·80	36·20	33·61	31·03	28·47	25·92	23·81	21·70	19·61	17·94
$8\frac{1}{2}$	215·9	43·07	39·93	37·25	34·59	31·94	29·30	26·68	24·51	22·34	20·19	18·47
$8\frac{3}{4}$	222·2	44·28	41·05	38·30	35·57	32·84	30·14	27·44	25·21	22·98	20·77	19·00
9	228·6	45·49	42·18	39·35	36·55	33·75	30·97	28·21	25·91	23·63	21·35	19·54
$9\frac{1}{8}$	234·9	46·70	43·30	40·41	37·53	34·66	31·81	28·97	26·61	24·27	21·93	20·07
$9\frac{1}{4}$	241·3	47·91	44·43	41·46	38·51	35·57	32·64	29·73	27·31	24·91	22·51	20·60
$9\frac{3}{8}$	247·6	49·12	45·55	42·51	39·49	36·47	33·48	30·49	28·02	25·55	23·09	21·13
10	254·0	50·33	46·68	43·56	40·47	37·38	34·31	31·25	28·72	26·19	23·67	21·67
$10\frac{1}{8}$	260·3	51·54	47·80	44·62	41·45	38·29	35·15	32·02	29·42	26·83	24·25	22·20
$10\frac{1}{4}$	266·7	52·75	48·93	45·67	42·43	39·20	35·98	32·78	30·12	27·47	24·83	22·73
$10\frac{3}{8}$	273·0	53·96	50·05	46·72	43·41	40·10	36·81	33·54	30·82	28·11	25·42	23·26
11	279·4	55·16	51·18	47·77	44·39	41·01	37·65	34·30	31·52	28·75	26·00	23·80
$11\frac{1}{8}$	285·7	56·37	52·30	48·83	45·37	41·92	38·48	35·06	32·23	29·40	26·58	24·33
$11\frac{1}{4}$	292·1	57·58	53·43	49·88	46·35	42·83	39·32	35·83	32·93	30·04	27·16	24·86
$11\frac{3}{8}$	298·4	58·79	54·55	50·93	47·33	43·73	40·15	36·59	33·63	30·68	27·74	25·39
12	304·8	60·00	55·68	51·98	48·31	44·64	40·99	37·35	34·33	31·32	28·32	25·92
$12\frac{1}{8}$	311·1	61·21	56·80	53·04	49·29	45·55	41·82	38·11	35·03	31·96	28·90	26·46
$12\frac{1}{4}$	317·5	62·42	57·93	54·09	50·26	46·45	42·66	38·88	35·73	32·60	29·48	26·99
$12\frac{3}{8}$	323·8	63·63	59·05	55·14	51·24	47·36	43·49	39·64	36·44	33·24	30·06	27·52
13	330·2	64·84	60·18	56·19	52·22	48·27	44·33	40·40	37·14	33·88	30·64	28·05
$13\frac{1}{8}$	336·5	66·05	61·30	57·25	53·20	49·18	45·16	41·16	37·84	34·53	31·22	28·59
$13\frac{1}{4}$	342·9	67·26	62·43	58·30	54·18	50·08	46·00	41·92	38·54	35·17	31·80	29·12
$13\frac{3}{8}$	349·2	68·47	63·55	59·35	55·16	50·99	46·83	42·69	39·24	35·81	32·38	29·65
14	355·6	69·68	64·68	60·40	56·14	51·90	47·67	43·45	39·94	36·45	32·96	30·18
		3·87	3·35	2·93	2·54	2·18	1·84	1·54	1·30	1·09	0·89	0·75

Note to Table.—If the External Diameter is given, subtract  
Lineal Foot of a Copper Tube 2 ins. external diameter,

WIRE GAUGE, 1884 (The Broughton Copper Co.) (*continued*).  
the specific gravity, 8·8917.

## OF COPPER.

8	9	10	11	12	13	14	15	16	17	18	19	20
0·160	0·144	0·128	0·116	0·104	0·092	0·080	0·072	0·064	0·056	0·048	0·040	0·036
$\frac{3}{8} f$	$\frac{9}{16} f$	$\frac{1}{2} f$	$\frac{7}{8} f$	$\frac{1}{2} b$	$\frac{3}{4} f$	$\frac{5}{8} f$	$\frac{3}{4} b$	$\frac{1}{2} f$	$\frac{1}{2} b$	$\frac{3}{8} f$	$\frac{3}{8} b$	$\frac{1}{4} f$
4·064	3·658	3·251	2·946	2·642	2·337	2·032	1·829	1·626	1·422	1·219	1·016	0·914

## FOOT IN POUNDS.

13·37	12·01	10·65	9·63	8·62	7·61	6·61	5·94	5·28	4·61	3·95	...	...
13·86	12·44	11·04	9·99	8·94	7·89	6·85	6·16	5·47	4·78	4·09	...	...
14·34	12·88	11·42	10·34	9·25	8·17	7·09	6·38	5·66	4·95	...	...	...
14·83	13·32	11·81	10·69	9·57	8·45	7·34	6·60	5·86	5·12	...	...	...
15·31	13·75	12·20	11·04	9·88	8·73	7·58	6·81	6·05	5·29	...	...	...
15·79	14·19	12·59	11·39	10·20	9·01	7·82	7·03	6·24	5·46	...	...	...
16·28	14·62	12·97	11·74	10·51	9·28	8·06	7·25	6·44	...	...	...	...
16·76	15·06	13·36	12·09	10·82	9·56	8·30	7·47	6·63	...	...	...	...
17·25	15·49	13·75	12·44	11·14	9·84	8·55	7·68	6·82	...	...	...	...
17·73	15·93	14·13	12·79	11·45	10·12	8·79	7·90	7·02	...	...	...	...
18·21	16·36	14·52	13·14	11·77	10·40	9·03	8·12	...	...	...	...	...
18·70	16·80	14·91	13·49	12·08	10·68	9·27	8·34	...	...	...	...	...
19·18	17·24	15·30	13·84	12·40	10·95	9·51	8·55	...	...	...	...	...
19·67	17·67	15·68	14·20	12·71	11·23	9·76	8·77	...	...	...	...	...
20·15	18·11	16·07	14·55	13·03	11·51	10·00	...	...	...	...	...	...
20·63	18·54	16·46	14·90	13·34	11·79	10·24	...	...	...	...	...	...
21·12	18·98	16·84	15·25	13·66	12·07	10·48	...	...	...	...	...	...
21·60	19·41	17·23	15·60	13·97	12·34	10·72	...	...	...	...	...	...
22·08	19·85	17·62	15·95	14·28	12·62	...	...	...	...	...	...	...
22·57	20·28	18·01	16·30	14·60	12·90	...	...	...	...	...	...	...
23·05	20·72	18·39	16·65	14·91	13·18	...	...	...	...	...	...	...
23·54	21·16	18·78	17·00	15·23	13·46	...	...	...	...	...	...	...
24·02	21·59	19·17	17·35	15·54	...	...	...	...	...	...	...	...
24·50	22·03	19·55	17·70	15·86	...	...	...	...	...	...	...	...
24·99	22·46	19·94	18·05	16·17	...	...	...	...	...	...	...	...
25·47	22·90	20·33	18·41	16·49	...	...	...	...	...	...	...	...
25·96	23·33	20·72	18·76	...	...	...	...	...	...	...	...	...
26·44	23·77	21·10	19·11	...	...	...	...	...	...	...	...	...
26·92	24·20	21·49	19·46	...	...	...	...	...	...	...	...	...
27·41	24·64	21·88	19·81	...	...	...	...	...	...	...	...	...
0·62	0·50	0·40	0·33	0·26	0·20	0·15	0·12	0·10	0·08	0·06	0·04	0·03

number at bottom of column ; for example—The Weight per  
12 I. W. G., is  $2·65 - 0·26 = 2·39$  lbs.  $f$ , full ;  $b$ , bare.

TABLE 162.—WEIGHT OF SEAMLESS COPPER TUBES :

Calculated on the basis of

		THICKNESS											
B. W. G.		0000	000	00	0	1	2	3	4	5	6	7	
Inches.	{	0.454	0.425	0.380	0.340	0.300	0.284	0.259	0.238	0.220	0.203	0.180	
Millimetres.		$\frac{3}{16}$	$\frac{3}{16}f$	$\frac{3}{16}f$	$\frac{1}{2}$	$\frac{1}{2}f$	$\frac{9}{32}f$	$\frac{1}{4}f$	$\frac{11}{32}f$	$\frac{7}{8}f$	$\frac{1}{2}$	$\frac{3}{8}b$	
		11.53	10.79	9.65	8.64	7.62	7.21	6.58	6.04	5.59	5.16	4.57	
Internal Diameter.		WEIGHT OF A LINEAL											
Inches.	Millim.	3.2	3.18	2.83	2.32	1.91	1.54	1.40	1.20	1.04	0.92	0.80	0.66
1	3.2	3.87	3.47	2.90	2.43	2.00	1.83	1.59	1.40	1.25	1.11	0.94	
1	6.3	4.55	4.11	3.47	2.94	2.45	2.26	1.99	1.76	1.58	1.42	1.21	
1	12.7	5.24	4.76	4.04	3.45	2.90	2.69	2.38	2.12	1.92	1.73	1.48	
1	15.9	5.92	5.40	4.62	3.97	3.36	3.12	2.77	2.48	2.25	2.03	1.75	
1	19.0	6.61	6.04	5.19	4.48	3.81	3.55	3.16	2.84	2.58	2.34	2.02	
1	22.2	7.30	6.68	5.77	5.00	4.26	3.98	3.55	3.20	2.91	2.65	2.30	
1	25.4	7.99	7.33	6.34	5.51	4.72	4.41	3.94	3.56	3.25	2.95	2.57	
1	28.6	8.67	7.97	6.92	6.03	5.17	4.84	4.34	3.92	3.58	3.26	2.84	
1	31.7	9.36	8.61	7.49	6.54	5.62	5.27	4.73	4.28	3.91	3.57	3.11	
1	34.9	10.04	9.25	8.07	7.05	6.08	5.70	5.12	4.64	4.24	3.87	3.39	
1	38.1	10.73	9.90	8.64	7.57	6.53	6.13	5.51	5.00	4.58	4.18	3.66	
1	41.3	11.42	10.54	9.22	8.08	6.99	6.56	5.90	5.36	4.91	4.49	3.93	
1	44.4	12.10	11.18	9.79	8.60	7.44	6.99	6.29	5.72	5.24	4.80	4.20	
1	47.6	12.79	11.82	10.37	9.11	7.89	7.42	6.69	6.08	5.58	5.10	4.47	
2	50.8	13.48	12.47	10.94	9.62	8.35	7.85	7.08	6.44	5.91	5.41	4.75	
2	54.0	14.16	13.11	11.52	10.14	8.80	8.28	7.47	6.80	6.24	5.72	5.02	
2	57.1	14.85	13.75	12.09	10.65	9.25	8.71	7.86	7.16	6.57	6.02	5.29	
2	60.3	15.54	14.40	12.66	11.17	9.71	9.14	8.25	7.52	6.91	6.33	5.56	
2	63.5	16.22	15.04	13.24	11.68	10.16	9.56	8.64	7.88	7.24	6.64	5.84	
2	66.7	16.91	15.68	13.81	12.20	10.62	9.99	9.04	8.24	7.57	6.94	6.11	
2	69.8	17.60	16.32	14.39	12.71	11.07	10.42	9.43	8.60	7.90	7.25	6.38	
2	73.0	18.28	16.97	14.96	13.22	11.52	10.85	9.82	8.96	8.24	7.56	6.65	
2	76.2	18.97	17.61	15.54	13.74	11.98	11.28	10.21	9.32	8.57	7.87	6.92	
3	82.5	20.34	18.89	16.69	14.77	12.88	12.14	10.99	10.04	9.23	8.48	7.47	
3	88.9	21.72	20.18	17.84	15.79	13.79	13.00	11.78	10.76	9.90	9.09	8.01	
3	95.2	23.09	21.47	18.99	16.82	14.70	13.86	12.56	11.48	10.57	9.71	8.56	
4	101.6	24.46	22.75	20.13	17.85	15.61	14.72	13.34	12.20	11.23	10.32	9.10	
4	107.9	25.84	24.04	21.28	18.88	16.51	15.58	14.13	12.92	11.90	10.94	9.65	
4	114.3	27.21	25.32	22.43	19.91	17.42	16.44	14.91	13.64	12.56	11.55	10.19	
4	120.6	28.58	26.61	23.58	20.94	18.33	17.29	15.69	14.36	13.23	12.16	10.73	
5	127.0	29.95	27.89	24.73	21.96	19.23	18.15	16.48	15.08	13.89	12.78	11.28	
5	133.3	31.33	29.18	25.88	22.99	20.14	19.01	17.26	15.80	14.56	13.39	11.82	
5	139.7	32.70	30.46	27.03	24.02	21.05	19.87	18.04	16.52	15.22	14.01	12.37	
5	146.0	34.07	31.75	28.18	25.05	21.96	20.73	18.83	17.24	15.89	14.62	12.91	
6	152.4	35.45	33.03	29.33	26.08	22.86	21.59	19.61	17.96	16.55	15.23	13.46	
6	158.7	36.82	34.32	30.48	27.11	23.77	22.45	20.39	18.68	17.22	15.85	14.00	
6	165.1	38.19	35.60	31.63	28.13	24.68	23.31	21.18	19.40	17.88	16.46	14.55	

*Note to Table.*—If the External Diameter is given, subtract  
The Weight per Lineal Foot of a Copper Tube 2 ins. external

BIRMINGHAM WIRE GAUGE (The Broughton Copper Co.).  
the specific gravity, 8·8917.

## OF COPPER.

8	9	10	11	12	13	14	15	16	17	18	19	20
0·165 $\frac{1}{16} b$	0·148 $\frac{9}{64} f$	0·134 $\frac{5}{16} b$	0·120 $\frac{1}{8} b$	0·109 $\frac{7}{64} f$	0·095 $\frac{3}{32} f$	0·083 $\frac{5}{64} f$	0·072 $\frac{3}{16} b$	0·065 $\frac{1}{16} f$	0·058 $\frac{1}{8} b$	0·049 $\frac{3}{32} f$	0·042 $\frac{1}{8} b$	0·035 $\frac{1}{16} f$
4·19	3·76	3·40	3·05	2·77	2·41	2·11	1·83	1·65	1·47	1·24	1·07	0·89

## FOOT IN POUNDS.

0·58	0·49	0·42	0·36	0·31	0·25	0·21	0·17	0·15	0·13	0·10	0·08	0·07
0·83	0·71	0·62	0·54	0·47	0·40	0·33	0·28	0·25	0·22	0·18	0·15	0·12
1·08	0·94	0·82	0·72	0·64	0·54	0·46	0·39	0·35	0·30	0·25	0·21	0·17
1·33	1·16	1·03	0·90	0·80	0·68	0·58	0·50	0·44	0·39	0·32	0·27	0·23
1·58	1·38	1·23	1·08	0·97	0·83	0·71	0·61	0·54	0·48	0·40	0·34	0·28
1·83	1·61	1·43	1·26	1·13	0·97	0·84	0·72	0·64	0·57	0·47	0·40	0·33
2·08	1·83	1·64	1·44	1·30	1·11	0·96	0·82	0·74	0·65	0·55	0·47	0·38
2·32	2·05	1·84	1·63	1·46	1·26	1·09	0·93	0·84	0·74	0·62	0·53	0·44
2·57	2·28	2·04	1·81	1·63	1·40	1·21	1·04	0·94	0·83	0·70	0·59	0·49
2·82	2·50	2·24	1·99	1·79	1·55	1·34	1·15	1·03	0·92	0·77	0·66	0·54
3·07	2·73	2·45	2·17	1·96	1·69	1·46	1·26	1·13	1·00	0·84	0·72	0·60
3·32	2·95	2·65	2·35	2·12	1·83	1·59	1·37	1·23	1·09	0·92	0·78	0·65
3·57	3·17	2·85	2·53	2·29	1·98	1·71	1·48	1·33	1·18	0·99	0·85	0·70
3·82	3·40	3·05	2·71	2·45	2·12	1·84	1·59	1·43	1·27	1·07	0·91	0·76
4·07	3·62	3·26	2·90	2·62	2·26	1·97	1·70	1·52	1·36	1·14	0·97	0·81
4·32	3·85	3·46	3·08	2·78	2·41	2·09	1·80	1·62	1·44	1·21	1·04	0·86
4·57	4·07	3·66	3·26	2·95	2·55	2·22	1·91	1·72	1·53	1·29	1·10	0·91
4·82	4·29	3·86	3·44	3·11	2·69	2·34	2·02	1·82	1·62	1·36	1·16	0·97
5·07	4·52	4·07	3·62	3·27	2·84	2·47	2·13	1·92	1·71	1·44	1·23	1·02
5·32	4·74	4·27	3·80	3·44	2·98	2·59	2·24	2·02	1·79	1·51	1·29	1·07
5·57	4·96	4·47	3·98	3·60	3·13	2·72	2·35	2·11	1·88	1·58	1·35	1·13
5·82	5·19	4·67	4·17	3·77	3·27	2·84	2·46	2·21	1·97	1·66	1·42	1·18
6·07	5·41	4·88	4·35	3·93	3·41	2·97	2·57	2·31	2·06	1·73	1·48	1·23
6·32	5·64	5·08	4·53	4·10	3·56	3·10	2·68	2·41	2·15	1·81	1·55	1·28
6·57	5·86	5·29	4·73	4·28	3·73	3·25	2·82	2·54	2·27	1·92	1·65	1·38
6·82	6·08	5·49	4·89	4·43	3·84	3·35	2·89	2·61	2·32	1·96	1·67	1·39
7·07	6·30	5·69	5·12	4·64	4·13	3·60	3·11	2·80	2·50	2·10	1·80	1·50
7·32	6·52	5·89	5·25	4·76	4·23	3·66	3·11	2·80	2·50	2·10	1·80	1·50
7·57	6·74	6·10	5·50	4·99	4·44	3·85	3·33	3·00	2·67	2·25	1·93	1·60
7·82	6·96	6·30	5·68	5·16	4·61	4·04	3·50	3·15	2·81	2·38	2·04	1·70
8·07	7·18	6·50	5·86	5·32	4·75	4·16	3·61	3·25	2·90	2·46	2·11	1·76
8·32	7·40	6·70	6·05	5·49	4·91	4·31	3·75	3·38	3·02	2·57	2·21	1·85
8·57	7·62	6·90	6·23	5·65	5·06	4·45	3·88	3·50	3·13	2·67	2·30	1·93
8·82	7·84	7·10	6·41	5·81	5·20	4·58	4·00	3·61	3·23	2·76	2·38	1·99
9·07	8·06	7·30	6·59	5·97	5·34	4·71	4·12	3·72	3·33	2·85	2·46	2·07
9·32	8·28	7·50	6·77	6·14	5·50	4·86	4·26	3·86	3·46	2·97	2·57	2·17
9·57	8·50	7·70	6·95	6·31	5·66	5·01	4·41	3·99	3·58	3·08	2·67	2·26
9·82	8·72	7·90	7·14	6·48	5·82	5·16	4·55	4·12	3·70	3·28	2·85	2·43
10·07	8·94	8·10	7·32	6·64	5·97	5·29	4·67	4·23	3·80	3·37	2·94	2·51
10·32	9·16	8·30	7·50	6·80	6·11	5·42	4·79	4·34	3·91	3·48	3·04	2·60
10·57	9·38	8·50	7·68	6·96	6·25	5·54	4·90	4·45	4·01	3·57	3·13	2·69
10·82	9·60	8·70	7·86	7·13	6·41	5·69	5·04	4·58	4·14	3·69	3·24	2·78
11·07	9·82	8·90	8·05	7·30	6·56	5·83	5·17	4·70	4·25	3·80	3·35	2·87
11·32	10·04	9·10	8·23	7·46	6·71	5·96	5·28	4·80	4·34	3·88	3·42	2·96
11·57	10·26	9·30	8·41	7·62	6·85	6·08	5·39	4·90	4·44	3·97	3·50	3·05
11·82	10·48	9·50	8·59	7·78	7·00	6·21	5·51	5·02	4·55	4·08	3·61	3·14
12·07	10·70	9·70	8·77	7·94	7·14	6·34	5·63	5·13	4·66	4·18	3·71	3·23
12·32	10·92	9·90	8·95	8·11	7·29	6·47	5·75	5·24	4·76	4·28	3·80	3·32
12·57	11·14	10·10	9·13	8·28	7·44	6·61	5·88	5·36	4·87	4·38	3·89	3·40
12·82	11·36	10·30	9·31	8·44	7·59	6·74	6·00	5·47	4·97	4·48	3·98	3·48
13·07	11·58	10·50	9·49	8·60	7·73	6·86	6·11	5·57	5·07	4·57	4·08	3·57

number given at bottom of column, pages 308, 309. For example—  
diameter, 12 B. W. G., is 2·78 -- 0·29 = 2·49 lbs. *f*, full; *b*, bare.

TABLE 162.—WEIGHT OF SEAMLESS COPPER TUBES: BIRMINGHAM.  
Calculated on the basis of

		THICKNESS										
B. W. G.		0000	000	00	0	1	2	3	4	5	6	7
Inches.	{	0.454	0.425	0.380	0.340	0.300	0.284	0.259	0.238	0.220	0.203	0.180
Millimetres.		$\frac{23}{16}$	$\frac{21}{16}f$	$\frac{19}{16}f$	$\frac{17}{16}$	$\frac{15}{16}f$	$\frac{9}{16}f$	$\frac{1}{2}f$	$\frac{13}{16}f$	$\frac{7}{8}f$	$\frac{3}{4}$	$\frac{1}{2}b$
		11.53	10.79	9.65	8.64	7.62	7.21	6.58	6.04	5.59	5.16	4.57
Internal Diameter.		WEIGHT OF A LINEAL										
Inches.	Millim.											
6 $\frac{3}{4}$	171.4	39.57	36.89	32.78	29.16	25.59	24.17	21.96	20.12	18.55	17.07	15.09
7	177.8	40.94	38.18	33.93	30.19	26.49	25.03	22.74	20.84	19.22	17.69	15.68
7 $\frac{1}{4}$	184.1	42.31	39.46	35.08	31.22	27.40	25.88	23.53	21.56	19.88	18.30	16.18
7 $\frac{1}{2}$	190.5	43.69	40.75	36.22	32.25	28.31	26.74	24.31	22.28	20.55	18.92	16.72
7 $\frac{3}{4}$	196.8	45.06	42.03	37.37	33.28	29.22	27.60	25.09	23.00	21.21	19.53	17.27
8	203.2	46.43	43.32	38.52	34.30	30.12	28.46	25.88	23.72	21.88	20.14	17.81
8 $\frac{1}{4}$	209.5	47.80	44.60	39.67	35.33	31.03	29.32	26.66	24.44	22.54	20.76	18.36
8 $\frac{1}{2}$	215.9	49.18	45.89	40.82	36.36	31.94	30.18	27.44	25.16	23.21	21.37	18.90
8 $\frac{3}{4}$	222.3	50.55	47.17	41.97	37.39	32.84	31.04	28.23	25.88	23.87	21.99	19.45
9	228.6	51.92	48.46	43.12	38.42	33.75	31.90	29.01	26.60	24.54	22.60	19.99
9 $\frac{1}{4}$	235.0	53.30	49.74	44.27	39.45	34.66	32.76	29.79	27.32	25.20	23.21	20.53
9 $\frac{1}{2}$	241.3	54.67	51.03	45.42	40.47	35.57	33.61	30.58	28.04	25.87	23.83	21.08
9 $\frac{3}{4}$	247.7	56.04	52.31	46.57	41.50	36.47	34.47	31.36	28.76	26.53	24.44	21.62
10	254.0	57.42	53.60	47.72	42.53	37.38	35.33	32.14	29.48	27.20	25.06	22.17
10 $\frac{1}{4}$	260.4	58.79	54.89	48.87	43.56	38.29	36.19	32.93	30.20	27.87	25.67	22.71
10 $\frac{1}{2}$	266.7	60.16	56.17	50.02	44.59	39.20	37.05	33.71	30.92	28.53	26.28	23.26
10 $\frac{3}{4}$	273.1	61.54	57.46	51.17	45.61	40.10	37.91	34.49	31.64	29.20	26.90	23.80
11	279.4	62.91	58.74	52.31	46.64	41.01	38.77	35.28	32.36	29.86	27.51	24.34
11 $\frac{1}{4}$	285.8	64.28	60.03	53.46	47.67	41.92	39.63	36.06	33.08	30.53	28.13	24.89
11 $\frac{1}{2}$	292.1	65.65	61.31	54.61	48.70	42.83	40.49	36.84	33.80	31.19	28.74	25.43
11 $\frac{3}{4}$	298.5	67.03	62.60	55.76	49.73	43.73	41.35	37.63	34.52	31.86	29.35	25.98
12	304.8	68.40	63.88	56.91	50.76	44.64	42.20	38.41	35.24	32.52	29.97	26.52
12 $\frac{1}{4}$	311.2	69.77	65.17	58.06	51.78	45.55	43.06	39.19	35.96	33.19	30.58	27.07
12 $\frac{1}{2}$	317.5	71.15	66.45	59.21	52.81	46.45	43.92	39.98	36.68	33.85	31.20	27.61
12 $\frac{3}{4}$	323.9	72.52	67.74	60.36	53.84	47.36	44.78	40.76	37.40	34.52	31.81	28.16
13	330.2	73.89	69.02	61.51	54.87	48.27	45.64	41.54	38.11	35.18	32.42	28.70
13 $\frac{1}{4}$	336.6	75.27	70.31	62.66	55.90	49.18	46.50	42.33	38.83	35.85	33.04	29.24
13 $\frac{1}{2}$	342.9	76.64	71.59	63.81	56.93	50.08	47.36	43.11	39.55	36.52	33.65	29.79
13 $\frac{3}{4}$	349.3	78.01	72.88	64.96	57.95	50.99	48.22	43.89	40.27	37.18	34.27	30.33
14	355.6	79.39	74.17	66.11	58.98	51.90	49.08	44.68	40.99	37.85	34.88	30.88
		4.99	4.37	3.49	2.80	2.18	1.95	1.62	1.37	1.17	1.00	0.78

Note to Table.—If the External Diameter is given, subtract per Lineal Foot of a Copper Tube 2 ins. external diameter,



HAM WIRE GAUGE (The Broughton Copper Co.) (*continued*).  
the specific gravity, 8·8917.

## OF COPPER.

8	9	10	11	12	13	14	15	16	17	18	19	20
0·165 $\frac{1}{8} b$	0·148 $\frac{9}{16} f$	0·134 $\frac{7}{8} b$	0·120 $\frac{3}{4} b$	0·109 $\frac{1}{2} f$	0·095 $\frac{3}{8} f$	0·083 $\frac{1}{4} f$	0·072 $\frac{5}{16} b$	0·065 $\frac{1}{8} f$	0·058 $\frac{1}{16} b$	0·049 $\frac{3}{32} f$	0·042 $\frac{1}{8} b$	0·035 $\frac{1}{16} f$
4·19	3·76	3·40	3·05	2·77	2·41	2·11	1·83	1·65	1·47	1·24	1·07	0·89

## FOOT IN POUNDS.

13·80	12·35	11·16	9·97	9·04	7·87	6·86	5·94	5·36	4·78	4·03	...	...
14·30	12·80	11·56	10·34	9·37	8·15	7·11	6·16	5·55	4·95	4·18	...	...
14·80	13·25	11·97	10·70	9·70	8·44	7·36	6·38	5·75	5·13	...	...	...
15·30	13·69	12·37	11·06	10·03	8·73	7·61	6·59	5·95	5·30	...	...	...
15·80	14·14	12·78	11·42	10·36	9·02	7·86	6·81	6·14	5·48	...	...	...
16·30	14·59	13·19	11·79	10·69	9·30	8·12	7·03	6·34	5·65	...	...	...
16·80	15·04	13·59	12·15	11·02	9·59	8·37	7·25	6·54	...	...	...	...
17·30	15·48	14·00	12·51	11·35	9·88	8·62	7·47	6·73	...	...	...	...
17·79	15·93	14·40	12·88	11·68	10·16	8·87	7·68	6·93	...	...	...	...
18·29	16·38	14·81	13·24	12·01	10·45	9·12	7·90	7·13	...	...	...	...
18·79	16·83	15·21	13·60	12·34	10·74	9·37	8·12	...	...	...	...	...
19·29	17·27	15·62	13·96	12·67	11·03	9·62	8·34	...	...	...	...	...
19·79	17·72	16·02	14·33	13·00	11·31	9·87	8·55	...	...	...	...	...
20·29	18·17	16·43	14·69	13·33	11·60	10·12	8·77	...	...	...	...	...
20·79	18·62	16·83	15·05	13·66	11·89	10·37	...	...	...	...	...	...
21·29	19·06	17·24	15·42	13·99	12·18	10·63	...	...	...	...	...	...
21·79	19·51	17·64	15·78	14·32	12·46	10·88	...	...	...	...	...	...
22·29	19·96	18·05	16·14	14·65	12·75	11·13	...	...	...	...	...	...
22·79	20·41	18·45	16·51	14·98	13·04	...	...	...	...	...	...	...
23·28	20·85	18·86	16·87	15·31	13·33	...	...	...	...	...	...	...
23·78	21·30	19·26	17·23	15·64	13·61	...	...	...	...	...	...	...
24·28	21·75	19·67	17·59	15·97	13·90	...	...	...	...	...	...	...
24·78	22·20	20·08	17·96	16·30	...	...	...	...	...	...	...	...
25·28	22·65	20·48	18·32	16·63	...	...	...	...	...	...	...	...
25·78	23·09	20·89	18·68	16·96	...	...	...	...	...	...	...	...
26·28	23·54	21·29	19·05	17·29	...	...	...	...	...	...	...	...
26·78	23·99	21·70	19·41	...	...	...	...	...	...	...	...	...
27·28	24·44	22·10	19·77	...	...	...	...	...	...	...	...	...
27·78	24·88	22·51	20·13	...	...	...	...	...	...	...	...	...
28·27	25·33	22·91	20·50	...	...	...	...	...	...	...	...	...
0·66	0·53	0·43	0·35	0·29	0·22	0·17	0·12	0·10	0·08	0·06	0·04	0·03

number given at bottom of column ; for example—The Weight  
12 B. W. G., is 2·78 - 0·29 = 2·49lbs. *f*, full ; *b*, bare.

TABLE 163.—WEIGHT OF SEAMLESS BRASS TUBES 70% OF COPPER AND 30% OF ZINC.  
Specific gravity 8.558. (The Broughton Copper Company.) IMPERIAL WIRE GAUGE, 1884.

1884.		THICKNESS OF BRASS.													WEIGHT OF A LINEAL FOOT IN POUNDS.												
I. W. G.	{ Inches. Millimetres.	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20										
		0.212 $\frac{5}{32}$ b	0.192 $\frac{3}{16}$ f	0.176 $\frac{11}{32}$ f	0.160 $\frac{5}{16}$ f	0.144 $\frac{9}{32}$ f	0.128 $\frac{1}{8}$ f	0.116 $\frac{7}{32}$ f	0.104 $\frac{5}{16}$ b	0.092 $\frac{3}{16}$ f	0.080 $\frac{5}{16}$ f	0.072 $\frac{5}{16}$ b	0.064 $\frac{1}{4}$ f	0.056 $\frac{3}{16}$ b	0.048 $\frac{3}{16}$ f	0.040 $\frac{1}{4}$ b	0.036 $\frac{3}{16}$ f										
		5.385	4.877	4.470	4.064	3.658	3.251	2.946	2.642	2.337	2.032	1.829	1.626	1.422	1.219	1.016	0.914										
External Diameter.																											
Inches.	Millim.																										
$\frac{3}{16}$	9.5	...	...	...	...	...	...	...	...	...	...	...	...	...	0.21	0.18	0.16										
$\frac{7}{16}$	11.1	...	...	...	...	...	...	...	...	...	...	...	...	0.28	0.25	0.22	0.18										
$\frac{1}{2}$	12.7	...	...	...	...	...	...	...	...	...	...	...	...	0.36	0.32	0.29	0.21										
$\frac{9}{16}$	15.9	...	...	...	...	...	...	...	...	...	...	...	...	0.46	0.42	0.37	0.27										
$\frac{5}{8}$	19.0	...	...	...	...	...	...	...	...	...	...	...	...	0.51	0.45	0.39	0.33										
$\frac{3}{4}$	22.2	...	...	...	...	...	...	...	...	...	...	...	...	0.60	0.53	0.46	0.39										
$\frac{7}{8}$	25.4	...	...	...	...	...	...	...	...	...	...	...	...	0.70	0.62	0.53	0.45										
1	28.6	...	...	...	...	...	...	...	...	...	...	...	...	0.86	0.78	0.70	0.62										
$1\frac{1}{8}$	31.7	...	...	...	...	...	...	...	...	...	...	...	...	0.97	0.88	0.79	0.70										
$1\frac{1}{4}$	34.9	...	...	...	...	...	...	...	...	...	...	...	...	1.09	0.99	0.88	0.78										
$1\frac{3}{8}$	38.1	...	...	...	...	...	...	...	...	...	...	...	...	1.21	1.09	0.98	0.86										
$1\frac{1}{2}$	41.3	...	...	...	...	...	...	...	...	...	...	...	...	1.32	1.20	1.07	0.94										
$1\frac{3}{4}$	44.4	...	...	...	...	...	...	...	...	...	...	...	...	1.44	1.30	1.16	1.02										
$1\frac{7}{8}$	47.6	...	...	...	...	...	...	...	...	...	...	...	...	1.56	1.41	1.26	1.10										
2	50.8	...	...	...	...	...	...	...	...	...	...	...	...	1.67	1.51	1.35	1.19										
$2\frac{1}{8}$	54.0	...	...	...	...	...	...	...	...	...	...	...	...	1.79	1.62	1.44	1.27										
		...	...	...	...	...	...	...	...	...	...	...	...	1.90	1.72	1.54	1.35										

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E 164.—WEIGHT OF SEAMLESS BRASS TUBES, CONTAINING 70% OF COPPER AND 30% OF ZINC  
(The Broughton Copper Company). BIRMINGHAM WIRE GAUGE.

B. W. G.		THICKNESS OF BRASS.																	WEIGHT OF LINEAL FOOT IN POUNDS.																
		5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20																		
Inches.	Inches.	0.220	0.203	0.180	0.165	0.148	0.134	0.120	0.109	0.095	0.083	0.072	0.065	0.056	0.049	0.042	0.035	Inches.	Inches.	Inches.	Inches.	Inches.	Inches.												
		$\frac{7}{32}f$	$\frac{13}{64}$	$\frac{3}{16}b$	$\frac{11}{64}b$	$\frac{5}{16}f$	$\frac{9}{64}b$	$\frac{1}{4}b$	$\frac{7}{64}$	$\frac{33}{32}f$	$\frac{5}{16}f$	$\frac{5}{16}b$	$\frac{1}{16}f$	$\frac{1}{16}b$	$\frac{5}{16}f$	$\frac{3}{16}b$	$\frac{3}{32}f$																		
Millimetres.	Millimetres.	5.59	5.16	4.57	4.19	3.76	3.40	3.05	2.77	2.41	2.11	1.83	1.65	1.47	1.24	1.07	0.89																		
External Diameter.																																			
Inches.	Millim.																																		
$\frac{3}{8}$	9.5	...	...	...	...	...	...	...	...	...	...	...	...	...	0.21	0.19	0.16	0.14	...	...	...	...	...												
$\frac{7}{16}$	11.0	...	...	...	...	...	...	...	...	...	...	...	0.28	0.26	0.22	0.19	0.10	...	...	...	...	...	...												
$\frac{1}{2}$	12.7	...	...	...	...	...	...	...	...	...	...	0.36	0.33	0.30	0.26	0.22	0.19	...	...	...	...	...	...												
$\frac{5}{8}$	15.9	...	...	...	...	...	...	...	...	...	0.52	0.46	0.42	0.38	0.33	0.28	0.24	...	...	...	...	...	...												
$\frac{3}{4}$	19.0	...	...	...	...	...	...	...	...	0.72	0.64	0.57	0.52	0.47	0.40	0.35	0.29	...	...	...	...	...	...												
$\frac{7}{8}$	22.2	...	...	...	...	...	...	...	0.97	0.86	0.76	0.67	0.61	0.55	0.47	0.41	0.34	...	...	...	...	...	...												
$1$	25.4	...	...	...	...	...	...	1.23	1.13	1.00	0.89	0.78	0.71	0.64	0.54	0.47	0.39	...	...	...	...	...	...												
$1\frac{1}{8}$	28.6	...	...	...	...	...	1.55	1.40	1.29	1.14	1.01	0.88	0.80	0.72	0.61	0.53	...	...	...	...	...	...	...												
$1\frac{1}{4}$	31.7	...	...	...	...	...	1.74	1.58	1.45	1.28	1.13	0.99	0.90	0.80	0.68	0.59	...	...	...	...	...	...	...												
$1\frac{3}{8}$	34.9	...	...	...	...	...	1.94	1.75	1.61	1.42	1.25	1.09	0.99	0.89	0.76	...	...	...	...	...	...	...	...												
$1\frac{1}{2}$	38.1	...	...	...	...	...	2.33	2.13	1.93	1.77	1.55	1.37	1.20	1.09	0.97	0.83	...	...	...	...	...	...	...												
$1\frac{3}{4}$	41.3	...	...	...	...	...	2.80	2.55	2.33	2.10	1.92	1.69	1.49	1.30	1.18	1.06	...	...	...	...	...	...	...												
$1\frac{7}{8}$	44.4	...	...	...	...	...	3.04	2.76	2.52	2.28	2.08	1.83	1.61	1.41	1.27	1.14	...	...	...	...	...	...	...												
$1\frac{1}{2}$	47.6	...	...	3.55	3.29	2.98	2.72	2.45	2.24	1.97	1.73	1.51	1.37	1.23	...	...	...	...	...	...	...	...	...												
$2$	50.8	...	...	3.81	3.53	3.19	2.91	2.63	2.40	2.11	1.85	1.62	1.46	1.31	...	...	...	...	...	...	...	...	...												

2 1/4	54.0	...	4.54	4.08	3.77	3.41	3.11	2.80	2.56	2.25	1.97	1.72	1.56	1.40	...	...
2 1/2	57.1	...	4.84	4.34	4.01	3.62	3.30	2.98	2.72	2.38	2.09	1.83	1.65	1.48	...	...
2 3/4	60.3	5.52	5.13	4.60	4.25	3.84	3.50	3.15	2.88	2.52	2.21	1.93	1.75	1.56	...	...
2 1/2	63.5	5.84	5.43	4.86	4.49	4.05	3.69	3.33	3.03	2.66	2.34	2.04	1.84	1.65	...	...
2 1/2	66.7	6.16	5.73	5.12	4.73	4.27	3.89	3.50	3.19	2.80	2.46	2.14	1.94	...	...	...
2 1/2	69.8	6.48	6.02	5.39	4.97	4.48	4.08	3.67	3.35	2.94	2.58	2.24	2.03	...	...	...
2 1/2	73.0	6.80	6.32	5.65	5.21	4.70	4.28	3.85	3.51	3.07	2.70	2.35	2.13	...	...	...
3	76.2	7.12	6.61	5.91	5.45	4.91	4.47	4.02	3.67	3.21	2.82	2.45	2.22	...	...	...
3 1/4	79.3	7.44	6.91	6.17	5.69	5.13	4.67	4.20	3.83	3.35	2.94	2.56	2.32	...	...	...
3 1/2	82.5	7.76	7.20	6.43	5.93	5.35	4.86	4.37	3.99	3.49	3.06	2.66	2.41	...	...	...
3 3/4	85.7	8.08	7.50	6.70	6.17	5.56	5.06	4.55	4.15	3.63	3.18	2.77	2.50	...	...	...
3 1/2	88.9	8.40	7.79	6.96	6.41	5.78	5.25	4.72	4.30	3.77	3.30	2.87	2.60	...	...	...
3 1/2	92.0	8.72	8.09	7.22	6.65	5.99	5.45	4.90	4.46	3.90	3.42	2.98	2.69	...	...	...
3 1/2	95.2	9.04	8.38	7.48	6.89	6.21	5.64	5.07	4.62	4.04	3.54	3.08	2.79	...	...	...
3 1/2	98.4	9.36	8.68	7.74	7.13	6.42	5.84	5.25	4.78	4.18	3.66	3.19	2.88	...	...	...
4	101.6	9.68	8.98	8.01	7.37	6.64	6.03	5.42	4.94	4.32	3.79	3.29	2.98	...	...	...
	1.12	0.96	0.74	0.64	0.50	0.41	0.33	0.27	0.21	0.16	0.12	0.10	0.08	0.06	0.05	0.03

*Note.*—If the internal diameter is given, add figure at bottom of Column ; for example—The weight per lineal foot of a Brass Tube 2 ins. internal diameter, 12 B. W. G. is  $2.40 + 0.27 = 2.67$  lb.  $f$ , full ;  $b$ , bare.

W. G.	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
Percentage	96.6	94.8	97.1	97.1	97.4	95.6	96.7	95.4	96.9	96.4	100.0	98.5	96.5	98.0	95.2	102.7

*Note.*—These numbers show the relative weights of Brass Tubes made to the Imperial Wire Gauge, 1884, and the Birmingham Wire Gauge, the latter being taken at 100.

TABLE 165.—COPPER NAILS AND RIVETS : SIZE AND WEIGHT.

Description.	Gauge.	Length.	Weight per 1,000.	
	No.	Inches.	Lb.	Oz.
Copper nails, wrought, clench, flat-head, full countersunk . . .	13	1	2	9
	13	1 $\frac{1}{8}$	2	15
	12	1 $\frac{1}{4}$	4	8
	11	1 $\frac{1}{2}$	6	6
	13	1 $\frac{3}{4}$	4	12
	11	1 $\frac{3}{4}$	7	8
	11	2	8	8
	10	2 $\frac{1}{4}$	12	12
	11	2 $\frac{3}{8}$	10	0
	11	2 $\frac{1}{2}$	10	10
	9	2 $\frac{1}{2}$	17	12
	9	2 $\frac{3}{4}$	19	4
	8	3	25	8
	8	3 $\frac{1}{4}$	28	0
	8	3 $\frac{1}{2}$	29	12
	7	3 $\frac{3}{4}$	36	0
	6	4	48	8
	6	4 $\frac{1}{2}$	55	4
	4	5	82	12
	3	5 $\frac{1}{2}$	108	0
	3	6	119	0
	4	6	107	12
	3	7	136	12
	3	7 $\frac{1}{2}$	146	4
	2	8	189	0
	2	8 $\frac{1}{2}$	199	0
Spike die-heads, with flat points .	12	1 $\frac{1}{2}$	4	12
	10	1 $\frac{3}{4}$	9	8
	9	2	12	0
	7	2 $\frac{1}{2}$	19	10
	6	3	30	0
	4	3 $\frac{1}{2}$	48	0
	2	4 $\frac{1}{2}$	84	8
Rose-heads, with flat points .	14	3 $\frac{3}{4}$	1	9
	13	1	2	4
	13	1 $\frac{1}{4}$	3	0
	12	1 $\frac{1}{2}$	4	6
	10	1 $\frac{3}{4}$	9	8
	10	2	10	12

TABLE 165.—COPPER NAILS AND RIVETS (*continued*).

Description.	Gauge.	Length.	Weight per 1,000.	
	No.	Inches.	Lb.	Oz.
Rose-heads, with flat points . . .	8	$2\frac{1}{4}$	16	14
"                    " . . .	8	$2\frac{1}{2}$	19	8
"                    " . . .	6	3	30	0
"                    " . . .	5	$3\frac{1}{2}$	42	8
"                    " . . .	4	4	53	12
"                    " . . .	3	$4\frac{1}{2}$	71	0
"                    " . . .	2	5	93	0
Clasp . . . . .	...	$2\frac{1}{2}$	13	0
" . . . . .	...	2	9	0
" . . . . .	...	$1\frac{1}{2}$	4	0
" . . . . .	...	$1\frac{1}{4}$	2	10
" . . . . .	...	1	1	12
" . . . . .	...	$1\frac{1}{2}$	...	
Cut copper nails, brads, billed . .	...	$\frac{5}{8}$	0	10
"                    " . . .	...	$\frac{3}{4}$	0	12
"                    " . . .	...	1	1	10
"                    " . . .	...	$1\frac{1}{4}$	2	4
"                    " . . .	...	$1\frac{1}{2}$	3	12
"                    " . . .	...	$1\frac{3}{4}$	5	8
Lightning conductor, countersunk {	6	$1\frac{1}{2}$	10	8
heads, and flat points, jagged . . }	5	$1\frac{3}{4}$	15	0
"                    " . . .	4	2	18	8
"                    " . . .	3	$2\frac{1}{4}$	26	0
"                    " . . .	1	$2\frac{1}{2}$	40	0
"                    " . . .	1	3	52	0
Scarf tacks, square flat-heads, with {	16	$\frac{1}{2}$	0	9
sharp points . . . . . }	16	...	0	11
"                    " . . .	16	$\frac{3}{4}$	1	1
"                    " . . .	15	$\frac{7}{8}$	1	6
Slating . . . . .	...	$1\frac{1}{2}$	...	
Coppersmith's rivets, flat pan-head.	2	$\frac{7}{8}$	22	4
"                    " . . .	4	$\frac{5}{8}$	13	12
"                    " . . .	6	$\frac{5}{8}$	9	12
"                    " . . .	7	$\frac{1}{2}$	6	14
"                    " . . .	10	$\frac{3}{8}$	3	0
"                    " . . .	11	$\frac{5}{16}$	2	4
"                    " . . .	12	$\frac{1}{4}$	1	4
"                    snap-heads .	Inches.			
"                    " . . .	$\frac{1}{2}$	$1\frac{1}{4}$	118	0
"                    " . . .	$\frac{7}{16}$	$1\frac{1}{4}$	91	0
"                    " . . .	$\frac{7}{16}$	1	78	0
"                    " . . .	$\frac{1}{2}$	1	102	0
"                    " . . .	$\frac{3}{8}$	$\frac{7}{8}$	55	0
"                    " . . .	$\frac{3}{8}$	$1\frac{1}{4}$	71	

TABLE 165.—COPPER NAILS AND RIVETS (*continued*).

Description.	Gauge.	Length.	Weight per 1,000.	
	No.	Inches.	Lb.	Oz.
Coppersmith's rivets, tinned for hoses—				
"    hose No. 1 .	8	$\frac{3}{8}$	4	8
"    hose No. 2 .	7	$\frac{7}{16}$	5	12
"    hose No. 3 .	7	8	6	8
"    hose No. 4 .	7	9	7	4
"    hose No. 4 .	7	11	8	4
"    washers for do.—				
"    hose No. 1 .	...	...	2	4
"    hose No. 2 .	...	...	2	12
"    hose No. 3 .	...	...	2	12
"    hose No. 4 .	...	...	3	4

Brazed Copper tubes weigh more per lineal foot than seamless tubes. An exact general multiple cannot be given, as the proportion of difference varies with the thickness, the diameter, and the kind of brazed joint.

Mandrel-drawn brazed Copper tubes weigh the same as Seamless tubes.

TABLE 166.—SHEET LEAD : WEIGHT PER SQUARE FOOT.

Usual size of Sheets, 32 feet  $\times$  7 feet.

Weight per Square Foot.	Thickness.	Weight per Square Foot.	Thickness.
Pounds.	Inch.	Pounds.	Inch.
2½	·042 or $\frac{1}{24}$	5½	·093 or $\frac{1}{11}$ full
3	·051 or $\frac{1}{20}$ full	6	·101 or $\frac{1}{10}$
3½	·059	6½	·110 or $\frac{1}{9}$
4	·067 or $\frac{1}{15}$ full	7	·118 or $\frac{2}{17}$
4½	·076 or $\frac{1}{13}$	7½	·126 or $\frac{1}{8}$ bare
5	·084 or $\frac{1}{12}$ full	8	·135 or $\frac{2}{15}$ full

TABLE 167.—SHEET LEAD. FRENCH PRACTICE.

Usual size of sheets, 2·80 metres and 3·88 metres wide, 8 to 10 metres long (9 feet 2 inches and 12 feet 9 inches wide, 26 feet to 33 feet long).

Thickness.	Weight per Square Metre.	Thickness.	Weight per Square Metre.
Millimetres.	Kilogsrs. or Lbs.	Millimetres.	Kilogsrs. or Lbs.
1	11·25 or 24·8	3	34·00 or 75·0
"	17·00 or 37·5	4	45·40 or 100·1
"	22·70 or 50·1	5	56·80 or 125·2
"	28·40 or 62·6	7	79·50 or 175·3



TABLE 168.—SOLID DR.

(Walkers, Park

SIZES AND WEIGHTS

Bore.	Length.	Weights of One Length for
Inches.	Feet.	Pounds.
$\frac{3}{16}$	15	15
$\frac{1}{4}$	15	10, 15, 20
$\frac{3}{8}$	15	10, 15, 20, 25
$\frac{1}{2}$	15	14, 15, 16, 18, 20, 22, 25, 27, 30, 35
$\frac{9}{16}$	15	16, 18, 20, 22
$\frac{5}{8}$	15	17, 21, 25, 30, 35, 40, 45
$\frac{3}{4}$	15	22, 24, 26, 28, 32, 36, 40, 45, 50, 55
$\frac{7}{8}$	15	28, 36
1	15	30, 36, 42, 45, 48, 52, 56, 60, 64, 70
$1\frac{1}{8}$	15	42, 52, 60, 68, 76
$1\frac{1}{4}$	12	28, 36, 42, 48, 52, 60, 64
$1\frac{1}{2}$	12	28, 36, 48, 56, 60, 72, 84, 96
$1\frac{3}{4}$	12	60, 72, 84, 96
2	12	36, 56, 72, 84, 96, 112, 120
$2\frac{1}{4}$	12	100, 132
$2\frac{1}{2}$	10	60, 70, 84, 96, 112, 120
$2\frac{3}{4}$	10	100
3	10	100, 112, 120, 130, 140, 150
$3\frac{1}{2}$	10	112, 130, 150, 160, 180
4	10	140, 160, 170, 200, 220
$4\frac{1}{2}$	10	140, 170, 220
5	10	150, 220, 250
$5\frac{1}{2}$	10	220
6	10	220

DRAWN SOIL PIPE.		
$2\frac{1}{2}$	10	36, 45, 60, 70
3	10	45, 53, 60, 68, 74, 80
$3\frac{1}{2}$	10	52, 60, 70, 90
4	10	56, 60, 70, 80, 100, 112
$4\frac{1}{2}$	10	70, 80, 90, 100, 112
5	10	75, 88, 100, 112
$5\frac{1}{2}$	10	90, 106
6	10	90, 106

TABLE 165.—COPPER DRAWN LEAD PIPES (*continued*).

DRAWN SQUARE SOIL PIPE.		
Bore.	Length.	Weights of One Length for Various Thicknesses
Inches.	Feet.	Pounds.
$3\frac{1}{2} \times 3\frac{1}{2}$	10	60, 80
$4 \times 3$	10	80, 100

COMPOSITION PIPE (Lead and Tin).		
Diameters, inches . . . . .	$\frac{1}{8}$ , $\frac{3}{16}$ , $\frac{1}{4}$ , $\frac{5}{16}$ , $\frac{3}{8}$ , $\frac{7}{16}$	About $\frac{1}{2}$ cwt. each coil.
Average length of coils, feet . . . . .	670, 240, 220, 170, 150, 120,	
Diameters, inches . . . . .	$\frac{1}{2}$ , $\frac{9}{16}$ , $\frac{5}{8}$ , $\frac{3}{4}$ , $\frac{7}{8}$ , 1, $1\frac{1}{4}$	
Average length of coils, feet . . . . .	100, 90, 70, 70, 60, 50, 40	

TABLE 169.—TIN PLATES : DIMENSIONS AND WEIGHTS.

Description.	Mark.	Dimen- sions of Sheets.	Number of Sheets in a Box.	Weight of each Box.
		Inches.	Sheets.	Pounds.
Common No. 1 . . . . .	IC	$14 \times 10$	225	108
Cross No. 1 . . . . .	IX	$14 \times 10$	225	136
Two crosses No. 1 . . . . .	IXX	$14 \times 10$	225	157
Three crosses No. 1 . . . . .	IXXX	$14 \times 10$	225	178
Four crosses No. 1 . . . . .	IXXXX	$14 \times 10$	225	199
Common No. 1 . . . . .	IC	$14 \times 20$	112	108
Cross No. 1 . . . . .	IX	$14 \times 20$	112	136
Two crosses No. 1 . . . . .	IXX	$14 \times 20$	112	157
Three crosses No. 1 . . . . .	IXXX	$14 \times 20$	112	178
Four crosses No. 1 . . . . .	IXXXX	$14 \times 20$	112	199
Common No. 1 . . . . .	IC	$28 \times 20$	56	108
Cross No. 1 . . . . .	IX	$28 \times 20$	56	136
Two crosses No. 1 . . . . .	IXX	$28 \times 20$	56	157
Three crosses No. 1 . . . . .	IXXX	$28 \times 20$	56	178
Four crosses No. 1 . . . . .	IXXXX	$28 \times 20$	56	199
Common No. 1 . . . . .	IC	$12 \times 12$	225	108
Cross No. 1 . . . . .	IX	$12 \times 12$	225	136
Two crosses No. 1 . . . . .	IXX	$12 \times 12$	225	157
Three crosses No. 1 . . . . .	IXXX	$12 \times 12$	225	178

TABLE 169.—TIN PLATES: DIMENSIONS AND WEIGHTS  
(continued).

Description.	Mark.	Dimen- sions of Sheets.	Number of Sheets in a Box.	Weight of each Box.
		Inches.	Sheets.	Pounds.
Four crosses No. 1 . . .	IXXXX	12×12	225	199
Common doubles . . .	DC	17×12 $\frac{1}{2}$	100	94
Cross doubles . . .	DX	17×12 $\frac{1}{2}$	100	122
Two cross doubles . . .	DXX	17×12 $\frac{1}{2}$	100	143
Three cross doubles . . .	DXXX	17×12 $\frac{1}{2}$	100	164
Four cross doubles . . .	DXXXX	17×12 $\frac{1}{2}$	100	185
Common doubles . . .	DC	17×25	50	94
Cross doubles . . .	DX	17×25	50	122
Two cross doubles . . .	DXX	17×25	50	143
Three cross doubles . . .	DXXX	17×25	50	164
Four cross doubles . . .	DXXXX	17×25	50	185
Common doubles . . .	DC	34×25	25	94
Cross doubles . . .	DX	34×25	25	122
Two cross doubles . . .	DXX	34×25	25	143
Three cross doubles . . .	DXXX	34×25	25	164
Four cross doubles . . .	DXXXX	34×25	25	185
Small common doubles . .	SDC	15×11	200	167
Small cross doubles . . .	SDX	15×11	200	188
Small two cross doubles . .	SDXX	15×11	200	209
Small three cross doubles .	SDXXX	15×11	200	230
Small four cross doubles .	SDXXXX	15×11	200	251
Small common doubles . .	SDC	15×22	100	167
Small cross doubles . . .	SDX	15×22	100	188
Small two cross doubles . .	SDXX	15×22	100	209
Small three cross doubles .	SDXXX	15×22	100	230
Small four cross doubles .	SDXXXX	15×22	100	251

*Note.*—The weights of the cross-marked boxes advance at the rate of 21 pounds per Cross.

TABLE 170.—BLOCK TIN PIPES: WEIGHT PER YARD.

Bore . . .	$\frac{1}{4}$ , $\frac{5}{16}$ , $\frac{3}{8}$ , $\frac{7}{16}$ , $\frac{1}{2}$ , $\frac{5}{8}$ , $\frac{3}{4}$ , $\frac{7}{8}$ , 1 inch.
Weight . . .	7, 9, 11, 14, 17, 23, 30, 38, 48 ounces.

TABLE 171.—ZINC SHEETS : ACCORDING TO THE V.M. ZINC GAUGE.

(Vielle-Montagne Company.)

V. M. Gauge.	Approximate Thickness.		Approximate Weight per Square Foot.			36 in. × 72 in.			36 in. × 84 in.			36 in. × 96 in.					
						Approximate Weight of Sheets.		Sheets per 500 Kilos, or 1102½ Lbs. English, about	Approximate Weight of Sheets.		Sheets per 500 Kilos, or 1102½ Lbs. English, about	Approximate Weight of Sheets.		Sheets per 500 Kilos, or 1102½ Lbs. English, about			
	Thousandths of an Inch.	Metric Equivalent in Thousandths of a Millimetre.	Pounds.	Ounces.	Drachms.	Pounds.	Ounces.		Drachms.	Pounds.		Ounces.	Drachms.				
1	0.004	0.100	...	2	5	Nos. 1 and 2 are only rolled to order and special dimensions.											
2	.006	.141	...	3	4												
3	.007	.171	...	3	15	4	6	14	249	5	2	11	213	5	14	8	187
4	.008	.209	...	4	13	5	6	10	204	6	5	1	175	7	3	8	153
5	.010	.247	...	5	11	6	6	6	172	7	7	7	147	8	8	8	129
6	.011	.291	...	6	11	7	8	6	146	8	12	7	126	10	...	8	110
7	.013	.337	...	7	12	8	11	8	126	10	2	12	108	11	10	...	95
8	.015	.386	...	8	14	9	15	12	110	11	10	6	95	13	5	...	83
9	.018	.450	...	10	5	11	9	10	95	13	8	9	81	15	7	8	71
10	.020	.500	...	11	7	12	13	14	86	15	...	3	73	17	2	8	64
11	.023	.580	...	13	5	14	15	10	74	17	7	9	63	19	15	8	55
12	.026	.660	...	15	2	17	0	4	65	19	13	10	56	22	11	...	49
13	.029	.740	1	...	15	19	0	14	57	22	3	11	50	25	6	8	43
14	.032	.820	1	2	12	21	1	8	52	24	9	12	45	28	2	...	39
15	.038	.950	1	5	12	24	7	8	45	28	8	12	39	32	10	...	34
16	.043	1.080	1	8	12	27	13	8	39	32	7	12	34	37	2	...	30
17	.048	1.210	1	11	11	31	2	6	35	36	5	7	30	41	8	8	27
18	.053	1.340	1	14	11	34	8	6	31	40	4	7	27	46	...	8	24
19	.058	1.470	2	1	11	37	14	6	29	44	3	7	25	50	6	8	22
20	.063	1.600	2	4	10	41	3	4	27	48	1	2	23	54	15	...	20
21	.070	1.780	2	8	12	45	13	8	24	53	7	12	21	61	2	...	18
22	.077	1.960	2	12	14	50	7	12	22	58	14	6	19	67	5	...	16
23	.084	2.140	3	1	1	55	3	2	20	64	6	5	17	73	9	8	15
24	.091	2.320	3	5	3	59	13	6	18	69	12	15	16	79	12	8	14
25	.098	2.500	3	9	5	64	7	10	17	75	3	9	15	85	15	8	13
26	.105	2.680	3	13	7	69	1	14	16	80	10	3	14	92	2	8	12

TABLE 172.—ZINC SHEETS: ACCORDING TO THE ENGLISH ZINC GAUGE.

(London Zinc Mills.)

Gauge No.	Approximate Weight per Square Foot.	Thousandths of an Inch.	7 ft. × 2 ft. 8 in.		7 ft. × 3 ft.		8 ft. × 3 ft.		Nearest Birmingham Wire Gauge.
			Weight per Sheet.	Number of Sheets in 10 Cwt.	Weight per Sheet.	Number of Sheets in 10 Cwt.	Weight per Sheet.	Number of Sheets in 10 Cwt.	
1	24	·004	2 10	427	...	...	...	...	41
2	34	·006	3 13	294	...	...	...	...	38
3	34	·007	...	...	4 15	227	...	...	37
4	44	·008	...	...	6 4	180	...	...	34
5	54	·010	...	...	7 9	148	...	...	31
6	64	·011	7 14	142	8 14	126	10 2	111	30
7	74	·013	9 1	124	10 3	110	11 10	96	29
8	9	·015	10 8	107	11 13	95	13 8	83	28
9	10	·017	11 11	96	13 2	85	15 0	75	27
10	11½	·019	13 7	83	15 2	74	17 4	65	25
11	13	·021	15 3	74	17 1	66	19 8	57	24
12	15	·025	17 8	64	19 11	57	22 8	50	23
13	17	·028	...	...	22 5	50	25 8	44	22
14	19	·031	...	...	24 15	45	28 8	39	21
15	22	·036	...	...	28 14	39	33 0	34	20
16	25	·041	...	...	32 13	34	37 8	30	19
17	28	·046	...	...	36 12	30	42 0	27	18
18	31	·051	...	...	40 11	28	46 8	24	...
19	35	·059	...	...	45 15	24	52 8	21	17
20	39	·065	...	...	51 3	22	58 8	19	16
21	43	·072	...	...	56 7	20	64 8	17	15

Sheets thicker than above are rolled to Birmingham Wire Gauge.

WIRE ROPES. *See* STRENGTH OF MATERIALS (pp. 386--400).

CHAINS AND CHAIN CABLES. *See* STRENGTH OF MATERIALS (pp. 400--408).

## STRENGTH OF MATERIALS.

## Strength of Beams.

The ultimate transverse strength of a cantilever or homogeneous beam of uniform square or rectangular section, fixed at one end and loaded at the other end, is usually expressed by the formula,—

$$W = \frac{bd^2s}{6l} \quad \text{or} \quad \frac{16667bd^2s}{l}$$

$W$  = breaking weight at the end of the beam.

$b$  = breadth of the beam in inches.

$d$  = depth of the beam in inches.

$l$  = length of the beam, between the fixed point and the load, in inches; or the distance apart of two supports.

$s$  = ultimate tensile strength of the beam per square inch.

This formula, it is known, is materially defective, in understating the actual strength.

The correct formula is:—

1. *Beam fixed at one end, loaded at the other end.*

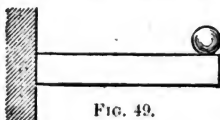


FIG. 49.

$$W = \frac{bd^2s}{3 \cdot 43l} \quad \text{or} \quad \frac{292bd^2s}{l} \quad (1)$$

$$s = \frac{3 \cdot 43Wl}{bd^2} \quad \text{or} \quad \frac{Wl}{292bd^2} \quad (2)$$

A beam freely supported at both ends, and loaded at the middle, bears four times the breaking weight of the cantilever:—

2. *Beam supported at both ends, loaded at the middle.*



FIG. 50.

$$W = \frac{1 \cdot 167bd^2s}{l} \quad (3)$$

$$s = \frac{Wl}{1.167bd^2} \quad (4)$$

A beam fixed at each end, and loaded at the middle, bears eight times the breaking weight of the cantilever :—

3. *Beam fixed at each end, loaded at the middle.*



FIG. 51.

$$W = \frac{2.333bd^2s}{l} \quad (5)$$

$$s = \frac{Wl}{2.333bd^2} \quad (6)$$

Beams on which the load is equally distributed, are capable of a breaking weight double the central load given in the foregoing formulæ :—

4. *Beam fixed at one end, and uniformly loaded.*

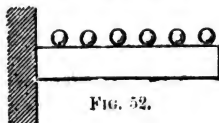


FIG. 52.

$$W = \frac{.583bd^2s}{l} \quad (7)$$

$$s = \frac{Wl}{.583bd^2} \quad (8)$$

5. *Beam supported at both ends, uniformly loaded.*

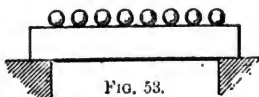


FIG. 53.

$$W = \frac{2.333bd^2s}{l} \quad (9)$$

$$s = \frac{Wl}{2.333bd^2} \quad (10)$$

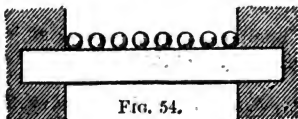
6. *Beam fixed at each end, uniformly loaded.*

FIG. 54.

$$W = \frac{4.667bd^2s}{l} \quad (11)$$

$$s = \frac{Wl}{4.667bd^2} \quad (12)$$

When a concentrated load is applied elsewhere than at the middle of a beam, the breaking weight is inversely proportional to the product  $mn$  of the segments  $m$  and  $n$  into which the beam is divided by the load. The product when the load is at the centre is  $(\frac{1}{2}l)^2$ , and the formula (3), for a beam supported at both ends, becomes—

7. *Beam supported at both ends and loaded at a point between the middle and one end.*

$$W = \frac{1.167bd^2ls}{mn} \quad (13)$$

In like manner—

8. *Beam fixed at each end, and loaded at a point between the middle and one end.*

$$W = \frac{2.333bd^2ls}{mn} \quad (14)$$

The breaking weight of a homogeneous beam of uniform square section, of which one diagonal is vertical, supported at both ends, is expressed by the formula—

9. *Square beam supported at both ends, loaded at the centre ; one of the diagonals vertical.*

$$W = \frac{.943bd^3s}{l} \quad (15)$$

showing that the diagonally placed square beam has only about 81 per cent. of the strength of the square set beam, formula (3).

The breaking weight of a homogeneous uniform cylindrical beam, supported at both ends, is given by the formula—



10. *Cylindrical beam supported at both ends, loaded at the centre.*

$$W = \frac{.726d^3s}{l} \quad . \quad . \quad . \quad . \quad . \quad . \quad (16)$$

It is deducible that the transverse strength of a cylindrical beam is only 90 per cent. of that of a square beam, laid square, of the same sectional area.

The breaking weight of a homogeneous uniform beam of elliptical section, laid with either axis vertical, is as follows :—

11. *Beam of elliptical section, supported at both ends, laid with one axis vertical.*

$$W = \frac{.726bd^2s}{l} \quad . \quad . \quad . \quad . \quad . \quad . \quad (17)$$

in which  $b$  is the length of the horizontal axis, and  $d$  is that of the vertical axis.

The strength of equal flanged or hollow beams may be calculated by the formula :—

*Symmetrical flanged or hollow beam. General formula.*

$$W = \frac{d''s(4a + 1.167a'')}{l} \quad . \quad . \quad . \quad . \quad . \quad . \quad (18)$$

$a$  = the sectional area of one flange, in square inches.

$a''$  = the area of the vertical web, or webs, in square inches, the reputed vertical height of the web being taken, for calculation, equal to the depth of the beam minus the thickness of one flange.

$d''$  = the reputed depth, equal to that of the web.

$s$  = the ultimate tensile strength in tons per square inch.

$l$  = the span in inches.

$W$  = the breaking load in tons at the centre.

For the strength of cast-iron flange beams, the following formula is applicable in which the tensile strength is taken as 7 tons per square inch :—

*Ultimate transverse strength of cast-iron beams.*

$$W = \frac{d''(7a + 2a'')}{3l} \quad . \quad . \quad . \quad . \quad . \quad . \quad (19)$$

$W$  = breaking weight in tons at the middle.

$a$  = sectional area of the lower flange, square inches.

$a''$  = sectional area of the web, taken at the reputed depth (total depth minus thickness of lower flange), square inches.

$l$  = span in feet.

For various tensile strengths per square inch, the following are the constants to be employed in the formula:—

Tons per Square Inch.		Constants in formula (19) for $a$	for $a''$ .
6	.	6	1.7
6½	.	6½	1.9
7	.	7	2.0
7½	.	7½	2.2
8	.	8	2.3
9	.	9	2.6
10	.	10	2.9

*Ultimate transverse strength of solid rolled joists, of wrought iron (approximate).*

$$W = \frac{7d(a + \frac{1}{4}a'')}{l} \quad (20)$$

*Note.*—The sectional area of the web ( $a''$ ) is, in this case, taken for the whole depth of the joist.

2. The ultimate tensile strength of the metal is taken at 20 tons per square inch.

3. For iron or steel of other than 20 tons tensile strength per square inch, substitute  $\frac{1}{3}$ rd of the other tensile strength, for the constant 7 in the formula.

*Ultimate transverse strength of riveted wrought-iron girders (approximate).*

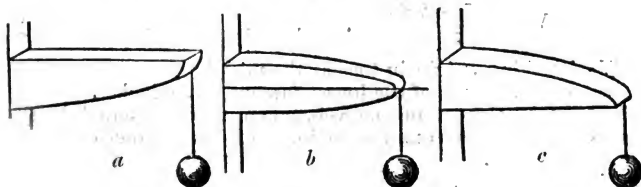
$$W = \frac{4\frac{1}{3}d(a' + \frac{1}{4}a'')}{l} \quad (21)$$

### Cantilevers and Beams of Uniform Strength.

The basic forms, exclusive of provision for shearing resistance, are as follows:—

1. *Cantilevers of uniform transverse strength, loaded at one end.*

1. When a cantilever is rectangular in section, it may be of either of the parabolic forms  $a$ ,  $b$ ,  $c$ , figs. 55—57.

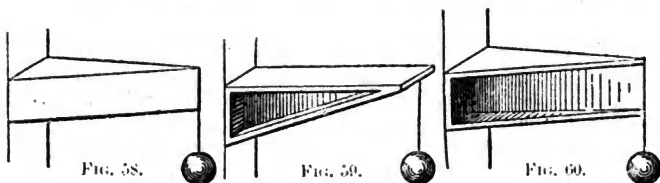


FIGS. 55—57.

2. When the section, fig. 58, is rectangular and the depth is constant, the breadth is in proportion to the distance from the end of the beam, and the beam is triangular in plan.

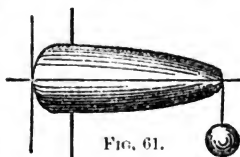
3. When the section is double-flanged, as in fig. 59, or hollow rectangular, and the breadth uniform, the form of the beam, in side elevation, is triangular, supposing that the resistance of the web is not calculated.

4. A double-flanged semi-beam, fig. 60, or hollow beam rect-



angular in section, of uniform depth, is triangular in plan, when calculated for the flanges only.

5. When the section of the semi-beam is circular, the outline is formed by the revolution of a cubic parabola on its axis, fig. 61.



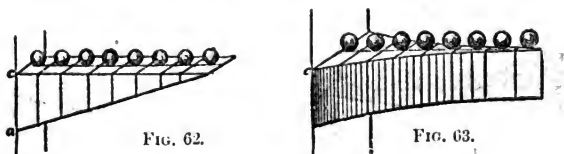
6. When the section of the semi-beam is annular, the form is generated by the revolution of a parabola on its axis. If the thickness varies with the diameter, the semi-beam is cubic-parabolic.

## 2. *Cantilevers of uniform strength, uniformly loaded.*

1. Rectangular in section, breadth uniform, triangular in side elevation, fig. 62.

2. Rectangular in section, depth uniform, breadth parabolic, fig. 63.

3. Hollow rectangular, or double-flanged, breadth uniform, depth parabolic, not reckoning webs, fig. 64.



4. Hollow rectangular, or double-flanged, depth uniform, breadth parabolic, fig. 65.

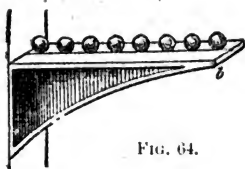


FIG. 64.

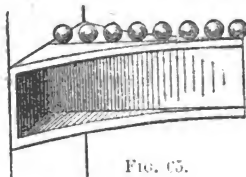


FIG. 65.

5. Section circular. The form is generated by the revolution of a semi-cubic parabola on its axis.

6. Section annular, conical form.

3. *Beams of uniform strength, loaded at the middle.*

1. Rectangular in section, breadth uniform, depth double-parabolic.

2. Rectangular in section, depth uniform, breadth double-triangular.

3. Hollow rectangular or double-flanged, breadth uniform, depth double-triangular, figs. 66, 67.



FIG. 66.



FIG. 67.

4. Hollow rectangular or double-flanged, depth uniform, breadth double-triangular, fig. 68.

5. Circular section ; form double-parabolic, fig. 69.

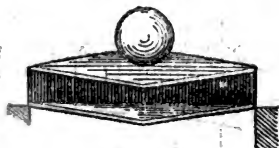


FIG. 68.



FIG. 69.

#### 4. Beams of uniform strength, uniformly loaded.

1. Rectangular section, breadth uniform, depth elliptical.
2. Rectangular section, depth uniform, breadth double-



FIG. 70.

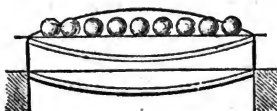


FIG. 71.

parabolic ; two parabolas having their vertices at the middle, and meeting at the points of support.

3. Hollow rectangular or double-flanged, breadth uniform, depth parabolic, fig. 70.

4. Hollow rectangular or double-flanged, depth uniform, breadth double-parabolic, fig. 71.

#### Approximate Deflection of Beams

In a beam of uniform depth and uniform strength, the form assumed under the load is that of a circular arc.

Let  $l$  = length of the span, or distance between the supports.

$b$  = breadth of the beam at the middle.

$d$  = depth of the beam at the middle.

$E$  = coefficient of elasticity, or the denominator of the fraction of the length by which the beam is extended or compressed per ton of direct stress per square inch of section.

$D$  = deflection of beam, at middle.

#### Deflection of Beams of Rectangular Section, supported at each End.

1. Rectangular section, of uniform strength, depth uniform, double-triangular in plan, load at the middle :—

$$D = \frac{Wl^3}{4 \cdot 67 b d^3 E} \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad \cdot \quad (22)$$

This formula signifies that the deflection varies directly as the weight, and as the cube of the span ; and that it varies inversely as the breadth, and as the cube of the depth, and as the coefficient of elasticity.

2. Rectangular beam, of uniform strength, breadth uniform, depth parabolic ; load at the middle.

$$D = \frac{Wl^3}{3 \cdot 11 bd^3 E} \quad (23)$$

3. Rectangular beam, of uniform section ; load at the middle.

$$D = \frac{Wl^3}{4 \cdot 67 bd^3 E} \quad (24)$$

4. Rectangular beam, of uniform strength ; depth uniform, uniformly loaded.

$$D = \frac{Wl^3}{9 \cdot 33 bd^3 E} \quad (25)$$

5. Rectangular beam, of uniform strength, breadth uniform ; elliptic in depth ; uniformly loaded.

$$D = \frac{Wl^3}{7 \cdot 47 bd^3 E} \quad (26)$$

6. Rectangular beam, of uniform section ; uniformly loaded.

$$D = \frac{Wl^3}{7 \cdot 47 bd^3 E} \quad (27)$$

### Deflection of Double-flanged or Hollow Rectangular Beams : Equal Flanges.

7. Double-flanged beam, of uniform strength ; uniform depth, double-triangular in breadth ; load at the middle.

*Case 1.* When the strength of both the flanges and the web is calculated :—

$$D = \frac{Wl^3}{4d''^2 E(4a + 1 \cdot 167a'')} \quad (28)$$

$d''$  = distance apart between centres of flanges.

$a$  = sectional area of one flange.

$a''$  = sectional area of the web, reckoned equal in height to  $d''$ .

From this equation it is inferred that the deflection varies inversely as a power of the depth greater than the square, and less than the cube.

*Case 2.* When the strength of the flanges alone is calculated :—

$$D = \frac{Wl^3}{16ad''^2 E} \quad (29)$$

8. Double-flange beam, of uniform strength, of uniform breadth, triangular in depth; loaded at the middle (figs. 66; 67).

*Case 1.* When the strength of both the flanges and the web is calculated:—

$$D = \frac{Wl^3}{2a''^2E(4a + 1.167a'')} \quad (30)$$

*Case 2.* When the strength of the flanges alone is calculated:—

$$D = \frac{Wl^3}{8ad''^2E} \quad (31)$$

9. Double-flange beam, of uniform section, loaded at the middle. See No. 7, formulæ 28 and 29.

10. Double-flange beam, of uniform strength, of uniform depth, breadth parabolic; uniformly loaded.

*Case 1.* When the strength of both the flanges and the web is calculated:—

$$D = \frac{Wl^3}{8d''^2E(4a + 1.167a'')} \quad (32)$$

*Case 2.* When the strength of the flanges only is calculated:—

$$D = \frac{Wl^3}{32ad''^2E} \quad (33)$$

11. Double-flange beam, of uniform strength, of uniform breadth, depth parabolic; uniformly loaded (fig. 70).

*Case 1.* When the strength of both the flanges and the web is calculated:—

$$D = \frac{Wl^3}{5.33d''^2E(4a + 1.167a'')} \quad (34)$$

*Case 2.* When the strength of the flanges only is calculated:—

$$D = \frac{Wl^3}{21.33ad''^2E} \quad (35)$$

12. Double-flange beam, of uniform section, uniformly loaded.

*Case 1.* When the strength of both the flanges and the web is calculated:—

$$D = \frac{Wl^3}{6.4d''^2E(4a + 1.167a'')} \quad (36)$$

*Case 2.* When the strength of the flanges only is calculated :—

$$D = \frac{Wl^3}{25 \cdot 6d^3 E} \quad (37)$$

*Note.*—The last-named beam—of uniform section, uniformly loaded—is the most frequently occurring in practice, in the character of rolled wrought-iron joists.

### Transverse Strength of Uniform Hollow Cylindrical Beams.

The transverse strength of a hollow cylinder is, of course, less than that of a solid cylinder of the same external diameter. The following coefficients may be substituted in formula (16) here repeated, with its converse, to find approximately the ultimate transverse strength of hollow cylinders, having bores of from  $\frac{1}{4}$ th to  $\frac{3}{4}$ ths of the external diameter of the cylinder :—

*Solid cylindrical beam.*

$$W = \frac{.726d^3s}{l} \quad (38)$$

$$s = \frac{Wl}{.726d^3} \quad (39)$$

*Coefficients to be substituted in the formula for bores of various proportions.*

					In parts of that of solid beam.	
					Coefficient.	Per cent.
Solid cylindrical beam . . . . .					.726	100
Hollow cylindrical beam, bore $\frac{1}{4}$ th of external (18) diameter }					.689	95
"	"	"	"	$\frac{1}{2}$	.614	84.6
"	"	"	"	$\frac{3}{4}$	.535	73.7
"	"	"	"	$\frac{1}{2}$	.452	62.2
"	"	"	"	$\frac{3}{4}$	.365	50.3
"	"	"	"	$\frac{1}{2}$	.269	37.0
"	"	"	"	$\frac{3}{4}$	.160	22.0

### Torsional Strength of Bars and Shafts.

The resistance of shafting to twisting or torsional stress is dependent upon its resistance to shearing stress. The ultimate torsional resistance of a uniform cylindrical bar or shaft is expressed by the following formulæ :—



*Torsional Strength of a solid cylindrical shaft.*

$$WR = .196d^3s \quad (40)$$

$$W = \frac{.196d^3s}{R} \quad (41)$$

The ultimate torsional resistance of a hollow cylindrical shaft is expressed by the formulæ :—

*Torsional Strength of a hollow cylindrical shaft.*

$$WR = \frac{.196(d^4 - d'^4)s}{d} \quad (42)$$

$$W = \frac{.196(d^4 - d'^4)s}{Rd} \quad (43)$$

$W$  = force applied at the end of the radius  $R$ , in tons.

$R$  = length of radius at the end of which the force  $W$  is applied, at right angles, in inches.

$d$  = diameter of the bar or shaft, in inches.

$d'$  = diameter of the interior of a hollow shaft in inches.

$b$  = breadth of side of square shaft.

$s$  = ultimate shearing resistance, in tons per square inch of section.

When the section of a hollow bar, as a tube, is thin, comparatively to the diameter, the following formula may be employed :—

*Torsional Strength of a thin tube.*

$$WR = 1.571d^2ts \quad (44)$$

$$W = \frac{1.571d^2ts}{R} \quad (45)$$

*Torsional Strength of a solid square bar or shaft.*

$$WR = .281b^3s \quad (46)$$

$$W = \frac{.281b^3s}{R} \quad (47)$$

TABLE 173.—ULTIMATE STRENGTH OF COLUMNS OF VARIOUS CONSTRUCTION, WITH FLAT ENDS.

Description of Column.	Formula.	Authority.
1. Round cast-iron, solid or hollow . . . . .	$W = \frac{36a}{1 + \frac{r^2}{400}}$	Gordon.
2. Rectangular cast-iron, solid or hollow . . . . .	$W = \frac{36a}{1 + \frac{r^2}{500}}$	Gordon.
3. Rectangular wrought-iron, solid . . . . .	$W = \frac{16a}{1 + \frac{r^2}{3000}}$	Stoney.
4. Angle, tee, channel, or cruciform iron . . . . .	$W = \frac{19a}{1 + \frac{r^2}{900}}$	Unwin.
5. Solid round, mild steel . . . . .	$W = \frac{3a}{1 + \frac{r^2}{1400}}$	Baker.
6. Solid round, strong steel . . . . .	$W = \frac{51a}{1 + \frac{r^2}{900}}$	Baker.
7. Solid rectangular, mild steel . . . . .	$W = \frac{30a}{1 + \frac{r^2}{2480}}$	Baker.
8. Solid rectangular, strong steel . . . . .	$W = \frac{51a}{1 + \frac{r^2}{1600}}$	Baker.

W = breaking weight, in tons.

a = sectional area of the material, in square inches.

r = ratio of length to diameter. The diameter for calculation is the shortest diameter of the section.

### Transverse Strength of Railway Rails.

The ordinary double-head rail, having heads of equal form and size, may be separated into the web for the whole depth, and the flange or overhung portion. The sectional area of

the flange portions can be ascertained by dividing them into narrow horizontal strips, calculating the area of each strip separately, and taking the sums.

*Transverse strength of a double-head rail.*

$$W = \frac{s(4a'd''^2 + 1.167t'd^2)}{l} \quad (48)$$

$W$  = breaking weight at the middle, in tons.

$a'$  = net sectional area of one flange, in inches (excluding the central portion pertaining to the web).

$d$  = total depth of the rail, in inches.

$d''$  = vertical distance apart of the centres of the flanges.

$t'$  = thickness of the web.

$l$  = length of span, between supports, in inches.

$s$  = ultimate tensile strength, in tons per square inch.

### Strength of Steel Springs.

The elasticity or deflection of laminated springs, with the working strength, are given by the following formulæ:—

$$E = \frac{1.66l^3}{bt^3n} \quad (49)$$

$$s = \frac{bt^2n}{11.3l} \quad (50)$$

$$n = \frac{1.66l^3}{Et^3} \quad (51)$$

$E$  = elasticity, or deflection, in sixteenths of an inch per ton of load.

$s$  = working strength, or load, in tons.

$l$  = span, when loaded, in inches.

$b$  = breadth of plates, in inches, taken as uniform.

$t$  = thickness of plates, in sixteenths of an inch.

$n$  = number of plates.

*Note.*—The span and the elasticity are those due to the spring when weighted.

2. When extra thick back and short plates are used, they must be replaced by an equivalent number of plates of the ruling thickness, prior to the employment of the formulæ 49 and 50. This is found by multiplying the number of extra thick plates by the cube of their thickness, and dividing by the cube of the ruling thickness. Conversely, the number of plates of the ruling thickness given by formula 51, requir



TABLE 174.—TENSILE AND COMPRESSIVE STRENGTH OF TIMBER.

Woods.	Specific Gravity.	Tensile Resistance per Square Inch.	Crushing Resistance per Square Inch.
		Tons.	Tons.
Oak, English . . . .	Water = 1. ·858, 893	1·713, 3·380	3·337
„ French . . . .	·976	3·617	3·547
„ Dantzig . . . .	·838	1·882	3·344
„ American White . .	·969	3·143	2·709
„ African (or Teak) .	·971	3·148	...
Teak, Moulmein . . .	·777	1·474	2·559
Iron Wood, Burmah . .	1·176	4·311	5·208
Greenheart . . . .	1·141	3·937	6·438
Sabicu . . . .	·917	2·481	3·776
Mahogany, Spanish . .	·765	1·692	2·863
„ Honduras . . . .	·659	1·338	2·853
Eucalyptus, Tewart . .	1·169	4·591	4·174
„ Mahogany . . . .	·996	1·312	3·198
„ Iron Bark . . . .	1·150	3·740	4·601
„ Blue Gum . . . .	1·049	2·700	3·078
Ash, English . . . .	·750	1·687	3·109
„ Canadian . . . .	·588	2·453	2·453
Beech . . . .	·705	2·166	...
Elm, English . . . .	·642	2·437	2·583
„ Rock, Canada . . .	·748	4·100	3·832
Hornbeam . . . .	·819	2·860	3·711
Fir, Dantzig . . . .	·603	1·442	3·102
„ Riga . . . .	·553	1·808	2·342
„ Spruce . . . .	·484	1·756	2·166
Larch, Russia . . . .	·649	1·876	2·596
Cedar . . . .	·469	1·281	2·000
Red Pine . . . .	·553	1·207	2·537
Yellow Pine . . . .	·551	1·120	1·877
Pitch Pine . . . .	·659	2·083	2·885
Kauri Pine . . . .	·544	1·803	2·867

The elastic tensile strength of timber is equal to, or nearly equal to, the ultimate tensile strength. Of Baltic timber, the elastic compressive strength is from 80 per cent. to 90 per cent. of the ultimate compressive resistance.

#### Columns of Timber.

From observations of the crushing resistance of columns

wood, Mr. Laslett deduced that the maximum resistance of square pieces to compression is exerted when the sectional area in square inches is to the length in inches proportionally as 4 is to 5, for equal seasoning and equal specific gravities. In this ratio, the maximum resistance to crushing of 12-inch square balks on end, would be exerted for a length of 15 feet.

### Timber Files.

TABLE 175.—ULTIMATE STRENGTH OF TIMBER COLUMNS.  
(Brereton and Stoney.)

Ratio of Length to Least Breadth.	Ultimate Weight that can be borne per Square Foot of Section.	Ratio of Length to Least Breadth.	Ultimate Weight that can be borne per Square Foot of Section.
	Tons.		Tons.
10	120	35	84
15	118	40	80
20	115	45	77
25	100	50	75
30	90		

### Transverse Strength of Timber Beams, of Large Scantling, supported at the Ends, Loaded at the Middle.\*

$$\text{Fir} \quad . \quad . \quad . \quad W = \frac{1.78bd^2}{l} \quad . \quad . \quad (53)$$

$$\text{Red pine} \quad . \quad . \quad . \quad W = \frac{1.39bd^2}{l} \quad . \quad . \quad (54)$$

$$\text{Quebec yellow pine} \quad . \quad W = \frac{1.39bd^2}{l} \quad . \quad . \quad (55)$$

$$\text{Pitch pine} \quad . \quad . \quad . \quad W = \frac{2.12bd^2}{l} \quad . \quad . \quad (56)$$

$$\text{English oak} \quad . \quad . \quad W = \frac{1.64bd^2}{l} \quad . \quad . \quad (57)$$

$$\text{French oak} \quad . \quad . \quad W = \frac{2.24bd^2}{l} \quad . \quad . \quad (58)$$

W = breaking weight in tons.

b = breadth in inches.

d = depth in inches.

l = span in inches.

\* *Manual of Rules, Tables and Data*, page 550.

**Deflection of Timber Beams of large Scantling, supported at the Ends, loaded at the Middle.**

$$\text{Fir} \quad . \quad . \quad . \quad . \quad D = \frac{Wl^3}{bd^3} \quad . \quad . \quad (59)$$

$$\text{Red pine} \quad . \quad . \quad . \quad D = \frac{Wl^3}{2434bd^3} \quad . \quad . \quad (60)$$

$$\text{Quebec yellow pine} \quad . \quad D = \frac{Wl^3}{2084bd^3} \quad . \quad . \quad (61)$$

$$\text{Pitch pine} \quad . \quad . \quad . \quad D = \frac{Wl^3}{2968bd^3} \quad . \quad . \quad (62)$$

$$\text{English oak} \quad . \quad . \quad D = \frac{Wl^3}{1848bd^3} \quad . \quad . \quad (63)$$

$$\text{French oak} \quad . \quad . \quad D = \frac{Wl^3}{2656bd^3} \quad . \quad . \quad (64)$$

**STRENGTH OF CAST-IRON.**

The strength of cast-iron varies according to the distribution and massiveness of the metal. Thicker pieces are less strong than thinner pieces : an inequality which arises from the fact that the outer portions, at and near the surface of a casting, are denser, harder, and stronger than the central portions.

The tensile strength of cast-iron may be taken generally as equal to from 6 tons to 7 tons per square inch of section. Dr. Anderson deduced an average of 6 tons from a long series of tests. Mr. Hodgkinson, comparing the tensile strengths of bars of cast-iron 1 inch, 2 inches, and 3 inches square, found that they were relatively, per square inch, as 100, 66, and 60.

The ultimate compressive strength of cast-iron was determined by Mr. Hodgkinson to average  $38\frac{1}{2}$  tons per square inch.

The tensile strength of cast-iron is increased by re-melting. Sir Frederick Bramwell proved that the tensile strength of Acadian iron was increased from  $7\frac{1}{2}$  tons to  $18\frac{1}{2}$  tons by 8 hours of continued fusion and re-melting. The compressive strength averaged  $3\frac{1}{2}$  times the tensile strength. Sir Wm. Fairbairn increased the compressive strength of Eglinton hot-blast iron from 44 tons to 88 tons per square inch.

Cast-iron under tension or compression does not exhibit any well-defined elastic limit. Mr. Hodgkinson tested 1-inch square bars of cast-iron, 10 feet long, under a load of 5 tons in tension, the bar extended  $\frac{1}{674}$ th part of its length; under the same load in compression, the bar extended  $\frac{1}{1105}$ th part of its length. In round numbers, it may be taken that elastic extension and elastic compression are each approximately  $\frac{1}{1000}$ th part of the length, under a stress of 5 tons per square inch, or  $\frac{1}{20000}$ th part of the length per ton per square inch, which is more than twice the rate of elastic extension of iron or of steel.

### *Influence of High Temperature.*

Cast-iron of average quality loses strength when heated above 120° F. ; and it becomes insecure at the freezing-point. At a red heat, its normal strength is reduced one-third.

### *Malleable Cast-iron.*

Cast-iron is rendered malleable by the extraction of part of the constituent carbon, approximating it to wrought-iron. The tensile strength of annealed malleable cast-iron is equivalent to over 25 tons per square inch ; and 10 tons load per square inch is borne without distortion.

### *Columns.*

TABLE 176.—SAFE LOAD ON HOLLOW CAST-IRON COLUMNS, WITH FLAT ENDS AND BASE PLATES : LENGTH=20 TO 30 DIAMETERS.

(Shields.)

Thickness.	Load per Square Inch of Sectional Area of Metal.	
	Length 20 to 24 Diameters.	25 to 30 Diameters.
Inch.	Tons.	Tons.
$\frac{3}{4}$ and upwards	2	$1\frac{3}{4}$
$\frac{5}{8}$	$1\frac{3}{4}$	$1\frac{1}{2}$
$\frac{3}{8}$	$1\frac{1}{2}$	$1\frac{1}{4}$
$\frac{1}{2}$	$1\frac{1}{4}$	1







TABLE 177.—CAST-IRON COLUMNS (*continued*).

Thickness of Metal.	MEAN EXTERNAL DIAMETER OF COLUMN, IN INCHES.											
	15				16				17			
	Area.	Weight per Lineal Foot.	Safe Load.		Area.	Weight per Lineal Foot.	Safe Load.		Area.	Weight per Lineal Foot.	Safe Load.	
Ins.	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.
1	63.62	200.4	127.2	68.33	215.2	136.7	73.04	230.1	146.1	77.75	245.9	155.5
1 1/4	73.03	230.0	146.1	78.34	246.7	156.7	83.84	264.1	167.7	89.34	281.4	178.7
1 1/2	81.68	257.3	162.4	87.96	277.1	175.9	94.25	296.9	188.5	100.53	316.7	201.1
2	90.12	283.9	180.2	97.19	306.1	194.4	104.26	328.4	208.5	111.33	350.7	222.7
2 1/4	98.17	308.2	196.3	106.03	334.0	212.1	113.88	358.7	227.8	121.74	383.48	243.5
2 1/2	105.83	323.4	211.7	114.47	360.6	228.9	123.11	387.8	246.2	131.75	415.01	263.5
3	113.10	350.3	226.2	122.52	385.9	245.0	131.95	415.6	263.9	141.37	445.3	282.7
	20				21				22			
	Area.	Weight per Lineal Foot.	Safe Load.		Area.	Weight per Lineal Foot.	Safe Load.		Area.	Weight per Lineal Foot.	Safe Load.	
	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.
1	59.69	188.0	119.3	62.83	197.9	125.7	65.97	207.8	131.9	69.11	217.7	138.2
1 1/4	73.63	231.9	147.3	77.56	244.3	155.1	81.48	256.6	162.9	85.41	269.0	170.8
1 1/2	87.18	274.6	174.4	91.89	289.4	183.8	96.61	304.3	193.2	101.31	319.1	202.6
2	100.33	311.5	200.7	105.83	323.4	211.7	111.33	350.7	222.7	116.83	368.0	233.7
2 1/4	113.1	356.2	226.2	119.38	376.0	238.7	125.66	395.8	251.3	131.94	415.6	263.9
2 1/2	125.47	395.2	251.9	132.54	417.5	265.1	139.60	439.7	279.2	146.67	462.0	293.3
3	137.44	432.9	274.9	145.30	457.7	290.6	153.15	482.4	306.3	161.01	507.2	322.0
	149.03	469.4	298.1	157.67	496.7	315.3	166.30	523.8	332.6	174.95	551.1	349.9
	160.22	504.7	320.4	169.65	534.4	339.3	179.07	564.1	358.1	188.50	593.8	377.0
	24				28				32			
	Area.	Weight per Lineal Foot.	Safe Load.		Area.	Weight per Lineal Foot.	Safe Load.		Area.	Weight per Lineal Foot.	Safe Load.	
	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.	Sq. Ins.	Lbs.	Tons.
1	72.26	227.6	144.5	89.34	281.4	178.7	106.03	334.0	212.1	122.32	385.3	244.6
1 1/4	89.34	281.4	178.7	106.03	334.0	212.1	122.32	385.3	244.6	138.23	435.4	276.5
1 1/2	106.03	334.0	212.1	122.32	385.3	244.6	138.23	435.4	276.5	153.74	494.3	307.5
2	122.32	385.3	244.6	138.23	435.4	276.5	153.74	494.3	307.5	168.86	531.9	337.7
2 1/4	138.23	435.4	276.5	153.74	494.3	307.5	168.86	531.9	337.7	183.59	578.3	367.1
2 1/2	153.74	494.3	307.5	168.86	531.9	337.7	183.59	578.3	367.1	197.92	623.4	395.8

**Transverse Strength of Cast-Iron.**

The strength of beams of cast-iron varies very much according to the scantling. The breaking weight of 1-inch square bars of cast-iron supported at the ends, loaded at the middle, as tested by Mr. Barlow, and subsequently by Mr. Robert Stephenson, was expressed by the formula (65).

$$W = \frac{bd^2}{l} \times 13.6 \quad . \quad . \quad . \quad (65)$$

in which  $W$  is the breaking weight in tons, and  $b$ ,  $d$ , and  $l$ , are the breadth, depth, and length of span in inches. With 12 for a co-efficient, the formula shows that the breaking weight of a 1-inch square bar, at 12 inches of span, is just one ton; and if the span be expressed in feet, the formula (66) becomes

$$W = \frac{bd^2}{l} \quad . \quad . \quad . \quad (66)$$

in which  $b$  and  $d$  are in inches, and  $l$  in feet.

For the reason given, no constant coefficient can be employed with accuracy. The subjoined formulæ (67) and (68) give results which may safely be taken; for a minimum factor of 7 tons tensile strength per square inch, with a wide margin in excess.

*Ultimate strength of rectangular bars of ordinary cast-iron, freely supported, loaded at the middle.*

$$W = \frac{8bd^2}{l} \quad . \quad . \quad . \quad (67)$$

*Ultimate strength of round bars of cast-iron.*

$$W = \frac{5d^3}{l} \quad . \quad . \quad . \quad (68)$$

$W$ , load in tons;  $b$ ,  $d$ , and  $l$  in inches.

**Deflection of Cast-iron Rectangular Bars of Uniform Section Loaded at the Middle.**

$$D = \frac{Wl^3}{28000bd^3} \quad . \quad . \quad . \quad (69)$$

$D$  the deflection, and  $b$ ,  $d$ , and  $l$  the breadth, depth, and span; all in inches.

**Torsional Strength of Cast-Iron.**

$$\text{Solid round shaft} \quad . \quad . \quad WR = 1.372d^3 \quad . \quad . \quad (70)$$

$$\text{Hollow round shaft} \quad . \quad . \quad WR = \frac{1.372(d^4 - d'^4)}{d} \quad . \quad . \quad (71)$$

$$\text{Square shaft} \quad . \quad . \quad . \quad WR = 1.967b^3 \quad . \quad . \quad (72)$$

$W$  = force applied, in tons.

$R$  = radius of force, in inches.

$d$  and  $d'$  = external and internal diameters, in inches.

$b$  = side of square, in inches.

These formulæ are based on a tensile strength of cast-iron equal to 7 tons per square inch.

**STRENGTH OF WROUGHT-IRON.***Mr. D. Kirkaldy's Early Experiments.*

From the original and extensive results of Mr. David Kirkaldy's test-trials of bars and plates for tensile strength, the following summary results are obtained. His specimen bars were formed with a head at each end, with a clear length of 7 inches. The elongation or extension of the bars is added:

TABLE 178.—ULTIMATE TENSILE STRENGTH OF ROUND BAR IRON. (Mr. Kirkaldy.)

Bars.	Tons per Square Inch.	Extension before Fracture.
Yorkshire rolled bars . . . . .	27.39	25.2 per cent.
Staffordshire " . . . . .	25.90	23.5 "
Lanarkshire " . . . . .	26.55	19.4 "
Rivet Iron " . . . . .	26.00	20.5 "
Average . . . . .	26.46	22.2 per cent.
Hammered scrap, forged down . . . . .	23.85	24.8 per cent.
Crank shaft, scrap iron, with fibre . . . . .	20.37	21.8 "
" " across fibre . . . . .	18.55	12.5 "
Armour plate, across fibre . . . . .	16.92	9.0 "

The contracted sectional area of specimens tested to fracture, varied considerably, from 29.5 per cent. of the original area for Swedish charcoal iron bars to 85.2 per cent. for common Scotch iron bars. Thus—

Iron.	Fractured Sectional Area.
Swedish charcoal . . . .	29.5 per cent.
Staffordshire charcoal . . . .	38.4 "
Yorkshire, Lowmoor . . . .	46.3 "
Staffordshire, B. B. Scrap . . . .	47.6 "
" S. C. Crown . . . .	53.4 "
Scotch, extra best best . . . .	58.5 "
" best best . . . .	68.9 "
" common . . . .	71.6 "
" common . . . .	85.2 "

The strength as the diameter was reduced by rolling down from  $1\frac{1}{4}$  to  $\frac{1}{2}$  inch, and intermediate sizes, was increased 19 per cent., or from 22.38 tons to 26.65 tons per square inch; whilst the extension was reduced from 28.3 per cent. to 23.8 per cent.

The strength of  $1\frac{1}{4}$  inch rolled bars, turned down to 1 inch in diameter, was increased 5 per cent.; and the extension was augmented from 17.2 per cent. to 19.3 per cent.

Four  $1\frac{1}{4}$  inch round bars, reduced by forging to 1 inch and  $\frac{3}{4}$  inch in diameter, showed an increase of 4 per cent. of strength; and the extension was reduced from 24.5 per cent. to 17.3 per cent.

Five different 1 inch bars, when reheated for repair, showed 3.8 per cent. less tensile strength; and the extension was increased from 10.1 per cent. to 32.6 per cent.

Two pieces of a  $\frac{3}{4}$  inch bar of iron were tested:—one in the ordinary condition; the other after having been heated to a welding heat, and cooled slowly. The strength was not materially affected, and the extension was reduced from 22.3 per cent. to 17.7 per cent.

To test the influence of intense cold, three pieces of a  $\frac{3}{4}$  inch bar were tested: one at 64° F., the others at 23° F. The colder bars broke with 2.4 per cent. less load; and with an extension of 23 per cent., against 24.9 per cent. at 64° F.

To test the effect of notching a bar, several 1 inch round bars of different makes were notched or grooved to a diameter of .7 inch, and broken at the notch; then turned down in the body to the same diameter, and broken through the body. The average tensile strengths per square inch, and the corresponding contracted sectional areas, were as follows:—

	Tensile Strength per Square Inch.	Contracted Sectional Area.
Notched . . . .	32.91 tons	85 per cent.
Turned down . . . .	27.61 "	58.4 "
Rough bar . . . .	26.04 "	59.9 "

Showing a remarkable excess of resistance at the notch relatively to the sectional area, and a relatively large contracted area.

The influence of screwing bolts of  $1\frac{1}{4}$  inch, 1 inch, and  $\frac{3}{4}$  inch in diameter, on the tensile strength, showed 25 per cent. average reduction of tensile strength per square inch. Chased screws were weaker than screws made with dies, whilst screws cut with blunt dies were less weakened than those cut with new and sharp dies.

The influence of ordinary welded joints in several irons, showed an average of 19·4 per cent. reduction of tensile strength, varying from 2·6 per cent. to 43·8 per cent.

The effect of the sudden application of tensile stress to 1 inch round bars of iron, without blow or jerk, as against the gradual application of stress, was to reduce the load necessary to cause fracture by 18·6 per cent., with an extension of 20·1 per cent. as against 24·6 per cent. with the gradual application of the stress.

Three pieces of iron cut out of a large crank shaft, were forged down and turned to 1 inch in diameter. Tested against two other pieces cut out, and simply turned to 1 inch in diameter, they showed 20 per cent. greater strength, but reduced extension.

The influence of the removal of the skin on strength of hammered iron, was shown by two  $1\frac{1}{2}$  inch square bars turned down to 1 inch in diameter, the tensile strength being  $5\frac{1}{2}$  per cent. more than that of 1-inch square hammered bars in their skins, with a greater degree of extension.

A  $1\frac{1}{4}$ -inch round bar of Bowling iron was cut into several pieces, which were turned, forged down and hardened, with the following results :--

Diameter.		Tons per Sq. In.	Extension.
Turned to 1 inch	.	27·15	28·5 per cent.
Forged to '87 "	hardened in water	32·79	19·6 "
" " '78 "	" oil	28·85	19·8 "
" " '70 "	" tar	28·06	22·4 "

The second of these tensile strengths, 32·79 tons per square inch, was the maximum tensile strength of iron observed by Mr. Kirkaldy.

By casehardening and cooling in water, or in oil, or slowly, an average of 8·4 per cent. reduction of tensile strength was effected, with only one-fourth of the extension.

In cold-rolling  $\frac{3}{4}$ -inch bars, the tensile strength was augmented 18 per cent., and the elongation reduced to one-half. By subsequent annealing, the gain of strength disappeared.

Angle-iron, ship-strap, and beam-iron are less in tensile strength by from 1 ton to 2 tons per square inch than bar iron; and the extensions also are less.

Mr. Kirkaldy found that the density of iron was diminished by cold-rolling:—

	Ordinary.	Cold Rolled.	Reduced.
Bar iron, specific gravity .	7·636	7·582	·7 per cent.
Boiler plate            „	7·566	7·539	·37    „

The specific gravity of iron was also reduced by stretching under tensile stress:—

	Specific Gravity.	
	Before stretching.	After stretching.
Three 1-inch Yorkshire iron bars, { stretched to ·90 inch diameter. }	7·752	7·674
Two ·83-inch Blochairn bars, { stretched to ·76-inch diameter. }	7·636	7·569
Average for five bars .	7·760	7·632

Showing an average of ·128 reduction of specific gravity, or 1·65 per cent.

### Swedish Hammered Bar Iron.

Mr. Kirkaldy tested round bars, 3 inches, 2 inches, 1 inch, and  $\frac{1}{2}$  inch in diameter, with flat bars  $\frac{1}{2}$  inch thick, by 3 inches, 2 inches, and  $1\frac{1}{2}$  inches wide, for tensile strength. The round specimens had 10 inches of clear length, and the flat specimens 15 inches.

The average ultimate strength of the round bars was 20·13 tons per square inch, with an extension of 24·6 per cent.; and that of the flat bars was 21·4 tons, with an extension of 16·7 per cent.  $1\frac{1}{2}$  inch turned specimens had an elastic strength of 11·05 tons, about 60 per cent. of the ultimate strength, 18·80 tons.

Under compressive stress three  $1\frac{1}{2}$  inch round specimens, respectively  $1\frac{1}{2}$ , 3, and 15 inches high, were crushed under a stress of 66·45, 37·90, and 12·53 tons per square inch.

A 1-inch cube failed under a load of 82·20 tons.

### French Bar Iron.

The strength of French bar iron of various denominations is given in Table 179.



TABLE 179.—FRENCH BAR IRON—TENSILE STRENGTH.  
(Debauve.)

Description.	Ultimate Strength in Tons per Square Inch.	Extension.
	Tons.	Per cent.
Creusot, No. 1, Rails . . . . .	26·03	10
„ No. 2, Merchant Iron . . . . .	24·00	15
„ No. 3, Horse-shoe Iron . . . . .	24·13	18
„ No. 4, Bolts and Rivets . . . . .	24·45	21
„ No. 5, Boiler Plates . . . . .	24·51	25
„ No. 6, Machinery Iron . . . . .	24·57	29
„ No. 7, Exceptional . . . . .	24·89	34
Chantillon and Commentry, No. 1, Axles	22·86	25
„ „ No. 5 . . . . .	26·35	13
Terre-Noire, La Voulte, and Bessèges :		
Ordinary . . . . .	18·42	17
Strong . . . . .	20·96	20
Superior . . . . .	21·59	25
Fine . . . . .	23·50	26
Saint Étienne, granular, No. 1 . . . . .	17·78	...
„ „ No. 7 . . . . .	22·86	12
„ fibrous, No. 1 . . . . .	16·51	2
„ „ No. 7 . . . . .	22·86	18
Porte Évêque (Isère), No. 1 . . . . .	6·35 to 12·70	...
„ „ No. 7 . . . . .	21·59	18
Lyons Railway Company :		
No. 1, fine charcoal . . . . .	24·13	25
No. 2, strong superior . . . . .	23·50	23
No. 3, strong . . . . .	22·23	18
No. 4, ordinary . . . . .	20·96	12

In general, good ordinary French wrought-iron takes a tensile breaking weight of from 22 tons to 24 tons per square inch. The limit of elasticity corresponds to  $6\frac{1}{2}$  tons per square inch, whilst the maximum stress allowed in construction is 6 kilogrammes per square millimetre, or 3·81 tons per square inch, about  $\frac{1}{10}$ th of the ultimate strength. In compression, the elastic limit is for fine-grain iron 3·81 tons, and for fibrous iron, 9 tons; with ultimate rupturing stresses of 22 tons and 51 tons respectively.

**Mr. Kirkaldy's Experiments with Iron Plates.**

The tensile strength of iron plates, from  $\frac{3}{8}$  inch to  $\frac{1}{2}$  inch thick, in specimens  $1\frac{1}{2}$  inches and 2 inches wide, is given in Table 180 :—

**TABLE 180.—ULTIMATE TENSILE STRENGTH OF IRON PLATES.**

(D. Kirkaldy.)

Plates.	Tons per Square Inch.		Extension.	
	With Fibre.	Across Fibre.	With Fibre.	Across Fibre.
	Tons.	Tons.	Per cent.	Per cent.
Yorkshire . .	24.75	22.64	13.4	8
Staffordshire . .	23.01	21.40	9.3	5.3
Durham . .	22.89	21.39	9.5	5.2
Shropshire . .	23.37	19.22	9.6	2.8
Lanarkshire . .	21.96	19.56	7.0	3.2
Averages . .	23.20	20.84	9.8	4.9

The tensile strength across the fibre is from  $1\frac{1}{2}$  tons to 4 tons per square inch less than that with the fibre. The average difference is 10 per cent.

*Fractured Sectional Area of Iron Plates.*

	With Fibre.	Across Fibre.
Yorkshire . .	63.5 per cent.	79.7 per cent. of original area.
" . .	76.5 "	83.7 "
Staffordshire {	78.5 "	89.9 "
S. C. Crown }		
Staffordshire {	84.3 "	92.0 "
Bradley . . }		
Scotch best boiler . . }	87.3 "	93.6 "
Staffordshire {	90.9 "	94.6 "
best best . }		
Scotch Ship . .	95.4 "	97.5 "
"  "  "  "  "	94.4 "	98.5 "
Averages . .	84.0	91.0

By cold-rolling, pieces of Blochairn plate  $\cdot 345$  inch thick, rolled to two-thirds of their thickness, were nearly doubled in strength, but the extension was annihilated. By annealing after cold-rolling, only  $2\frac{1}{2}$  tons of the gain of strength remained, and the extension was doubled.

### Krupp Iron Plates.

Mr. Kirkaldy tested a number of Krupp iron plates, and, for comparison, Lowmoor plates,  $\frac{3}{8}$  inch,  $\frac{1}{2}$  inch, and  $\frac{5}{8}$  inch thick, for which testing specimens 2 inches wide, 10 inches long for extension were prepared. The specimens were tested lengthwise, crosswise, annealed and unannealed. The total average results were as follows :—

	Krupp.	Yorkshire.
Elastic strength per square inch	11·2 tons	12·2 tons
Ultimate " " "	21·5 "	20·2 "
Ratio of elastic to ultimate strength	52·1 per cent.	60·4 per cent.
Extension at 30,000 pounds per square inch	1·94 "	·85 "
Ultimate extension	22·6 "	14·8 "
Sectional area of fracture	66·2 "	81·4 "

The elastic strength of the annealed specimens was from  $\cdot 30$  to  $\cdot 60$  tons less than that of the unannealed specimens.

TABLE 181.—ULTIMATE TENSILE STRENGTH OF GALVANISED IRON SHEETS.

Thickness.	Extension in 10 inches.	Resistance per Square Inch.
	Per cent.	Tons.
B. W. G. No. 25, with fibre	9	27·4
" " across fibre	7·4	21·8
" No. 23, with fibre	8·5	26·2
" " across fibre	6·3	22·1
" No. 21, with fibre	9·9	24·6
" " across fibre	11·2	21·0

### French Plate Iron and Sheet Iron.

Iron plates and sheets are generally disposed in six classes. For example :—

		Tensile Strength per Square Inch.		Extension.
Creusot :—				
No. 2	.	21.08 tons	6	per cent.
" 3	.	21.40	" 10	"
" 4	.	22.03	" 14	"
" 5	.	22.10	" 18	"
" 6	.	22.61	" 22	"
" 7	.	23.30	" 26	"

Denain and Anzin :—				
No. 2	.	19.05 tons	3	per cent.
" 3. Boilers	.	19.05	" 5	"
" 4. Common for the Marine	.	20.96	" 8	"
" 5. Ordinary	"	22.22	" 12	"
" 6. Superior	"	22.86	" 18	"
" 7. Fine	"	23.50	" 20	"

In general, the resistance of the plates for the marine across the grain is from  $2\frac{1}{2}$  tons to  $3\frac{3}{4}$  tons less than with the grain.

### Influence of Temperature on the Tensile Strength of Wrought-Iron.

According to the results of Sir Wm. Fairbairn's experiments, the strength of ordinary Staffordshire plates, either with or across the grain, remained the same for temperatures varying from  $0^{\circ}$  F. to  $400^{\circ}$  F. This higher temperature is that of steam of 235 lbs. effective pressure per square inch. At higher temperatures, the strength declined until, at a red heat, it fell from an average of 20 tons to  $15\frac{1}{4}$  tons per square inch.

TABLE 182.—DECREASE IN TENSILE STRENGTH OF  
WROUGHT-IRON WITH RISE OF TEMPERATURE.

(Kollman.)

Temperature.			Temperature.		
		Decrease in Strength.			Decrease in Strength.
Centigrade.	Fahrenheit.	Per cent.	Centigrade.	Fahrenheit.	Per cent.
0	32	...	600	1112	81
200	392	5	700	1292	84
300	572	10	800	1472	89
400	752	27	1000	1832	96
	932	62			

M. Debauxe states that the statical resistance is not affected by cold ; but that the resistance to shocks is diminished by it. For temperatures from 0° C. to 100° C., or 32° F. to 212° F., there is no change ; at 200° C., or 392° F., the tensile resistance is reduced 5 per cent. ; at 300° C., or 572° F., reduced 10 per cent. ; at 500° C., or 932° F., 60 per cent. ; at 700° C., or 1292° F., 80 per cent. ; at 900° C., or 1,652° F., 90 per cent. ; at 1,000° C., or 1,832° F., the reduction of strength amounts to 95 per cent., leaving 5 per cent. of resisting strength. These results have been obtained for fibrous iron, fine grain iron, and Bessemer steel.

### Working Temperatures.

The leading temperatures at which iron is worked are these :—

*Brown-Red Heat*, about 700° C., or 1,300 F. : the lower limit for working iron.

*Cherry-Red Heat*, about 950° C., or 1,730° F. : iron can be dressed, or rectified.

*Red-White Heat*, about 1,300° C., or 2,370° F. ; iron easily worked.

*Welding Heat*, about 1,500° C., or 2,730° F.

### Experiments of the Steel Committee of Civil Engineers, with Bar Iron.

1½ inch round bars of Lowmoor iron, and S. C. Crown. Staffordshire iron, were tested for tensional strength and compressive strength, to the elastic limit, as well as for ultimate tensile strength. The bars were in lengths of 10 feet, for tension and for compression.

The summary average results of the tests are given in Table 183 (p. 355).

### Transverse Strength of Wrought-Iron.

The general formula (3), page 322, as follows :—

$$W = \frac{1.167bd^2s}{l} \quad . \quad . \quad . \quad (73)$$

gives the transverse strength of wrought-iron beams, supported at both ends and loaded at the middle, by substituting for  $s$  the ultimate tensile strength of the metal. Taking  $s = 20$  tons per square inch.

*Transverse Strength of Wrought-Iron Beams or Bars supported at both ends, loaded at the middle.*

$$\text{Square or Rectangular } W = \frac{23 \cdot 3 b d^2}{l} \quad . \quad . \quad . \quad (74)$$

$$\text{Round } . \quad . \quad . \quad W = \frac{14 \cdot 6 d^3}{l} \quad . \quad . \quad . \quad (75)$$

$W$  = load at middle, in tons.

$b$  = breadth of beam, in inches.

$d$  = depth or diameter, in inches.

$l$  = span, in inches.

For wrought-iron beams of other tensile strength, the co-efficients to be employed in equations (74) and (75), are as follows :—

Tensile Strength.	Coefficient for Equation (74).	For Equation (75).
21 tons . . . . .	24·5	15·3
22 „ . . . . .	25·7	16·0
23 „ . . . . .	26·8	16·8
24 „ . . . . .	28·0	17·5
25 „ . . . . .	29·2	18·2

*Elastic Transverse Strength of Wrought-Iron.*

$$\text{Rectangular section } . \quad . \quad D = \frac{W l^3}{47,000 b d^3} \quad . \quad . \quad (76)$$

$$\text{Round section } . \quad . \quad D = \frac{W l^3}{32,000 d^4} \quad . \quad . \quad (77)$$

$D$  = deflection in inches.

$W$  = load at middle, in tons.

$b$  = breadth in inches.

$d$  = depth, or diameter, in inches.

$l$  = span in inches.

**Torsional Strength of Wrought-Iron Bars or Shafts.**

Taking the ultimate tensile strength of wrought-iron bars and shafts at  $22\frac{1}{2}$  tons per square inch, on an average, the formulæ for the torsional strength of wrought iron are (356) :—

TABLE 183.—STRENGTH OF ROUND WROUGHT-IRON BARS,  $1\frac{1}{2}$  INCHES DIAMETER, 10 FEET LONG.  
(The Steel Committee.)

I. TENSILE STRENGTH (Summary Averages).

Description of Iron.	Elastic Strength in Tons per Square Inch.	Elastic Extension in parts of the Length.		Breaking Weight in Tons per Square Inch.	Perma- nent Exten- sion.	Ratio of Elastic to Breaking Strength.	Sec- tional Area of Fracture.
		Total.	Per cent. ·103, or 1 in 974 ·096, or 1 in 1046				
Yorkshire . . . . .	Tons. 13·0	Per cent. ·103, or 1 in 974	Length = 1. ·000079, or $\frac{1}{1253}$	Tons. 25·8	Per cent. 12·5	Per cent. 50·6	Per cent. 64·6
S. C. Crown, Staffordshire . . . . .	11·8	·096, or 1 in 1046	·000081, or $\frac{1}{1235}$	22·6	17·5	52·2	52·3
Mean . . . . .	12·4	·100, or 1 in 1000	·000080, or $\frac{1}{1250}$	24·2	15·0	51·4	58·4

II. COMPRESSIVE STRENGTH (Summary Averages).

Description of Iron.	Elastic Compression.		Perma- nent Exten- sion.	Ratio of Elastic to Breaking Strength.	Sec- tional Area of Fracture.
	Total.	Per cent. ·097, or 1 in 1030 ·097, or 1 in 1030			
Yorkshire . . . . .	12·6	·097, or 1 in 1030	·000077, or $\frac{1}{1297}$	...	...
S. C. Crown, Staffordshire . . . . .	11·7	·097, or 1 in 1030	·000083, or $\frac{1}{1203}$	...	...
Mean . . . . .	12·1	·097, or 1 in 1030	·000080, or $\frac{1}{1250}$	...	...

*Ultimate Torsional Strength of Wrought-Iron Bars or Shafts.*

$$\text{Round bar or shaft } WR = 4.41d^3 \quad . \quad . \quad . \quad (78)$$

$$\text{" " " } d = .283 \sqrt{WR} \quad . \quad . \quad . \quad (79)$$

$$\text{Square " " } WR = 6.32b^3 \quad . \quad . \quad . \quad (80)$$

$$\text{" " " } b = .251 \sqrt[3]{WR} \quad . \quad . \quad . \quad (81)$$

The elastic torsional strength is about 40 per cent. of the ultimate torsional strength.

Torsional deflection of wrought-iron bars and shafts within the elastic limit, is given by the formula :—

*Elastic Torsional Deflection of Wrought-Iron Bars and Shafts.*

$$D = \frac{WRl}{1072d^4} \quad . \quad . \quad . \quad (82)$$

W = force in tons

R = radius of force, in inches.

WR = moment of force, in statical inch-tons.

d = diameter of round shaft, in inches.

b = side of square shaft, in inches.

l = length of shaft subject to torsional action, in inches.

D = total angular deflection in parts of one revolution.

**STRENGTH OF STEEL.**

The qualities of iron and steel depend principally on the proportion of constituent carbon, thus :—

	Percentage of Carbon.
Ordinary iron . . . . .	0 to 0.15
Either soft or mild steel . . . . .	
Granular iron . . . . .	0.15 to 0.45
Soft or mild steel . . . . .	
Steely iron or puddled steel . . . . .	0.45 to 0.55
Semi-mild steel . . . . .	
Cemented steel . . . . .	0.55 to 1.50
Hard steel . . . . .	
Cast-iron . . . . .	1.5 to 5

**Mr. Kirkaldy's Experiments.**

Steel bars of from  $\frac{1}{2}$  inch to 1 inch in diameter were tested, and proved to from an average of 59 tons per square inch for tool steel, to an average of 29 tons for puddled steel. The



greatest observed ultimate strength was 66·2 tons per square inch for tool-steel. The general results are given in Table 184.

TABLE 184.—BAR STEEL: TENSILE STRENGTH.

(Mr. Kirkaldy—Summary.)

Name.	Treatment.	Size.	Breaking	Extension.
			Weight per Sq. Inch (average).	
		Inch.	Tons.	Per cent.
Tool steel . . .	Forged	·53 to ·59	59·21	5·3
Chisel steel . . .	"	·56 to ·60	55·75	7·1
Shear steel . . .	"	·56 and ·57	52·87	13·5
Drift steel . . .	"	·57	51·76	13·3
Bessemer tool steel	"	·65 to ·75	49·75	5·5
Rivet steel . . .	Rolled	·75	47·75	10·5
Blister steel . . .	Forged	·57 to ·60	46·56	9·7
Steel for taps . . .	"	·57 and ·59	45·15	10·8
Krupp's bolt steel.	Rolled	·91 to ·93	41·08	15·3
Homogeneous metal . . . }	"	·56	40·47	13·7
" " " "	Forged	·75	40·05	11·9
Spring steel . . .	"	·55 to ·57	32·37	18·0
Puddled steel . . .	Rolled	·75 to 1	31·32	11·3
" " " "	Forged	·75 and ·77	29·40	13·4

### Experiments of the Steel Committee with Bar Steel.\*

In the second series of experiments made at Woolwich Dockyard the object was to make experiments on the tension of long steel bars and iron bars, measuring the changes of length directly from the bars. For this purpose 91 round bars of steel and iron, each 14 feet long, 1½ inches in diameter, were procured, consisting of 33 bars of crucible steel, 34 bars of Bessemer steel, 12 bars of Lowmoor iron, 6 bars of best Yorkshire iron, and 6 bars of usual S. C. Crown, or Staffordshire iron. The extensions were measured on 10 feet length of each bar, and for compressive tests, the bars were cut to a length of 12 feet, and the measurements made on a length of 10 feet. The bars were tested in their natural skins. They were thoroughly examined, straightened, and gauged before being

\* For a detailed notice of these important experiments, see *Manual Rules, Tables, and Data*, pages 579, 596.

TABLE 185.—STRENGTH OF STEEL BARS  $1\frac{1}{2}$  INCHES IN DIAMETER, 10 FEET LONG.

(The Steel Committee.)

## I. TENSILE STRENGTH (SUMMARY AVERAGES.)

Description of Steel.	Elastic Strength in Tons per Square Inch.	Elastic Extension, in parts of the Length.		Breaking Weight in Tons per Square Inch.	Permanent Extension.	Ratio of Elastic to Breaking Stress.	Sectional Area of Fracture.
		Total.	Per ton per Square Inch.				
		Per cent.	Length = 1.		Per cent.	Per cent.	
Crucible.	Tons. 23·4	·182, or 1 in 550	·000078, or $\frac{1}{12750}$	Tons. 40·88	5·1	58·0	90·6
Bessemer.	18·4	·144, or 1 in 695	·000078, or $\frac{1}{12750}$	34·22	12·0	53·8	62·5
Mean	20·9	·163, or 1 in 613	·000078, or $\frac{1}{12750}$	37·55	8·5	55·9	76·6

## II. COMPRESSIVE STRENGTH (SUMMARY AVERAGES.)

Description of Steel.	Elastic Strength in Tons per Square Inch.	Elastic Compression.		Breaking Weight in Tons per Square Inch.	Permanent Extension.	Ratio of Elastic to Breaking Stress.	Sectional Area of Fracture.
		Total.	Per ton per Square Inch.				
		Per cent.	Length = 1.		Per cent.	Per cent.	
Crucible.	23·3	·175, or 1 in 570	·000076, or $\frac{1}{13050}$	...	...	...	...
Bessemer.	17·8	·137, or 1 in 732	·000077, or $\frac{1}{13050}$	...	...	...	...
Mean	20·5	·156, or 1 in 641	·000076, or $\frac{1}{13050}$	...	...	...	...
Bars tested for Compression, but not for Tension.							
Crucible: axles, rails, tyres.	23·0	·172, or 1 in 581	·000073, or $\frac{1}{13650}$	...	...	...	...
Bessemer: axles, rails, tyres.	24·0	·182, or 1 in 550	·000074, or $\frac{1}{13550}$	...	...	...	...

tested. The summary results have been given for bar iron, page 349, and those for the steel bars in Table 185, preceding.

The average compositions of the foregoing steels and the Yorkshire iron tested at the same time were as follows:—

	Crucible Steel. Per cent.	Bessemer Steel. Per cent.	Yorkshire Iron. Per cent.
Iron . . . . .	98·89	99·20	99·49
Carbon . . . . .	·62	·33	·23
Silicon . . . . .	·114	·022	·10
Manganese . . . . .	·34	·39	·08
Sulphur . . . . .	·01	·035	·02
Phosphorus . . . . .	·026	·02	·08
	<hr/>	<hr/>	<hr/>
	100·000	99·997	100·00
Specific gravity . . . . .	7·842	7·855	7·758

### Hadfield's Manganese Steel.

Though steel becomes brittle when the constituent manganese exceeds 2·75 per cent., yet it has been proved by Mr. R. A. Hadfield that when there is a proportion of not less than 7 per cent. of manganese, up to about 20 per cent., the product is a new metal, of superior strength. The Table 186 gives comparative tensile strengths and extensions of Siemens and Bessemer steels, including manganese steel of the following composition:—iron, 98·00, carbon, ·85, silicon, ·23, sulphur, ·08, phosphorus, ·09, and manganese, 13·75 per cent.

TABLE 186.—MANGANESE STEEL AND OTHER MILD STEELS.

Description.	Breaking Loads.	Extension.
	Tons.	Per cent.
Siemens . . . . .	26·16 to 28·51	31·25 to 35·69
Siemens . . . . .	26·26 „ 28·21	32·78 „ 37·50
Bessemer . . . . .	20·21 „ 28·44	31 „ 35
Siemens . . . . .	25·10 „ 27·21	31 „ 34
Basic Bessemer . . . . .	22·20 „ 25·80	30 „ 34
Siemens . . . . .	26·54 „ 28·29	28 „ 31
Manganese steel . . . . .	57 „ 65	39·8 „ 50·7

TABLE 187.—COMPRESSED STEEL : TENSILE STRENGTH.  
(W. H. Greenwood.)

Description.	Elastic limit, per Sq. Inch.	Ultimate Strength per Sq. Inch.	Contraction of Area at Fracture.	Extension in Four Inches.
I. <i>Test pieces cut longitudinally :—</i>	Tons.	Tons.	Per cent.	Per cent.
Unpressed ingot.	11·11	29·18	4·41	8·76
Pressed ingot .	14·45	29·53	7·90	12·51
II. <i>Test pieces cut transversely :</i>				
Unpressed ingot.	11·43	28·04	3·61	7·91
Pressed ingot .	12·38	30·07	7·57	12·74

**Whitworth Compressed Steel.**

Steel subjected by the Whitworth process to compression while fluid, under a pressure of from 4 tons to 12 tons per square inch, gains in solidity and strength. In one instance the specific gravity of sound crucible steel containing 0·54 per cent. of carbon, was increased by compression from 7·8542 to 7·8795. The density of steel as a whole is increased by from 8 per cent. to 12 per cent. by compression pressure. Two sample ingots, pressed and unpressed, contained respectively 0·5 per cent. and 0·39 per cent. of carbon, and 0·35 per cent. and 0·4 per cent. of manganese. The results of tests for tensile strength are given in Table 187, the data of which are given by Mr. W. H. Greenwood. There is practically very little difference in the strengths of pieces cut longitudinally and transversely. But there is a considerable augmentation of elastic strength by compression.

**Strength of Steel Plates.**

Mr. Kirkaldy tested a number of steel plates for tensile strength, the results of which are summarised in Table 189. The plates were from  $\frac{3}{16}$  inch to  $\frac{5}{16}$  inch thick ; and it is shown that whilst the puddled steels possessed about 10 per cent. less ultimate strength across the fibre than with it, the cast steel plates were at least as strong crosswise as lengthwise.

Landore steel plates tested by Mr. Kirkaldy were shown to have the same resisting strength lengthwise and crosswise as in the following Table 188. It is shown that the annealed samples have about  $7\frac{1}{2}$  per cent. less tensile resistance than unannealed samples.

TABLE 188.—LANDORE STEEL PLATES: TENSILE STRENGTH.

	Tensile Strength per Square Inch.			
	With the Grain.		Across the Grain.	
	Annealed.	Un-annealed.	Annealed.	Un-annealed.
Elastic strength, tons	12·8	14·5	12·8	14·4
Ultimate strength „	28·8	31·1	28·8	31·2
Contraction of area at fracture, p. cent. )	43·2	41·1	44·9	40·5
Extension „	24·6	23·4	23·6	23·5

TABLE 189.—STEEL PLATES: TENSILE STRENGTH.  
(Mr. Kirkaldy—Summary.)

Description of Steel.	Thickness of Plate.	Breaking Weight per Square Inch.		Extension in parts of the Length.	
		With Fibre.	Across Fibre.	With Fibre.	Across Fibre.
	Inch.	Tons.	Tons.	Per cent.	Per cent.
Cast steel . . . . .	$\frac{3}{16}$ to $\frac{1}{2}$	38·82	39·90	12·90	13·96
Puddled steel . . . . .	$\frac{1}{8}$ to $\frac{5}{16}$	41·56	35·34	5·12	2·82
Mild puddled steel . . . . .	$\frac{1}{4}$ to $\frac{9}{32}$	33·16	30·22	4·90	5·70
Hard puddled steel . . . . .	$\frac{1}{4}$	45·80	38·11	4·90	3·30
Total averages	$\frac{3}{16}$ to $\frac{1}{2}$	39·83	35·90	6·95	6·44

The following results of tests of hematite steel and Krupp steel are given as examples comprising ultimate compressive strength :—

	Hematite.	Krupp.
Elastic tensile strength, per square inch . . . . .	18·63 tons	19·10 tons
Ultimate tensile strength, per square inch . . . . .	32·27 „	42·07 „
Extension . . . . .	19·2 per cent.	7·9 per cent.
Elastic compressive strength .	23·21 tons	21·13 tons
Ultimate „ „ . . . . .	71·24 „	89·30 „

## Strength of Steel as affected by its Chemical Composition.

TABLE 190.—BESSEMER STEEL (FOR TYRES): CHEMICAL COMPOSITION AND TENSILE STRENGTH.  
(J. O. Arnold—Summary.)

Chemical Composition.							Tensile Strength.				Fracture.
Iron.	Carbon.	Chromium.	Manganese.	Silicon.	Sulphur.	Phosphorus.	Ultimate, in Tons per Sq. Inch.	Extension.	Reduction of Area.		
Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Tons.	Per cent.	Per cent.		
98.24	.28	...	1.25	.07	.08	.08	37	26	47	{ Gray granular. Convex and concave.	
97.74	.25	...	1.75	.03	.12	.11	42.1	18	26.3	{ Gray granular, flat.	
97.49	.28	.42	1.54	.08	.10	.09	49.8	15	26	{ Finely crystalline, flat.	
97.69	.32	.30	1.46	.11	.05	.07	50	16	29	{ Coarse granular.	
97.42	.28	.64	1.41	.11	.07	.07	50.4	10	13.8	{ Crystalline.	
SPRING STEEL.											
98.24	.50	...	1.10	.07	.09	.08	{ 50.8 69.4 88.0	14.9 10.9 3.1	31.4 30.0 4.9	Description. Unhardened. Water hardened. Oil hardened.	

The Table 190, gives the experimental results of tests of Bessemer tyre-steel, conducted by Mr. J. O. Arnold, with the chemical composition of the steels tested. These comprise samples containing various proportions of chromium and manganese, as well as of carbon. An example of spring steel is introduced in this Table, showing the hardening influence of water and of oil.

Another Table 191, of the transverse strength of steel rails, shows also the variations of transverse strength with the percentage of carbon. The rails were double-headed,  $5\frac{1}{2}$  inches deep, weighing 86 pounds per yard; and whilst the carbon increased from 40 per cent. to 55 per cent., the ultimate loads were increased from 40 tons to  $52\frac{1}{2}$  tons.

TABLE 191.—TRANSVERSE STRENGTH OF STEEL RAILS IN RELATION TO THE CONSTITUENT CARBON.

Span 43·5 inches. Load applied at the middle.

Con- stituent Carbon.	Ultimate Strength.			Elastic Strength.			
	Load.	Deflection.	Set.	Load.		Deflection.	Set.
Per cent.	Tons.	Inch.	Inch.	Tons.	Per cent.	Inch.	Inch.
40	40	3·94	3·74	15	37·5	10	01
46	40	2·64	2·34	20	50	14	05
49	50	4·18	3·77	22·5	45	165	03
50	52·5	4·68	4·28	22·5	43	130	01
55	52·5	4·40	4·02	25	48	165	04

TABLE 192.—TENSILE STRENGTH OF STEEL RAILS IN RELATION TO THE CONSTITUENT CARBON.

Constituent Carbon.	Ultimate Tensile Strength, in Tons per Square Inch.	Constituent Carbon.	Ultimate Tensile Strength, in Tons per Square Inch.
Soft Rails.		Hard Rails.	
Per cent.	Tons.	Per cent.	Tons.
28	30·90	36	37·01
29	32·60	39	41·41
30	32·94	40	37·68
31	32·67	43	39·10
32	33·04	44	41·02
		45	44·00
		50	45·79
		57	50·42

Thirty Bessemer steel rails, manufactured at Barrow-in-Furness, comprising various proportions of constituent carbon, were tested for tensile strength, with the results given by Mr. J. T. Smith in Table 192, showing that the tensile strength increased from 30·9 tons to 50·42 tons per square inch, with the proportions of carbon from ·28 to ·57 per cent.

TABLE 193.—TENSILE STRENGTH OF STEEL IN RELATION TO THE CONSTITUENT CARBON.

Description of Steel.	Constituent Carbon (Approximate).	Breaking Weight per Square Inch.	Extension.
	Per cent.	Tons.	Per cent.
Webb steel . . .	·20	28·0	...
Vickers No. 2 . . .	·33	30·4	9·8
„ No. 4 . . .	·43	34·0	9·8
„ No. 5 . . .	·48	37·5	8·9
„ No. 6 . . .	·53	42·5	8·0
„ No. 8 . . .	·63	45·0	7·1
„ No. 10 . . .	·74	45·5	5·0
„ No. 12 . . .	·84	55·0	8·0
„ No. 15 . . .	1·00	60·0	5·0
„ No. 20 . . .	1·25	69·0	4·4

The influence of the constituent carbon on the tensile strength of steel was well exemplified by Mr. T. Edward Vickers in 1861, as shown in the Table 193. To render the table fuller, the strength and constituent carbon of Mr. Webb's steel for boiler plates are prefixed, in the first line. The specimens of Mr. Vickers were made of crucible steel from Swedish iron. They were turned to a diameter of 1 inch for a clear length of 14 inches. It is shown that the ultimate tensile strength increases with the carbon from 28 tons, with  $\frac{1}{5}$ th per cent. of carbon, to 69 tons per square inch with  $1\frac{1}{4}$  per cent. of carbon.

M. Debaue gives the following evidence of the influence of the constituent carbon, in the case of steel bars tempered in oil:—

Constituent carbon } ·15, ·49, ·709, ·875 per cent.

Elastic limit . 20·32, 27·94, 43·18, 57·15 tons per square inch.



Ultimate strength } 29·21, 46·45, 67·94, 67·31 tons per square inch.

Extension in inches } 28, 12, 4, 1 per cent.

### Strength of Long Round Steel Columns.

The safe working load for long round steel columns is given by means of the following formula :—

$$W = 1400 \frac{d^3}{l^2} \quad . \quad . \quad . \quad . \quad . \quad (83)$$

$W$  = safe load in cwts.

$d$  = diameter of column in inches.

$l$  = length of column between supports or brackets, in feet.

This formula is specially applicable to the case of hydraulic lifts, as well as to the case of fixed loads. It may be properly employed for columns of from 3 inches to 5 inches in diameter, and for lengths of from 25 feet up to 50 feet, for columns not less than 3 inches in diameter ; and up to 80 feet for 5-inch columns. Table 194 has been calculated by means of the above formula.

TABLE 194.—SAFE LOAD ON LONG ROUND STEEL COLUMNS.

Diameter of Column.	Length of Column between Supports, in Feet.								
	25	30	35	40	45	50	60	70	80
Inches.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.	Cwts.
3	60·5	42·0	30·8	23·6	18·6	15·1	...	...	...
3½	76·8	53·4	39·2	30·0	23·7	19·2	...	...	...
3½	96·0	66·7	49·0	37·5	29·6	24·0	16·7	...	...
4	143·0	99·6	73·1	56·0	44·2	35·8	25·0	...	...
4½	204·1	141·7	104·1	79·7	63·0	51·0	35·4	26·0	...
5	280·0	194·4	143·0	109·4	86·4	70·0	48·6	35·7	27·3

### Transverse Strength of Steel.

Taking the ordinary standard of ultimate tensile strength, 32 tons per square inch, for steel, the formula for its ultimate transverse strength is :—

*Ultimate Transverse Strength of Steel Beams of Rectangular Section, supported at the Ends, loaded at the Middle.*

$$W = \frac{37 \cdot 3 b d^2}{l} \quad . \quad . \quad . \quad . \quad . \quad (84)$$

For some other values of tensile strength, the numerical coefficients annexed are to be substituted in this equation :—

## Ultimate Tensile Strength.

Tons.	Coefficient.
28 . . . . .	32·7
30 . . . . .	35·0
35 . . . . .	40·8
40 . . . . .	46·7
45 . . . . .	52·5
50 . . . . .	58·4

The proper coefficient for any other tensile strength is found by multiplying the strength in tons per square inch by 1·167.

*Elastic Deflection of Steel Bars or Beams, of Rectangular Section, supported at the Ends, Loaded at Middle.*

$$\text{Square} \quad D = \frac{Wl^3}{56,000bd^3} \quad (85)$$

$$\text{Round} \quad D = \frac{Wl^3}{38,000bd^3} \quad (86)$$

## Ultimate Torsional Strength of Steel Bars or Shafts.

$$\text{Round bar or shaft} \quad WR = 6\cdot27d^3 \quad (87)$$

$$\text{" " " } \quad d = \cdot252 \sqrt[3]{WR} \quad (88)$$

$$\text{Square bar or shaft} \quad WR = 8\cdot99b^3 \quad (89)$$

$$\text{" " " } \quad b = \cdot223 \sqrt[3]{WR} \quad (90)$$

*Elastic Torsional Deflection of Steel Bars or Shafts.*

$$D = \frac{WRI}{152d^4} \quad (91)$$

## TENSILE STRENGTH OF COPPER, LEAD, ETC.

	Tons per Square Inch.
Cast copper . . . . .	8½ to 11½
Wrought copper . . . . .	15
Copper bolts . . . . .	16
Copper bolts, with 1 per cent. of phosphorus . . . . .	7·56 to 19·20
"    "    2    "    "    "    . . . . .	20·25
"    "    3    "    "    "    . . . . .	21·38
"    "    4    "    "    "    . . . . .	22·32

Solid drawn copper tube, 10 inches in diameter, ¼ inch thick (Broughton Copper Company):—

Unannealed (elastic limit, 16·34 tons per square inch)	18·64
Annealed (    "    5·26    "    "    )	15·35

Brazed copper tubes (Mr. Mallison):—

Plain sheet used for steam pipes (35·7 per cent. extension)	14·81
Brazed and hammered . . . (13·83    "    "    )	14·49
Brazed, not hammered . . . (17·14    "    "    )	13·47

Tons per  
Square Inch.

Drawn copper tubes, 3 inches in diameter, .131 inch to .093 inch thick (Goodwin & How) :—				
Unannealed, longitudinally (extension 16·9 per cent.)				18·6
"    transversely (    "    15·2    "    )				18·3
Annealed, longitudinally (    "    38·0    "    )				14·7
"    transversely (    "    35·2    "    )				14·9

Elmore's deposited copper tubes (Elmore Metal Copper Depositing Company) :—

For pressure purposes, tensile strength over 20 tons per square inch, with elongation of not less than 10 per cent. measured on 10 inches.

Up to 30 tons per square inch with elongation 6 per cent.

For such purposes as liners, rollers, and like articles, with elongation down to 1 per cent., with hardness stated to be greater than that of any of the brasses and bronzes which have been tested against the Elmore Metal.

Cold planishing : increase of strength :—

Solid plate, cold,  $\frac{3}{4}$  per cent.

    "    "    hot (from 330° to 410°) 5 per cent.

Joint, cold, 17½ per cent.

    "    hot, 11½ " "

Strength the same, longitudinally and transversely.

Brazed joint in plain sheet, with care in workmanship, parts of solid joint, 75 per cent.

Brazed joint in pipe, under steam of 150lb. pressure, 60 to 62 per cent.

Brazing metal : spelter, 49·15 per cent., copper, 58·85 per cent.

### Tensile Strength of Alloys of Copper.

Aluminium bronze, castings :—

Tons per  
Square Inch.

Copper 89, aluminium 11 (extension, 0 to 5 per cent.)				45 to 50
"    90,    "    10 (    "    4 to 25    "    )				40 to 32
"    95,    "    5 (    "    35 to 50    "    )				15 to 21
"    97½,    "    2½ (    "    45 to 60    "    )				12 to 15
"    98¾,    "    1¼ (    "    20 to 35    "    )				9 to 12

Aluminium brass, castings :—

No. 1. Aluminium bronze, and zinc (extension, 10 to 14 per cent.) . . . . .23 to 27

No. 2. Aluminium bronze, and zinc (extension, 8 to 11 per cent.) . . . . .36 to 38

	Tons per Sq. In.
Brass, fine or yellow, 2 copper, 1 zinc . . . . .	12·90
Brass tube, 62 copper, 38 zinc . . . . .	46
" " 70 " 30 " . . . . .	36
Muntz metal, 60 copper, 40 zinc . . . . .	22
Bronze, ordinary (extension, 1·2 to 4 per cent.)	9·06 to 10·58
Delta metal: Copper $\frac{3}{4}$ , zinc $\frac{1}{4}$ , with 2 per cent. of iron :—	
Cast in sand. Diam. ·611 in. Extension in 4 ins. 20·5 per cent.	

	2 "	21·0 "
	1 "	21·0 "
Elastic limit of stress, per sq. in.		11·54 tons.
Maximum stress		23·89 "
Gun metal, 12 copper, 1 tin . . . . .		12·94
" 11 " 1 " . . . . .		13·71
" 10 " 1 " . . . . .		14·73
" 9 " 1 " . . . . .		17·00

Parsons' Manganese Bronze :—

	No. 1, Annealed.	No. 2.
Elastic limit . .	11 to 16 tons	16 to 19 tons.
Breaking weight .	27 to 32 "	28 to 33 "
Extension in 5 inches	20 to 45 per cent.	13 to 22 per cent.

Manganese bronze: copper 88, tin 10, iron and manganese, 2 :—

Cast under pressure (extension, 12·4 to 22 per cent.)		31·9 to 35
Rods rolled hot, )	( " 33·4 to 44·6 "	29
annealed . . )		
Rods rolled hot, )	( " 23·3 to 26·5 "	31·5
from rolls . . )		
Rods rolled hot, )	( " 11·6 "	39·6
finished cold )		
Plates rolled hot, )	( " 28·8 to 47·8 "	30·10
annealed, with )		
fibre . . . . )		
Plates rolled hot, )	( " 23·2 to 34·1 "	28·5 to 30·8
annealed, across )		
fibre . . . . )		
Phosphor-bronze . ( " 3·6 to 33·4 .		9·7 to 22·7

Bull's metal (extension in 8 inches, 16·4 per cent.),  
Elastic limit 23·5 tons; breaking stress . . . . . 32·82

Sterro-metal (Dr. Anderson) :—

Copper 10, iron 10, zinc 80 . . . . .	3·17
" 60, " 3, " 39, tin, 1·5 . . . . .	24
" 60, " 4, " 44, " 2 :—	
Cast in sand . . . . .	19·25
Cast in iron, annealed . . . . .	24·25
Cast in iron, forged red hot . . . . .	31

	Tons per Sq. In.
Copper 60, iron 2, zinc 37, tin 1 . . . . .	34
" 60, " 2, " 35, " 2 . . . . .	38
" 55, " 1.77, " 42.36, " .83 :—	
Cast . . . . .	27
Forged red hot . . . . .	34
Drawn cold . . . . .	38

### Ultimate Tensile Strength of Lead, Tin, Zinc, and Glass.

	Tons per Sq. In.
Lead, cast . . . . .	.81
" sheet . . . . .	.86
" pipe . . . . .	1.00
Tin, cast . . . . .	2.11
" banco . . . . .	.95
" solder, soft (2 tin, 1 lead) . . . . .	3.35
Zinc, cast . . . . .	1.34
" sheet, with grain (London Zinc Mills) (extension, 14.2 per cent.) . . . . .	14.6
Glass, flint, annealed . . . . .	1.07
" green . . . . .	1.29
" crown . . . . .	1.14
" thin globes . . . . .	2.23

TABLE 195.—ULTIMATE TENSILE STRENGTH OF WIRES.  
(Mr. Kirkaldy.)

Wires from  $\frac{1}{16}$  to  $\frac{1}{4}$  in. thick, except Phosphor bronze,  $\frac{1}{8}$  in. thick.

Wire.	Ultimate Tensile Strength per Square Inch.		Extension, annealed.	Twists in Five Inches of Length.	
	Unannealed.	Annealed.		Unannealed.	Annealed.
	Tons.	Tons.	Per cent.	Twists.	Twists.
Coke iron . . . . .	28.71	27.36	17	26	44
Charcoal iron . . . . .	29.05	23.99	28	48	87
Steel . . . . .	54.07	33.32	10.9	*	79
Copper . . . . .	28.18	16.52	34.1	86.8	96
Brass . . . . .	36.23	23.01	36.5	14.7	57
Phosphor bronze, No. 1 . . . . .	71.21	26.27	46.6	13.3	66
" No. 2 . . . . .	67.46	28.86	42.8	15.8	60
" No. 3 . . . . .	62.12	24.15	44.9	17.3	53
" No. 4 . . . . .	53.98	23.83	42.4	13	124

Silicium-bronze wire, No. 14, B. W. G., 29 tons per square in.

\* Of the eight pieces of steel tested, 3 stood 40 to 45 turns, and 5 stood  $1\frac{1}{2}$  to 4 turns.

TABLE 196.—COMPARATIVE TENACITY OF METAL WIRES AT DIFFERENT TEMPERATURES.

The wires tested were about  $\frac{1}{80}$ th inch thick, except the iron wires, which were  $\frac{1}{148}$ th inch thick.

	Tons per Square Inch.		
	At 32° F.	At 212° F.	At 392° F.
Gold . . . . .	11·90	9·85	8·25
Platinum . . . . .	14·50	12·60	11·25
Copper . . . . .	18·20	15·90	13·75
Silver . . . . .	18·05	15·20	11·85
Palladium . . . . .	23·30	20·75	17·85
Iron . . . . .	131·75	124·70	134·5

The steel wire,  $\frac{1}{10}$  inch thick, of the Brooklyn cable railway, was proved to an average ultimate tensile strength of 70·40 tons per square inch, with an extension of 7·3 per cent.

### RESISTANCE OF STONES AND OTHER BUILDING MATERIALS.

TABLE 197.—RESISTANCE OF STONES TO CRUSHING STRESS.

(Fairbairn.)

Stone.	Cube.	Fractured at.	Crushed at.	Crushing Force.	
				Per Sq. In.	Per Sq. Ft.
	Inches.	Tons.	Tons.	Tons.	Tons.
Greywacke, Penmaenmaur . . . . .	2	18·1	30·2	7·5	1080
Granite, Mount Sorrel . . . . .	2	22·9	22·9	5·7	821
Syenite . . . . .	2	21·1	21·1	5·3	763
Granite, Bonar, Inverary . . . . .	1½	7·8	10·9	4·9	706
Limestone . . . . .	1½	7·7	8·6	3·8	547
Sandstone . . . . .	1	1·4	1·6	1·6	230
„ . . . . .	2	4·6	5·5	1·4	202
Victoria Stone (granite and Portland cement, steeped in a solution of flint). . . . .				3·71	534

TABLE 197.—RESISTANCE OF STONES TO CRUSHING STRESS  
(continued).

(L. Clark.)				
RED SANDSTONE, average weight, 130.6 lbs. per cubic foot ; 17 cubic feet per ton.				
Specimen.	Cube.	Crush- ing Load.	Load per Sq. In.	Load per Sq. Ft.
	Inches.	Tons.	Tons.	Tons.
No. 6. Quite dry, set between boards	3	8.21	.91	131.0
No. 7. Set in cement, moderately damp	3	5.16	.57	82.1
No. 8. Set in cement, very wet . . .	3	4.36	.48	69.1
No. 9. Set in cement. . . . .	6	63.07	1.75	252.0
Average . . . . .			.93	133.8
Note.—Gave way suddenly.				
ANGLESEA LIMESTONE. Weight, 165.25 lbs. per cubic foot ; 13½ cubic feet per ton.				
No. 11. Set between boards	3	26.58	2.95	424.8
No. 12. " " " began } to crack at 25 tons " . . . }	3	32.30	3.60	518.4
No. 13. Set between boards . . .	3	30.95	3.44	495.4
No. 14. Three separate 1 inch cubes } set between boards . . . }	...	9.37	3.12	449.3
Average . . . . .			3.28	472.3
(Debaue.)				
	Weight per Cubic Foot.	Crushing Force per Sq. Inch.	Crushing Force per Sq. Foot.	
	Pounds.	Tons.	Tons.	
Granite : hard, fine grain . . . .	...	6.4 to 9.6	922 to 1382	
" " coarse grain . . . .	...	4.4 to 6.4	634 to 922	
" slowly decomposes in water : fine grain . . . .	...	3.8 to 5.7	547 to 821	
coarse grain . . . .	...	2.5 to 3.8	360 to 547	
Basalt . . . . .	...	12.1	1742	
Lava . . . . .	112.3	2.7	389	
Porphyry . . . . .	...	8.2	1181	
Jasper . . . . .	...	11.7	1685	
Sandstone : hard . . . . .	131 to 156	2.2 to 4.9	317 to 706	
" semi-hard, or tender . . . .	118.5 to 131	.51 to 1.9	73 to 274	
Limestone : for building . . . .	87.4 to 174.7	.13 to 7.6	19 to 1094	
" hard . . . . .	137 to 175	1.4 to 7.6	202 to 1094	
" soft . . . . .	87.4 to 137	.51 to 1.4	73 to 202	

TABLE 198.—RESISTANCE OF SLATES TO RUPTURE.

(Debauve.)

Pieces of Anjou slate, 10 inches square, resting by their four edges on a flat frame bearing, were loaded on a central space 4 inches square.

Thickness.		Breaking Load.		Thickness.		Breaking Load.	
Millims.	Inch.	Kilogr.	Pounds.	Millims.	Inch.	Kilogr.	Pounds.
1	·0394	8	17·6	5	·1968	120	264
2	·0787	35	77	6	·2362	150	330
3	·1181	50	110	7	·2756	170	374
4	·1575	90	198				

TABLE 199.—RESISTANCE OF BRICKS AND BRICKWORK TO CRUSHING STRESS.

Description.	Crushing Force per Square Inch.	Crushing Force per Square Foot.
	Tons.	Tons.
Red . . . . .	·358	51·6
Yellow-faced, baked . . . . .	·446	64·2
"    burned . . . . .	·643	92·6
Gault clay, pressed . . . . .	1·111	160
"    wire-cut . . . . .	·884	127·3
"    perforated . . . . .	1·180	169·9
Stock . . . . .	1·044	150·3
Fareham red . . . . .	2·500	360
Staffordshire blue, pressed with frogs. . . . .	3·100	446·4
"    rough, with- out frogs . . . . .	3·275	471·6
"    Hamblet's (Kirkcaldy) . . . . .	7·390	824
Stourbridge fireclay . . . . .	·718	103·4
Tividale blue . . . . .	·620	89·3
Silex ferrine . . . . .	7·332	1056·2
Vitrified granite, Candy's . . . . .	3·091	445·2
Terra-cotta fire and sound proof (before cracking) . . . . .	·315	45·3
Glass . . . . .	12·31 to 14·23	1773



TABLE 199.—RESISTANCE OF BRICKS AND BRICKWORK TO CRUSHING STRESS (*continued*).

Cemented Brickwork. Best quality.					
	Cube.	Weight.	Crush- ing Load.	Load per Square Inch.	Load per Square Foot.
	Inches.	Pounds.	Tons.	Tons.	Tons.
No. 1, 9-inch cube set between deal boards }	9	54	19.94	.25	36.0
No. 2, 9-inch cube in cement . . . }	9	53	22.15	.27	38.9
No. 3, 9-inch cube in cement . . . }	9	52	16.42	.20	28.8
No. 4, 9½-inch cube in cement . . . }	9½	55½	21.72	.27	38.9
No. 5, 9-inch cube, be- tween boards . . }	9	54½	15.50	.19	27.4
Average . . .	. . .	. . .	. . .	.23	34.0

*Note.*—Irregular cracks occurred a considerable time before the blocks gave way.

TABLE 200.—RESISTANCE OF PORTLAND CEMENT CONCRETE BLOCKS TO CRUSHING STRESS.

(Grant.)

Portland Cement Concrete Blocks : 12 inch cubes compressed, 12 months old.					
	Cube.	Weight.	Crush- ing Load.	Load per Square Inch.	Load per Square Foot.
	Inches.	Pounds.	Tons.	Tons.	Tons.
1 cement to 1 sand and gravel }	12	...	170.5	1.18	170.5
1     "     3     "     }	12	...	115.5	.81	115.5
1     "     6     "     }	12	...	91.0	.63	91.0

TABLE 201.—ULTIMATE TENSILE STRENGTH OF STONES.  
(Debaube.)

Stone.	Tensile Resist- ance per Square Inch.	Tensile Resist- ance per Square Foot.
	Tons.	Tons.
Basalt (Auvergne) . . . .	·49	70·6
Portland limestone . . . .	·38	54·7
Compact " . . . .	·20	29
Silicious " . . . .	·14	20·2
Oolitic " . . . .	·09	13
Brick of good quality . . . .	·11 to ·13	16·8 to 18·7
Bagneux rock (near Paris) . .	·09	13
Soft stone (le Vergelet) . . .	·045	6·5
Stoneware pipes . . . . {	21lb. to 350lb. or ·15 ton.	1·35 to 21·6

TABLE 202.—Average Working Loads for Building Materials  
and Structures (Austrian Association of Engineers).

## (1) WEIGHT OF MATERIALS.

Material.	Lbs. per Cubic Foot.
<b>TIMBER :—</b>	
Oak . . . . .	50
Pine . . . . .	44
Fir . . . . .	44
Red pine . . . . .	41
Pitch pine . . . . .	
Larch . . . . .	44
<b>METAL :—</b>	
Wrought iron (per cubic inch, ·28 lb.) .	490
Cast iron ( " ·27 lb.) . .	468
Lead ( " ·40 lb.) . .	711
Copper ( " ·32 lb.) . .	555
Zinc ( " ·26 lb.) . .	449
<b>BRICK AND STONE :—</b>	
	(Wet.) (Dry.)
Hollow bricks . . . . .	87 75
Ordinary " . . . . .	106 94
Flemish " . . . . .	125 119
Rubble Masonry . . . . .	150
Concrete . . . . .	150
Ashlar sandstone . . . . .	150 to 156
limestone . . . . .	162 to 169
ite . . . . .	175

TABLE 202.—(1) WEIGHT OF MATERIALS (*continued*).

Material.	Lbs. per Cubic Foot.
VARIOUS MATERIALS :—	
Broken stone . . . . .	87
Fine dry sand . . . . .	77
Coarse dry sand . . . . .	84
Clay, loam, dry . . . . .	94
"    wet . . . . .	119
Lime mortar, cement mortar . . . . .	106
Asphalte, pure . . . . .	69
"    concrete . . . . .	100
"    compressed . . . . .	113
Gypsum . . . . .	72
Window glass . . . . .	165

TABLE 202.—(2) WORKING STRESS.

Material.	Tensile, per Square Inch.	Compressive, per Square Inch
	Tons.	Tons.
Wrought iron . . . . .	6·0	6·0
Cast iron . . . . .	1·5	4·5
Oak . . . . .	·60	·42
Pine . . . . .	·54	·36
Fir . . . . .	·42	·36
Red pine . . . . .	·42	·33
Larch . . . . .	·42	·33

TABLE 202.—(3) WORKING LOADS ON FOUNDATIONS.

Foundation.	Tons per Square Foot.
Moist clay and sand (protected against lateral spreading) . . . . .	1·36
Coarse sand and dry clay . . . . .	2·27
Firm bedded broken stones on dry clay . . . . .	3·18
Loose impermeable beds, with piling . . . . .	1·82
"    "    "    and concrete . . . . .	2·73

TABLE 202.—(4) WORKING LOAD ON STONE WALLS AND COLUMNS.

Material.	Thick Ashlar walls and single bed-stones and columns, where diameter is not less than half the height.	Block-in-course work and columns where diameter is from half to one-twelfth of height.	Columns where diameter is less than one-twelfth of height.
	Lbs. per Sq. Inch.	Lbs. per Sq. Inch.	Lbs. per Sq. Inch.
Granite, porphyry . . . . .	712	570	285
Hard stone . . . . .	356	285	...
Medium stone . . . . .	214	142	...
Soft stone . . . . .	108	...	...

TABLE 202.—(5) WORKING LOADS ON BRICKWORK, MASONRY, &amp;C.

Description of Work.	Walls not less than 18 inches thick, and columns where diameter is not less than one-sixth of height.	Walls under 18 inches thick, and columns where diameter is from one-sixth to one-eighth of height.	Columns where diameter is from one-eighth to one-twelfth of height.
	Lbs. per Sq. Inch.	Lbs. per Sq. Inch.	Lbs. per Sq. Inch.
Brickwork in lime mortar . . . . .	72	36	...
"          cement " . . . . .	108	72	...
"          Portland cement . . . . .	142	108	44
Rubble masonry in lime mortar . . . . .	58	...	...
"          cement " . . . . .	72	...	...
Pressed bricks in " " . . . . .	128	114	108
"          Portland cement } . . . . .	172	142	114
Flemish bricks in " " . . . . .	214	172	142
Portland cement concrete . . . . .	100	...	...

TABLE 202.—(6) WORKING LOADS ON FLOORS, STAIRS, AND ROOFS.

Location.	Lbs. per Square Foot.			
Live loads on floors :—				
Attic floors . . . . .	30·8			
Dwelling-room floors . . . . .	51·2			
Libraries, dancing saloons, &c. . . . .	71·7			
Stairs and passages . . . . .	82·0			
Business premises, workrooms, &c. . . . .	92·2			
Hay and fruit lofts . . . . .	102·5			
Workshops and warehouses . . . . .	112·7			
Theatres, concert rooms, warehouses and workshops with heavy machinery or special loads . . . . .	Loads specially adapted.			
Dead loads, snow and wind, on roofs—in lbs. per square yard on horizontal plane :—				
	Slope of Roof.	Dead Load.	Snow and Wind.	Total.
		Lbs.	Lbs.	Lbs.
Single tile roof . . . . .	1 horizontal to 1·25 vertical	27·7	25·6	53·3
Double „ . . . . .		33·8	25·6	59·4
Single slate . . . . .	1 „ 2·25	15·4	19·5	34·9
Double „ . . . . .	1 „ 2·25	23·6	19·5	43·1
Zinc or galvanised iron . . . . .	1 „ 4	8·2	15·4	23·6
Carton-Pierre . . . . .	1 „ 4	8·2	15·4	23·6
Sheet iron or iron purlins . . . . .	1 „ 5	4·1	15·4	19·5

TABLE 202.—(7) SNOW AND WIND.

Weight of snow on horizontal surface . . . . .	} allow 15·5 lbs. per sq. foot.
Wind pressure on surface at right angles to line of impact . . . . .	
Do. do. in specially exposed positions . . . . .	
	„ 24·6 „ „
	„ 31·0 „ „

### RIVETED JOINTS IN BOILER PLATES.

The proportion by which maximum strength of riveted joints is attained, are given in Table 203, in terms of thickness of plates and diameter of rivets.

TABLE 203.—PROPORTIONS OF RIVETED JOINTS OF MAXIMUM STRENGTH.

thickness of plates . . . .	= unity.
diameter of rivets . . . .	= thickness of plate $\times 2$ .
pitch of rivets (single riveting) . . . .	= thickness of plate $\times 5\frac{1}{4}$ .
pitch of rivets (double riveting) . . . .	= diameter of rivets $\times 2\frac{3}{4}$ .
pitch of rivets (double riveting) . . . .	= thickness of plates $\times 8$ .
pitch of rivets (double riveting) . . . .	= diameter of rivets $\times 4$ .
diagonal pitch (double riveting) . . . .	= longitudinal pitch $\times \frac{3}{4}$ .
diagonal pitch (double riveting) . . . .	= diameter of rivets $\times 3$ .
"spacing" (double riveting) . . . .	= longitudinal pitch $\times \cdot 56$ , or $\frac{9}{16}$ .
lap (single riveting) . . . .	= thickness of plate $\times 6$ .
lap (single riveting) . . . .	= diameter of rivets $\times 3$ .
lap (double riveting) . . . .	= thickness of plate $\times 10\cdot 48$ , or $10\frac{1}{2}$ .
lap (double riveting) . . . .	= diameter of rivets $\times 5\cdot 24$ , or $5\frac{1}{4}$ .

In conformity with the above proportions, the upper part of the following Table 204, shows the dimensions of rivet-joints in plates from  $\frac{1}{8}$  inch to  $\frac{11}{16}$  inch thick, for the last of which  $1\frac{1}{8}$  inch rivets are provided. This is the largest size of rivets ordinarily used in boiler construction. For plates thicker than  $\frac{11}{16}$  inch, the joints are to be made with  $1\frac{1}{8}$  inch rivets, suitably pitched, for equal resistance of net section of plate and shearing resistance of rivets; and, therefore, for maximum strength when  $1\frac{1}{8}$  inch rivets are used, as given in the lower part of the Table.

For boiler plates of iron and of steel  $\frac{3}{8}$  inch in thickness, the breaking or ultimate strength of riveted joints in parts of that of the entire plate, are given in the Table 205. These relative values are deduced from the results of numerous experimental tests. The nominal diameter of rivets—not that of the rivet-holes—is adopted in calculation.

The percentage of breaking strength in the last two columns of Table 205 may be adopted for other thicknesses of plate up to  $\frac{11}{16}$  inch, as in Table 204, upper part; except the values for single-riveted lap and singlegelt, which for thinner than  $\frac{3}{8}$  inch plates are higher; and for thicker plates are lower. For plates thicker than  $\frac{11}{16}$  inch, as in the lower part of Table 204, the breaking strengths may be taken as approximately in the proportion of the net sections of plate as percentages of the entire section. These are here subjoined in Table 206 :—

TABLE 204.—DIMENSIONS OF RIVET JOINTS.  
(Plates  $\frac{1}{8}$  inch to  $\frac{11}{16}$  inch thick).

Thick- ness of Plates.	Diameter of Rivets.	Pitch of Rivets.				Lap.	
		Single- Rivet- ing.	Double Riveting.			Single- Rivet- ing.	Double- Rivet- ing.
			Longitu- dinal.	Diagonal.	Spacing.*		
Inches.	Inches.	Inches.	Inches.	Inches.	Inches.	Inches.	Inches.
$\frac{1}{8}$	$\frac{1}{4}$	$\frac{2}{3}$	1	$\frac{3}{4}$	$\frac{9}{16}$	$\frac{3}{4}$	$1\frac{5}{16}$
$\frac{3}{16}$	$\frac{3}{8}$	1	$1\frac{1}{2}$	$1\frac{1}{8}$	$\frac{27}{32}$	$1\frac{1}{8}$	2
$\frac{1}{4}$	$\frac{1}{2}$	$1\frac{1}{8}$	2	$1\frac{1}{2}$	$1\frac{1}{8}$	$1\frac{1}{2}$	$2\frac{5}{8}$
$\frac{5}{16}$	$\frac{5}{8}$	$1\frac{3}{8}$	$2\frac{1}{2}$	$1\frac{7}{8}$	$1\frac{13}{32}$	$1\frac{7}{8}$	$3\frac{1}{4}$
$\frac{3}{8}$	$\frac{3}{4}$	2	3	$2\frac{1}{4}$	$1\frac{11}{16}$	$2\frac{1}{4}$	$3\frac{15}{16}$
$\frac{7}{16}$	$\frac{7}{8}$	$2\frac{1}{4}$	$3\frac{1}{2}$	$2\frac{5}{8}$	2	$2\frac{5}{8}$	$4\frac{5}{8}$
$\frac{1}{2}$	1	$2\frac{3}{4}$	4	3	$2\frac{1}{4}$	3	$5\frac{1}{4}$
$\frac{9}{16}$	$1\frac{1}{8}$	3	$4\frac{1}{2}$	$3\frac{3}{8}$	$2\frac{1}{2}$	$3\frac{3}{8}$	$5\frac{7}{8}$
$\frac{5}{8}$	$1\frac{1}{4}$	$3\frac{1}{8}$	5	$3\frac{3}{4}$	$2\frac{13}{16}$	$3\frac{3}{4}$	$6\frac{1}{2}$
$\frac{11}{16}$	$1\frac{3}{8}$	$3\frac{3}{8}$	$5\frac{1}{2}$	$4\frac{1}{8}$	$3\frac{1}{16}$	$4\frac{1}{8}$	$7\frac{1}{4}$
$\frac{3}{4}$	$1\frac{3}{4}$	3.475	5.156	3.867	2.900	$4\frac{1}{8}$	$7\frac{1}{4}$
$\frac{13}{16}$	$1\frac{7}{8}$	3.318	4.866	3.650	2.737	$4\frac{1}{8}$	$7\frac{1}{4}$
$\frac{7}{8}$	$1\frac{7}{8}$	3.179	4.616	3.462	2.597	$4\frac{1}{8}$	$7\frac{1}{4}$
$\frac{15}{16}$	$1\frac{7}{8}$	3.059	4.401	3.301	2.475	$4\frac{1}{8}$	$7\frac{1}{4}$
1	$1\frac{7}{8}$	2.953	4.212	3.159	2.370	$4\frac{1}{8}$	$7\frac{1}{4}$
$1\frac{1}{16}$	$1\frac{7}{8}$	2.860	4.045	3.034	2.275	$4\frac{1}{8}$	$7\frac{1}{4}$
$1\frac{1}{8}$	$1\frac{7}{8}$	2.778	3.895	2.921	2.191	$4\frac{1}{8}$	$7\frac{1}{4}$

TABLE 205.—ULTIMATE RELATIVE STRENGTH OF RIVETED JOINTS IN  $\frac{3}{8}$ -INCH BOILER PLATES.

$\frac{3}{8}$ -inch Plate Joint.	Thickness of Plate.	Rivets.		Nominal net sec- tion of plate in parts of that of whole plate.	Breaking Strength in Parts of that of Whole Plate.	
		Dia- meter.	Pitch longitu- dinally.		Iron.	Steel.
	Inch.	Inch.	Inches.	Per cent.	Per cent.	Per cent.
Single-riveted lap . .	$\frac{3}{8}$	$\frac{3}{8}$	2	62.5	56	60
„ single welt	$\frac{3}{8}$	$\frac{3}{8}$	2	62.5	50	58
„ double welt	$\frac{3}{8}$	$\frac{3}{8}$	2	62.5	60	65
Double-riveted lap . .	$\frac{3}{8}$	$\frac{3}{8}$	3	75	70	80
„ single welt	$\frac{3}{8}$	$\frac{3}{8}$	3	75	65	78
„ double welt	$\frac{3}{8}$	$\frac{3}{8}$	3	75	72	80

\* Note.—“Spacing” is the pitch of the longitudinal centre-lines of rivets in double-riveted joints.

TABLE 206.—NET PLATE SECTION OF PLATES  $\frac{3}{4}$  INCH AND UPWARDS IN THICKNESS.

Thickness of Plate.	Diameter of Rivets.	Net Plate Section in parts of Whole Section.	
		Single Riveting.	Double riveting.
Inches.	Inches.	Per cent.	Per cent.
$\frac{3}{4}$	$1\frac{1}{8}$	60·4	73·5
$\frac{13}{16}$	$1\frac{3}{8}$	58·6	71·7
$\frac{7}{8}$	$1\frac{3}{8}$	56·8	70·2
$\frac{15}{16}$	$1\frac{3}{8}$	55·0	68·8
1	$1\frac{3}{8}$	53·4	67·4
$1\frac{1}{16}$	$1\frac{3}{8}$	51·9	66·0
$1\frac{1}{8}$	$1\frac{3}{8}$	50·5	64·7

The most suitable pitches for given diameters of rivets, or, on the contrary, the most suitable diameters of rivets for given pitches, in order to form joints of equal resistance, may be calculated by means of the following formulæ (92) and (93), as, of course, pitches and diameters may be adopted other than those which are above-recommended :—

$$\text{single riveted lap joint :—} \begin{cases} p = \cdot 835 \frac{d^2}{t} + d & . \quad . \quad . \quad (92) \\ d = \sqrt{1\cdot 20 \, t \, p + \cdot 36 \, t^2} - \cdot 60 \, t . & (93) \end{cases}$$

These formulæ are applicable also for single-riveted single-welt and double-welt joints.

$$\text{double riveted lap joints :—} \begin{cases} p = 1\cdot 5 \frac{d^2}{t} + d & . \quad . \quad . \quad (94) \\ d = \sqrt{\frac{2}{3} \, t \, p + \frac{t^2}{9}} - \frac{t}{3} & . \quad (95) \end{cases}$$

These formulæ are applicable also for double-riveted single-welt and double-welt joints.

### BOILER SHELLS.

The bursting strength per square inch of a cylindrical boiler shell is twice as much longitudinally, that is to say, parallel to the axis, as it is transversely.

$$\text{Bursting pressure} \quad p = \frac{4480ts}{d} \quad . \quad . \quad . \quad (96)$$

$$\text{Thickness of plates} \quad t = \frac{dp}{4480s} \quad . \quad . \quad . \quad (97)$$



$$\text{Ultimate tensile strength of plates } s = \frac{dp}{4480t} \quad (98)$$

$d$  = internal diameter, in inches.

$t$  = thickness of plate, in inches.

$s$  = ultimate tensile strength of plate, in tons per square inch.

$p$  = effective steam pressure, in pounds per square inch.

When the shell is constructed with riveted joints, the tensile strength  $s$  is to be reduced in the ratio of the ultimate strength of the whole plate to that of the joint.

The resistance of a hollow sphere to internal pressure is twice as much as that of a tube of equal diameter and equal thickness.

### Strength of Ends of Cylindrical Steam Boilers.

For a flat end-plate forming the termination of a cylindrical shell, unstayed or unsupported except at the circumference, the ultimate elastic deflection under internal pressure is given by the formulæ :—

$$\delta = \frac{\text{radius}}{22} = \frac{r}{22} \quad (99)$$

$$\delta = \frac{\text{diameter}}{44} = \frac{d}{44} \quad (100)$$

$\delta$  = deflection at the centre in inches.

$r$  = radius of the cylinder, in inches.

$d$  = diameter of the cylinder in inches.

The relative internal pressure and stress in the end-plate strained to the elastic limit, are given by this formula :—

$$p = \frac{815ts}{d} \quad (101)$$

$p$  = effective internal pressure, in lbs. per square inch.

$t$  = thickness of end-plate, in inches.

$s$  = tensile stress in end-plate, in tons per square inch at the elastic limit.

This formula is applicable for steel plates, as for iron plates, taking the elastic limit to be the same for both metals, namely,  $\frac{1}{1000}$ th of the length. The elastic strength,  $s$ , is, for iron, 12 tons; for steel 14 tons per square inch. Substituting these values in formula (101), the final formulæ are derived for the elastic strength of circular flat end-plates of iron and of steel, of uniform thickness, fastened at the circumference, exposed to bulging pressure uniformly distributed :—

for iron, 
$$p = 10,000 \frac{t}{d} \quad . \quad . \quad . \quad . \quad (102)$$

for steel, 
$$p = 11,500 \frac{t}{d} \quad . \quad . \quad . \quad . \quad (103)$$

$p$  = bulging pressure, in lbs. per square inch.

$t$  = thickness of the plate, in inches.

$d$  = diameter of the plate, in inches, measured to the circular line of junction.

### *Flat Cast-iron Ends.*

The elastic strength of flat cast-iron ends, adopting an extension of  $\frac{1}{1000}$ th part of the length, as for iron and steel, corresponding to a tensile stress of 5 tons per square inch, is expressed by the formulæ :—

$$\delta = \frac{d}{44} \quad . \quad . \quad . \quad . \quad (104)$$

$$p = 4000 \frac{t}{d} \quad . \quad . \quad . \quad . \quad (105)$$

$\delta$  = deflection at centre, within the elastic limit, in inches.

$d$  = diameter of the line of fastening, in inches.

$t$  = thickness of the plate in inches.

$p$  = elastic bulging pressure, in lbs. per square inch, uniformly distributed.

For cast-iron of stronger quality, the co-efficient in formula (105) is to be increased in proportion.

### *Segmental Ends.*

The relation of the internal pressure and stress in a segmental or spherical end of a cylindrical shell, is given by the formula :—

$$p = \frac{8960ts}{\frac{r^2}{v} + v} \quad . \quad . \quad . \quad . \quad (106)$$

$p$  = internal pressure, in lbs. per square inch.

$t$  = thickness of segmental end, in inches.

$s$  = tensile stress in the plate, in tons per square inch.

$r$  = radius of the circular junction, in inches.

$v$  = versed sine or rise of the segment, in inches.

Substituting for the values of  $s$  : 12 tons for wrought iron,

14 tons for steel, and 5 tons for cast iron, the formula becomes :—

$$\text{Wrought iron,} \quad p = \frac{108,000t}{\frac{r^2}{v} + v} \quad . \quad . \quad . \quad (107)$$

$$\text{Steel,} \quad p = \frac{125,000t}{\frac{r^2}{v} + v} \quad . \quad . \quad . \quad (108)$$

$$\text{Cast-iron,} \quad p = \frac{45,000t}{\frac{r^2}{v} + v} \quad . \quad . \quad . \quad (109)$$

The versed sine or rise at the centre of a spherical segment having the same elastic strength as the body of the cylinder, measured by the internal pressure, is, say, one-fourth of the radius of the end of the cylinder, or one-eighth of its diameter.

*Strength of Stayed Flat Plates of Steam Boilers.*

The relative internal pressure and stress in a flat-stayed plate, strained to the elastic limit, are given by the formula :—

$$p = \frac{407ts}{d} \quad . \quad . \quad . \quad (110)$$

$p$  = internal pressure in lbs. per square inch.

$t$  = thickness of the plate in inches.

$d$  = clear distance apart between the bolts in rectangular arrangement.

$s$  = tensile stress in the plate, in tons per square inch, at the elastic limit.

When the pitches of the staybolts, vertically and transversely, are not equal to each other, the greater clear distance is to be taken for calculation.

Reducing the above formula (110) for iron and for steel plates, of which the values of  $s$  are taken as 12 tons and 14 tons respectively, and also inverting the formulæ to find the thickness of plate, and the clear distance apart of the staybolts, the following formulæ are obtained :—

$$\begin{array}{ll} \text{For iron.} & \text{For steel.} \\ p = 5,000 \frac{t}{d} & p = 5,700 \frac{t}{d} \end{array} \quad . \quad . \quad . \quad (111)$$

$$t = \frac{pd}{5,000} \quad . \quad . \quad t = \frac{pd}{5,700} \quad . \quad . \quad (112)$$

$$d = \frac{5,000t}{p} \quad . \quad . \quad d = \frac{5,700t}{p} \quad . \quad . \quad (113)$$

The proper diameter of screwed stay bolts, at the base of the thread, strained to the elastic limit, simultaneously with the plate, is given by formula :—

$$d' = .0024 \sqrt{\frac{P P' p}{s}} \quad . \quad . \quad . \quad (114)$$

$d$  = diameter of staybolts, at base of thread.

$P$  = pitch of staybolts between centres, longitudinally.

$P'$  = " " " transversely.

$p$  = maximum effective elastic pressure, in lbs. per square inch, on the plate.

$s$  = elastic tensile strength of staybolts, in tons per square inch.

For bolts of iron, steel, and copper, having respectively 12 tons, 14 tons, and 8 tons, elastic tensile strength per square inch, the special formulæ for the proper diameter of the staybolts, at the base of the thread, are :—

$$\text{Iron } d' = .00069 \sqrt{P P' p}; \text{ or } d' = \frac{\text{When } P' = P}{.00069} P \sqrt{p} \quad (115)$$

$$\text{Steel } d' = .00064 \sqrt{P P' p}; \text{ or } d' = .00064 P \sqrt{p} \quad . \quad (116)$$

$$\text{Copper } d' = .00084 \sqrt{P P' p}; \text{ or } d' = .00084 P \sqrt{p} \quad . \quad (117)$$

### *Collapsing Resistance of Furnace-tubes.*

Plain furnace-tubes of Lancashire and Cornish steam-boilers, without stiffening joints, have the maximum resistance to collapsing pressure under steam, according to the formula :—

$$p = \frac{200,000 t^2}{d^{1.75}} \quad . \quad . \quad . \quad (118)$$

$p$  = collapsing pressure, in lbs. per square inch.

$t$  = thickness of the plates of the furnace-tube in inches.

$d$  = internal diameter of the furnace tube in inches.

This formula is applicable to furnace-tubes of lengths of over 9 feet. Tubes of shorter length derive natural assistance from the end fastenings.

### *Segmental Crowns of Furnaces.*

The elastic resistance of a segmental crown of a cylindrical face, to collapsing pressure externally may be formulated

in the same terms as the resistance to bursting pressure internally, here repeated :—

$$p = \frac{8960 \, t \, s}{r^2 + v} \quad . \quad . \quad . \quad . \quad . \quad (119)$$

$t$  = thickness of plate, in inches.

$r$  = radius of circular junction, in inches.

$v$  = versed sine, or rise of segment, in inches.

$p$  = external collapsing pressure, in lbs. per square inch.

$s$  = compressive stress in the segment, in tons per square inch.

For the application of this formula, it is assumed that the spherical segment is perfectly formed. A segment of which the rise is one-eighth of the diameter of the cylindrical base is equally stressed with the base, under equal external pressure per square inch.

When the spherical segment is a hemisphere, made of plates equal in thickness to those of the cylinder, it is stressed to only half the extent per square inch to which the cylinder is stressed.

### Hydraulic, Steam, and other Hollow Cylinders.

The resistance of, say, a hydraulic ram, to bursting pressure is unequally distributed over the transverse section of the ram, being a maximum at the interior surface, diminishing radially to a minimum at the outer surface. The inequality of active resistance arises from the stretching of the material exposed to pressure, up to and beyond the elastic limit.

The formulas for resistance, in their most general form, are as follows :—

$$p = s \times \text{hyp log. } R. \quad . \quad . \quad . \quad . \quad (120)$$

$$s = \frac{p}{\text{hyp log. } R.} \quad . \quad . \quad . \quad . \quad (121)$$

$$\text{hyp log. } R = \frac{p}{s} \quad . \quad . \quad . \quad . \quad (122)$$

$$d' = d \times R \quad . \quad . \quad . \quad . \quad (123)$$

$$t = \frac{d(R-1)}{2} \quad . \quad . \quad . \quad . \quad (124)$$

$d$  = inside diameter, in inches.

$d'$  = outside diameter, in inches.

$p$  = internal pressure in tons per square inch.

$s$  = maximum tensile stress, in tons per square inch.

$R$  = ratio of outside diameter to inside diameter, or  $\frac{d'}{d}$

*Note.*—The pressure and stress may be expressed in hundred-weights or in pounds.

In cases where the internal tensional stress on the material exceeds the elastic limit, the formulas are to be taken as only approximate. But it is believed that in such cases they are substantially correct for practical purposes. They are taken as correct for maximum tensional stress not exceeding the elastic limit.

The average tensional stress on the metal is equal to  $\frac{p d}{d' - d}$ .

That is to say, it is equal in tons per square inch to the product of the inside diameter by the internal pressure in tons per square inch, divided by the difference of the inside and outside diameters.

*Example.*—To find the bursting pressure of a cast-iron cylinder 8 inches in diameter inside, and 25 inches outside, the ultimate tensile strength of the metal being 7 tons per square inch. The ratio of the diameters is  $(25 \div 8 =) 3.12$ , of which the hyperbolic logarithm is 1.1378. By formula (120), the bursting pressure is  $(7 \times 1.1378 =) 7.96$  tons per square inch. The average stress over the whole sectional area of the metal is equal to  $(8 \times 7.96) \div (25 - 8) = 3.75$  tons per square inch of section of metal.

*2nd Example.*—To find the bursting pressure of a hydraulic tube  $1\frac{1}{8}$  inches in bore,  $\frac{5}{16}$  inch thick; the direct ultimate tensile strength being 22 tons per square inch. The ratio of the outside and inside diameters is  $(2\frac{1}{8} \div 1\frac{1}{8} =) 1.33$ , the hyperbolic logarithm of which is .2852. By formula (120), the bursting pressure is 6.27 tons, or 14,045 pounds per square inch. The tube had been proved to a pressure of 11,000 pounds without failure.

In cases where the diameter is considerable in relation to the thickness, the transverse resistance to bursting pressure is taken as equal to the direct tensile strength per square inch of sectional area, according to the common rules already given.

## WIRE ROPES AND HEMP ROPES.

The comprehensive Tables 207 to 211—of the weight and strength of wire ropes manufactured by Messrs. Dixon & Corbitt and R. S. Newall & Co.—comprise qualities varying from annealed iron having an ultimate tensile strength of 15 tons per square inch, and charcoal iron wire of 34 tons per

square inch, to special or extra plough steel wire of 150 tons. The "patent steel" is crucible steel or open hearth steel hardened and tempered by a special process.

The breaking strengths have been carefully ascertained. They are based on the most common system of construction :—round ropes of 6 strands of 7 wires each, or 6 strands of 6 wires each. In the first there are 6 wires over a central wire ; in the second, 6 wires over a hemp core. With such proportions, the cylindrical form is best maintained, and splicing is most readily effected. But ropes are made with from 3 to 12 strands. Wires vary from '010 inch to '212 inch in diameter for 6-strand ropes of 7 wires in each strand. But conductor or guide-ropes of 7 wires forming a strand have been made of  $\frac{5}{8}$  inch rods.

Tables 212 and 213 give the sizes and strength of hemp ropes by Messrs. Dixon & Corbitt and R. S. Newall & Co. For the dimensions of cotton ropes, the same firm assume that cotton is equal in strength to hemp ; and for coir ropes, that coir, or cocoa-fibre, is of half the strength.

For vertical winding at a high speed, they adopt one-tenth of the breaking stress as a safe working load. But the load may, with suitable working conditions, be increased to a value of one-eighth. The gross weight hanging over the pulley is taken as the working load.

For hauling, the working load is usually taken by them at one-sixth of the breaking stress ; and the following form of calculation for determining the proper size of rope, has been found by experience to be satisfactory :—Take an inclined plane, say, 800 yards in length ; load, 20 tons ; maximum inclination of road, 7 degrees, or 1 in 8·14.

*Calculation for Resistance.*

	cwts.	qrs.	lbs.
Gravity of load, 20 tons $\times$ 272·93 lbs. per ton	49	0	16
Friction of load, 20 tons $\times$ 20 lbs. per ton	3	2	8
Gravity of rope, 800 yards, at 2 lbs. per yard, =			
1600 lbs. $\div$ 8·14	1	3	1
Friction of rope, 1600 lbs. $\div$ 20	0	2	24
Total working stress or load	55	0	21

TABLE 207.—ROUND WIRE ROPES: WEIGHT

Sizes.		Weights per Fathom.		Charcoal Iron.			Bessemer Steel, or Ingot Iron.			Phosphor Bronze.		
Diameter.	Circumference.	6 Strands.		Breaking Strain.	Working Load.		Breaking Strain.	Working Load.		Breaking Strain.	Working Load.	
		1 Wires.	6 Wires.		Pit.	Incline.		Pit.	Incline.		Pit.	Incline.
Ins.	Ins.	Lbs.	Lbs.	Tons.	Cwts.	Cwts.	Tons.	Cwts.	Cwts.	Tons.	Cwts.	Cwts.
$\frac{11}{32}$	$1\frac{1}{8}$	1.2	1.1	1.4	3	5	2.2	4	7	2.2	4	7
$\frac{13}{32}$	$1\frac{1}{4}$	1.5	1.3	2.2	4	7	2.6	5	8	2.6	5	8
$\frac{15}{32}$	$1\frac{3}{8}$	1.8	1.6	2.7	5	9	3.2	6	10	3.2	6	10
$\frac{17}{32}$	$1\frac{1}{2}$	2.1	1.9	3.3	6	11	3.8	7	12	3.8	7	12
$\frac{19}{32}$	$1\frac{5}{8}$	2.5	2.3	4.0	8	13	4.6	9	15	4.6	9	15
$\frac{21}{32}$	$1\frac{3}{4}$	2.9	2.6	4.5	9	15	5.2	10	17	5.2	10	17
$\frac{23}{32}$	$1\frac{7}{8}$	3.3	3.0	5.2	10	17	6.0	12	20	6.0	12	20
$\frac{25}{32}$	2	3.8	3.5	6.2	12	20	7.0	14	23	7.0	14	23
$\frac{27}{32}$	$2\frac{1}{8}$	4.3	4.0	7.0	14	23	8.0	16	26	8.0	16	26
$\frac{29}{32}$	$2\frac{1}{4}$	4.8	4.4	7.7	15	25	8.8	18	29	8.8	18	29
$\frac{31}{32}$	$2\frac{3}{8}$	5.3	4.9	8.5	17	28	9.8	20	32	9.8	20	32
$\frac{33}{32}$	$2\frac{1}{2}$	5.9	5.5	9.6	19	32	11.4	22	36	11.0	22	36
$\frac{35}{32}$	$2\frac{5}{8}$	6.6	6.0	10.5	21	35	12.9	24	40	12.0	24	40
$\frac{37}{32}$	$2\frac{3}{4}$	7.1	6.6	11.5	23	38	13.2	26	44	13.2	26	44
$\frac{39}{32}$	$2\frac{7}{8}$	7.8	7.2	12.6	25	42	14.4	28	48	14.4	28	48
$\frac{41}{32}$	3	8.5	7.8	13.6	27	45	15.6	31	52	15.6	31	52
$\frac{43}{32}$	$3\frac{1}{8}$	9.2	8.5	14.8	29	49	17.0	34	56	17.0	34	56
$\frac{45}{32}$	$3\frac{1}{4}$	9.9	9.1	15.9	31	53	18.2	36	60	18.2	36	60
$\frac{47}{32}$	$3\frac{3}{8}$	10.7	9.9	17.5	34	57	19.8	39	66	19.8	39	66
$\frac{49}{32}$	$3\frac{1}{2}$	11.5	10.6	18.5	37	61	21.2	42	70	21.2	42	70
$\frac{51}{32}$	$3\frac{5}{8}$	12.3	11.4	19.6	39	66	22.8	45	76	22.8	45	76
$\frac{53}{32}$	$3\frac{3}{4}$	13.2	12.2	21.3	42	71	24.4	48	81	24.4	48	81
$\frac{55}{32}$	$3\frac{7}{8}$	14.1	13.0	22.7	45	75	26.0	52	86	26.0	52	86
$\frac{57}{32}$	4	15.0	13.9	24.3	48	81	27.8	55	92	27.8	55	92
$\frac{59}{32}$	$4\frac{1}{8}$	16.0	14.8	25.4	51	85	29.6	59	98	29.6	59	98
$\frac{61}{32}$	$4\frac{1}{4}$	17.0	15.7	27.4	54	91	31.4	62	104	31.4	62	104
$\frac{63}{32}$	$4\frac{3}{8}$	18.0	16.6	29.0	58	96	33.2	66	110	33.2	66	110
$\frac{65}{32}$	$4\frac{1}{2}$	19.0	17.6	30.8	61	102	35.2	70	117	35.2	70	117
$\frac{67}{32}$	$4\frac{3}{4}$	21.2	19.6	34.3	68	114	39.2	78	130	39.2	78	130
$\frac{69}{32}$	$4\frac{5}{8}$	22.0	20.6	36.0	72	126	41.2	82	137	41.2	82	137
$\frac{71}{32}$	5	23.5	21.7	37.9	75	126	43.4	86	144	43.4	86	144
$\frac{73}{32}$	$5\frac{1}{4}$	26.0	24.0	42.0	84	140	48.0	96	160	48.0	96	160
$\frac{75}{32}$	$5\frac{1}{2}$	28.5	26.3	45.5	91	151	52.6	105	175	52.6	105	175
$\frac{77}{32}$	$5\frac{3}{4}$	31.1	28.7	50.2	100	167	57.4	114	191	57.4	114	191
$\frac{79}{32}$	6	34.0	31.3	54.7	109	182	62.6	125	208	62.6	125	208



AND STRENGTH (Dixon & Corbitt).

Crucible Steel.			Patent Steel.			Plough Steel.			Extra Plough Steel.		
Breaking Strain.	Working Load.		Breaking Strain.	Working Load.		Breaking Strain.	Working Load.		Breaking Strain.	Working Load.	
	Pit.	Incline.		Pit.	Incline.		Pit.	Incline.		Pit.	Incline.
Tons.	Cwts.	Cwts.	Tons.	Cwts.	Cwts.	Tons.	Cwts.	Cwts.	Tons.	Cwts.	Cwts.
2.7	5	9	3.4	6	11	4.2	8	14	4.9	10	16
3.2	6	10	4.0	8	13	4.9	10	16	5.8	12	19
4.0	8	13	5.0	10	16	6.1	12	20	7.2	14	24
4.7	9	15	5.9	12	20	7.2	14	24	8.5	17	28
5.7	11	18	7.2	14	24	8.7	17	29	10.3	21	34
6.5	13	21	8.0	16	26	9.9	20	33	11.7	24	39
7.5	15	25	9.4	19	31	11.4	23	37	13.5	27	45
8.7	17	29	10.9	22	36	13.3	26	44	15.7	31	52
10.0	20	33	12.6	25	42	15.3	30	50	18.0	36	60
11.0	22	36	13.8	28	46	16.8	33	55	19.8	40	66
12.2	24	40	15.3	31	51	18.7	37	62	22.0	44	73
13.7	27	45	17.2	35	57	21.0	42	70	24.7	49	82
15.0	30	50	19.9	39	66	22.9	46	76	27.0	54	90
16.5	33	55	20.8	43	69	25.1	50	84	29.7	59	99
18.0	36	60	22.6	45	75	27.5	55	91	32.4	64	108
19.5	39	65	24.5	49	81	29.8	59	99	35.1	70	117
21.2	42	70	26.7	53	89	32.5	65	108	38.2	76	127
22.7	45	75	28.6	57	95	34.8	69	116	40.0	82	136
24.7	49	82	31.1	62	103	37.8	75	126	44.5	89	148
26.5	53	88	33.3	67	111	40.5	80	135	47.7	95	159
28.5	57	94	35.9	72	119	43.6	87	145	51.3	102	171
30.5	61	101	38.4	77	128	46.6	93	155	54.0	108	180
32.5	65	108	40.9	82	136	49.7	99	165	58.5	117	195
34.7	69	115	43.7	87	145	53.1	106	177	62.5	125	208
37.0	74	123	46.6	93	155	56.6	113	188	66.6	133	222
39.2	78	130	49.4	99	164	60.0	120	200	70.6	141	235
41.5	83	138	52.2	105	174	63.4	127	211	74.7	149	249
44.0	88	146	55.4	111	184	67.3	134	224	79.2	158	264
49.0	98	163	61.7	123	205	74.9	150	249	88.2	176	294
51.5	103	171	64.8	130	216	78.8	157	262	92.7	185	309
54.2	108	180	68.3	137	227	83.0	166	276	97.6	195	325
60.0	120	200	75.6	151	252	91.8	183	306	108.0	216	360
65.7	131	219	82.8	175	275	100.5	201	335	118.3	238	394
71.7	143	239	90.3	180	301	109.7	219	365	129.1	258	430
78.2	156	260	98.5	197	328	119.7	239	399	140.8	281	469

The next higher working load for Extra Plough Steel Ropes on inclines, in Table 207, is 60 cwt., for which a  $2\frac{1}{2}$ -inch rope is required.

The subjoined table shows the inclination of inclined ways, in inches per yard, and the length for a rise of 1, corresponding to a given number of degrees of inclination; together with the resistance of gravity for each incline.

TABLE 208.—INCLINATION AND RESISTANCE OF INCLINED WAYS.

(Dixon & Corbitt.)

Inclination.	Inclination in Inches per Yard.	Inclination.	Resistance of Gravity due to Incline.	Inclination.	Inclination in Inches per Yard.	Inclination.	Resistance of Gravity due to Incline.
Degs.	Inches.	1 in	Pounds per Ton.	Degs.	Inches.	1 in	Pounds per Ton.
1	0.63	57.29	39.08	19	12.39	2.90	729.27
2	1.26	28.63	78.18	20	13.10	2.74	766.12
3	1.88	19.09	117.24	21	13.82	2.60	802.74
4	2.51	14.29	156.26	22	14.54	2.47	839.12
5	3.15	11.42	195.24	23	15.27	2.35	875.23
6	3.78	9.51	234.14	24	16.02	2.24	911.09
7	4.42	8.14	272.98	25	16.78	2.14	946.66
8	5.06	7.11	311.74	26	17.56	2.05	981.94
9	5.70	6.31	350.40	27	18.34	1.96	1016.93
10	6.34	5.67	388.97	28	19.14	1.88	1051.61
11	6.99	5.14	427.41	29	19.95	1.80	1085.97
12	7.65	4.70	465.71	30	20.78	1.73	1120.0
13	8.31	4.33	503.88	31	21.62	1.66	1153.68
14	8.97	4.01	541.90	32	22.49	1.60	1187.02
15	9.64	3.73	579.75	33	23.37	1.54	1219.99
16	10.32	3.48	617.43	34	24.28	1.48	1252.58
17	11.0	3.27	654.90	35	25.20	1.42	1284.81
18	11.69	3.07	692.20				

TABLE 209.—FLAT WIRE ROPES : STRENGTH AND WEIGHT.  
(Dixon & Corbitt.)

Sizes.			Weights per Fathom.		Charcoal Iron.		Bessemer or Ingot Iron.		Crucible Steel.		Patent Steel.		Plough Steel.	
					Breaking Strain.	Working Load.	Breaking Strain.	Working Load.	Breaking Strain.	Working Load.	Breaking Strain.	Working Load.	Breaking Strain.	Working Load.
Ins.	Ins.	Lbs.	Tons.	Cwts.	Tons.	Cwts.	Tons.	Cwts.	Tons.	Cwts.	Tons.	Cwts.	Tons.	Cwts.
2 $\frac{1}{8}$ ×	7 $\frac{7}{16}$	9	10	20	14	28	19	38	23	46	36	72	42	84
2 $\frac{3}{8}$ ×	7 $\frac{7}{16}$	10	12	24	16	32	22	44	27	54	42	84	49	98
2 $\frac{1}{2}$ ×	7 $\frac{7}{16}$	12	14	28	19	38	25	50	32	64	49	98	56	112
2 $\frac{3}{4}$ ×	7 $\frac{7}{16}$	14	16	32	22	44	29	58	36	72	56	112	65	130
3 ×	9 $\frac{9}{16}$	16	18	36	25	50	34	68	42	84	65	130	74	148
3 $\frac{1}{4}$ ×	9 $\frac{9}{16}$	18	21	42	29	58	38	76	48	96	74	148	83	166
3 $\frac{1}{2}$ ×	9 $\frac{9}{16}$	20	23	46	32	64	43	86	54	108	83	166	93	186
3 $\frac{3}{4}$ ×	9 $\frac{9}{16}$	22	26	52	36	72	49	98	61	122	93	186	102	204
4 ×	11 $\frac{11}{16}$	25	29	58	40	80	54	108	67	134	102	204	115	230
4 $\frac{1}{4}$ ×	11 $\frac{11}{16}$	28	32	64	44	88	58	116	73	146	115	230	124	248
4 $\frac{1}{2}$ ×	11 $\frac{11}{16}$	30	35	70	48	96	64	128	81	162	124	248	135	270
4 $\frac{3}{4}$ ×	11 $\frac{11}{16}$	32	37	74	52	104	70	140	88	176	135	270	146	292
5 ×	13 $\frac{13}{16}$	34	40	80	57	114	76	152	95	190	146	292	160	320
5 $\frac{1}{8}$ ×	13 $\frac{13}{16}$	36	44	88	62	124	83	166	104	208	160	320	172	344
5 $\frac{1}{4}$ ×	13 $\frac{13}{16}$	38	48	96	67	134	89	178	112	224	172	344	184	368
5 $\frac{1}{2}$ ×	15 $\frac{15}{16}$	40	52	104	72	144	96	192	120	240	184	368	200	400
5 $\frac{3}{4}$ ×	15 $\frac{15}{16}$	42	56	112	78	156	104	208	130	260	200	400	213	426
6 ×	17 $\frac{17}{16}$	45	60	120	83	166	111	222	138	276	213	426	228	456
6 $\frac{1}{4}$ ×	17 $\frac{17}{16}$	48	64	128	90	180	120	240	150	300	228	456	254	508
6 $\frac{1}{2}$ ×	17 $\frac{17}{16}$	13	15	30	22	44	27	54	36	72	54	108	64	128
6 $\frac{3}{4}$ ×	17 $\frac{17}{16}$	16	18	36	26	52	32	64	43	86	64	128	73	146
7 ×	19 $\frac{19}{16}$	18	20	40	30	60	37	74	48	96	73	146	85	170
7 $\frac{1}{8}$ ×	19 $\frac{19}{16}$	21	24	48	34	68	43	86	56	112	85	170	97	194
7 $\frac{1}{4}$ ×	19 $\frac{19}{16}$	24	27	54	38	76	49	98	64	128	97	194	108	216
7 $\frac{1}{2}$ ×	19 $\frac{19}{16}$	27	30	60	43	86	55	110	72	144	108	216	123	246
7 $\frac{3}{4}$ ×	19 $\frac{19}{16}$	29	34	68	48	96	63	126	81	162	123	246	135	270
8 ×	21 $\frac{21}{16}$	32	38	76	53	106	70	140	89	178	135	270	150	300
8 $\frac{1}{4}$ ×	21 $\frac{21}{16}$	36	41	82	58	116	76	152	97	194	150	300	162	324
8 $\frac{1}{2}$ ×	21 $\frac{21}{16}$	39	46	92	65	130	84	168	108	216	162	324	175	350
8 $\frac{3}{4}$ ×	21 $\frac{21}{16}$	42	50	100	70	140	92	184	119	238	175	350	187	374
9 ×	23 $\frac{23}{16}$	44	54	108	76	152	99	198	126	252	187	374	208	416
9 $\frac{1}{4}$ ×	23 $\frac{23}{16}$	47	59	118	83	166	109	218	139	278	208	416	224	448
9 $\frac{1}{2}$ ×	23 $\frac{23}{16}$	50	63	126	89	178	117	234	149	298	224	448	240	480
9 $\frac{3}{4}$ ×	23 $\frac{23}{16}$	54	68	136	96	192	126	252	160	320	240	480		

TABLE 210.—WIRE CORDS FOR CLOCKS, SASH-LINES, &c. :  
STRENGTH.  
(Dixon & Corbitt.)

No.	Diameter.	Copper.		Phosphor Bronze.		Iron.		Steel.		Patent Steel (Crucible or Open Hearth).	
		Breaking Stress.	Working Load.	Breaking Stress.	Working Load.	Breaking Stress.	Working Load.	Breaking Stress.	Working Load.	Breaking Stress.	Working Load.
	Inch.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
4	·108	181	45	363	90	318	79	493	123	697	174
3½	·117	213	53	428	107	374	93	576	144	817	204
3	·126	248	62	496	124	435	108	671	167	949	237
2¾	·135	286	71	572	143	500	125	778	194	1127	281
2½	·144	324	81	648	162	565	141	875	219	1240	310
2	·153	367	91	734	183	640	160	1005	251	1410	352
1¾	·171	459	114	918	229	802	200	1248	312	1750	437
1¾	·189	560	140	1121	280	981	245	1539	384	2123	530
1½	·207	671	167	1342	335	1173	293	1815	454	2560	640
1½	·225	790	197	1580	395	1382	345	2129	532	2974	743
1¼	·252	992	248	1984	496	1735	434	2673	668	3790	947
1¼	·288	1294	323	2588	647	2264	566	3500	875	5606	1400
1	·324	1651	410	3283	820	2865	716	4439	1109	6286	1500

Note.—Cords made of six strands of six wires each.

TABLE 211.—SUNDRY WIRE CORDS AND ROPES.  
(Dixon & Corbitt.)

GALVANIZED SIGNAL AND FENCING STRAND.												
7 Wires.	No.	00	0	1	2	3	4	5	6	7	8	9
Diameter.	Inch.	·345	·318	·294	·267	·255	·240	·213	·198	·186	·171	·147
Weight per 100 yards.	Lbs.	73	62½	53	44	40	35½	27¾	24½	21½	18	13½
CAGE GUIDE ROPES.												
Inches circumference		2¼	2½	2¾	3	3¼	3½	3¾	4	4¼	4½	4¾
Weight per fathom.	Lbs.	6¾	8¾	10	11¾	13¾	16	18½	21	23½	26½	29½
ELECTRO-GILT AND SILVER PICTURE CORDS.												
Reference No.				1	2	3	4	5	6			
Breaking strain in lbs.				48	90	120	200	400	600			
Working load				12	22	30	50	100	150			

TABLE 212.--ROUND HEMP ROPES: WEIGHT AND STRENGTH.

(Dixon & Corbitt.)

Sizes.		Tarred Russian.			White Manilla.		
Dia- meter.	Circum- ference.	Weight per Fathom.	Break- ing Strain.	Work- ing Load.	Weight per Fathom.	Break- ing Strain.	Work- ing Load.
Inches.	Inches.	Lbs.	Tons.	Cwts.	Lbs.	Tons.	Cwts.
$\frac{5}{8}$	2	1.0	1.0	4	.7	1.2	5
$\frac{23}{32}$	$2\frac{1}{4}$	1.2	1.2	5	.9	1.5	6
$\frac{25}{32}$	$2\frac{1}{2}$	1.5	1.5	6	1.2	2.1	8
$\frac{27}{32}$	$2\frac{3}{4}$	1.8	1.8	8	1.3	2.3	9
$\frac{7}{8}$	$2\frac{3}{4}$	2.2	2.2	9	1.6	2.8	11
$\frac{15}{16}$	3	2.5	2.5	10	1.9	3.3	13
$1\frac{1}{32}$	$3\frac{1}{4}$	3.0	3.0	12	2.2	3.8	15
$1\frac{1}{8}$	$3\frac{1}{2}$	3.5	3.5	14	2.6	4.5	18
$1\frac{3}{16}$	$3\frac{3}{4}$	4.0	4.0	16	2.9	5.0	20
$1\frac{1}{4}$	4	4.5	4.5	18	3.3	5.7	23
$1\frac{11}{32}$	$4\frac{1}{4}$	5.0	5.0	20	3.7	6.4	25
$1\frac{5}{16}$	$4\frac{1}{2}$	5.5	5.5	22	4.1	7.1	28
$1\frac{13}{32}$	5	6.2	6.2	25	4.5	7.8	31
$1\frac{3}{4}$	$5\frac{1}{2}$	7.4	7.4	29	5.5	9.6	38
$1\frac{29}{32}$	6	8.8	8.8	35	6.5	11.3	45
$2\frac{1}{16}$	$6\frac{1}{2}$	10.4	10.4	41	7.6	13.3	53
$2\frac{1}{4}$	7	12.0	12.0	48	8.9	15.5	62
$2\frac{3}{8}$	$7\frac{1}{2}$	13.8	13.8	55	10.2	17.8	71
$2\frac{17}{32}$	8	15.7	15.7	60	11.6	20.3	81
$2\frac{3}{4}$	$8\frac{1}{2}$	17.7	17.7	68	13.0	22.7	91
$2\frac{27}{32}$	9	19.8	19.8	76	14.6	25.5	102
3	$9\frac{1}{2}$	22.1	22.1	88	16.3	28.5	114
$3\frac{3}{16}$	10	24.4	24.4	99	18.0	31.5	126
$3\frac{3}{8}$	$10\frac{1}{2}$	27.0	27.0	108	19.9	34.8	139
$3\frac{1}{2}$	11	29.6	29.6	116	21.8	38.1	152
$3\frac{5}{8}$	$11\frac{1}{2}$	32.4	32.4	131	23.8	41.6	166
$3\frac{13}{16}$	12	35.2	35.2	141	26.0	45.5	182
4	$12\frac{1}{2}$	38.2	38.2	153	28.2	49.3	197
$4\frac{5}{32}$	13	41.4	41.4	167	30.5	53.9	215
$4\frac{3}{16}$	$13\frac{1}{2}$	44.6	44.6	176	32.8	57.4	229
$4\frac{7}{16}$	14	48.0	48.0	192	35.3	61.7	247
$4\frac{5}{8}$	$14\frac{1}{2}$	51.5	51.5	204	37.8	66.1	264
$4\frac{3}{4}$	15	55.0	55.0	220	40.5	70.0	280
5	16	62.6	62.6	248	46.1	80.6	322
$5\frac{13}{32}$	17	70.7	70.7	280	52.0	91.0	364
$5\frac{3}{4}$	18	79.2	79.2	317	58.3	102	408

TABLE 213.—FLAT HEMP ROPES : WEIGHT AND STRENGTH.

(Dixon &amp; Corbitt.)

SIZES.	TARRED RUSSIAN.			COMBINED RUSSIAN AND MANILLA.		
	Weight per Fathom.	Break- ing Stress.	Working Load.	Weight per Fathom.	Break- ing Stress.	Working Load.
Inches.	Pounds.	Tons.	Cwts.	Pounds.	Tons.	Cwts.
FOUR ROPES.						
$3\frac{1}{2} \times 1$	10	10	20	9 $\frac{1}{2}$	11	22
$4 \times 1\frac{1}{16}$	13 $\frac{1}{2}$	13 $\frac{1}{2}$	27	12 $\frac{1}{2}$	15	30
$4\frac{1}{2} \times 1\frac{3}{16}$	17	17	34	16	19	38
$5 \times 1\frac{1}{2}$	21	21	42	19 $\frac{1}{2}$	23	46
$5\frac{1}{2} \times 1\frac{1}{2}$	25	25	50	23 $\frac{1}{2}$	28	56
$6 \times 1\frac{1}{2}$	30	30	60	28	33	66
$6\frac{1}{2} \times 1\frac{3}{4}$	34	34	68	32	38	76
$7 \times 1\frac{1}{2}$	38	38	76	36	43	86
$7\frac{1}{2} \times 2$	43	43	86	40	48	96
SIX ROPES.						
$4 \times \frac{13}{16}$	10	10	20	9 $\frac{1}{2}$	11	22
$4\frac{1}{2} \times \frac{13}{16}$	13	13	26	12	14	28
$5 \times 1$	16	16	32	14 $\frac{1}{2}$	17	34
$5\frac{1}{2} \times 1\frac{1}{2}$	19	19	38	16	20	40
$6 \times 1\frac{1}{4}$	22	22	44	20	24	48
$6\frac{1}{2} \times 1\frac{3}{8}$	25	25	50	22 $\frac{1}{2}$	27	54
$7 \times 1\frac{1}{2}$	28	28	56	25	30	60
$7\frac{1}{2} \times 1\frac{1}{2}$	32	32	64	29	34	68
$8 \times 1\frac{1}{2}$	36	36	72	33	39	78

TABLE 214.—HEMP ROPES AND WIRE ROPES: SIZE AND WEIGHT FOR EQUAL STRENGTHS.

(J. Shaw.)

## I. ROUND ROPES.

Hemp.		Crucible Cast Steel.		Charcoal Wire.		Strength.	
Circumference.	Weight per Fathom (approximate).	Circumference.	Weight per Fathom (approximate).	Circumference.	Weight per Fathom (approximate).	Breaking Stress.	Working Load (approximate).
Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.	Tons.	Cwts.
3½	3	1½	1½	1½	2	2¾	9
4	4	1¾	1¾	1¾	2¾	4	15
4½	5	1½	2	2	3¼	6	20
5	6½	1¾	2¾	2¼	4½	7½	24
5½	7½	1¾	3	2½	5½	9½	30
6	8½	2	3¼	2¾	6½	11½	36
6½	10	2¼	4½	3	7¾	14	45
7	12	2½	5½	3¼	8½	16	52
7½	14	2¾	6	3½	10½	19	62
8	16	2¾	6½	3¾	12½	22	74
8½	18	3	7¾	4	14	25	80
9	20	3¼	9¼	4¼	16	28	95
9½	23	3½	10¾	4½	18	32	105
10	26	3¾	12½	4¾	20	36	120
10½	29	4	14¼	5	22	40	135
11	31	4¼	15	5¼	25	45	150
11½	34	4¼	16	5½	28	50	160
12	37	4½	18	5¾	31	55	170
13	41	4¾	20	6	35	60	180

## II. FLAT ROPES.

Sizes. Inches.		Sizes. Inches.		Sizes. Inches.			
3½ × 1	12	...	...	2¼ × ½	10	18	40
4 × 1½	15	...	...	2½ × ½	12	20	45
4½ × 1½	20	...	...	2¾ × ¾	14	23	51
5 × 1¾	24	2¼ × ½	10	3 × ¾	16	27	56
5½ × 1¾	27	2½ × ½	12	3¼ × ¾	18	30	60
6¼ × 1¾	30	2¾ × ¾	14	3½ × ¾	20½	33	68
6½ × 2	33	3 × ¾	16	3¾ × ¾	22½	36	78
7 × 2	36	3¼ × ¾	18½	4 × ¾	25	39	90
7¼ × 2½	39	3½ × ¾	21	4¼ × ¾	28	42	106
8 × 2½	42	3¾ × ¾	22½	4½ × ¾	32	45	118

TABLE 215.—STEEL WIRE ROPES : BREAKING STRESS.  
(J. Shaw.)

Plough Steel Wire Rope.		Hard Steel Ropes.		Iron Wire Guides, or Conducting Rods.	
Circumference.	Breaking Stress.	Circumference.	Breaking Stress.	Circumference.	Weight per Fathom.
Inches.	Tons.	Inches.	Tons.	Inches.	Pounds.
1½	12	1½	9½	2¾	13
1¾	15½	1¾	11½	3	15
2	18	2	14	3¼	18
2¼	24	2¼	17	3½	21
2½	27	2½	21	3¾	24
2¾	31½	2¾	26	4	28
3	38	3	31		
3¼	46	3¼	37		
3½	53	3½	42		
3¾	59	3¾	50		
4	68	4	55		
4¼	76	4¼	63		
4½	88	4½	71		
5	100	5	90		

### Duboul's Experiments on the Strength of Ropes.

M. Duboul tested ropes and cables of white hemp and tarred hemp, Italian, Russian, and French ; of long fibre, hand spun, with from fifty to fifty-five twists to the yard ; 1½ yards of rope yarn sufficing to make one yard of cable. A selection of results is given in Table 216.

Flat tarred ropes were proved to a mean strength of from 3·43 tons to 3·75 tons per square inch, rupture taking place at the points of attachment. The extension rarely exceeded from 5 to 6 per cent.

The average ultimate tensile strength of rope was as follows:—

	Tons.	Tons.
White hemp . . . . .	4·76 to 5·08	per square inch.
Tarred hemp . . . . .	3·54 „ 3·81	„ „ „
White Manilla . . . . .	4·44 „ 4·76	„ „ „
White aloes . . . . .	2·54 „ 3·17	„ „ „
Flat ropes of tarred hemp, or	3·54 „ 3·81	„ „ „
Tarred Manilla . . . . .		
Esparto and cocoa fibres . . . . .	1·00 „ 1·25	„ „ „

M. Duboul deduced from results of practice that round ropes and cables may be worked at a stress equal to one-third of the ultimate strength ; and flat ropes at one-fourth. In ordinary practice, the proportion is often not more than from one-sixth to one-eighth.



TABLE 216.—RESULTS OF TESTS OF ROUND ROPES.  
(M. Duboul.)

	White Hemp.	Tarred Hemp.	White Manila.	White Aloes.
Circumference before rupture . . . Inches	4.33	4.25	3.94	4.33
" after . . . "	3.86	3.70	3.27	3.54
Length tested . . . Feet	32.8	32.8	32.8	32.8
" measured for testing extension . . . "	13.1	13.1	13.1	13.1
Extension . . . Inches	27.2	25.6	22.8	26.0
Section of the four strands . . . Square Inch	.819	.819	.819	.819
Section of the piece . . . " Tons	1.490	1.481	1.246	1.491
Resistance . . . of the four strands per square inch . . . "	7.94	5.22	5.44	3.99
" of the piece per square inch . . . "	9.78	6.35	6.60	4.83
Weight of the whole piece tested . . . Pounds	5.27	3.49	4.32	2.67
	17.4	18.7	15.0	15.0
	17.6	19.6	15.2	15.4

M. Duboul estimates that ropes and cables of galvanized charcoal-iron wire unannealed, have two-tenths of the diameter of hemp cables of equal strength; or three-tenths for annealed wire.

	Ultimate Strength per Square Inch, Section of Metal.	Extension.	Elasticity.
Rope of unannealed wire	25.4 to 31.7 tons	7 to 9 %	1 to 2 %
" annealed "	22.2 to 25.4 "	12 to 15 "	3 to 4 "

The galvanized wire tested by itself, yields 10 per cent. more resistance to rupture than in the form of rope.

Wire-ropes for mining service, of the first quality, have an ultimate strength of from 40 to 45 tons per square inch of metal section.

Cast-steel wire ropes stretch from 4 to 6 per cent. before rupture, with an elastic limit of from 2 to 3½ per cent. They bear three-fourths of the breaking stress before exhibiting any sign of failure.

TABLE 217.—STEEL WIRE ROPE, FOR STANDING RIGGING.  
(Admiralty.)

Size of Rope (Girth).	Number of Strands.	Wires in one Strand.	Thick- ness of Wires.	Weight per Fathom.	Length of one Coil.	Breaking Stress (Mini- mum).
Inches.	Strands.	Wires.	I. W. G.	Pounds.	Fathoms.	Tons.
8	6	19	6	62	100	160
7½	6	19	7	53	100	141
7	6	19	8	46	100	123
6½	6	19	6	40	100	106
6	6	19	10	34	100	90
5½	6	19	10	28	100	76
5	6	19	12	23	100	63
4½	6	19	12	19	150	51
4	6	19	14	15½	150	40
3½	6	7	10	11½	150	32
3¼	6	7	11	10	150	27
3	6	7	12	8	200	24
2¾	6	7	13	7	200	19
2½	6	7	13	6	200	16
2¼	6	7	14	5	200	13
2	6	7	15	4	200	10
1¾	6	7	16	3	200	8
1½	6	7	18	2	200	6
1¼	6	7	18	1½	200	3¼
1	6	7	20	1	200	2½

TABLE 218.—STEEL WIRE ROPES, FOR HAWSERS AND  
RUNNING RIGGING.  
(Admiralty.)

Size of Rope (Girth).	Number of Strands.	Wires in one Strand.	Thick- ness of Wires.	Weight per Fathom.	Length of one Coil.	Breaking Stress (Mini- mum).
Inches.	Strands.	Wires.	L. W. G.	Pounds.	Fathoms.	Tons.
8	6	30	9	...	150	...
7	6	30	11	...	150	...
6½	6	30	12	35	150	98
6	6	30	12	31	150	84
5½	6	25	12	28	150	71
5	6	25	13	23	150	59
4½	6	12	12	15	150	39
4	6	12	13	12	240	31
3½	6	12	14	9	360	24
3¼	6	12	15	8	360	20
3	6	12	16	7	360	17
2¾	6	12	17	5½	360	14½
2½	6	12	17	4½	360	11¾
2¼	6	12	18	3¾	300	9
2	6	12	19	2¾	300	7
1¾	6	12	20	2	300	5½
1½	6	12	21	1¾	300	4
1¼	6	12	22	1¼	300	2⅞
1	6	12	24	¾	300	1¾

**Resistance of Ropes to Bending Stress.**

The resistance of ropes to bending stress in passing over a pulley or a barrel is expressed by the following formulas, the equivalents in English measures of Longraire's formulas:—

*Hemp Ropes, either White or Tarred.*

$$S = \cdot 0328 T \frac{w}{D} \quad . \quad . \quad . \quad (125)$$

*Iron Wire Ropes (Hemp Core).*

$$S = (3\cdot 61 + \cdot 00262 T) \frac{w}{D} \quad . \quad . \quad . \quad (126)$$

*Steel Wire Ropes (Hemp Core).*

$$S = (6.314 + .00262 T) \frac{w}{D} \quad . \quad . \quad (127)$$

*Steel Wire Ropes, rusted.*

$$S = (5.412 + .00262 T) \frac{w}{D} \quad . \quad . \quad (128)$$

*Steel Wire Ropes, Lubricated in Oil Bath.*

$$S = (3.428 + .00172 T) \frac{w}{D} \quad . \quad . \quad (129)$$

$S$  = resistance to bending stress ; or the total tensile stress or pull minus the resisting stress in the rope, in the advancing limb of the rope.

$T$  = resisting stress on the rope, in the advancing limb of the rope.

$w$  = weight of rope per fathom, in pounds.

$D$  = diameter of pulley or barrel, in feet.

The foregoing formulas apply to ropes which are new or nearly new ; and for wire ropes of wire 3 millimetres, or about  $\frac{1}{8}$  inch thick. The resistance may be reduced ultimately by wear by 20 per cent. for iron ropes, and 33 per cent. for steel ropes. The experiments were made with wire ropes of from 6 lbs. to 13 lbs. per fathom, or from .83 inch to 1.30 inch in diameter.

## CHAINS AND CHAIN-CABLES.

Cables for use in the naval and merchant service are made of round iron, in lengths of 15 fathoms, with stud-links. For standing rigging and crane chain, short or unstudded links are employed.

Chains are made of puddled iron, bars of which have, or ought to have, an ultimate tensile strength of 23 tons per square inch, stretching from 20 to 25 per cent. in a length of 10 inches ; with a contraction of sectional area of from 45 to 50 per cent.

The links of chain-cables and short links generally are geometrically similar for all sizes, according to the following proportions, which are those of the links after having been submitted to the proof stress : the length of the common stud-link being 6 diameters, and the width about  $3\frac{1}{2}$  diameters, whilst the length and width of the short-link are respectively about 5 diameters and  $3\frac{1}{2}$  diameters.

	Diameter of iron . . .	Stud-Link, 1	Short-Link, 1
Common Links	{ Length of link outside . . .	6	4.9
	{ Width of link outside . . .	3.6	3.5
	{ Radius of each end inside . . .	.58	.60
	{ Length of stud at crown . . .	1.6	—
	{ Width in parts of length 60 per cent. 71 per cent.		
Enlarged Links	{ Diameter of iron . . .	1.1	1.1
	{ Length of link outside . . .	6.5	5.7
	{ Width of link outside . . .	4.0	3.8
	{ Radius of each end inside . . .	.64	.63
End Links	{ Diameter of iron . . .	1.2	1.2
	{ Length of link outside . . .	6.5	6.6
	{ Width of link outside . . .	4.0	4.1

The length of one link varies as the size or diameter, whilst the weight is as the cube of the diameter. The weight per unit of length,—say, one fathom,—varies, therefore, as the square of the diameter, and is expressed by the following formulæ, in which  $d$  is the size or diameter in inches, and  $W$  is the weight per fathom in pounds :—

$$(\text{Stud-link chains}) \quad . . . \quad W = 53.76 d^2 \quad . . . \quad (130)$$

$$(\text{Short-link or crane chain}) \quad . \quad W = 55 d^2 \quad . . . \quad (131)$$

The proof tensile strength also varies as the square of the diameter, and therefore it varies as the weight.

	Stud-Link,	Short-Link,	
The actual ultimate strength of good ordinary cable, in tons . . .	$\left. \begin{array}{l} \\ \end{array} \right\} = 29d^2 \text{ to } 26.7d^2$	$27.3d^2 \text{ to } 25.1d^2$	(132)

The statutory ultimate strength in tons . . .	$\left. \begin{array}{l} \\ \end{array} \right\} = 27d^2 \text{ to } 25.2d^2$	$24d^2$	(133)
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The statutory proof strength in tons . . .	$\left. \begin{array}{l} \\ \end{array} \right\} = 18d^2$	$12d^2$	(134)
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The safe-working stress (half the proof strength) . . .	$\left. \begin{array}{l} \\ \end{array} \right\} = 9d^2$	$6d^2$	(135)
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It is here shown that whilst the actual ultimate strength (132) of short-links is little less than that of stud-links, the

D D

proof stress and the safe-working stress, (134) and (135), for the short-links, are only two-thirds of those for the stud-links, by reason of the lower elastic limit of the short links.

The Tables 219 and 220, from which the foregoing formulæ have been deduced, give the dimensions, weight, and strength of stud-link and short-link chain-cables. In Table 220, for short-links, there are no statutory tests for cables above 1½ inches in diameter; but the appropriate stresses, with actual strengths for the larger sizes, calculated and supplied by Mr. T. Traill (in "*Chain-Cables and Chains*") are added in the table. In the second last column are given the safe-working strengths of cables, the factor of strength averaging for stud-links a little over 3; and for short-links about 4½.

The safe-working load in tons is approximately expressed by the following formulæ:—

$$\text{Short-link chain} \quad . \quad . \quad \frac{D^2}{10} \quad . \quad . \quad (136)$$

$$\text{Stud-link chain.} \quad . \quad . \quad \frac{D^2}{7} \quad . \quad . \quad (137)$$

in which D is the diameter of the iron in eighths of an inch. The values thus obtained are about 7 per cent. too high for the short-link chain, and about 1 per cent. too high for the stud-link chain.

The Admiralty have special proportions for iron chain rigging and crane work, for which the sizes and weights are given in Table 222. The Admiralty chain moorings are noted in Table 221, in which the sizes, weights, and proof stresses are given. They are of unstudded or open links, and these are shaped differently from the ordinary short-link, being made thicker at the ends, the wearing parts. Mooring chains are in consequence heavier than short-link chains of the same sizes.

The India Office prescribe for all services, except Marine, short-link chains, of which the common links are not to exceed 4½ diameters in length, and 3½ diameters in width. The weight and conditions of test are given in Table 223.

In the Trinity House contracts, it is specified that mooring chains, chain cables, crane and rigging chains, and appurtenances, except the stay-pins and steel pins, are to be of fibrous iron, to have a tensile stress of not less than 23 tons per square inch, with a contraction of sectional area at the fracture of not less than 40 per cent. of the original area. The cast iron of which the stay-pins are made is to have a compressive stress of not less than 52 tons per square inch of

TABLE 219.—STUD-LINK CHAIN-CABLES: DIMENSIONS, WEIGHT, AND STRENGTH.

Diameter of Iron.	Length of One Link, Outside.	Width of One Link, Outside.	Radius of End of Link, Inside.	Length of Stud at Crown.	Weight of		Statutory Proof Tensile Stress, for each 15 Fathoms separately.	Statutory Ultimate Strength or Breaking Stress, on Three Links in each 15 Fathoms.	Actual Breaking Stress.		Safe-Working Stress (Half the Proof Stress).	Ultimate or Breaking Stress per Square Inch of Good Ordinary Cable.
					100 Fathoms.	One Fathom (Six Feet).			Good Ordinary Cable.	High Breaking Stress.		
Inches.	Inches.	Inches.	Inches.	Inches.	Cwts.	Pounds.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
$1\frac{1}{16}$	$2\frac{5}{8}$	$1\frac{13}{16}$	$\frac{1}{4}$	$\frac{23}{32}$	9.2	11.3	3.4	5.1	5.4	5.4	1.7	18.0
$\frac{1}{2}$	3	$1\frac{13}{16}$	$\frac{9}{32}$	$\frac{13}{16}$	12	13.4	4.5	$6\frac{3}{4}$	$7\frac{1}{8}$	7.6	2.1	18.1
$\frac{5}{16}$	$3\frac{1}{8}$	$2\frac{1}{2}$	$\frac{11}{32}$	$\frac{23}{32}$	15.2	17.2	5.8	8.4	9	9.8	2.81	18.1
$\frac{3}{8}$	$3\frac{3}{4}$	$2\frac{1}{2}$	$\frac{11}{32}$	$\frac{23}{32}$	18.75	21	7	10.5	11.2	11.9	$3\frac{1}{2}$	18.2
$\frac{7}{16}$	$4\frac{1}{4}$	$2\frac{15}{16}$	$\frac{13}{32}$	$1\frac{1}{8}$	22.7	25.4	8.5	12.3	13.6	14.5	4.1	18.3
$\frac{1}{2}$	$4\frac{1}{2}$	$2\frac{11}{16}$	$\frac{1}{16}$	$1\frac{1}{8}$	27	30.2	10.4	$15\frac{1}{8}$	16.2	17.3	$5\frac{1}{16}$	18.3
$\frac{9}{16}$	$4\frac{7}{8}$	$2\frac{13}{16}$	$\frac{1}{16}$	$1\frac{1}{8}$	31.7	35.5	11.4	17.8	19	20.8	5.94	18.3
$\frac{5}{8}$	5.4	$3\frac{1}{2}$	$\frac{1}{16}$	$1\frac{1}{8}$	36.75	41.2	13.4	20.8	22.4	23.8	6.7	18.3
$\frac{11}{16}$	5.8	$3\frac{3}{4}$	$\frac{1}{16}$	$1\frac{1}{8}$	42.2	47.2	15.8	23.7	25.4	27.1	7.9	18.4
$\frac{3}{4}$	6	$3\frac{13}{16}$	$\frac{1}{16}$	$1\frac{1}{8}$	48	53.8	18	27	29	31.1	9	18.5
$1\frac{1}{16}$	$6\frac{3}{8}$	$3\frac{27}{32}$	$\frac{1}{8}$	$1\frac{1}{8}$	54.2	60.7	20.3	30.4	32.8	34.9	10.15	18.4
$1\frac{1}{8}$	$6\frac{3}{4}$	$4\frac{1}{16}$	$\frac{1}{8}$	$1\frac{1}{8}$	60.75	69	22.4	34.4	36.5	39	11.8	18.3
$1\frac{3}{16}$	$7\frac{1}{8}$	$4\frac{5}{8}$	$\frac{1}{8}$	$1\frac{1}{8}$	67.7	75.8	25.8	38	40.5	43.8	12.69	18.3
$1\frac{1}{4}$	$7\frac{1}{2}$	$4\frac{1}{2}$	$\frac{1}{4}$	2	75	84	28.8	42.4	44.4	47.9	$14\frac{1}{8}$	18.2
$1\frac{5}{16}$	$7\frac{7}{8}$	$4\frac{23}{32}$	$\frac{1}{4}$	$2\frac{1}{8}$	82.4	92	31	46.5	49.4	52.8	$15\frac{1}{2}$	18.2
$1\frac{3}{8}$	8.4	$4\frac{15}{16}$	$\frac{1}{4}$	$2\frac{1}{8}$	90.75	101.6	34	51	53.4	57.5	17	18.1

TABLE 219.—STUD-LINK CHAIN-CABLES (*continued*).

Dia- meter of Iron.	Length of One Link, Out- side.	Width of One Link, Out- side.	Radius of End of Link, Inside.	Length of Stud at Crown.	Weight of		Statutory Proof Tensile Stress, for each 15 Fathoms sepa- rately.	Statutory Ultimate Strength or Break- ing Stress, on Three Links in each 15 Fathoms.	Actual Breaking Stress.		Safe- Working Stress (Half the Proof Stress).	Ultimate or Break- ing Stress per Square Inch of Good Ordinary Cable.
					100 Fathoms.	One Fathom (Six Feet).			Good Ordinary Cable.	High Break- ing Stress.		
Inches.	Inches.	Inches.	Inch.	Inches.	Cwts.	Pounds.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
$1\frac{1}{16}$	8 $\frac{5}{8}$	$3\frac{3}{16}$	$\frac{37}{32}$	$2\frac{5}{16}$	99.5	111	37 $\frac{1}{2}$	55 $\frac{1}{2}$	58 $\frac{1}{2}$	62.7	18.56	18.0
$1\frac{1}{2}$	9	$5\frac{13}{32}$	$\frac{37}{32}$	$2\frac{13}{32}$	108	121	40.5	58.7	63.6	68	20 $\frac{1}{2}$	18.0
$1\frac{9}{16}$	9 $\frac{1}{2}$	$5\frac{5}{8}$	$\frac{37}{32}$	$2\frac{1}{2}$	116.8	131	43.9	61.4	68.7	73.6	22	17.9
$1\frac{1}{8}$	9 $\frac{3}{4}$	$5\frac{11}{16}$	$\frac{37}{32}$	$2\frac{1}{2}$	126.75	142	47.5	66.5	74	79.3	23 $\frac{1}{2}$	17.8
$1\frac{1}{16}$	10 $\frac{1}{8}$	$6\frac{3}{32}$	1	$2\frac{23}{32}$	138.7	152	51.1	71.3	79 $\frac{1}{2}$	85.2	25 $\frac{1}{2}$	17.8
$1\frac{1}{4}$	10 $\frac{1}{2}$	$6\frac{5}{16}$	$1\frac{1}{16}$	$2\frac{1}{2}$	147	164.6	55 $\frac{1}{2}$	77 $\frac{1}{2}$	85 $\frac{1}{2}$	91 $\frac{1}{2}$	27 $\frac{1}{2}$	17.7
$1\frac{13}{16}$	10 $\frac{3}{4}$	$6\frac{17}{32}$	$1\frac{1}{16}$	$2\frac{23}{32}$	158	176	59 $\frac{1}{2}$	82 $\frac{1}{2}$	91.2	97 $\frac{1}{2}$	29 $\frac{1}{2}$	17.7
$1\frac{7}{8}$	11 $\frac{1}{4}$	$6\frac{3}{4}$	$1\frac{1}{8}$	3	168.75	189	63 $\frac{1}{2}$	88.5	97 $\frac{1}{2}$	104 $\frac{1}{2}$	31 $\frac{1}{2}$	17.6
$1\frac{15}{16}$	11 $\frac{1}{2}$	$6\frac{11}{16}$	$1\frac{1}{8}$	$3\frac{3}{16}$	180	201	67.5	94.5	103 $\frac{1}{2}$	110.8	33 $\frac{1}{2}$	17.6
2	12	$7\frac{7}{16}$	$1\frac{1}{2}$	$3\frac{3}{16}$	192	215	72	100.8	109.9	117 $\frac{1}{2}$	36	17.5
$2\frac{1}{16}$	12 $\frac{1}{2}$	$7\frac{13}{16}$	$1\frac{5}{8}$	$3\frac{5}{16}$	203	228	76.5	107.1	116.4	124.5	38 $\frac{1}{2}$	17.4
$2\frac{1}{8}$	12 $\frac{3}{4}$	$7\frac{21}{32}$	$1\frac{5}{8}$	$3\frac{13}{32}$	216.75	242.8	81 $\frac{1}{2}$	113 $\frac{1}{2}$	123 $\frac{1}{2}$	131.9	40 $\frac{1}{2}$	17.3
$2\frac{3}{16}$	13 $\frac{1}{8}$	$7\frac{23}{32}$	$1\frac{3}{4}$	$3\frac{1}{2}$	229	259	86 $\frac{1}{2}$	120.5	130.1	139 $\frac{1}{2}$	43	17.3
$2\frac{1}{4}$	13 $\frac{1}{4}$	$8\frac{1}{8}$	$1\frac{7}{8}$	$3\frac{1}{2}$	243	276.2	91 $\frac{1}{2}$	127.5	137 $\frac{1}{2}$	146 $\frac{1}{2}$	45 $\frac{1}{2}$	17.2
$2\frac{5}{16}$	13 $\frac{3}{8}$	$8\frac{5}{16}$	$1\frac{7}{8}$	$3\frac{13}{32}$	256	289	96 $\frac{1}{2}$	134 $\frac{1}{2}$	144 $\frac{1}{2}$	154 $\frac{1}{2}$	48 $\frac{1}{2}$	17.2
$2\frac{3}{8}$	13 $\frac{1}{2}$	$8\frac{11}{16}$	$1\frac{7}{8}$	$3\frac{17}{32}$	270.75	303.2	101.5	142.1	151 $\frac{1}{2}$	162.4	50 $\frac{1}{2}$	17.1
$2\frac{7}{16}$	14 $\frac{1}{8}$	$8\frac{25}{32}$	$1\frac{3}{4}$	$3\frac{33}{32}$	285	319	106.9	149 $\frac{1}{2}$	159.2	170.4	53 $\frac{1}{2}$	17.1
$2\frac{1}{2}$	14 $\frac{1}{4}$	$9$	$1\frac{3}{4}$	4	300	336	112.5	157.5	166 $\frac{1}{2}$	178 $\frac{1}{2}$	56 $\frac{1}{2}$	17.0



TABLE 220.—SHORT-LINK OR UNSTUDDED CHAIN-CABLES: DIMENSIONS, WEIGHT, AND STRENGTH.

Dia- meter of Iron.	Length of One Link, Out- side.	Width of One Link, Out- side.	Radius of End of Link, Inside.	Weight of One Fathom (Six Feet).	Statutory Proof Tensile Stress, for each 15 Fathoms separately.	Statutory Breaking Stress, or Ultimate Strength, in Three Links in each 15 Fathoms.	Actual Breaking Stress.		Safe- Working Stress (Half the Proof Stress).	Ultimate Breaking Stress per Sq. Inch of Good Ord- inary Cable.
							Good Ordinary Cable.	High Breaking Stress.		
Inches.	Inches.	Inches.	Inch.	Pounds.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
$\frac{1}{4}$	$1\frac{3}{32}$	$\frac{7}{8}$	$\frac{3}{32}$	3.44	$\frac{3}{4}$	$1\frac{1}{2}$	$1\frac{1}{8}$	1.7	$\frac{3}{8}$	16.6
$\frac{5}{16}$	$1\frac{11}{32}$	$1\frac{3}{32}$	$\frac{3}{16}$	5.1	$1\frac{1}{8}$	2.1	2.6	2.8	$\frac{9}{16}$	16.8
$\frac{3}{8}$	$1\frac{13}{32}$	$1\frac{5}{16}$	$\frac{7}{32}$	8	$1\frac{1}{2}$	3.1	3.2	3.9	$\frac{3}{4}$	17.0
$\frac{7}{16}$	$2\frac{1}{8}$	$1\frac{11}{16}$	$\frac{9}{32}$	10.1	2.1	4.1	5.1	5.3	$1\frac{1}{8}$	17.1
$\frac{1}{2}$	$2\frac{3}{8}$	$1\frac{3}{4}$	$\frac{11}{32}$	13.1	3	6	6.1	7	$1\frac{1}{2}$	17.1
$\frac{9}{16}$	$2\frac{5}{8}$	$1\frac{13}{16}$	$\frac{11}{16}$	17	$3\frac{3}{4}$	7.1	8.1	8.9	$1\frac{3}{4}$	17.2
$\frac{5}{8}$	$2\frac{11}{8}$	$2\frac{1}{2}$	$\frac{3}{8}$	22	$4\frac{1}{2}$	9.1	10.1	11	2.1	17.2
$\frac{11}{16}$	$3\frac{1}{8}$	$2\frac{13}{16}$	$\frac{13}{32}$	26	$5\frac{1}{2}$	11.1	12.8	13.4	$2\frac{1}{2}$	17.2
$\frac{3}{4}$	$3\frac{1}{4}$	$2\frac{3}{4}$	$\frac{13}{32}$	30	$6\frac{1}{4}$	13.1	15.1	16	$3\frac{1}{8}$	17.3
$\frac{13}{16}$	$3\frac{3}{4}$	$3\frac{1}{8}$	$\frac{1}{2}$	36	7.9	15.8	17.9	18.8	4	17.3
$\frac{7}{8}$	$4\frac{1}{8}$	$3\frac{1}{16}$	$\frac{17}{32}$	42	9.1	18.1	20.8	21.7	$4\frac{1}{2}$	17.3
$\frac{15}{16}$	$4\frac{13}{16}$	$3\frac{9}{16}$	$\frac{9}{16}$	49	$10\frac{1}{2}$	21	23.9	25.1	$5\frac{1}{4}$	17.4
1	$4\frac{3}{4}$	$3\frac{11}{16}$	$\frac{41}{64}$	55	12	24	27.3	28.1	6	17.4
$1\frac{1}{16}$	$5\frac{1}{16}$	$3\frac{33}{64}$	$\frac{21}{32}$	60	$13\frac{1}{2}$	27	30.7	32.1	$6\frac{3}{4}$	17.3
$1\frac{1}{8}$	$5\frac{1}{8}$	$3\frac{11}{16}$	$\frac{11}{16}$	68	$15\frac{1}{4}$	$30\frac{1}{4}$	34.3	36	$7\frac{1}{2}$	17.2
$1\frac{3}{16}$	$5\frac{13}{16}$	$4\frac{1}{8}$	$\frac{33}{64}$	76	16.9	33.8	38.1	39.9	$16\frac{1}{2}$	17.1
$1\frac{1}{4}$	6.1	$4\frac{3}{8}$	$\frac{7}{4}$	84	18.1	37.1	42.1	44.1	$9\frac{3}{8}$	17.0

TABLE 220.—SHORT-LINK CHAIN CABLES (*continued*).

Dia- meter of Iron.	Length of One Link, Out- side.	Width of One Link, Out- side.	Radius of End of Link, Inside.	Weight of One Fathom (Six Feet).	Statutory Proof Tensile Stress, for each 15 Fathoms separately.	Statutory Breaking Stress, or Ultimate Strength, in Three Links in each 15 Fathoms.	Actual Breaking Stress.		Safe- Working Stress (Half the Proof Stress).	Ultimate Breaking Stress per Sq. Inch of Good Ordini- ary Cable.
							Good Ordinary Cable.	High Breaking Stress.		
Inches.	Inches.	Inches.	Inches.	Pounds.	Tons.	Tons.	Tons.	Tons.	Tons.	Tons.
$1\frac{5}{16}$	$6\frac{7}{16}$	$4\frac{13}{16}$	$\frac{35}{32}$	93	20 $\frac{3}{8}$	41 $\frac{1}{4}$	46 $\frac{1}{4}$	48 $\frac{1}{2}$	10 $\frac{1}{4}$	17.0
$1\frac{3}{8}$	$6\frac{3}{4}$	$4\frac{13}{16}$	$\frac{35}{32}$	102	22 $\frac{3}{8}$	45 $\frac{1}{4}$	50 $\frac{1}{2}$	53	11 $\frac{1}{4}$	17.0
$1\frac{7}{16}$	$7\frac{3}{32}$	$5\frac{1}{2}$	$\frac{7}{8}$	111	24 $\frac{3}{8}$	49 $\frac{1}{2}$	55 $\frac{1}{2}$	57.8	12 $\frac{3}{8}$	17.0
$1\frac{1}{2}$	$7\frac{11}{32}$	$5\frac{1}{2}$	$\frac{29}{32}$	120	27	54	59.8	62.7	13 $\frac{1}{2}$	16.9
$1\frac{1}{16}$	$7\frac{11}{32}$	$5\frac{15}{32}$	$\frac{11}{16}$	131	29 $\frac{1}{2}$	58 $\frac{1}{2}$	64 $\frac{3}{8}$	67.8	14 $\frac{3}{8}$	16.9
$1\frac{1}{8}$	$7\frac{33}{32}$	$5\frac{11}{16}$	1	144	31 $\frac{3}{8}$	63 $\frac{1}{4}$	69.7	73	15 $\frac{3}{4}$	16.8
$1\frac{11}{16}$	$8\frac{9}{32}$	$5\frac{29}{32}$	$1\frac{1}{32}$	159	34 $\frac{3}{8}$	68 $\frac{1}{4}$	74.9	78 $\frac{1}{2}$	17	16.8
$1\frac{3}{4}$	$8\frac{11}{32}$	$6\frac{1}{8}$	$1\frac{1}{16}$	168	36 $\frac{3}{4}$	73 $\frac{1}{2}$	80.3	84 $\frac{1}{2}$	18 $\frac{3}{8}$	16.8
$1\frac{13}{16}$	$8\frac{7}{8}$	$6\frac{11}{32}$	$1\frac{1}{8}$	181	39.4	78.8	85.8	90	19 $\frac{3}{4}$	16.7
$1\frac{7}{8}$	$9\frac{3}{16}$	$6\frac{15}{16}$	$1\frac{1}{4}$	196	42 $\frac{1}{2}$	84 $\frac{1}{4}$	91 $\frac{1}{2}$	95.9	21	16.6
$1\frac{15}{16}$	$9\frac{1}{2}$	$6\frac{31}{32}$	$1\frac{5}{16}$	207	45	90	97.4	102	22 $\frac{1}{2}$	16.5
2	$9\frac{13}{16}$	7	$1\frac{3}{8}$	220	48	96	103.4	108 $\frac{3}{8}$	24	16.4
$2\frac{1}{16}$	10 $\frac{1}{8}$	$7\frac{7}{32}$	$1\frac{1}{4}$	233	51	102	109 $\frac{1}{8}$	114.8	25 $\frac{1}{2}$	16.4
$2\frac{1}{8}$	$10\frac{13}{32}$	$7\frac{7}{16}$	$1\frac{9}{32}$	248	54 $\frac{1}{2}$	108 $\frac{1}{4}$	115.9	121.4	27	16.3
$2\frac{1}{16}$	$10\frac{23}{32}$	$7\frac{23}{32}$	$1\frac{1}{16}$	262	57.4	114.8	122.4	128.2	28 $\frac{3}{4}$	16.3
$2\frac{1}{4}$	$11\frac{25}{32}$	$7\frac{7}{8}$	$1\frac{11}{16}$	272	60 $\frac{3}{4}$	121 $\frac{1}{2}$	129	135 $\frac{1}{4}$	30 $\frac{3}{8}$	16.2
$2\frac{5}{16}$	$11\frac{11}{32}$	$8\frac{3}{8}$	$1\frac{13}{16}$	290	64 $\frac{1}{8}$	128 $\frac{1}{4}$	135 $\frac{3}{4}$	142 $\frac{1}{4}$	32	16.2
$2\frac{3}{8}$	$11\frac{13}{32}$	$8\frac{13}{16}$	$1\frac{7}{8}$	304	67 $\frac{3}{8}$	135 $\frac{1}{4}$	142.8	149.4	33 $\frac{3}{8}$	16.1
$2\frac{7}{16}$	$11\frac{15}{32}$	$8\frac{13}{16}$	$1\frac{13}{16}$	319	71 $\frac{1}{4}$	142 $\frac{3}{4}$	149 $\frac{1}{8}$	156 $\frac{1}{8}$	35 $\frac{3}{8}$	16.1
$2\frac{1}{2}$	12 $\frac{1}{4}$	$8\frac{3}{4}$	$1\frac{1}{2}$	336	75	150	157	164.4	37 $\frac{1}{2}$	16.0

original area of section, with a reduction in length of not less than 10 per cent. The steel pins for retaining the joining shackle-bolt, are to be capable of bearing a tensile stress not less than 35 tons per square inch, with a contraction at the fracture of not less than 45 per cent. of the original area. Mooring and close-link crane and rigging chains are to be proved to a stress of 8.47 tons per square inch of section of the sides of the link, or 466 pounds per circular  $\frac{1}{8}$  inch of section. Defective links are to be cut out and replaced. Stud-chain cables are to be proved according to the Act, as already described. Four-feet sample lengths of chain are to be tested for ultimate strength, which is not to be less than 16 tons per square inch of section of both sides of the links, or 880 pounds per circular  $\frac{1}{8}$ -inch.

The  $1\frac{1}{2}$ -inch mooring chain is made in lengths of 15 fathoms, with a joining shackle to each length, and a swivel for every 30 fathoms. The  $1\frac{1}{4}$  inch,  $1\frac{1}{8}$  inch, 1 inch, and  $\frac{7}{8}$  inch mooring chains are in lengths of from 8 fathoms to 45 fathoms. Stud-chain cables are made in lengths of  $12\frac{1}{2}$  fathoms. The common links of mooring chains are 6 diameters in length, the breadth is 3.5 diameters. The ordinary end link is of iron, 1.2 diameters,  $6\frac{1}{2}$  diameters in length, 4.1 in breadth.

TABLE 221.—CHAIN MOORINGS, IN TEN-FATHOM LENGTHS :  
OPEN OR UNSTUDDED LINKS : SIZES, WEIGHT, AND  
PROOF-STRESS.

(Admiralty.)

Size, or Diameter of Iron at Sides of Link.	Greater Diameter at the Ends of Link.	Weight of Ten Fathoms.	Proof-Stress.
Inches	Inches.	Cwts.	Tons.
$2\frac{3}{4}$	3.025	40	72
$2\frac{7}{8}$	3.162	45	79
3	3.3	50	86
$3\frac{1}{8}$	3.437	55	93
$3\frac{1}{4}$	3.575	60	101
$3\frac{1}{2}$	3.85	75	117
$3\frac{3}{4}$	4.125	87	134

*Note.*—The breaking stress must be not less than 1.40 times the proof stress ; that is, 40 per cent. more.

TABLE 222.—CHAIN-RIGGING, CRANE CHAINS (SHORT LINK): SIZE AND WEIGHT.  
(Admiralty.)

Size or Diameter of Iron.	Weight of One Fathom.	Size or Diameter of Iron.	Weight of One Fathom.	Size or Diameter of Iron.	Weight of One Fathom.
Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.
$\frac{1}{8}$	2	$\frac{9}{16}$	21	$1\frac{1}{8}$	73
$\frac{3}{16}$	3	$\frac{5}{8}$	25	$1\frac{1}{4}$	92
$\frac{1}{4}$	4 $\frac{3}{4}$	$\frac{11}{16}$	30	$1\frac{3}{8}$	108
$\frac{5}{16}$	5 $\frac{3}{4}$	$\frac{3}{4}$	36	$1\frac{1}{2}$	132
$\frac{3}{8}$	6 $\frac{3}{4}$	$\frac{13}{16}$	39	$1\frac{5}{8}$	155
$\frac{7}{16}$	9 $\frac{1}{2}$	$\frac{7}{8}$	48	$1\frac{3}{4}$	179
$\frac{1}{2}$	13 $\frac{1}{4}$	$\frac{15}{16}$	53		
	17	1	61		

TABLE 223.—SHORT-LINK CHAINS: WEIGHT AND CONDITIONS OF TEST.  
(India Stores Department.)

Diameter of Iron.	Weight of One Fathom.	Proof Stress.	Load on Test Piece.	Elongation of Test Piece on Thirty-six Inches.
Inches.	Pounds.	Tons.	Tons.	Inches.
$\frac{1}{8}$	1	$\frac{7}{16}$	$\frac{7}{16}$	6
$\frac{3}{16}$	2 $\frac{1}{4}$	$\frac{2}{5}$	1	7
$\frac{1}{4}$	3 $\frac{3}{4}$	$\frac{3}{4}$	$1\frac{1}{4}$	8 $\frac{1}{4}$
$\frac{5}{16}$	6	$1\frac{1}{8}$	3	9 $\frac{1}{4}$
$\frac{3}{8}$	8 $\frac{1}{2}$	$1\frac{5}{8}$	4 $\frac{1}{4}$	8 $\frac{5}{8}$
$\frac{7}{16}$	11 $\frac{1}{2}$	2 $\frac{1}{4}$	5 $\frac{3}{4}$	8 $\frac{3}{4}$
$\frac{1}{2}$	15	3	7	7 $\frac{1}{8}$
$\frac{9}{16}$	19	3 $\frac{3}{4}$	8 $\frac{1}{2}$	8 $\frac{1}{4}$
$\frac{5}{8}$	23 $\frac{1}{2}$	4 $\frac{5}{8}$	11 $\frac{3}{4}$	10
$\frac{11}{16}$	28 $\frac{1}{2}$	5 $\frac{5}{8}$	13 $\frac{3}{4}$	8 $\frac{1}{4}$
$\frac{3}{4}$	34	6 $\frac{3}{4}$	16 $\frac{1}{4}$	9 $\frac{1}{4}$
$\frac{13}{16}$	40	7 $\frac{9}{16}$	18 $\frac{3}{4}$	9 $\frac{3}{4}$
$\frac{7}{8}$	46	9 $\frac{1}{8}$	22	8 $\frac{5}{8}$
$\frac{15}{16}$	53	10 $\frac{1}{2}$	24 $\frac{1}{2}$	8 $\frac{3}{8}$
1	60	12	29	8 $\frac{7}{16}$
$1\frac{1}{8}$	76	15 $\frac{1}{8}$	36 $\frac{1}{4}$	8 $\frac{5}{8}$
$1\frac{1}{4}$	94	18 $\frac{3}{4}$	41 $\frac{3}{4}$	9 $\frac{3}{4}$
$1\frac{3}{8}$	114	22 $\frac{5}{8}$	51 $\frac{3}{4}$	10 $\frac{5}{8}$
$1\frac{1}{2}$	135	27	64	11 $\frac{3}{8}$

## FRAMING.

## Cranes.

When a crane  $abc$ , fig. 72, is loaded at  $c$  by the weight  $W$ , the stresses in the three members  $ab$ ,  $ac$ , and  $bc$ , due to the load, are measured proportionally by the respective lengths of

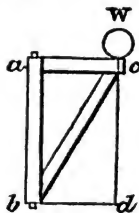


FIG. 72.—Crane.

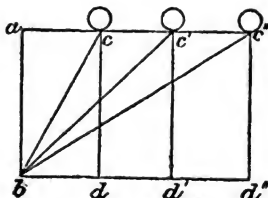


FIG. 73.—Crane.

these members; the vertical stress in the member  $ab$ , being equal to the load  $W$ . The diagonal and horizontal stresses increase with the overhang, as shown in fig. 73, by the increasing lengths of the diagonal and horizontal members,  $bc''$ , &c., and  $ac''$ , &c.; the vertical  $ab$  being constant.

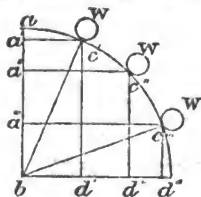


FIG. 74.—Crane.

Again, the diagonal stress increases proportionally with the obliquity of the jib  $bc''$ , &c., fig. 74, taken as constant in length.

Where both the diagonal and the tie member are oblique, as  $bc$  and  $ac$ , fig. 75, the stresses in the triangular figure,  $abc$ , as before, are measured proportionally by the lengths of the members;  $ab$  being the measure of the load  $W$ . The horizontal pull at  $a$ , is measured by the horizontal length  $ac'$ .

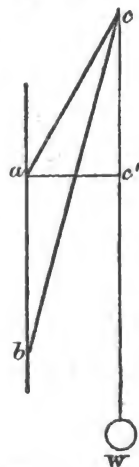


FIG. 75.—Crane.

## Truss.

The truss or triangular frame  $abc$ , fig. 76, having equal limbs,  $ac$ ,  $bc$ , supports the load  $W$  at the apex. In the parallelogram  $ache$ ,  $ce$  is the weight,  $cd$  is half the weight, and  $ca$  and  $cb$  are oblique compressive stresses. The horizontal tensional stress in  $ab$

is equal to the product of the weight by the span, divided

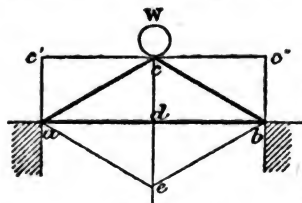


FIG. 76.—Truss.

by 4 times the rise. The horizontal thrust at the apex is equal to the tension in  $ab$ .

### Framed Girders.

The tensional stress, or unit stress, in the extreme horizontal members  $aa'$  and  $b'b$ , fig. 77, showing a Warren girder, is equal to  $\cdot 2885 W$ , in which  $W$  is the load at the centre. The stress, whether tensional or compressive, on any bay is equal to the product of the unit-stress by the order-number of

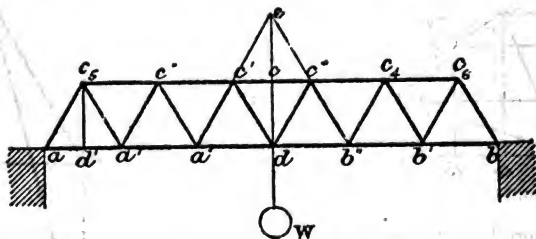


FIG. 77.—Warren Girder.

the bay ; above or below, reckoned from the extreme bay as 1, towards the middle. The stress on the central bay, also, is equal to the product of the unit-stress by  $\frac{n+1}{2}$ , in which  $n$  is the total number of bays. The stress on the middle pair of bays, tensional or compressive, is equal to the product of the unit-stress by  $\frac{n-1}{2}$ . In fig. 44, the stress on the central bay  $c'e'$ , is  $1\cdot 731 W$  ; in the central pair, it is  $1\cdot 443 W$ . The stress in the braces is  $\cdot 577 W$ , or twice the unit-stress in the flange.

**Truss Roofs.**

In the ordinary triangular roof truss, *abc*, fig. 78, in which the total weight, including the load, is uniformly distributed, the tension in the horizontal member *ab*, is equal to  $\frac{Wl}{8d}$ , or the product of the weight by the span, divided by 8 times the rise. The horizontal thrust at the ridge *c* is equal to the tension in the horizontal tie.

When the horizontal tie, *ab*, is applied at any higher level, the tension in it is increased inversely as the depth *cd*.

In the A roof truss, fig. 45, there are two trusses, each of which goes to form half the roof, and the horizontal tierod E. Let the span *ab* be 40 feet, the rise 10 feet, and the depth *cd* 8 feet. The rafters *ac* and *bc* are 22.5 feet long; the struts F are 3.33 feet long, the tension bars C and D are 11.75 feet long. The weight on the couple is 8 tons, uniformly distributed, of which 4 tons is supported on each rafter, say 1 ton at *a*, the abutment, 2 tons at F, and 1 ton at the ridge *c*. The

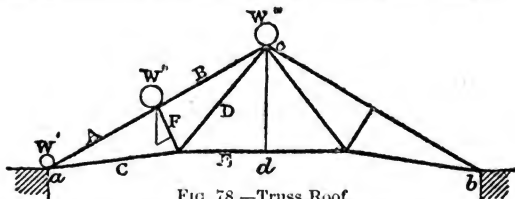


FIG. 78.—Truss Roof.

pressure at F, 2 tons, being vertical, is resolved, as indicated by diagram, into 1.8 tons stress on F, and .875 tons on A. The stress on F is resolved into 3.18 tons on each of the tie-rods C and D. The tension in E is by formula  $\frac{Wl}{8d}$ , equal to

$\frac{8 \times 40}{8 \times 8} = 5$  tons, which is resolved into  $4\frac{1}{4}$  tons in C, and .875 ton in F. This tension in F is resolved into 1.54 tons in each of C and D. Summing up the tensile stresses, there are  $(3.18 + 4.75 + 1.54 =) 9.47$  tons in C;  $(3.18 + 1.54 =) 4.72$  tons in D; and 5 tons in E.

**HARDNESS OF METALS, ALLOYS, AND STONES.**

Messrs. F. Crace Calvert and R. Johnson tested the comparative hardness of metals by the indentation made by a steel point under pressure. The steel point was about  $\frac{1}{4}$  inch long,  $1\frac{1}{2}$  millimetres or .049 inch wide at the point. Weights were added until the point entered to the extent of  $3\frac{1}{2}$  millime-  
 or .128 inch in the course of half an hour. The Table 224

the comparative hardness of several metals; and Table 225 gives the result for several alloys of copper, zinc, tin, lead, and antimony. The highest degree of hardness is that of cast iron, and it is, for the purpose of comparison, taken as 1000.

In the last column of the Table of alloys, the degree of hardness is calculated in terms of the elements separately, for simple mixtures.

The results from the alloys of copper and zinc, Table 225, No. 1, show that all the alloys having excess of copper are much harder than the metals composing them; and that increase of hardness is due to the zinc, the softer metal. But, if the zinc exceeds in proportion fifty per cent. of the alloy, the alloy becomes so brittle as to break as the point penetrates. The alloy Zn Cu, consisting of equal weights of copper and zinc, is remarkable for its hardness, which is about three times the calculated degree of hardness.

In section 4, of Table 225, may be noted the softness of the bronze with excess of tin. Also, that an increase of quantity of so malleable a metal as copper should so suddenly render the alloy brittle, until for Sn Cu<sup>10</sup>, brittleness ceases, and the hardness is nearly equal to that of wrought iron.

In section 5, Table 225, it is notable that the calculated hardness of alloys of tin and zinc, is not very different from the actual hardness: indicating a state of simple mixture of the elements.

In Table 226, is given the comparative hardness of granites and other stones according to M. Reynaud.

TABLE 224.—COMPARATIVE HARDNESS OF METALS.  
(F. Crace Calvert & R. Johnson.)

Metal.	Comparative Hardness Cast Iron = 1000.
Cast Iron, Staffordshire cold-blast, grey, No. 3	1000
Steel	958
Wrought Iron (made from above cast iron)	948
Platinum	375
Copper, pure	301
Aluminium	271
Silver, pure	208
Zinc, "	183
Gold, "	167
Antimony, pure	108
Lead, "	52
"	27
"	16



TABLE 225.—COMPARATIVE HARDNESS OF ALLOYS.

ALLOYS.	Proportions per cent., by Weight.	Comparative Hardness. Cast Iron = 1000.	Calculated Hardness. Cast Iron = 1000.
1. <i>Copper and Zinc.</i>			
Zn Cu <sup>5</sup> . . .	{ C 82.95 }	427	281
	{ Z 17.05 }		
Zn Cu <sup>4</sup> . . .	{ C 79.56 }	469	277
	{ Z 20.44 }		
Zn Cu <sup>3</sup> . . .	{ C 74.48 }	469	276
	{ Z 25.52 }		
Zn Cu <sup>2</sup> . . .	{ C 66.06 }	473	261
	{ Z 33.94 }		
Zn Cu . . .	{ C 49.32 }	604	243
	{ Z 50.68 }		
Cu Zn <sup>2</sup> . . .	{ C 32.74 }	Broke	...
	{ Z 67.26 }		
Cu Zn <sup>3</sup> . . .	{ C 24.64 }	"	...
	{ Z 75.36 }		
Cu Zn <sup>4</sup> . . .	{ C 19.57 }	"	...
	{ Z 80.43 }		
Cu Zn <sup>5</sup> . . .	{ C 16.30 }	"	...
	{ Z 83.70 }		
2. <i>Lead &amp; Antimony.</i>			
Pb Sb <sup>5</sup> . . .	{ L 24.31 }	Broke	...
	{ A 75.69 }		
Pb Sb <sup>4</sup> . . .	{ L 28.64 }	"	...
	{ A 71.36 }		
Pb Sb <sup>3</sup> . . .	{ L 34.86 }	...	...
	{ A 65.14 }		
Pb Sb <sup>2</sup> . . .	{ L 44.53 }	...	...
	{ A 55.47 }		
Pb Sb . . .	{ A 38.39 }	...	...
	{ L 61.61 }		
Pb Sb <sup>2</sup> . . .	{ A 23.68 }	...	...
	{ L 76.32 }		
Pb Sb <sup>3</sup> . . .	{ A 17.20 }	...	...
	{ L 82.80 }		
Pb Sb <sup>4</sup> . . .	{ A 13.48 }	...	...
	{ L 86.52 }		
Pb Sb <sup>5</sup> . . .	{ A 11.08 }	...	...
	{ L 88.92 }		

TABLE 225.—COMPARATIVE HARDNESS OF ALLOYS (*cont.*).

ALLOYS.	Proportions per cent., by Weight.	Comparative Hardness. Cast Iron = 1000.	Calculated Hardness. Cast Iron = 1000.
3. <i>Commercial Brasses.</i>			
"Large bearings"	Copper 82.05	562	259
	Tin 12.82		
	Zinc 5.13		
Mud plugs . . .	Copper 80	750	262
	Tin 10		
	Zinc 10		
Yellow brass . . .	Copper 64	520	258
	Zinc 56		
	Copper 80		
Pumps and pipes.	Tin 5	343	257
	Zinc 7.5		
	Lead 7.5		
4. <i>Copper and Tin (Bronze).</i>			
Cu Sn <sup>5</sup> . . .	C 9.73	83	52
	T 90.27		
Cu Sn <sup>4</sup> . . .	C 11.86	96	60
	T 88.14		
Cu Sn <sup>3</sup> . . .	C 15.21	104	69
	T 84.79		
Cu Sn <sup>2</sup> . . .	C 21.21	135	85
	T 78.79		
Cu Sn . . .	C 34.98	Broke	...
	T 65.02		
Sn Cu <sup>2</sup> . . .	T 51.83	"	...
	C 48.17		
Sn Cu <sup>3</sup> . . .	T 38.29	"	...
	C 61.79		
Sn Cu <sup>4</sup> . . .	T 31.73	"	...
	C 68.27		
Sn Cu <sup>5</sup> . . .	T 27.10	"	...
	C 72.90		
Sn Cu <sup>10</sup> . . .	T 15.68	917	257
	C 84.32		
Sn Cu <sup>15</sup> . . .	T 11.03	773	271
	C 88.97		
Sn Cu <sup>20</sup> . . .	T 8.51	640	278
	C 91.49		
Cu <sup>25</sup> . . .	T 6.83	602	279
	C 98.17		

TABLE 225.—COMPARATIVE HARDNESS OF ALLOYS (*cont.*).

ALLOYS.	Proportions per cent., by Weight.	Comparative Hardness. Cast Iron = 1000.	Calculated Hardness. Cast Iron = 1000.
5. Tin and Zinc.			
Zn Sn <sup>2</sup> . . .	Z 21.65	65	61
	T 78.35		
Zn Sn . . .	Z 35.60	69	83
	T 64.40		
Sn Zn <sup>2</sup> . . .	Z 47.49	83	110
	T 52.51		
Sn Zn <sup>3</sup> . . .	Z 37.57	94	125
	T 62.43		
Sn Zn <sup>4</sup> . . .	Z 31.14	105	131
	T 68.86		
Sn Zn <sup>5</sup> . . .	Z 26.57	125	142
	T 73.43		
Sn Zn <sup>6</sup> . . .	Z 15.32	121	158
	T 84.68		
6. Lead and Tin.			
Pb Sn <sup>5</sup> . . .	L 26.03	42	24
	T 73.97		
Pb Sn <sup>4</sup> . . .	L 30.57	41	24
	T 69.43		
Pb Sn <sup>3</sup> . . .	L 36.99	32	23
	T 63.01		
Pb Sn <sup>2</sup> . . .	L 46.82	26	20
	T 53.18		
Pb Sn . . .	L 63.78	21	20
	T 36.22		
Sn Pb <sup>2</sup> . . .	T 22.11	26	18
	L 77.89		
Sn Pb <sup>3</sup> . . .	T 15.91	21	17
	L 84.09		
Sn Pb <sup>4</sup> . . .	T 12.43	26	17
	L 87.57		
Sn Pb <sup>5</sup> . . .	T 10.20	23	17
	L 89.80		

TABLE 226.—COMPARATIVE HARDNESS OF STONES.  
(Reynaud.)

Stone.	Comparative Hardness: White-veined Marble = 1.
White-veined marble . . . . .	1·00
Syenite (red granite) . . . . .	10·08
Green granite . . . . .	9·70
Granite (deadleaf) . . . . .	9·30
Grey granite of the Vosges . . . . .	8·92
"    "    Bretagne . . . . .	8·56
"    "    Normandy . . . . .	7·00
Dark grey marble . . . . .	1·28
Lias limestone . . . . .	·88

The following scale of hardness is that adopted by the Technical High School at Prague. The substances are arranged in ascending order, from the softest to the hardest. The test is made by drawing a conically pointed cylindrical piece of one of the metals tabulated along a polished surface of the metal to be tested. If the pointed pieces become blunted without marking the surface, the metal under test is harder than the pointed pieces employed. If neither point nor metal surface be abraded, the hardness is taken as equal. If the surface be scratched, the metal under test is taken as softer than the pointed metal :—

1. Pure soft lead.
2. Pure tin.
3. Pure hard lead.
4. Pure annealed copper.
5. Fine cast copper.
6. Soft bearing metal (copper, 85 ; tin, 10 ; zinc, 5).
7. Cast iron (annealed).
8. Fibrous wrought iron.
9. Fine grained light grey cast iron.
10. Toughened cast iron (melted with 10 per cent. of wrought-iron turnings).
11. Soft ingot iron, having ·15 per cent. of carbon (will not harden).
12. Steel, having ·45 per cent. of carbon (not hardened).
13. Steel, having ·96 per cent. of carbon (not hardened).
14. Crucible cast steel, hardened and tempered blue.
15. Crucible steel, hardened and tempered violet to orange-yellow.

16. Crucible steel, hardened and tempered straw-yellow.
17. Hard bearing metal (copper 83, tin 17).
18. Crucible steel, glass hard.

### LABOUR OF ANIMALS.

*Men.*—The average net daily work of an ordinary labourer at a pump, a winch, or a crane, may be taken at 3,300 foot-pounds per minute, for 8 hours a day. But, for shorter periods, from four to five times the rate may be exerted.

*Horses and Bullocks.*—Boulton and Watt estimated that a dray-horse could exert a power of 33,000 foot-pounds per minute, for 8 hours a day. Rennie's estimate of the average work of horses, strong and weak, was at the rate of 22,000 foot-pounds per minute for 8 hours a day.

A pair of well-fed bullocks can raise water at the rate of 8,000 foot-pounds per minute, for a morning's work of 4½ hours.

### MECHANICAL PRINCIPLES.

THE statical *moment* of a force or of a body, with respect to a given point, or axis, or plane, is expressed by the product of the weight of the body by its perpendicular distance from the point, axis, or plane.

In *levers*, the moment of the weight or resistance about the fulcrum, is equal to the moment of the power or force applied to counteract the resistance. Let  $P$  = the power,  $W$  = the weight or resistance,  $L$  and  $l$  respectively the lengths of the arms of the lever, taken as straight, then

the moment  $P \times L$  = the moment  $W \times l$ ,

and any one of the four quantities  $P$ ,  $L$ ,  $W$ , and  $l$ , can be found by a simple adaptation of the above equation, thus:—

$$P = \frac{W \times l}{L} \quad . \quad . \quad . \quad . \quad (1)$$

$$W = \frac{P \times L}{l} \quad . \quad . \quad . \quad . \quad (2)$$

$$L = \frac{W \times l}{P} \quad . \quad . \quad . \quad . \quad (3)$$

$$l = \frac{P \times L}{W} \quad . \quad . \quad . \quad . \quad (4)$$

In these equations, it is assumed that the power and resistance act on the lever at right angles to it. If the lever be bent, or if the forces act obliquely, equilibrium or equality of moments may be maintained. Draw a horizontal line through the fulcrum to meet the vertical lines through the power and the weight. The moments of the power and the weight are calculated on the horizontal lengths, and they are equal to each other.

If two or more levers are connected consecutively one to the other, as one system, and the power and the weight are applied at the two extremes, in equilibrium, the power is to the weight as the compound inverse ratio of the levers. Suppose, for instance, the arms of the levers are successively as 3 to 1, 4 to 1, and 5 to 1, the compound ratio is the product of the three ratios, or it is as  $(3 \times 4 \times 5 =) 60$  to 1; and the power is to the weight as 1 to 60.

In simple *pulleys* on fixed bearings, there is no leverage, or augmentation of force; they simply transmit power, or change its direction. They act as levers having arms of equal lengths. But the pulley may be employed so as to augment the leverage, by suspending the weight to the axis of the pulley, and fixing one end of the cord, and pulling at the other end. The leverage is as 2 to 1, in this case: the weight acting at the length of the radius of the pulley from the fixed cord, and the power at the length of the diameter.

Pulleys may be combined in a pair of blocks, or sets of two or more on one axis; of which one block is fixed in position, and the other is moveable, taking the weight. The rope is usually fixed by one end to the stationary block, and is passed over the fast and moveable pulleys successively, the power being applied to the loose end. The force required at the loose end of the rope to balance the weight, irrespective of frictional and other external resistances, is equal to the quotient of the weight divided by the number of ropes by which it is carried, or the ropes proceeding from the moveable block. This number is equal to twice the number of moveable pulleys.

Conversely, to find the weight or resistance that will be balanced by a given power, irrespective of external resistances, multiply the power by the number of ropes proceeding from the moveable block.

When the fixed end of the rope is fastened to the moveable block, the divisor or multiplier is equal to twice the number of moveable pulleys plus 1.

The *wheel and axle* resemble two pulleys on one axis, having different diameters. If a weight be lifted by means of a rope wound over the axle or a roller on the axle, the

power being applied at the rim of the wheel, the action is like that of a lever of which the shorter arm is equal to the radius of the axle plus half the thickness of the rope ; and the longer arm is equal to the radius of the wheel. The power and the weight are to each other as the radial lengths inversely, irrespective of external resistance ; or they are as the diameters inversely. As with the lever, so with the wheel and axle,

the moment  $P \times L = \text{the moment } W \times l$ ,

in which  $P$  is the power or force at the circumference of the wheel,  $W$  the weight on the axle or barrel, and  $L \times l$  respectively the radii of the wheel and the axle. Where,

$$P = \frac{W \times l}{L} \quad . \quad . \quad . \quad . \quad . \quad (5)$$

$$W = \frac{P \times L}{l} \quad . \quad . \quad . \quad . \quad . \quad (6)$$

*On the inclined plane*, if a weight be raised by a force applied parallel to the plane, the sides of the triangle formed by the plane, its base, and its height, are proportional respectively to the weight, the pressure of the weight on the plane, and the power applied.

Let  $l$  be the length of an inclined plane, and  $h$  the height  $P$  the power, and  $W$  the weight drawn up the plane.

$$P = \frac{Wh}{l} \quad . \quad . \quad . \quad . \quad . \quad (7)$$

$$W = \frac{Pl}{h} \quad . \quad . \quad . \quad . \quad . \quad (8)$$

When the raising force is applied to the weight in a direction parallel to the base, the plane, its base, and its height are proportional respectively to the pressure of the weight on the plane, the weight, and the power applied.

The *wedge* is a pair of inclined planes united by their bases. The wedge is employed for the purpose of forcibly separating two bodies, or breaking or splitting a body ; or for fastening bodies together. In the application of pressure to the head or butt-end of the wedge, to cause it to penetrate a resisting body, the power is to the resistance as the thickness of the wedge is to its length. Let  $t$  be the thickness,  $l$  the length,  $W$  the resistance, and  $P$  the power or pressure on the head of the wedge. Then,—

$$P = \frac{Wt}{l} \quad . \quad . \quad . \quad . \quad . \quad (9)$$

$$W = \frac{Pl}{t} \quad . \quad . \quad . \quad . \quad . \quad (10)$$

The *screw* is an inclined plane lapped round a cylinder. The effect of a screw is reckoned in terms of the pitch or height of the plane for one revolution, and the radius of the handle or wheel by which it is turned. The power applied at the end of the radius describes, for one turn of the screw, a circle of which the diameter is twice the radius. The circumference of the circle is equal to 6.28 times the radius, and the power is to the resistance as the pitch of the screw is to 6.28 times the radius of the power, or to 3.14 times the diameter. Let  $p$  be the pitch of the screw-thread,  $r$  the radius of the lever or wheel by which the power is applied,  $W$  the weight, load, or resistance on the screw, and  $P$  the power. Then,

$$6.28 Pr = Wp \quad . \quad . \quad . \quad . \quad (11)$$

$$P = \frac{Wp}{6.28r} \quad . \quad . \quad . \quad . \quad (12)$$

$$W = \frac{6.28Pr}{p} \quad . \quad . \quad . \quad . \quad (13)$$

$$p = \frac{6.28Pr}{W} \quad . \quad . \quad . \quad . \quad (14)$$

$$r = \frac{Wp}{6.28P} \quad . \quad . \quad . \quad . \quad (15)$$

If the power be applied through a wheel, the diameter of the wheel may be substituted for the radius, when half the co-efficient—3.14—is to be employed in the formulæ.

The relations are the same whether the nut be turned upon the screw, or the screw be turned within the nut.

### Mechanical Centres.

There are various mechanical centres in solid or quasi-solid bodies—the centre of gravity, the centre of gyration, the centre of oscillation. The first is statical; the second and third are dynamical, inasmuch as these are only developed in bodies in motion.

### Centre of Gravity.

The centre of gravity of a body is that point within the body about which the gravitation of the particles of the body is self-balanced. It is a resultant centre of action, at which the body may be supposed to be concentrated: at which it can be freely supported or suspended in any position in a state of rest. In various classes of calculation the whole weight or mass of a body is taken as massed at the centre of gravity when at rest, or when in motion rectilinearly.



The centre of gravity of regular plane figures or solids—as, for instance, a straight line, a square, a parallelogram, a regular polygon, a circle, the circumference of a circle, an ellipse, a prism, a cylinder, a ring, a sphere, a spheroid, a regular solid—is the same as the geometrical centre.

The centre of gravity of a plane triangle is found by drawing a straight line from one of the angles to the middle of the opposite side, and setting off one-third of this line from the side. Or, drawing two such straight lines from two of the angles, their intersection is the centre of gravity.

The centre of gravity of a trapezium is found by drawing the diagonals, and joining the centres of each alternate pair of triangles so formed. The final intersection is the centre of gravity.

In a cone or a pyramid, the centre of gravity is in the axis, at a distance of one-fourth of its length from the base.

For an arc of a circle, multiply the bisecting radius by the chord of the arc, and divide by the length of the arc. The quotient is the distance of the centre of gravity from the centre of the circle.

For a segment of a circle, cube the chord and divide by 12 times the area of the segment. The quotient is the distance of the centre of gravity from the centre of the circle.

In a sector of a circle, the centre of gravity is two-thirds of the distance of that of an arc, from the centre of the circle. Or, multiply the radius by twice the chord of the arc, and divide by three times the length of the arc; the quotient is the distance of the centre of gravity from the centre of the circle.

In a semicircle, multiply the radius by  $\cdot 4244$ ; the product is the distance of the centre of gravity from the centre of the circle.

In a solid hemisphere, the centre of gravity is at a distance of three-eighths of the radius from the centre.

For a solid spherical segment, deduct half the versed sine from the radius, and square the difference; multiply this square by the square of the versed sine and by  $3\cdot 1416$ ; and divide by the content of the segment. The quotient is the distance of the centre of gravity from the centre of the segment.

In a hemispherical surface, spherical-segment surface, or spherical-zone surface, the centre of gravity is at half the height of the axis.

In a parabola, the centre of gravity is in the axis, at a distance of three-fifths of the height from the vertex.

In a semiparabola, the centre of gravity is at the same

height as in a parabola, but it is situated at a distance from the axis, of three-eighths of the semibase.

In a paraboloid, the centre of gravity is in the axis, at a distance of two-thirds of the axis from the vertex.

For two bodies, fixed one at each end of a straight bar, the common centre of gravity is in the bar, at that point which divides the distance between their respective centres of gravity in the inverse ratio of the weights. In this solution, the weight of the bar is not reckoned for. But it may be taken as a third body, and allowed for as in the following directions.

For more than two bodies connected in one system, find the common centre of gravity of two of them; and find the common centre of these two jointly with a third body, and so on to the last body of the group.

For any plane figure, the centre of gravity may be found mechanically, by suspending the figure by any point near its edge, and marking on it the direction of a plumb-line hung from that point; then suspending it from some other point near the edge, and again marking the direction of the plumb-line. The intersection of the directions is the centre of gravity.

### Centre of Gyration.

The centre of gyration, revolution, or whirling, is the resultant centre of the force or work accumulated in the revolving mass; so situated that if all parts of the body were concentrated there, the work accumulated in the body, at the same angular speed, would be the same as in the original body. To find the position of this point, the centre of gyration, suppose the revolving body to consist of an indefinitely great number of equal particles; as the work accumulated in each particle is proportional to the square of its velocity, and as the velocity is proportional to the radius of revolution, or distance of the particle from the axis of revolution, the work in each particle is proportional to the square of its distance from the axis. Multiply the weight of each particle by the square of its distance from the axis: the product is the moment of inertia of the particle, and the sum of all the products is the moment of inertia of the whole mass. Divide the moment of inertia by the weight of the body; the quotient is the square of the radius of gyration, or of the distance of the resultant centre of gyration from the axis; and the square root of the quotient is the radius of gyration. The moment of inertia is usually represented by the symbol  $I$ . Let the total revolving weight equal  $w$ , and the radius of gyration

equal  $r$ . The relations of these quantities are expressed thus :—

$$I = wr^2 \quad . \quad . \quad . \quad (16)$$

$$\frac{I}{w} = r^2 \quad . \quad . \quad . \quad (17)$$

$$r = \sqrt{\frac{I}{w}} \quad . \quad . \quad . \quad (18)$$

Concisely expressed thus :—

*The moment of inertia* is equal to the product of the weight by the square of the radius of gyration.

*The moment of inertia divided by the weight* is equal to the square of the radius of gyration.

*The radius of gyration* is equal to the square root of the quotient of the moment of inertia divided by the weight.

In calculating the radius of gyration, it is advisable in practice to divide the body into a considerable number of small parts—the more numerous the more nearly exact is the result. When these parts are equal, the radius of gyration may be determined by simply taking the mean of all the squares of the distances of the parts from the axis of revolution, and finding the square root of the mean square.

The radius of gyration of a straight bar, revolving about one end, is equal to the length of the bar multiplied by  $\cdot 5773$ .

That of a thin rectangular plate revolving facewise on one of its edges, is equal to the radial length of the plate multiplied by  $\cdot 5773$ .

That of a straight bar or a thin rectangular plate, revolving about its mid-length or centre, is equal to the length multiplied by  $\cdot 2886$ .

That of a straight bar or a thin rectangular plate revolving on any point between the extremities, is, generally, equal to

$\sqrt{\frac{a^3 + b^3}{3(a+b)}}$ , in which  $a$  and  $b$  are the lengths of the two parts of the bar or plate. That is to say, divide the sum of the cubes of the two sub-lengths, by three times the length of the bar ; the square root of the quotient is equal to the radius of gyration.

That of a circular plate, a solid wheel of uniform thickness, or a solid cylinder of any length, revolving on its axis, is equal to the geometrical radius multiplied by  $\cdot 7071$ .

That of a flat ring or hollow cylinder revolving on its axis, is equal to  $\sqrt{\frac{R^2 + r^2}{2}}$ , in which  $R$  and  $r$  are the outer and inner geometrical radii of the ring. That is to say, the radius

of gyration is equal to the square root of half the sum of the squares of the inner and outer radii.

That of the circumference of a circle revolving about its axis, is equal to the geometrical radius.

That of the circumference of a circle revolving about a diameter, is equal to the geometrical radius of the circle multiplied by .7071.

That of a very thin circular plate revolving about one of its diameters, is equal to half the geometrical radius of the circle.

That of a solid cylinder revolving on a diameter at mid-length, is equal to  $\sqrt{\frac{l^2}{12} + \frac{r^2}{4}}$ , in which  $l$  and  $r$  are the length and the geometrical radius respectively. That is to say, divide the square of the length by 12, and the square of the radius by 4; the radius of gyration is equal to the square root of the sum of the quotients.

That of a hollow cylinder revolving on a diameter at mid-length is equal to  $\sqrt{\frac{l^2}{12} + \frac{R^2 + r^2}{4}}$ , in which  $l$ ,  $R$ , and  $r$ , are the length, and the outer and the inner geometrical radius respectively. That is to say, divide the square of the length by 12, and the sum of the squares of the inner and outer radii by 4; the radius of gyration is equal to the square root of the sum of these two quotients.

That of a very thin hollow cylinder revolving on a diameter at mid-length, is equal to  $\sqrt{\frac{l^2}{12} + \frac{R^2}{2}}$ , in which  $l$  and  $R$  are the length and the outer geometrical radius of the cylinder respectively. That is to say, divide the square of the length by 12, and the square of the radius by 2; the radius of gyration is equal to the square root of the sum of the quotients.

That of a solid sphere revolving about a diameter, is equal to the geometrical radius of the sphere multiplied by .6325.

That of a hollow sphere revolving about a diameter is equal to  $\sqrt{\frac{2(R^5 - r^5)}{5(R^3 - r^3)}}$ , in which  $R$  and  $r$  are the outer and inner geometrical radii respectively. That is to say, divide twice the difference of the fifth powers of the radii by five times the difference of the cubes of the radii; the radius of gyration is equal to the square root of the quotient.

That of the surface of a sphere, or a very thin hollow sphere, revolving about a diameter, is equal to the geometrical radius of the sphere multiplied by .8165.

That of a solid cone revolving about its axis is equal to the geometrical radius of the base multiplied by ·5477.

That of a solid cone revolving about its vertex is equal to  $\sqrt{\frac{12l^2 + 3r^2}{20}}$ , in which  $l$  is the length, and  $r$  is the geometrical radius of the base. That is to say, to 12 times the square of the length add 3 times the square of the radius; divide the sum of these by 20; the radius of gyration is equal to the square root of the quotient.

When the cone is right-angled—the radius of the base being equal to the length,—the radius of gyration is equal to the length multiplied by ·8660.

That of a paraboloid revolving on the axis is equal to the geometrical radius of the base multiplied by ·5773.

That of a parallelopiped revolving in its own plane about one of the ends at a point midway of its breadth, is equal to

$\sqrt{\frac{4l^2 + b^2}{12}}$ , in which  $l$  is the length, and  $b$  the breadth. That

is to say, to 4 times the square of the length add the square of the breadth, and divide the sum by 12; the radius of gyration is equal to the square root of the quotient.

### Centre of Oscillation.

The centre of oscillation of a body vibrating about a fixed axis or point of suspension, by the action of gravity, is the resultant centre of the force or work alternately accumulated and neutralised by gravitation in the oscillating mass during each vibration. It is so situated that if all parts of the body were concentrated there, the quantity of work alternately accumulated and neutralised would continue unaltered, and the body would continue to vibrate in the same time. The centre of oscillation is in the straight line which joins the centre of gravity to the axis of oscillation. The particles of the body have velocities varying with the distance of the particles from the axis, and if the moment of inertia of the body, the method of finding which has already been explained, be divided by the weight of the body, and by the distance of the centre of gravity from the centre of suspension, the quotient will be the length of the resultant radius of oscillation, at the end of which is the centre of oscillation. Putting  $I$  and  $w$ , as before, for the moment of inertia and the weight of the body respectively,  $r/o$  for the radius of oscillation, and  $r/g$  for the radius of the centre of gravity, then,—

$$r/o = \frac{I}{w \times r/g} \quad . \quad . \quad . \quad . \quad (19)$$

$$\text{and } r/o \times r/g = \frac{I}{w} \quad . \quad . \quad . \quad . \quad (20)$$

But  $\frac{I}{w}$  is equal to  $\sqrt{\frac{I}{w}} \times \sqrt{\frac{I}{w}}$ , or  $(r \times r)$ , the square of the radius of gyration, consequently,

$$r/g : r :: r : r/o \quad . \quad . \quad . \quad . \quad (21)$$

That is to say, the radius of oscillation is a third proportional to the radius of the centre of gravity and the radius of gyration, and finally,

$$\text{Radius of oscillation} = \frac{\text{radius}^2 \text{ of gyration}}{\text{radius of centre of gravity}} \quad . \quad (22)$$

In a straight line, or a uniform thin bar or cylinder, suspended by one end, oscillating about it as an axis, the centre of oscillation is at  $\frac{2}{3}$ rd of the length of the rod from the axis.

In a straight line or thin bar of uniform thickness, but in which the density of its particles increase as the distance from the axis, the centre of oscillation is at  $\frac{3}{4}$ ths of the length of the rod from the axis.

In a straight line or uniform thin bar, suspended at a point one-third of the length below the upper end of the bar, the centre of oscillation is at  $\frac{2}{3}$ rd of the length below the axis, or it is coincident with the lower end of the bar. That is to say, whether a thin bar be suspended at one end or at a point one-third of its length below the upper end, the vibrations will be performed in the same time. The limit of transition of the axis is at half the length of the bar, round which point it does not oscillate at all, the centre of oscillation being indefinitely removed.

The lengths of the radius of oscillation of a few regular plane figures or thin plates, suspended by the vertex or uppermost point, are as follows :—

1st. When the vibrations are flatwise, or perpendicular to the plane of the figure :

In an isosceles triangle the radius of oscillation is equal to  $\frac{2}{3}$ ths of the height of the triangle.

In a circle,  $\frac{2}{3}$ ths of the diameter.

In a parabola,  $\frac{2}{3}$ ths of the height.

2nd. When the vibrations are edgewise, or in the plane of the figure :

In a circle the radius of oscillation is  $\frac{2}{3}$ ths of the diameter.

In a rectangle suspended by one angle,  $\frac{2}{3}$ rd of the diagonal.

In a parabola, suspended by the vertex,  $\frac{2}{3}$ ths of the height, plus  $\frac{1}{3}$ rd of the parameter.

In a parabola, suspended by the middle of the base,  $\frac{2}{3}$ ths of the height plus  $\frac{1}{2}$  the parameter.

In a sector of a circle suspended by the centre,  $\frac{3}{4}$ ths of the geometrical radius multiplied by the length of the arc, and divided by the length of the chord.

The length of the radius of oscillation of a cone is  $\frac{3}{4}$ ths of the height, plus the quotient obtained by dividing the square of the radius of the base by five times the height. If a right-angled cone be suspended at its vertex, the centre of oscillation will coincide with the centre of its base, and the cone will vibrate in the same time as a simple pendulum of which the length is equal to the height of the cone.

That of a sphere suspended by a cord is  $\frac{3}{4}$ ths of the square of the geometrical radius, divided by the length of the cord measured to the centre of the sphere, plus the length of the chord so taken. For example, in a sphere 8 inches in diameter, suspended by a cord or a light rod 20 inches long, as measured between the centre of suspension and the centre of the sphere, the radius of oscillation is equal to,—

$$\frac{2 \times 4^2}{5 \times 20} + 20 = \cdot 32 + 20 = 20 \cdot 32 \text{ inches,}$$

or  $\cdot 32$  inch below the centre of the sphere.

If the point of suspension be at the surface of the sphere, or at the extremity of a geometrical radius, the radius of oscillation is equal to  $\frac{3}{4}$ ths of the radius, or  $\frac{3}{10}$ ths of the diameter.

### Centre of Percussion.

The centre of percussion of a body oscillating or vibrating about a fixed axis, is identical with the centre of oscillation, which is the point at which, if a blow is struck, the percussive action is the same as if the whole mass of the body were concentrated at the point.

### The Pendulum.

A "simple pendulum" is defined as a heavy particle attached to one end of a cord or a rod without weight, and caused to vibrate on the centre of suspension. The time of vibration of an ordinary pendulum depends on the angle or arc of vibration; but for arcs of vibration not exceeding 4 or 5 degrees, the time of vibration is sensibly the same for any length of arc within that limit. This uniformity of time of vibration is called isochronism.

The length or radius of oscillation of the pendulum vibrating seconds, at the level of the sea, in the latitude of London, is 39·1393 inches. The lengths for other places are given

in page 430. A few of these are here reproduced in inches:—

	Inches.
Equator . . . . .	39·0168
Latitude 45° . . . . .	39·1164
Paris . . . . .	39·1308
London . . . . .	39·1393
Berlin . . . . .	39·1428
Edinburgh . . . . .	39·1548
Aberdeen . . . . .	39·1584
Pole . . . . .	39·2184

The times of vibration of pendulums within the limits already given, are as the square roots of the lengths of the pendulums. The lengths of pendulums are to each other as the squares of the times of one vibration; or inversely as the squares of the numbers of vibrations in a given time.

The square root of the length of the pendulum vibrating seconds at London, or  $\sqrt{39\cdot1393} = 6\cdot2561$ ; and the time of a vibration of any pendulum is equal to the square root of the given length in inches divided by  $6\cdot2561$ , or,

$$t = \frac{\sqrt{l}}{6\cdot2561} \quad . \quad . \quad . \quad (23)$$

$t$  = the time of one vibration in seconds.

$l$  = the length of the pendulum in inches.

$n$  = the number of vibrations per second, or per minute.

To find the number of vibrations per second of a pendulum of a given length, divide  $6\cdot2561$  by the square root of the length in inches.

The number of vibrations per minute is found by dividing  $375\cdot366$  by the square root of the length in inches; or,

$$(\text{per second}) \ n = \frac{6\cdot2561}{\sqrt{l}} \quad . \quad . \quad . \quad (24)$$

$$(\text{per minute}) \ n = \frac{375\cdot366}{\sqrt{l}} \quad . \quad . \quad . \quad (25)$$

The length of a pendulum in inches to make one vibration in a given time, is found by multiplying the square of the time in seconds by  $39\cdot1393$ ; or,

$$l = t^2 \times 39\cdot1393 \quad . \quad . \quad . \quad (26)$$

The length of a pendulum in inches to make a given number of vibrations per second is equal to the quotient of  $39\cdot1393$  divided by the square of the number of vibrations.



Or, when the number of vibrations per minute is given, divide 140,900 by the square of the number ; or,

$$l = \frac{39 \cdot 1393}{n^2 \text{ (per second)}} \quad (27)$$

$$l = \frac{140,900}{n^2 \text{ (per minute)}} \quad (28)$$

The time of vibration of a pendulum may be varied by the addition of a weight, which, when applied at a point above the centre of suspension, counteracts the lower weight, and lengthens the period of vibration. By varying the height of the upper weight the time is varied.

To find the weight of the upper bob of a compound pendulum, necessary to vibrate seconds, when the weight of the lower bob is given, with the distances of the weights from the point of suspension, the following is the formula :—

$$w = W \frac{(39 \cdot 1393 + D) - D^2}{(39 \cdot 139 + d) + d^2} \quad (29)$$

$W$  = the weight of the lower bob.

$w$  = the weight of the upper bob.

$D$  = the distance of the lower bob from the centre, in inches.

$d$  = the distance of the upper bob from the centre, in inches.

Thus, by means of a second bob, short pendulums may be constructed to vibrate as slowly as longer pendulums.

### Gravity and Fall of Bodies.

The motion and velocity of a body freely falling vertically, is uniformly accelerated, equal additions of velocity being acquired in equal times. There are three elements concerned in the fall of a body, *height* fallen through, *velocity* acquired, and *time* of fall.

The force of gravity is expressed by the velocity in feet per second, communicated by gravity to a body falling freely in a second, namely, 32·189, or, say, 32·2 feet per second, as at London ; and it is represented by the symbol  $g$ .

The force of gravity varies slightly according to the latitude, as is shown by the following table, in which the length of the pendulum beating seconds is added :—

TABLE 227.—GRAVITY ; LENGTH OF SECONDS PENDULUM.

Locality.	Latitude.	Force of Gravity at the Level of the Sea : Value of $g$ .	Length of Pendulum beating Seconds, at the Level of the Sea.
	Degs. Secs.	Feet per Second.	Feet.
Equator . . . . .	0 0	32·091	3·2514
Latitude 45° . . . . .	45 0	32·173	3·2597
Paris . . . . .	48 50	32·183	3·2609
Greenwich (London). . . . .	51 29	32·191	3·2616
Berlin . . . . .	52 30	32·194	3·2619
Dublin . . . . .	53 21	32·196	3·2621
Manchester . . . . .	53 29	32·196	3·2622
Edinburgh . . . . .	55 57	32·203	3·2629
Aberdeen . . . . .	57 9	32·206	3·2632
Pole . . . . .	90 0	32·255	3·2682

The relations of time, height of fall, and velocity, are expressible as follows :—

Total time as . . . . . 1, 2, 3, 4, &c.

Velocity acquired as . . . . . 1, 2, 3, 4, &c.

Height of Fall as . . . . . 1, 4, 9, 16, &c.

Or as . . . . . 1, 2<sup>2</sup>, 3<sup>2</sup>, 4<sup>2</sup>, &c.

Whilst the velocity is increased simply with the time, the height fallen increases as the square of the time, and as the square of the velocity. These relations are formulated in the following rules, in which,—

$t$  = time, in seconds.

$h$  = height fallen, in feet.

$v$  = velocity acquired, in feet per second.

RULE 1.—To find the *velocity acquired*, given the height of fall, multiply the height by 64·4, and take the square root of the quotient.

Or, multiply the square root of the height by 8. The exact value of the coefficient is 8·025, but 8 is usually taken for ordinary calculations.

These rules are formulated thus :—

$$v = \sqrt{64\cdot4 h} \quad . \quad . \quad . \quad (30)$$

$$\text{Or } v = 8\sqrt{h} \quad . \quad . \quad . \quad (31)$$

RULE 2.—To find the *velocity acquired*, given the time of fall. Multiply the time in seconds by 32·2. Or,

$$v = 32\cdot2 t \quad . \quad . \quad . \quad (32)$$

RULE 3.—To find the *height of fall*, given the velocity acquired. Square the velocity, and divide by 64·4. Or,

$$h = \frac{v^2}{64\cdot4} \quad . \quad . \quad . \quad . \quad (33)$$

RULE 4.—To find the *height of fall*, given the time. Multiply the square of the time by 16·1. Or,

$$h = 16\cdot1 t^2 \quad . \quad . \quad . \quad . \quad (34)$$

RULE 5.—To find the *height of fall*, given the velocity and the time. Multiply the velocity by the time, and divide by 2. Or,

$$h = \frac{vt}{2} \quad . \quad . \quad . \quad . \quad (35)$$

RULE 6.—To find the *time of fall*, given the velocity acquired. Divide the velocity by 32·2. Or,

$$t = \frac{v}{32\cdot2} \quad . \quad . \quad . \quad . \quad (36)$$

RULE 7.—To find the *time of fall*, given the height. Divide the height by 16·1; and find the square root of the quotient.

Or, multiply the square root of the height by ·2492.

Or, take one-fourth of the square root of the height, to find the time very nearly (within one-tenth of one per cent. of error by excess). Or,

$$t = \sqrt{\frac{h}{16\cdot1}} \quad . \quad . \quad . \quad . \quad (37)$$

$$\text{Or, } t = \cdot 2492 \sqrt{h} \quad . \quad . \quad . \quad . \quad (38)$$

$$\text{Or, } t = \frac{1}{4} \sqrt{h} \text{ (very nearly)} \quad . \quad . \quad . \quad . \quad (39)$$

The above rules, drawn for falling bodies, are available also for the case of bodies projected freely upwards in opposition to gravity and uniformly retarded by it. The symbol  $v$  is expressive of the initial velocity with which the ascending body is propelled;  $h$  is the height to which it rises;  $t$  is the time of ascent.

The formula (33) for the height due to the velocity may be adapted for finding the head due to a velocity  $v_1$  expressed in miles per hour. A speed of 1 mile per hour is equivalent to 1·46 feet per second, and the formula becomes by substitution,  $h = \frac{1\cdot46 v_1^2}{64\cdot4}$ .

By reduction, the following rule is obtained:—

RULE 7.—To find the *height* due to the velocity or speed in miles per hour. Divide the square of the speed by 29·94. Or

$$h = \frac{v_1^2}{29\cdot94} \quad . \quad . \quad . \quad . \quad (40)$$

The following table contains the times of fall, and the final velocities due to given heights of fall; Table 229 gives, conversely, the heights of fall due to given velocities; Table 230 gives the heights of fall and the final velocities due to given times of fall; Table 231 gives the heights of fall due to given speeds in miles per hour.

TABLE 228.—FALLING BODIES:—HEIGHT OF FALL, AND CORRESPONDING TIME OF FALL, AND FINAL VELOCITY.

$$t = .2492 \sqrt{h.}$$

$$v = 8.025 \sqrt{h.}$$

Height of Fall.	Time of Fall.	Velocity acquired in Feet per Second.	Height of Fall.	Time of Fall.	Velocity acquired in Feet per Second.	Height of Fall.	Time of Fall.	Velocity acquired in Feet per Second.
Feet.	Secs.	Feet per Sec.	Feet.	Secs.	Feet per Sec.	Feet.	Secs.	Feet per Sec.
.01	.025	.803	1.4	.295	9.50	4.5	.529	17.03
.02	.035	1.14	1.5	.305	9.83	4.6	.534	17.21
.03	.043	1.39	1.6	.315	10.15	4.7	.540	17.40
.04	.050	1.61	1.7	.325	10.46	4.8	.546	17.58
.05	.056	1.80	1.8	.334	10.77	4.9	.552	17.78
.06	.061	1.97	1.9	.344	11.06	5.0	.557	17.99
.07	.066	2.12	2.0	.353	11.35	5.25	.571	18.41
.08	.071	2.27	2.1	.361	11.63	5.5	.585	18.82
.09	.075	2.41	2.2	.370	11.90	5.75	.598	19.24
.1	.079	2.54	2.3	.378	12.17	6.0	.611	19.66
.15	.097	3.11	2.4	.386	12.43	6.25	.623	20.07
.2	.112	3.59	2.5	.394	12.69	6.5	.635	20.46
.25	.125	4.01	2.6	.402	12.94	6.75	.647	20.85
.3	.137	4.40	2.7	.410	13.19	7.0	.659	21.23
.35	.147	4.75	2.8	.417	13.43	7.25	.672	21.61
.4	.158	5.07	2.9	.424	13.67	7.5	.683	21.97
.45	.167	5.38	3.0	.432	13.90	7.75	.694	22.33
.5	.176	5.68	3.1	.439	14.13	8.0	.705	22.69
.55	.185	5.95	3.2	.446	14.36	8.25	.716	23.05
.6	.193	6.22	3.3	.453	14.58	8.5	.727	23.40
.65	.201	6.47	3.4	.459	14.80	8.75	.737	23.74
.7	.209	6.71	3.5	.466	15.01	9.0	.746	24.07
.75	.216	6.95	3.6	.473	15.22	9.25	.757	24.40
.8	.223	7.18	3.7	.480	15.43	9.5	.768	24.73
.85	.230	7.40	3.8	.486	15.64	9.75	.778	25.06
.9	.236	7.61	3.9	.492	15.85	10	.788	25.38
.95	.243	7.82	4.0	.498	16.05	10.5	.808	26.01
1.0	.249	8.03	4.1	.505	16.25	11	.827	26.62
	.261	8.42	4.2	.511	16.45	11.5	.845	27.22
	.273	8.79	4.3	.517	16.64	12	.863	27.80
	.284	9.15	4.4	.523	16.84	12.5	.881	28.37

TABLE 228.—FALL, TIME, AND VELOCITY (*continued*).

Height of Fall.	Time of Fall.	Velocity acquired in Feet per Second.	Height of Fall.	Time of Fall.	Velocity acquired in Feet per Second.	Height of Fall.	Time of Fall.	Velocity acquired in Feet per Second.
Feet.	Secs.	Feet per Sec.	Feet.	Secs.	Feet per Sec.	Feet.	Secs.	Feet per Sec.
13	·899	28·93	43	1·634	52·62	160	3·152	101·5
13·5	·916	29·49	44	1·653	53·23	170	3·250	104·6
14	·933	30·03	45	1·672	53·83	180	3·344	107·9
14·5	·949	30·56	46	1·690	54·43	190	3·435	110·6
15	·965	31·08	47	1·709	55·02	200	3·525	113·5
15·5	·981	31·59	48	1·727	55·60	225	3·738	120·4
16	·997	32·00	49	1·745	56·17	250	3·941	126·9
16·1	1·000	32·20	50	1·762	56·74	275	4·133	133·1
16·5	1·013	32·60	52	1·797	57·87	300	4·317	139·0
17	1·028	33·09	54	1·831	58·97	325	4·493	144·7
17·5	1·033	33·57	56	1·865	60·05	350	4·663	150·1
18	1·057	34·05	58	1·898	61·12	375	4·826	155·4
18·5	1·072	34·52	60	1·930	62·16	400	4·981	160·5
19	1·086	34·98	62	1·962	63·19	425	5·138	165·4
19·5	1·101	35·44	64	1·994	64·20	450	5·287	170·2
20	1·115	35·89	66	2·025	65·20	475	5·432	174·9
21	1·141	36·77	68	2·055	66·18	500	5·573	179·9
22	1·167	37·64	70	2·085	67·14	550	5·845	188·2
23	1·194	38·49	72	2·115	68·09	600	6·105	196·6
24	1·221	39·31	74	2·144	69·03	650	6·354	204·6
25	1·246	40·12	76	2·173	69·96	700	6·594	212·3
26	1·271	40·92	78	2·201	70·87	750	6·825	219·8
27	1·295	41·70	80	2·229	71·78	800	7·049	226·9
28	1·319	42·47	82	2·257	72·67	850	7·266	234·0
29	1·342	43·22	84	2·284	73·55	900	7·477	240·7
30	1·365	43·95	86	2·311	74·42	950	7·681	247·3
31	1·388	44·68	88	2·338	75·28	1000	7·881	253·8
32	1·410	45·39	90	2·364	76·13	1500	9·652	310·8
33	1·432	46·10	92	2·390	76·97	2000	11·15	358·9
34	1·453	46·79	94	2·416	77·81	2500	12·46	401·2
35	1·474	47·47	96	2·442	78·63	3000	13·65	439·5
36	1·495	48·15	98	2·467	79·45	3500	14·74	474·7
37	1·516	48·81	100	2·492	80·25	4000	15·76	507·5
38	1·536	49·47	110	2·614	84·17	4500	16·72	538·3
39	1·556	50·11	120	2·730	87·91	5000	17·62	567·4
40	1·576	50·75	130	2·842	91·50	7500	21·58	695·0
41	1·596	51·38	140	2·949	94·95	10000	24·92	802·5
42	1·615	52·01	150	3·052	98·28			

TABLE 229.—FALLING BODIES:—FINAL VELOCITY AND CORRESPONDING HEIGHT OF FALL.

$$h = \frac{v^2}{64.4}$$

Velocity in Feet per Second.	Height of Fall.	Velocity in Feet per Second.	Height of Fall.	Velocity in Feet per Second.	Height of Fall.	Velocity in Feet per Second.	Height of Fall.
Feet per Sec.	Feet.	Feet per Sec.	Feet.	Feet per Sec.	Feet.	Feet per Sec.	Feet.
·25	·0010	24	8·94	56	48·7	87	117·5
·50	·0039	25	9·71	57	50·4	88	120·2
·75	·0087	26	10·5	58	52·2	89	123·0
1·00	·016	27	11·3	59	54·1	90	125·8
1·25	·024	28	11·2	60	55·9	91	128·6
1·50	·035	29	13·1	61	57·8	92	131·4
1·75	·048	30	14·0	62	59·7	93	134·3
2	·062	31	14·9	63	61·6	94	137·2
2·5	·097	32	15·9	64	63·6	95	140·1
3	·140	33	16·9	65	65·6	96	143·1
3·5	·190	34	17·9	66	67·6	97	146·1
4	·248	35	19·0	67	69·7	98	149·1
4·5	·314	36	20·1	68	71·8	99	152·2
5	·388	37	21·3	69	73·9	100	155·3
6	·559	38	22·4	70	76·1	105	171·2
7	·761	39	23·6	71	78·3	110	187·9
8	·994	40	24·9	72	80·5	115	205·4
9	1·26	41	26·1	73	82·7	120	223·6
10	1·55	42	27·4	74	85·0	130	262·4
11	1·88	43	28·7	75	87·4	140	304·3
12	2·24	44	30·1	76	89·7	150	349·4
13	2·62	45	31·4	77	92·1	175	475·5
14	3·04	46	32·9	78	94·5	200	621
15	3·49	47	34·3	79	96·9	300	1397
16	3·98	48	35·8	80	99·4	400	2484
17	4·49	49	37·3	81	101·9	500	3882
18	5·03	50	38·8	82	104·4	600	5590
19	5·61	51	40·4	83	107·0	700	7609
20	6·21	52	42·0	84	109·5	800	9938
21	6·85	53	43·6	85	112·2	900	12578
22	7·52	54	45·3	86	114·8	1000	15528
23	8·21	55	47·0				

TABLE 230.—FALLING BODIES:—TIME OF FALL AND CORRESPONDING HEIGHT OF FALL AND FINAL VELOCITY.

$$h = 16.1 t^2.$$

$$v = 32.2 t.$$

Time of Fall.	Height of Fall.	Velocity acquired in Feet per Second.	Time of Fall.	Height of Fall.	Velocity acquired in Feet per Second.	Time of Fall.	Height of Fall.	Velocity acquired in Feet per Second.
Secs.	Feet.	Feet per Sec.	Secs.	Feet.	Feet per Sec.	Secs.	Feet.	Feet per Sec.
1	16.1	32.2	12	2318	386.4	23	8517	740.6
2	64.4	64.4	13	2721	418.6	24	9273	772.8
3	144.9	96.6	14	3156	450.8	25	10062	805.0
4	257.6	128.8	15	3623	483.0	26	10884	837.2
5	402.5	161.0	16	4122	515.2	27	11737	869.4
6	579.6	193.2	17	4653	547.4	28	12622	901.6
7	788.9	225.4	18	5217	579.6	29	13540	933.8
8	1030	257.6	19	5812	611.8	30	14490	966.0
9	1304	289.8	20	6440	644.0	31	15473	998.2
10	1610	322.0	21	7100	676.2	32	16487	1030
11	1948	354.2	22	7792	708.4			

TABLE 231.—FALLING BODIES:—SPEED IN MILES PER HOUR AND HEIGHT DUE TO THE SPEED.

$$h = \frac{\text{speed}^2}{29.938}.$$

Speed in Miles per Hour.	Velocity in Feet per Second.	Height due to the Speed.	Speed in Miles per Hour.	Velocity in Feet per Second.	Height due to the Speed.
Miles.	Feet.	Feet.	Miles.	Feet.	Feet.
1	1.46	.033	50	73.33	83.51
5	7.33	.835	60	87.99	120.2
10	14.66	3.34	70	102.66	163.7
20	29.33	13.36	80	117.33	213.8
30	43.99	30.07	90	131.99	270.6
40	58.66	53.44	100	146.66	334.0

### Accelerating and Retarding Forces in General.

The formulæ for falling bodies acted on by gravity, may be adapted for the action of uniformly accelerating and retarding forces generally. Let  $t$  be the time in seconds

during which an accelerating force is applied to the body, supposing that the body is started from a state of rest ;  $v$  the final velocity acquired ;  $s$  the space in feet traversed by the body during the time—the equivalent of the height in the rules for gravity ;  $f$  the accelerating force in pounds ;  $w$  the weight of the body in pounds. The velocity acquired is directly as the accelerating force, and inversely as the weight of the body.

### Rules for Accelerated Motion.

RULE 1.—To find *the final velocity*, given the weight, the force, and the space. Multiply the force by the space, and divide by the weight ; find the square root of the quotient, and multiply by 8. Or,

$$v = 8 \sqrt{\frac{fs}{w}} \quad . \quad . \quad . \quad (41)$$

RULE 2.—To find *the final velocity*, given the weight, the force, and the time. Multiply the force by the time, and by 32.2, and divide by the weight. Or,

$$v = \frac{32.2 ft}{w} \quad . \quad . \quad . \quad (42)$$

RULE 3.—To find *the force*, given the weight, the final velocity, and the space. Multiply the weight by the square of the final velocity, and divide by the space, and by 64.4. Or,

$$f = \frac{wv^2}{64.4s} \quad . \quad . \quad . \quad (43)$$

RULE 4.—To find *the force*, given the weight, the final velocity, and the time. Multiply the weight by the velocity, and divide by the time, and by 32.2. Or,

$$f = \frac{wv}{32.2t} \quad . \quad . \quad . \quad (44)$$

RULE 5.—To find *the weight*, given the force, the velocity, and the space. Multiply the force by the space, and by 64.4, and divide by the square of the velocity. Or,

$$w = \frac{64.4fs}{v^2} \quad . \quad . \quad . \quad (45)$$

RULE 6.—To find *the space*, given the weight, the final velocity, and the force. Multiply the weight by the square of the velocity, and divide by the force, and by 64.4. Or,

$$s = \frac{wv^2}{64.4f} \quad . \quad . \quad . \quad (46)$$



**RULE 7.**—To find *the space*, given the weight, the force, and the time. Multiply the force by the square of the time, and by 16·1, and divide by the weight. Or,

$$s = \frac{16\cdot1 ft^2}{w} \quad . \quad . \quad . \quad . \quad (47)$$

**RULE 8.**—To find *the space*, given the velocity and the time. Multiply the velocity by the time, and divide by 2.

$$s = \frac{vt}{2} \quad . \quad . \quad . \quad . \quad (48)$$

**RULE 9.**—To find *the time*, given the weight, the force, and the final velocity. Multiply the weight by the velocity, and divide by the force, and by 32·2. Or,

$$t = \frac{wv}{32\cdot2f} \quad . \quad . \quad . \quad . \quad (49)$$

**RULE 10.**—To find *the time*, given the weight, the force, and the space. Multiply the weight by the space, and divide by the force; find the square root of the quotient, and divide by 4. Or,

$$t = \frac{1}{4} \sqrt{\frac{ws}{f}} \quad . \quad . \quad . \quad . \quad (50)$$

The foregoing formulæ are available for calculating questions of retarded motion;  $v$  being the initial velocity,  $f$  the retarding force,  $w$  the weight of the body,  $s$  the space in which the motion is reduced to nothing, and  $t$  the time of retardation.

**RULE 11.**—To find the *accelerating or retarding force* in a body which is in motion at the beginning and end of the space traversed, when the space is given, and also the velocities at the beginning and the end of the space. Divide the difference of the squares of the velocities by the space and by 64·4, and multiply by the weight. The product is the accelerating or retarding force, according as the less or the greater velocity is the initial velocity. Or,

$$f = w \left( \frac{v^2 - v_1^2}{64\cdot4s} \right) \quad . \quad . \quad . \quad . \quad (51)$$

*Note.*—When the weight and the force are in simple relation to each other, expressible by a simple fraction, the terms of the fraction may be substituted for  $w$  and  $f$  in the formulæ (41), (42), (46), (47), (49), (50), and calculation simplified.

### Descent of Bodies on Inclined Planes.

The descent of a body on an inclined plane by the gravitation of the body, is a case of an accelerating force less than

that of gravity on a vertically falling body ; to be solved by the aid of the general formulas for accelerating forces. The accelerating force of gravitation on an inclined plane is to the direct force of gravity in the ratio of the height of the plane to the length of the plane ; and it is therefore inversely proportional to the length of the plane, when the height is the same. The accelerating force  $v$  is determined by multiplying the weight of the descending body by the height of the plane, and dividing the product by the length of the plane. For instance, a body weighing 100 lbs., on an inclined plane 1000 feet long and 20 feet high, is controlled by an accelerating force of  $(100 \times \frac{20}{1000} = 100 \times \frac{1}{50} =) 2$  pounds. But, inasmuch as the accelerating force acts through a space, or length of incline, proportionally longer as the force is less, the time of descent is also proportionally longer, and the final velocity acquired at the foot of the incline is equal to that due to the vertical height for a falling body. These relations are deduced without allowance for external resistances.

To adjust formula (50) for finding the time of free descent of an inclined plane :— $w$  and  $f$  being in proportion to  $l$ , the length of the plane, and  $h$  the height of it, these may be sub-

stituted for  $w$  and  $f$  in the formula, and  $t = \frac{1}{4} \sqrt{\frac{ws}{f}}$  becomes

$t = \frac{1}{4} \sqrt{\frac{ls}{h}}$  ; and, as  $s = l$ ,  $t = \frac{1}{4} \sqrt{\frac{l^2}{h}}$  ; or, finally,

$$t = \frac{l}{4\sqrt{h}} \quad . \quad . \quad . \quad . \quad . \quad (52)$$

**RULE 1.**—To find the *time* of descent, given the length and the height of the inclined plane. Divide the length of the plane by 4 times the square root of the height of the plane.

### Central Forces.

When a body revolves about an axis or centre, it is subject to centrifugal force, by which it is urged to fly from the centre ; and to centripetal force, the reactive force by which the centrifugal force is balanced, and by which the body is constrained to move in a circular path. These are known as central forces.

Central force varies as the square of the speed of revolution, whether in terms of the linear or circumferential velocity, or of the angular speed in revolutions per unit of time.

It varies as the radius of the circle of revolution.

It varies as the mass or weight of the revolving body.

Let :—

$w$  = the weight of the revolving body, in pounds.

$\frac{w}{g} = \frac{w}{32.2}$  = the mass of the body ;  $g$  representing gravity.

$v$  = the linear or circumferential velocity in feet per second.

$v_1$  = the angular velocity, or revolutions per second.

$f$  = the centrifugal force in pounds.

$r$  = the radius of gyration of the revolving body, in feet.

*Rules for Centrifugal Force in terms of Circumferential Velocity.*

RULE 1.—To find the *centrifugal force*, given the weight, the linear velocity, and the radius of gyration. Multiply the weight by the square of the linear velocity, and divide by 32.2 times the radius of gyration. Or,

$$f = \frac{wr^2}{32.2r} \quad . \quad . \quad . \quad . \quad . \quad (53)$$

RULE 2.—To find the *linear velocity*, when the weight, the centrifugal force, and the radius of gyration are given. Multiply the centrifugal force by the radius of gyration, and by 32.2, and divide by the weight ; take the square root of the quotient. Or,

$$v = \sqrt{\frac{32.2fr}{w}} \quad . \quad . \quad . \quad . \quad . \quad (54)$$

RULE 3.—To find the *weight*, when the centrifugal force, the linear velocity, and the radius of gyration are given. Multiply the centrifugal force by the radius of gyration, and by 32.2, and divide by the square of the velocity. Or,

$$w = \frac{32.2fr}{v^2} \quad . \quad . \quad . \quad . \quad . \quad (55)$$

RULE 4.—To find the *radius of gyration*, when the weight, the linear velocity, and the centrifugal force are given. Multiply the weight by the square of the velocity, and divide by the centrifugal force, and by 32.2. Or,

$$r = \frac{wr^2}{32.2f} \quad . \quad . \quad . \quad . \quad . \quad (56)$$

*Rules for Centrifugal Force in terms of Angular Velocity.*

The linear velocity  $v$  is equal to the angular velocity,  $v_1$ , multiplied by the radius of gyration and by 6.2832 (twice 3.1416). Or,

$$v = 6.2832v_1r \quad . \quad . \quad . \quad . \quad . \quad (57)$$

By substitution, in equation (53), and reduction, formula (58) is produced.

**RULE 5.**—To find *the centrifugal force*, when the weight, the angular velocity, and the radius of gyration are given. Multiply the weight by the square of the angular velocity and by the radius of gyration, and by 1.226. Or,

$$f = 1.226 w v_1^2 r \quad . \quad . \quad . \quad (58)$$

**RULE 6.**—To find *the angular velocity*, when the weight, the centrifugal force, and the radius of gyration are given. Multiply the weight by the radius of gyration, and by 1.226; divide the centrifugal force by the product so produced; and take the square root of the quotient. Or,

$$v_1 = \sqrt{\frac{f}{1.226 w r}} \quad . \quad . \quad . \quad (59)$$

**RULE 7.**—To find *the weight*, when the centrifugal force, the angular velocity, and the radius of gyration are given. Multiply the square of the angular velocity by the radius of gyration, and by 1.226; divide the centrifugal by the product. Or,

$$w = \frac{f}{1.226 v_1^2 r} \quad . \quad . \quad . \quad (60)$$

**RULE 8.**—To find *the radius of gyration*, when the weight, the angular velocity, and the centrifugal force are given. Multiply the weight by the square of the angular velocity, and by 1.226; and divide the centrifugal force by the product. Or,

$$r = \frac{f}{1.226 w v_1^2} \quad . \quad . \quad . \quad (61)$$

### Work.

The English unit of work is one foot-pound.

The French unit is one kilogrammetre.

One kilogrammetre is equal to 7.233 foot-pounds.

One foot-pound is equal to .1382 kilogrammetre.

One horse-power is equal to work done at the rate of 33,000 pounds lifted one foot high, or 33,000 foot-pounds, per minute; or to 550 foot-pounds per second; or to  $(33,000 \times 60 = )$  1,980,000 foot-pounds per hour—nearly 2 millions.

One cheval-vapeur, or cheval (French horse-power) is equal to 75 kilogrammetres, or 542.5 foot-pounds, per second.

One cheval is equal to .9863 horse-power.

One horse-power is equal to 1.0139 chevaux.

One kilogramme per cheval is equal to 2·235 pounds per horse-power.

One pound per horse-power is equal to ·447 kilogramme per cheval.

If the work of a horse-power, expressed in foot-pounds, be divided by 772, the quotient is the equivalent expression of horse-power in heat-units; or,  $(33,000 \div 772 =) 42\frac{3}{4}$  heat-units per minute.

The work, known also as *vis viva*, done by gravity on a falling body is equal to the weight of the body multiplied by the height of the fall: the evidence of which is the velocity of motion acquired by the body.

The quantity of work stored in a body in motion is equal to the work which would be accumulated in it by gravity in falling from such a height as would suffice to generate the same velocity of motion. Consequently, the formulas proper for the action of gravity are applicable for calculations affecting bodies in motion, and the product of the height due to the velocity by the weight of the body, is expressive of the work stored in the body.

The height due to the velocity is equal to the square of the velocity divided by 64·4, according to formula (33), page 431, and as tabulated, page 434, and

$$U = \frac{wv^2}{64\cdot4} \quad . \quad . \quad . \quad (62)$$

$$\text{or } U = w \times h \quad . \quad . \quad . \quad (63)$$

$U$  = the work accumulated in the body, in foot-pounds.

$w$  = the weight of the body in pounds.

$v$  = the velocity of the body in feet per second.

$r_1$  = the angular velocity of a revolving body, in revolutions per second.

$r_{11}$  = the same in revolutions per minute.

$h$  = the height due to the velocity, in feet.

$r$  = the radius of gyration, in feet.

**RULE 1.**—To find the *work stored* in a moving body, given the weight of the body and the velocity. Multiply the weight of the body by the square of the velocity, and divide by 64·4.

**RULE 2.**—To find the *work stored* in a moving body, given the weight of the body, and the height due to the velocity. Multiply the weight by the height.

The work stored in a revolving body is calculated by either of the above rules, when linear velocity is given. But when the angular velocity is given, the equivalent to the linear velocity is found by substituting the expression  $6\cdot2832r_1r_{11}$

already deduced, page 439, for  $v$  in the formula (1), and reducing, thus :—

$$U = \cdot 613 \, w r_{11}^2 r^2 \quad . \quad . \quad . \quad . \quad . \quad (64)$$

**RULE 3.**—To find the *work stored* in a revolving body, given the weight of the body, the angular velocity in revolutions per second, and the radius of gyration. Multiply the weight by the square of the angular velocity, and by the square of the radius of gyration, and by  $\cdot 613$ .

When the angular velocity is given as the number of revolutions per minute, it is either to be divided by 60, before being brought into calculation, in accordance with the foregoing rule; or the expression  $\frac{6 \cdot 2832 \, r_1 r}{60}$  is to be substituted

for  $v$  in the formula (1), when the expression becomes,

$$U = \frac{w}{64 \cdot 4} \times \left( \frac{6 \cdot 2832 \, r_1 r}{60} \right)^2, \text{ or reducing :—}$$

$$U = \cdot 00017 \, w r_{11}^2 r^2 \quad . \quad . \quad . \quad . \quad . \quad (65)$$

$$\text{or } U = \frac{w r_{11}^2 r^2}{5868} \quad . \quad . \quad . \quad . \quad . \quad (66)$$

**RULE 4.**—To find the *work stored* in a revolving body, given the weight of the body, the angular velocity in revolutions per minute, and the radius of gyration. Multiply the weight by the square of the angular velocity, by the square of the radius of gyration, and by  $\cdot 00017$ .

**RULE 5.**—For the same purpose, proceed as in rule 4, except to divide by 5868, instead of multiplying by  $\cdot 00017$ .

The work done by percussive force is simply measurable by the product of the weight of the colliding mass, and the height due to the velocity of the moment of impact plus the space moved through by the colliding mass after striking. Supposing that the blow be delivered fairly, without causing vibratory action, the work of resistance is equal to the work of impact. In the driving of a wedge, for instance, the product of the advance of the wedge by the resistance, cohesive and frictional, is equal to the work stored in the striking body. In the driving of a pile, similarly, the product of the frictional resistance by the advance of the pile under the blow of a ram is equal to the work stored in the ram. Of course, the stored work may to some extent be dissipated in vibratory action, leaving but a part of the stored work for useful performance.

**MILL GEARING, SHAFTING, &c.****Driving Belts.**

The ultimate tensile strength of leather belts of good quality, about  $\frac{1}{4}$  inch thick, is about 1,000 pounds per inch of width. That of ordinary belts is about 750 pounds per inch of width. At laced junctions of ends of belts, the ultimate tensile strength is only about 200 pounds per inch of width. Taking Briggs and Towne's data, and assuming one-third of 200 pounds, or 66 $\frac{2}{3}$  pounds per inch wide, as the maximum working stress, the Table 232 gives the driving power of leather belts.

**TABLE 232.—DRIVING POWER OF LEATHER BELTS,  
22 INCH THICK. (Clark's *Manual*.)**

Arcs of Contact.	Maximum Working Stress transmitted per Inch Wide.	Power transmitted per Inch Wide.			Sum of the Tensions on both Sides of a Belt per Inch Wide.	Resultant Pressure on the Journals per Inch Width of Belt.
		At One Foot per Second, Velocity of Belt.	Per Foot of Diameter of Pulley and per Turn per Minute.			
Degrees.	Pounds.	H. P.	H. P.	Ft.-lbs.	Pounds.	Pounds.
90	32.33	.059	.00308	102	101.00	71.42
100	34.80	.063	.00331	109	98.53	75.47
110	37.07	.067	.00353	116	96.26	78.85
120	39.18	.071	.00373	123	94.15	81.53
135	42.06	.076	.00400	132	91.27	84.32
150	44.64	.081	.00425	140	88.69	85.67
180	49.01	.089	.00467	154	84.32	84.32
210	52.52	.095	.00500	165	80.81	78.05
240	53.33	.100	.00527	174	78.00	67.59
270	57.58	.105	.00548	181	75.75	53.56

The Table 233 of the horse-power of belting is calculated for pulleys of nearly equal diameters, or which are well apart, allowing the belt to lap half round the smaller pulley.

Where the arc of contact is sensibly less than a semicircle, the tabular power transmitted is to be reduced in the same proportion.

The Table 233 is based on an allowance of 800 feet per minute travel of belting 1 inch width per horse-power; equivalent to about 41 lbs. tension per 1 inch width of belt.

TABLE 233.—DRIVING POWER OF LEATHER BELTS. (F. A. Halsey.)

Diameter of Pulley.	Revolutions of the Pulley per Minute.												Horse-Power Transmitted by each Inch Wide of Single Belt.											
	50	60	70	80	90	100	125	150	175	200	250	300	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.		
Inches.																								
12	.20	.24	.28	.32	.35	.39	.49	.59	.69	.79	.98	1.18	1.38	1.58	1.84	2.10	2.36	2.62	2.89	3.15	3.41	3.67	3.94	
14	.23	.28	.32	.37	.41	.46	.57	.69	.80	.92	1.14	1.31	1.48	1.64	1.81	2.00	2.29	2.58	2.87	3.15	3.43	3.72	4.00	
16	.26	.32	.37	.42	.47	.53	.66	.79	.92	1.05	1.31	1.48	1.64	1.81	2.00	2.29	2.58	2.87	3.15	3.43	3.72	4.00	4.29	
18	.30	.35	.41	.47	.53	.59	.74	.89	1.04	1.18	1.44	1.64	1.81	2.00	2.29	2.58	2.87	3.15	3.43	3.72	4.00	4.29	4.58	
20	.33	.39	.46	.52	.59	.65	.82	.98	1.14	1.31	1.58	1.81	2.00	2.29	2.58	2.87	3.15	3.43	3.72	4.00	4.29	4.58	4.87	
24	.39	.47	.55	.63	.71	.79	.98	1.18	1.38	1.58	1.97	2.29	2.62	2.96	3.30	3.63	3.97	4.30	4.63	4.97	5.30	5.63	5.97	
28	.46	.55	.64	.73	.83	.92	1.15	1.38	1.61	1.84	2.29	2.62	2.96	3.30	3.63	3.97	4.30	4.63	4.97	5.30	5.63	5.97	6.30	
32	.52	.63	.73	.84	.94	1.05	1.31	1.57	1.84	2.10	2.62	2.96	3.30	3.63	3.97	4.30	4.63	4.97	5.30	5.63	5.97	6.30	6.63	
36	.59	.71	.83	.95	1.06	1.18	1.48	1.77	2.06	2.36	2.96	3.30	3.63	3.97	4.30	4.63	4.97	5.30	5.63	5.97	6.30	6.63	6.97	
40	.65	.79	.92	1.04	1.18	1.31	1.64	1.96	2.29	2.62	3.29	3.63	3.97	4.30	4.63	4.97	5.30	5.63	5.97	6.30	6.63	6.97	7.30	
44	.72	.87	1.01	1.15	1.30	1.45	1.80	2.16	2.53	2.89	3.60	3.93	4.27	4.60	4.93	5.27	5.60	5.93	6.27	6.60	6.93	7.27	7.60	
48	.79	.94	1.10	1.26	1.42	1.57	1.96	2.36	2.75	3.15	3.93	4.27	4.60	4.93	5.27	5.60	5.93	6.27	6.60	6.93	7.27	7.60	7.93	
54	.89	1.06	1.24	1.42	1.59	1.77	2.22	2.66	3.10	3.55	4.43	4.72	5.00	5.28	5.56	5.84	6.12	6.40	6.68	6.96	7.24	7.52	7.80	
60	.98	1.18	1.38	1.57	1.77	1.96	2.46	2.95	3.44	3.93	4.91	5.20	5.49	5.78	6.07	6.36	6.65	6.94	7.23	7.52	7.81	8.10	8.39	
66	1.08	1.30	1.52	1.73	1.95	2.17	2.71	3.25	3.79	4.33	5.41	5.70	5.99	6.28	6.57	6.86	7.15	7.44	7.73	8.02	8.31	8.60	8.89	
72	1.18	1.42	1.65	1.89	2.13	2.36	2.95	3.54	4.13	4.72	5.90	6.19	6.48	6.77	7.06	7.35	7.64	7.93	8.22	8.51	8.80	9.09	9.38	
78	1.28	1.53	1.79	2.04	2.30	2.56	3.20	3.84	4.48	5.11	6.40	6.69	6.98	7.27	7.56	7.85	8.14	8.43	8.72	9.01	9.30	9.59	9.88	
84	1.38	1.65	1.93	2.21	2.48	2.75	3.44	4.13	4.81	5.51	6.89	7.18	7.47	7.76	8.05	8.34	8.63	8.92	9.21	9.50	9.79	10.08	10.37	
90	1.48	1.77	2.06	2.36	2.66	2.96	3.68	4.43	5.18	5.90	7.38	7.68	7.98	8.28	8.58	8.88	9.18	9.48	9.78	10.08	10.38	10.68	10.98	
96	1.57	1.89	2.21	2.53	2.84	3.15	3.95	4.73	5.51	6.31	7.89	8.20	8.51	8.82	9.13	9.44	9.75	10.06	10.37	10.68	10.99	11.30	11.61	



**Rules for Speed of Belt-Pulleys.**

To find the diameter of the driving pulley. Multiply the diameter of the driven pulley by the speed, or the number of revolutions it is to make per minute, and divide the product by the revolutions of the driving pulley per minute. The quotient is the diameter of the driver.

To find the diameter of the driven pulley. Multiply the diameter of the driving pulley by its speed, and divide the product by the speed of the driven pulley. The quotient is the diameter of the driven pulley.

To find the speed of the driven pulley. Multiply the diameter of the driving pulley by its speed; and divide the product by the diameter of the driven pulley. The quotient is the speed of the driven pulley.

**Weight of Belt-Pulleys (Clark's Manual).**

Pulleys of from 1 foot to 4 feet in diameter, turned and finished; Midland district:—

$$W = 7d - 1.75 \quad (1)$$

$W$  = weight of pulley in pounds per inch wide.

$d$  = diameter, in feet.

This formula is probably applicable for pulleys of from 10 inches to 10 feet in diameter.

Pulleys of from 1 foot to 7 feet in diameter, turned and finished; London district:—

$$\text{Not exceeding 2 feet in diameter } W = 3d^2 - .625d + 2.75 \quad (2)$$

$$2 \text{ feet and upwards } \quad \quad \quad W = 11.625d - 9.25 \quad (3)$$

**TABLE 234.—WEIGHT OF ROUND WROUGHT-IRON  
SHAFTING.**

Diameter of Shaft.	Weight per Lineal Foot	Diameter of Shaft.	Weight per Lineal Foot.	Diameter of Shaft.	Weight per Lineal Foot.	Diameter of Shaft.	Weight per Lineal Foot.
Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.
1	2.62	2 $\frac{3}{4}$	19.8	5 $\frac{1}{2}$	79.2	11	317
1 $\frac{1}{4}$	4.09	3	23.6	5 $\frac{3}{4}$	86.6	12	377
1 $\frac{1}{2}$	5.89	3 $\frac{1}{4}$	27.7	6	94.2	13	398
1 $\frac{3}{8}$	6.91	3 $\frac{1}{2}$	32.1	6 $\frac{1}{2}$	111	14	462
1 $\frac{3}{4}$	8.02	3 $\frac{3}{4}$	33.5	7	128	15	530
1 $\frac{7}{8}$	9.20	4	41.9	7 $\frac{1}{2}$	147	16	670
2	10.5	4 $\frac{1}{4}$	47.3	8	168	17	759
2 $\frac{1}{8}$	11.8	4 $\frac{1}{2}$	53.0	8 $\frac{1}{2}$	189	18	848
2 $\frac{1}{4}$	13.3	4 $\frac{3}{4}$	59.1	9	212	19	945
2 $\frac{3}{8}$	14.8	5	65.5	9 $\frac{1}{2}$	236	20	1040
2 $\frac{1}{2}$	16.4	5 $\frac{1}{4}$	72.2	10	262		

Note.—To find the weight of steel shafting, multiply the tabular values by 1.02.

TABLE 235.—HORSE-POWER OF SHAFTING.

Diameter of the Shaft.	Speed or Revolutions per Minute.										
	50	60	70	80	90	100	125	150	175	200	300
Horse-Power transmitted by the Shaft.											
Inches.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.	H. P.
1	.40	.48	.56	.64	.72	.80	1.00	1.20	1.40	1.60	H. P.
1 1/4	.78	.94	1.09	1.25	1.40	1.56	1.95	2.34	2.73	3.12	2.40
1 1/2	1.35	1.62	1.89	2.16	2.43	2.70	2.87	4.05	4.72	5.40	4.00
1 3/4	1.72	2.06	2.41	2.75	3.10	3.44	4.30	5.16	6.02	6.88	8.10
2	2.14	2.57	3.00	3.43	3.86	4.29	5.36	6.43	7.50	8.58	10.32
2 1/4	2.64	3.17	3.70	4.23	4.76	5.27	6.59	7.91	9.23	10.55	12.86
2 1/2	3.20	3.84	4.48	5.12	5.76	6.40	8.00	9.60	11.20	12.80	15.82
2 3/4	3.83	4.60	5.37	6.14	6.91	7.67	9.58	11.50	13.42	15.33	19.20
3	4.55	5.46	6.37	7.28	8.19	9.11	11.39	13.66	15.94	18.22	23.00
3 1/4	5.36	6.43	7.50	8.57	9.64	10.72	13.40	16.08	18.76	21.44	27.33
3 1/2	6.25	7.50	8.75	10.00	11.25	12.50	15.62	18.75	21.87	25.00	32.16
3 3/4	8.33	10.00	11.67	13.34	15.01	16.67	20.83	25.00	29.17	33.33	37.50
4	10.80	12.96	15.12	17.28	19.44	21.60	27.00	32.40	37.80	43.20	50.00
4 1/4	13.73	16.48	19.23	21.98	24.73	27.46	34.33	41.19	48.05	54.93	64.80
4 1/2	17.15	20.58	24.01	27.44	30.87	34.30	42.88	51.45	60.03	68.60	82.39
4 3/4	21.09	25.31	29.53	33.75	37.97	42.17	52.71	63.25	73.79	84.33	102.90
5	25.60	30.72	35.84	40.96	46.08	51.20	64.00	76.80	89.60	102.40	126.50
5 1/4	30.71	36.85	42.99	49.13	55.27	61.41	76.76	92.12	107.47	122.82	153.00
5 1/2	36.45	43.74	51.03	58.32	65.61	72.90	91.13	109.35	127.58	145.80	182.25
5 3/4	42.87	51.44	60.01	68.58	77.15	85.74	107.17	128.61	150.04	171.47	218.70
6	50.00	60.00	70.00	80.00	90.00	100.00	125.00	150.00	175.00	200.00	250.00
6 1/4	57.88	69.45	81.02	92.59	104.16	115.74	144.68	173.60	202.54	231.47	289.35
6 1/2	66.55	79.86	93.17	106.48	119.79	133.12	166.39	199.68	233.96	267.24	339.36
6 3/4	76.04	91.25	106.46	121.67	136.88	152.08	190.10	228.12	266.14	304.16	380.20
7	86.40	103.68	120.96	138.24	155.52	172.80	216.00	259.20	302.40	345.60	432.00

**Horse-Power of Shafting.**

The Table 235 is calculated by means of the formula :—

$$HP = \frac{d^3 \times t}{125} \quad . \quad . \quad . \quad . \quad (4)$$

HP = horse-power.

$d$  = diameter of shaft in inches.

$t$  = speed in turns per minute.

**Toothed Wheels.**

The Table 236 of the driving power of toothed wheels is based on the formula :—

$$HP = \frac{p \times f \times d \times t}{850} \quad . \quad . \quad . \quad . \quad (5)$$

HP = horse-power transmitted.

$p$  = pitch in inches.

$f$  = width of face of teeth, in inches.

$d$  = diameter of wheel, in inches.

$t$  = turns per minute.

By this formula a pressure of about 150 pounds is exerted on the teeth of a wheel of 1 inch pitch and 1 inch face ; with a proportionate stress on teeth of other pitches.

**Weight of Cast-Iron Spur-Wheels of from 1 inch to 6 inches Pitch** (Clark's *Manual*).

*Applicable for diameters up to 20 feet.*

$$W = (.05 + .08p)d \times (1 + .10d) \quad . \quad . \quad (6)$$

W = weight of wheel per inch of face, in cwts.

$d$  = diameter in feet.

$p$  = pitch in inches.

**Weight of Cast-Iron Spur-Wheels of Pitches less than 1 inch.**  
Pitch.

$$\left. \begin{array}{l} \frac{7}{8} \\ \frac{3}{4} \end{array} \right\} W = .0935d + .0235d^2 \quad . \quad . \quad . \quad (7)$$

$$\frac{1}{2} \left\{ W = .069d + .0345d^2 \quad . \quad . \quad . \quad (8)$$

$$\left. \begin{array}{l} \frac{1}{4} \\ \frac{3}{8} \end{array} \right\} W = .080d + .0530d^2 \quad . \quad . \quad . \quad (9)$$

*Mortise Wheels* are of the same weight as spur-wheels of equal diameter.

*Bevil Wheels* and *Mitre Wheels* weigh from two-thirds to three-fourths of spur-wheels for the larger diameters, to about seven-eighths for the smaller diameters.



TABLE 237.—TRANSMISSION OF POWER.  
(Harpers.)

Toothed Wheels (Double-flanged Wheel one-third more powerful).		Power that can be transmitted per 100 Feet of Circumferential Velocity per Minute.		Steel Shafting.		Single Belting.		One Rope.	
Breadth of Teeth.	Pitch of Teeth.	Spur.	Bevel.	Diameter.	Power that can be transmitted per 10 Revolutions per Minute.	Breadth.	Power that can be transmitted for every 100 Feet of Velocity per Minute.	Diameter.	Power that can be transmitted for every 100 Feet of Velocity per Minute.
Inches.	Inches.	H. P.	H. P.	Inches.	H. P.	Inches.	H. P.	Inches.	H. P.
2	1	$\frac{3}{8}$	$\frac{1}{4}$	$1\frac{1}{2}$	$\frac{1}{2}$	3	$\frac{3}{8}$	$\frac{3}{4}$	$\frac{1}{4}$
3	$1\frac{1}{4}$	$\frac{3}{4}$	$\frac{1}{2}$	2	$1\frac{1}{8}$	4	$\frac{1}{2}$	1	$\frac{1}{2}$
4	$1\frac{1}{2}$	$1\frac{1}{4}$	$\frac{3}{4}$	$2\frac{1}{2}$	2	5	$\frac{3}{4}$	$1\frac{1}{4}$	$\frac{3}{4}$
5	$1\frac{3}{4}$	2	$1\frac{1}{2}$	3	$2\frac{1}{4}$	6	$1\frac{1}{2}$	$1\frac{3}{4}$	$1\frac{1}{2}$
6	2	$3\frac{1}{4}$	$2\frac{3}{4}$	$3\frac{1}{2}$	$3\frac{1}{2}$	7	$1\frac{3}{4}$	$2\frac{1}{4}$	$1\frac{3}{4}$
7	$2\frac{1}{4}$	$4\frac{1}{4}$	$3\frac{1}{2}$	4	6	8	2	2	2
8	$2\frac{1}{2}$	$6\frac{1}{4}$	$4\frac{1}{2}$	$4\frac{1}{2}$	9	9	1	...	...
9	$2\frac{3}{4}$	$8\frac{1}{2}$	$5\frac{1}{2}$	5	13	10	$1\frac{1}{4}$	...	...
10	3	$11\frac{1}{4}$	$6\frac{1}{2}$	$5\frac{1}{2}$	18	12	$1\frac{1}{2}$	...	...
11	$3\frac{1}{4}$	$14\frac{1}{4}$	$8\frac{1}{2}$	6	24	15	$1\frac{3}{4}$	...	...
12	$3\frac{1}{2}$	19	11	...	31	18	$2\frac{1}{4}$	...	...
			14		...				

### Friction-Wheel Gearing.

The grooves of friction-wheels are of **V** shape, forming the angle 50 degrees; usually at  $\frac{3}{8}$ -inch pitch. Compared with leather belts, frictional gearing, worked under a pressure equal to the tension of the belts, has been proved to have greater adhesive force: 30 per cent. more, in one case.

### Transmission of Power (J. Bagshaw & Sons).

**BELTING.**—*To find the horse-power which can be transmitted by single leather belts.*—Multiply the breadth of belt in inches by 70, and by the speed of belt in feet per minute; and divide by 33,000. The quotient is the horse-power.

Double belts transmit  $1\frac{1}{2}$  times as much power as single belts.

*To find the width of single belt for transmitting a given horse-power.*—Multiply the horse-power by 33,000, and divide by 70 times the speed of the belt in feet per minute. The quotient is the width of belt in inches.

These rules are sufficiently approximate where there is no great degree of inequality in the diameters of the pulleys.

**SHAFTING.**—*To find the horse-power which can be transmitted by a wrought iron shaft.*—Multiply the cube of the diameter of the shaft in inches by the number of revolutions per minute, and divide by 80. The quotient is the horse-power.

*To find the diameter of a wrought iron shaft required to transmit a given horse-power.*—Multiply the horse-power by 80, and divide by the number of revolutions per minute. The cube root of the quotient is the diameter in inches.

**ROPES.**—*To find the horse-power that can be transmitted by ropes.*—Multiply the sectional area of one rope in square inches by 100 times the speed of the rope in feet per minute, and divide by 33,000. The quotient is the horse-power for one rope.

Or, multiply the sectional area of one rope by the speed, and divide by 330.

**TOOTHED WHEELS.**—*To find the horse-power that can be transmitted by toothed wheels.*—Multiply the velocity of the pitch-line in feet per second by the breadth of the teeth in inches, and by the square of the pitch in inches, and divide by 15. The quotient is the horse-power.

For bevel wheels, the mean diameter and mean pitch are to be taken.

**Change-Wheels for Screw-Cutting Lathes.**

(Richard Lloyd &amp; Co.)

14 Pitch.— $\frac{3}{16}$  inch full,  $\frac{9}{16}$  inch wide on face; suitable for 3-inch centre lathes. Number of teeth in each wheel, rising by one tooth from 15 to 75; thence, 77, 79, 80, 81, 82, 83, 84, 85, 87, 89, 90, 91, 92, 93, 94, 97, 99, 100, 101, 110, 120, 130, 140, 150, 180.

12 Pitch.— $\frac{1}{4}$  inch full,  $\frac{13}{16}$  inch wide on face; suitable for 4-inch or 5-inch centre lathes. Teeth, rising by one tooth, from 15 to 40; thence, 42, 44, 45, 46, 48, 50, 52, 54, 55, 56, 58, 60, 65, 70, 75, 80, 85, 90, 95, 96, 100, 105, 110, 115, 120, 130, 140, 150.

10 Pitch.— $\frac{5}{16}$  inch, 1 inch wide; suitable for 6-inch or 7-inch centre lathes. Teeth rising by one tooth, from 15 to 25; thence, 26, 28, 30, 32, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80, 85, 90, 95, 100, 105, 110, 115, 120, 130, 140, 150, 160.

8 Pitch.— $\frac{3}{8}$  inch,  $1\frac{1}{4}$  inch wide; suitable for 8-inch or 9-inch centre lathes. Teeth, rising by one tooth, from 15 to 20; thence, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 38, 40, 42, 44, 45, 46, 48, 50, 52, 54, 55, 56, 58, 60, 62, 63, 64, 65, 66, 68, 70, 72, 74, 75, 76, 78, 80, 85, 90, 95, 100, 105, 110, 115, 120, 130, 140, 150, 174, 200.

7 Pitch.— $\frac{7}{16}$  inch full,  $1\frac{1}{2}$  inch wide; suitable for 10-inch to 12-inch centre lathes. Teeth, 15, 16, 18, 20, 22, 24, 25, 26, 28, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80, 85, 88, 90, 95, 100, 105, 110, 115, 120, 130, 140, 150.

6 Pitch.— $\frac{1}{2}$  inch full,  $1\frac{1}{2}$  inch wide; suitable for 12-inch to 15-inch centre lathes. Teeth, 15, 16, 17, 18, 19, 20, 22, 23, 25, 26, 28, 30, 32, 34, 35, 36, 38, 40, 42, 44, 45, 46, 48, 50, 52, 55, 60, 65, 70, 72, 75, 80, 85, 90, 95, 100, 105, 110, 115, 120, 150.

**RULE I.**—The pitch is calculated on the Manchester principle. Divide the number of teeth in the wheel by the diameter of the pitch-line. The quotient is the pitch.

**RULE II.**—The diameter is equal to the quotient of the number of teeth divided by the pitch.

The relations of the several factors are combined in the equation:—

$$ABC = DEF,$$

in which A is the number of threads per inch to be cut; B, the number of teeth in the wheel on the mandril; C, the number of teeth in the stud pinion; D, the number of threads per inch on the lead screw; E, the number of teeth in the wheel on the lead screw; F, the number of teeth in the stud wheel.

TABLE 238.—PITCH-LINE DIAMETERS OF  
(Lister

Number of Teeth.	PITCH IN									
	$\frac{1}{4}$	$\frac{3}{8}$	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	$1\frac{1}{8}$	$1\frac{1}{4}$	$1\frac{1}{2}$
1	.08	.12	.1591	.1988	.2386	.2784	.3182	.3580	.3978	.4774
12	.95	1.43	1.91	2.38	2.86	3.34	3.82	4.28	4.77	5.73
13	1.05	1.55	2.07	2.58	3.10	3.62	4.14	4.64	5.17	6.21
14	1.11	1.67	2.23	2.78	3.34	3.90	4.46	4.99	5.57	6.68
15	1.19	1.79	2.39	2.98	3.58	4.18	4.77	5.35	5.97	7.16
16	1.29	1.91	2.55	3.18	3.82	4.48	5.09	5.70	6.37	7.64
17	1.35	2.03	2.70	3.38	4.06	4.73	5.41	6.06	6.77	8.12
18	1.43	2.15	2.86	3.58	4.30	5.01	5.73	6.42	7.17	8.60
19	1.51	2.27	3.02	3.78	4.54	5.29	6.05	6.78	7.56	9.08
20	1.59	2.38	3.18	3.98	4.77	5.57	6.36	7.13	7.96	9.55
21	1.67	2.50	3.34	4.18	5.05	5.85	6.68	7.49	8.36	10.02
22	1.75	2.64	3.50	4.38	5.25	6.12	7.00	7.85	8.76	10.50
23	1.85	2.74	3.66	4.58	5.49	6.40	7.32	8.25	9.16	10.98
24	1.91	2.86	3.82	4.77	5.73	6.68	7.64	8.56	9.55	11.46
25	1.98	2.98	3.97	4.98	5.97	6.96	7.96	8.29	9.06	11.94
30	2.38	3.58	4.77	5.96	7.16	8.35	9.55	10.70	11.93	14.32
35	2.78	4.17	5.57	6.96	8.35	9.75	11.14	12.73	14.27	15.91
40	3.18	4.97	6.36	7.95	9.54	11.14	12.73	14.27	15.91	19.10
45	3.58	5.37	7.16	8.91	10.74	12.53	14.32	16.05	17.90	21.40
50	3.98	5.96	7.96	9.94	11.93	13.92	15.91	17.83	19.89	23.87
55	4.37	6.56	8.75	10.94	13.12	15.32	17.50	19.62	21.88	26.26
60	4.77	7.16	9.55	11.93	14.32	16.71	19.09	21.40	23.87	28.64
65	5.17	7.75	10.34	12.93	15.51	18.10	20.68	23.19	25.86	31.03
70	5.57	8.35	11.14	13.92	16.70	19.49	22.27	24.97	27.85	33.42
75	5.96	8.94	11.93	14.92	17.89	20.89	23.86	26.75	29.84	35.81
80	6.36	9.54	12.73	15.91	19.09	22.28	25.46	28.54	31.82	38.19
85	6.76	10.14	13.52	16.90	20.28	23.67	27.05	30.32	33.81	40.58
90	7.16	10.73	14.32	17.90	21.47	25.06	28.64	32.19	35.80	42.97
95	7.55	11.34	15.11	18.89	22.68	26.45	30.23	33.89	37.79	45.36
100	7.95	11.93	15.91	19.89	23.86	27.85	31.82	35.67	39.78	47.74
110	8.75	13.12	17.50	21.88	26.24	30.63	35.00	39.24	43.76	52.51
120	9.54	14.31	19.09	23.87	28.63	33.42	38.18	42.81	47.74	55.70
130	10.34	15.51	20.68	25.86	31.02	36.20	41.36	46.37	51.72	62.06
140	11.13	16.75	22.27	27.85	33.40	38.99	44.54	49.94	55.70	66.84
150	11.93	17.89	23.86	29.83	35.79	41.77	47.73	53.51	59.67	71.61
160	12.72	19.09	25.45	31.87	38.18	44.56	50.91	57.08	63.65	75.38
170	13.52	20.28	27.04	33.81	40.56	47.34	54.10	60.64	67.63	81.16
180	14.32	21.47	28.64	35.80	42.95	50.13	57.28	64.21	71.60	85.93
190	15.11	22.66	30.23	37.79	45.33	52.91	60.46	67.78	75.58	90.71
200	15.91	23.86	31.82	39.78	47.72	55.70	63.64	71.35	79.56	95.48

DECIMAL  
EQUIVALENTS  $\left\{ \begin{array}{l} .03125 = \frac{1}{32} \\ .0625 = \frac{1}{16} \\ .125 = \frac{1}{8} \end{array} \right.$



TOOTHED WHEELS, CIRCULAR PITCH.  
& Co.)

INCHES.										Num ber of Teeth
1½	2	2½	2¾	2½	3	3½	3¾	4		
55.70	63.66	71.35	79.58	87.54	95.18	108.5	111.4	127.3		1
6.68	7.64	8.56	9.59	10.50	11.46	12.41	13.37	15.28		12
7.24	8.28	9.28	10.35	11.55	12.42	13.45	14.48	16.55		13
7.80	8.91	9.99	11.14	12.26	13.37	14.48	15.60	17.83		14
8.36	9.55	10.70	11.94	13.13	14.32	15.52	16.71	19.10		15
8.91	10.19	11.41	12.73	14.01	15.28	16.55	17.81	20.37		16
9.47	10.82	12.13	13.53	14.88	16.23	17.59	18.94	21.64		17
10.03	11.46	12.84	14.32	15.76	17.19	18.62	20.05	22.92		18
10.58	12.10	13.56	15.12	16.63	18.14	19.66	21.17	24.19		19
11.14	12.73	14.27	15.92	17.51	19.10	20.69	22.08	25.46		20
11.70	13.37	14.98	16.71	18.38	20.05	21.72	23.40	26.74		21
12.25	14.01	15.70	17.51	19.26	21.01	22.76	24.67	28.01		22
12.81	14.64	16.41	18.30	20.13	21.96	23.79	25.62	29.28		23
13.37	15.28	17.12	19.10	21.01	22.92	24.83	26.74	30.56		24
13.93	15.92	17.84	19.90	21.89	23.87	25.86	27.85	31.84		25
16.71	19.10	21.41	23.87	26.26	28.64	31.04	33.42	38.21		30
19.10	22.28	24.97	27.85	30.64	33.41	36.21	38.99	44.57		35
22.28	25.46	28.54	31.83	35.02	38.19	41.38	44.56	50.94		40
25.07	28.65	32.11	35.81	39.39	42.97	46.55	50.13	57.30		45
27.85	31.83	35.67	39.79	43.77	47.14	51.73	55.71	63.67		50
30.64	35.01	39.24	43.77	48.15	52.51	56.90	61.28	70.04		55
33.42	38.20	42.81	47.75	52.52	57.29	62.07	66.85	76.40		60
36.21	41.38	46.38	51.72	56.90	62.06	67.24	72.42	82.77		65
38.99	44.56	49.94	55.71	61.28	66.84	72.42	77.99	89.13		70
41.78	47.75	53.51	59.69	65.65	71.61	77.59	83.56	95.50		75
44.56	50.96	57.08	63.66	70.03	76.38	82.76	89.13	101.87		80
47.35	54.11	60.65	67.64	74.41	81.16	87.93	94.70	108.23		85
50.13	57.29	64.21	71.62	78.78	85.93	93.11	100.27	114.60		90
52.91	60.47	67.78	75.60	83.16	90.70	98.28	105.83	120.16		95
55.70	63.66	71.35	79.58	87.54	95.48	103.45	111.40	127.32		100
61.27	70.03	78.48	87.54	96.29	105.03	113.80	122.55	140.05		110
66.84	76.39	85.02	95.50	105.05	114.58	124.14	133.69	152.78		120
72.41	82.76	92.75	103.45	113.80	124.12	134.50	144.83	165.52		130
77.98	89.12	99.89	111.41	122.56	133.67	144.83	155.97	178.25		140
83.55	95.59	107.03	119.37	131.31	143.22	155.18	167.12	190.98		150
89.12	101.86	114.16	127.33	140.06	152.77	165.52	178.26	203.71		160
94.69	108.22	121.29	135.29	148.82	162.32	175.87	189.40	216.44		170
100.26	114.59	128.43	143.24	157.57	171.86	186.21	200.54	229.18		180
105.83	120.95	135.57	151.21	166.33	181.41	196.56	211.68	241.91		190
111.40	127.32	142.70	159.16	175.08	190.96	206.90	222.82	254.64		200

25	=	1	625	=	25
375	=	15	75	=	3
5	=	125	875	=	35

TABLE 239.—WHEELS FOR DIVIDING WHEEL WITH 180  
TEETH, SINGLE THREAD WORM.

(Lister &amp; Co.)

Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.	Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.	Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.	Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.
10	90	45	9	56	90	56	2	104	45	52	2	171	80	76	1
11	72	44	10	57	80	76	3	106	45	53	2	172	45	43	1
12	90	60	10	58	90	58	2	108	60	72	2	174	60	58	1
13	90	52	8	59	90	59	2	110	72	44	1	176	45	44	1
14	90	56	8	60	90	60	2	111	60	74	2	177	60	59	1
15	90	60	8	61	90	61	2	112	45	56	2	178	90	89	1
16	90	64	8	62	90	62	2	114	60	76	2	180	90	45	1
17	90	68	8	63	80	56	2	115	72	46	1	182	90	91	1
18	92	72	8	64	90	64	2	116	90	58	1	183	60	61	1
19	90	76	8	65	72	52	2	117	80	52	1	184	45	46	1
20	90	60	6	66	60	44	2	118	90	59	1	185	72	74	1
21	80	56	6	67	90	67	2	120	90	60	1	186	60	62	1
22	60	44	6	68	90	68	2	122	90	61	1	188	45	47	1
23	60	46	6	69	61	46	2	123	60	41	1	190	72	76	1
24	90	72	6	70	72	56	2	124	90	62	1	192	60	64	1
25	72	60	6	71	90	71	2	126	80	56	1	194	90	97	1
26	72	52	5	72	90	72	2	128	90	64	1	196	45	49	1
27	80	60	5	73	90	73	2	129	60	43	1	198	80	44	1
28	72	56	5	74	90	74	2	130	72	52	1	200	72	80	1
29	72	58	5	75	72	60	2	132	60	44	1	201	60	67	1
30	90	60	4	76	90	76	2	134	90	67	1	204	60	68	1
31	90	62	4	77	90	77	2	135	80	60	1	205	72	41	1
32	90	64	4	78	60	52	2	136	90	68	1	207	80	46	1
33	60	44	4	79	90	79	2	138	60	46	1	208	45	52	1
34	90	68	4	80	72	64	2	140	72	56	1	212	45	53	1
35	72	56	4	81	80	72	2	141	60	47	1	213	60	71	1
36	80	64	4	82	45	41	2	142	90	71	1	215	72	43	1
37	90	74	4	83	90	43	2	144	90	72	1	216	60	72	1
38	90	76	4	84	60	56	2	145	72	58	1	219	60	73	1
39	60	52	4	85	72	68	2	146	90	73	1	220	72	44	1
40	72	64	4	86	45	43	2	147	60	49	1	222	60	74	1
41	45	41	4	87	60	58	2	148	90	74	1	224	45	56	1
42	60	56	4	88	45	54	2	150	72	60	1	225	72	90	1
43	45	43	4	89	90	89	2	152	90	76	1	228	60	76	1
44	45	44	4	90	90	45	1	153	80	68	1	230	72	46	1
45	80	60	3	91	90	91	2	154	90	77	1	231	60	77	1
46	45	46	4	92	45	46	2	155	72	62	1	232	45	58	1
47	46	47	4	93	60	62	2	156	60	52	1	234	80	52	1
48	60	64	4	94	45	47	2	158	90	79	1	235	72	47	1
49	45	49	4	95	72	76	2	159	60	53	1	236	45	59	1
50	72	80	4	96	60	64	2	160	72	64	1	237	60	79	1
51	60	68	4	97	90	97	2	162	80	72	1	240	60	80	1
52	45	52	4	98	45	49	2	164	45	41	1	244	45	61	1
53	45	53	4	99	80	44	1	166	90	83	1	245	72	49	1
54	60	72	4	100	72	80	2	168	60	56	1	246	60	41	1
55	72	44	2	102	60	68	2	170	72	68	1	248	45	62	1

TABLE 239.—WHEELS FOR DIVIDING WHEEL WITH 180 TEETH, SINGLE THREAD WORM (*continued*).

Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.	Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.	Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.	Divisions Required.	Wheel on Worm Shaft.	Wheel on Handle Shaft.	Turns of Handle.
249	60	83	1	288	45	72	1	328	45	41	1	370	72	74	1
252	80	56	1	290	72	58	1	332	45	38	1	372	66	62	1
256	45	64	1	291	60	97	1	333	80	74	1	376	45	47	1
258	60	43	1	292	45	73	1	335	72	67	1	380	72	76	1
260	72	52	1	294	60	49	1	336	60	56	1	384	60	64	1
261	80	58	1	295	72	59	1	340	72	68	1	385	72	77	1
264	60	44	1	296	45	74	1	342	80	76	1	388	45	97	1
265	72	53	1	300	72	60	1	344	45	48	1	392	45	49	1
267	60	89	1	304	45	76	1	348	60	58	1	395	72	79	1
268	45	67	1	305	72	61	1	352	45	44	1	396	80	44	1
270	60	90	1	306	80	68	1	354	60	59	1	400	72	80	1
272	45	68	1	308	45	77	1	355	72	71	1	402	60	67	1
273	60	91	1	310	72	62	1	356	45	89	1	405	80	45	1
276	60	46	1	312	60	52	1	360	45	90	1	408	60	68	1
279	80	62	1	316	45	79	1	364	45	91	1	410	72	41	1
280	72	56	1	318	60	53	1	365	72	78	1	416	45	52	1
282	60	47	1	320	45	80	1	366	60	61	1	424	45	53	1
284	45	71	1	324	80	72	1	368	45	46	1	426	60	71	1

For a 90 Dividing Wheel, halve the turns or halve the handle shaft wheel, or double the worm shaft wheel.

For a 360 Dividing Wheel, double the turns or handle shaft wheel, or halve the worm shaft wheel.

This Table shows 256 different divisions cut by the use of 33 change wheels.

CHANGE WHEELS	41	43	44	45	46	47	49
	52	53	54	56	58	59	
	60	61	62	64	67	68	
	71	72	73	74	74	77	79
	80	83	89	90	91	92	97

TABLE 240.—CHANGE WHEELS, ETC., FOR DIVIDING WHEEL WITH 240 TEETH, SINGLE THREAD WORM.

(Lister &amp; Co.)

Number of Teeth.	Wheel on Worm Shaft.	Handle Shaft.	Turns.	Number of Teeth.	Wheel on Worm Shaft.	Handle Shaft.	Turns.	Number of Teeth.	Wheel on Worm Shaft.	Handle Shaft.	Turns.
A	B.	C	D	A	B	C	D	A	B	C	D
3	20	100	16	39	65	100	4	75	75	120	2
4	20	120	10	40	40	120	2	76	95	50	6
5	20	120	8	41	41	120	2	77	77	120	2
6	20	100	8	42	35	100	2	78	65	100	2
7	35	100	12	43	43	120	2	79	79	120	2
8	20	100	6	44	110	100	6	80	40	60	2
9	45	100	12	45	45	120	2	81	54	80	2
10	20	120	4	46	115	100	6	82	41	60	2
11	55	100	12	47	47	120	2	83	83	120	2
12	20	100	4	48	20	50	3	84	35	50	2
13	65	100	12	49	49	120	2	85	85	120	2
14	35	100	6	50	25	60	2	86	43	60	2
15	25	100	4	51	51	120	2	87	58	40	4
16	40	100	6	52	65	50	6	88	110	50	6
17	85	100	12	53	53	120	2	89	89	120	2
18	45	100	6	54	45	100	2	90	45	60	2
19	95	100	12	55	55	120	2	91	91	120	2
20	20	120	2	56	70	50	6	92	115	100	3
21	35	100	4	57	95	100	4	93	62	80	2
22	55	100	6	58	58	60	4	94	47	60	2
23	115	100	12	59	59	120	2	95	95	120	2
24	20	100	2	60	30	60	2	96	40	50	2
25	25	120	2	61	61	120	2	97	97	120	2
26	65	100	6	62	62	120	2	98	49	60	2
27	45	100	4	63	105	100	4	99	33	80	1
28	70	100	6	64	80	50	6	100	50	60	2
29	58	120	4	65	65	120	2	102	51	60	2
30	30	120	2	66	55	100	2	104	65	50	3
31	62	120	4	67	67	120	2	106	53	60	2
32	80	100	6	68	85	50	6	108	45	50	2
33	55	100	4	69	115	100	4	110	55	60	2
34	85	100	6	70	70	120	2	112	70	25	6
35	35	120	2	71	71	120	2	114	95	50	4
36	30	100	2	72	30	50	2	116	58	60	2
37	74	120	4	73	73	120	2	118	59	60	2
38	95	100	6	74	74	60	4	120	60	60	2

TABLE 240.—CHANGE WHEELS, ETC., FOR DIVIDING WHEEL WITH 240 TEETH, SINGLE THREAD WORM (*continued*).

Number of Teeth.	Wheel on Worm Shaft.	Handle Shaft.	Turns.	Number of Teeth.	Wheel on Worm Shaft.	Handle Shaft.	Turns.	Number of Teeth.	Wheel on Worm Shaft.	Handle Shaft.	Turns.
A	B	C	D	A	B	C	D	A	B	C	D
122	61	60	2	174	58	40	2	256	80	25	3
124	62	60	2	176	110	25	6	260	65	60	1
125	75	72	2	178	89	60	2	264	55	50	1
126	105	50	4	180	45	30	2	268	67	60	1
128	80	25	6	182	91	120	2	272	85	25	3
130	65	60	2	184	115	50	3	276	115	50	2
132	55	50	2	186	62	40	2	280	70	60	1
134	67	60	2	188	47	60	1	284	71	60	1
135	45	80	1	190	95	120	1	288	60	50	1
136	85	25	6	192	40	50	1	292	73	60	1
138	115	50	4	194	97	120	1	296	37	30	1
140	70	60	2	196	49	60	1	300	75	60	1
142	71	60	2	198	33	40	1	304	95	25	3
144	60	50	2	200	50	60	1	308	77	60	1
146	73	60	2	204	51	60	1	312	65	50	1
148	37	30	2	208	65	25	3	316	79	60	1
150	75	60	2	212	53	60	1	320	40	30	1
152	95	25	6	216	45	50	1	324	54	20	1
154	77	60	2	220	55	60	1	328	41	30	1
156	65	50	2	224	70	25	3	332	83	60	1
158	79	60	2	228	95	50	2	336	35	25	1
160	40	30	2	232	58	30	2	340	85	60	1
162	54	40	2	236	59	60	1	344	43	30	1
164	41	30	2	240	60	60	1	348	58	20	2
166	83	60	2	244	61	60	1	352	110	25	3
168	85	25	2	248	62	30	2	356	89	60	1
170	85	60	2	252	105	50	2	360	45	30	1
172	43	30	2								

For a 120 Dividing Wheel, halve either the number of turns or the handle shaft wheel, or double the worm shaft wheel.

Column A = number of divisions required.

" B = " change wheels on worm shaft.

" C = " " on handle shaft.

" D = " turns to handle shaft.

**MILLING.**

(Lister &amp; Co.)

**Use of Cutters.**

All cutters should be kept *sharp*. All cutters and arbors should run *true*. All arbors should be as *strong* as possible.

It is more satisfactory to run cutters up to *nearly* maximum speed, with a comparatively light feed, than to reduce the speed of the cutter and over feed the work; there being less stress upon the Machine, the Cutter, the Arbor, and the Work; and more accurate and better finished work being produced in the same time.

NOTE.—Care should be taken that in all cases the work should be fed *against* the cutter, in order to avoid the cutter dragging the work, and producing bad finish.

**Speed of Cutters.**

This varies considerably with the kind of material operated upon, the intelligent workman will be called upon to use his judgment in the matter. We give a few average speeds for ordinary material; these may in some instances require to be reduced, in others considerably increased; as the material may be found to demand or admit. Work of a frail character, or requiring small cutters or small arbors, will necessitate a comparatively *light feed*, at the same time maintaining a good cutter speed.

AVERAGE CUTTING SPEEDS, PERIPHERY SPEED OF CUTTER (IN FEET) PER MINUTE.

	Brass.	Wrought Iron.	Cast Iron.	Cast Steel.
Roughing . . . .	80	40	30	20
Finishing . . . .	100	60	40	25
Feed per min., inches	2½"	¾" to 2"	½" to 1½"	¼" to ½"

The *rate of feed* will vary from  $\frac{1}{16}$ " to  $\frac{3}{16}$ " per foot of cutter speed, according to the strength of the work or the cutter and arbor, also the finish required and the material operated on. Thus, taking a 4" dia. of cutter, and maintaining the average cutting speed of 41 feet per minute (say 40 revolutions of cutter), the rate of feed may require to vary from  $\frac{1}{4}$ " to  $2\frac{1}{4}$ " per minute, according to the various conditions of the work and also the breadth of cut; as a rule, the broader the cutter and the deeper the cut the slower should be the feed, although this to a great extent depends upon the power and stability of the machine.

**FEEDS IN RELATION TO DEPTH AND WIDTH OF CUT IN  
ORDINARY CAST IRON, GIVING REVOLUTIONS OF CUTTER  
FOR ONE INCH OF FEED.**

Diameter of Cutters	2"		3"		4"		6"	
Width of Cut . . .	$\frac{1}{2}$ "	2"	$\frac{1}{2}$ "	2"	$\frac{1}{2}$ "	2"	$\frac{1}{2}$ "	2"
Revolutions, rough- ing $\frac{1}{8}$ " to $\frac{1}{4}$ " deep }	45	40	30	25	25	22	15	12
Finishing, $\frac{1}{16}$ " deep .	35	30	22	20	18	15	10	9

This will average for roughing  $\frac{1}{20}$ " feed of work to each 12" of cutter circumf. For finishing,  $\frac{1}{16}$ " or each 4" of cutter dia.

For broader cuts and harder material the number of revolutions per inch of feed will be increased.

### Cutters.

These should be made of high-class steel; some of the Sheffield houses will now undertake to harden any cutters made from their steel free of charge, and taking the risk.

The average pitch of teeth should be from  $\frac{1}{4}$ " to  $\frac{3}{8}$ "; for ordinary cutters they should be radial on the face, that is, they should have little, if any, undercut. Cutters over 1" wide should be cut *spiral*, the spiral being about 20" pitch. Cutters from 3" to 5" dia. are best size for ordinary work.

For rapid wrought-iron milling it is advisable to direct a stream of oil or soap water on to the cutter by means of overhead sud tank or a pump.

### Milling Cutters compared with Shapers, Planes, &c.

Metal may be cut away by Milling Cutters at from 4 to 10 times the speed at which it can be cut by any ordinary tool such as a shaper, plane, &c., and in reciprocating machines the tool is only actually *cutting* during half the time, the period of reversing and return stroke being totally lost; again, the Milling Cutter will preserve its sharpness infinitely longer than single point tools. It has been proved in practice that Milling has an advantage over the Shaping Machine of at least 2 to 1 in plain work, up to 20 to 1 in duplicate and intricate work in point of time, and also in accuracy and finish.

### No. 2 Milling Machine.

The countershaft is provided with two loose pulleys 18' diameter to be driven from the main shaft by two belts, one belt driving the fast pulley 80 and the other 120 revolutions per minute, so that by moving the belt from the lower to the

higher speed, a suitable increase is made from roughing to finishing without altering the belt in the cones.

TABLE OF SPEEDS.

Step of Cone.	Revolutions per Minute.	Suitable for Cutters.	Speed of Countershaft.
No. 1 (large)	18 20 28	9 to 10 dia. 7 to 8 " 5 to 6 "	80 123 80
No. 2	42 56	3 to 4 " 2 to 2½ "	120 80
No. 3	84 120	1½ to 1¾ " 1 " ¾ "	123 80 120
No. 4 (small)	180		

NOTE.—These speeds are *below* the *maximum*.

The speed of *High-speed* spindle through support arm ranges from 78 to 1,080 or to 4,000 revolutions per minute when driven direct without the long pulley.

**SPIRALS.**—A few general and useful pitches are given below. To gear for any other spiral, the following calculations will give the gears:—

The dividing wheel has 90 teeth; each turn of the hollow shaft in the knee moves the table  $\frac{1}{4}$ ", so that 90 turns with equal gears will give a complete revolution to the dividing arbor, and a movement to the table of  $22\frac{1}{4}$ "; this may be termed the natural pitch.

To obtain other pitches—*e.g.*, say we require a 10" pitch spiral, that is a complete revolution in 10" of length—multiply the pitch required by 4 to obtain the total turns of hollow shaft, the result divided by 90 gives the gear ratio, thus:—

$$\frac{10'' \times 4}{90} = \frac{40}{90} \text{ on the spiral head}$$

$$\frac{15'' \times 4}{90} = \frac{60}{90} \text{ on the spiral head}$$

Required 15" pitch. }  $\frac{15 \times 4}{90} = \frac{60}{90}$  on the sliding shaft; and so on.

USEFUL PITCHES.

Angle of Cutter Spindle.	Pitch. Inches.	Wheel on Spiral Head.	Wheel on Sliding Shaft.	Suitable for
20°30'	3.75	20	120	$\frac{1}{4}$ " Twist Drill
20°12'	5	20	90	" " "
20°0'	6.25	25	90	" " "
19°50'	7.5	30	90	" " "
19°20'	8.75	35	90	1" " "
20°0'	10.0	40	90	1½" " "
	22.5	60	60	Spiral Cutters.



## TRANSMISSION OF MOTIVE POWER TO GREAT DISTANCES.

### Transmission by Hemp Ropes.

For the driving gear of large steam engines, hemp ropes are much employed to take off the power from the circumference of the fly-wheel, which is grooved. The tension on the ropes is usually about 100lb. per square inch of section. The usual speed is from 4,500 to 5,500 feet per minute.

TABLE 241.—HORSE-POWER BY MANILLA ROPES.  
(Leavitt.)

Speed of Rope, in Feet per Minute.	1000	1500	2000	2500	3000	3500	4000	4500	5000
Diameter of Rope.	Horse Power.								
Inches.									
$\frac{3}{4}$	13 $\frac{1}{2}$	23 $\frac{3}{4}$	34 $\frac{1}{2}$	44 $\frac{1}{2}$	54 $\frac{1}{2}$	64 $\frac{1}{2}$	7	84 $\frac{1}{2}$	9
1	34 $\frac{1}{2}$	47 $\frac{1}{2}$	61 $\frac{1}{2}$	8	10	11	13	15	16
1 $\frac{1}{4}$	54 $\frac{1}{2}$	74 $\frac{1}{2}$	104 $\frac{1}{2}$	13	15	18	20	23	26
1 $\frac{1}{2}$	74 $\frac{1}{2}$	11	15	18	22	26	30	34	37
1 $\frac{3}{4}$	10	15	20	25	30	35	40	45	50
2	13	19 $\frac{1}{2}$	26	33	39	46	52	59	65

### Transmission of Motive Power by Wire-Rope.

In one case, power was transmitted from a water-wheel through a horizontal distance of 400 feet by means of an iron wire-rope  $\frac{1}{4}$  inch in diameter, which passed over two grooved cast-iron pulleys 6.56 feet in diameter, lined in the groove with compressed and tarred leather. The rope was formed of a central ply of Bologna hemp, tarred, around which were twisted six strands, each of eight iron wires,  $\frac{1}{32}$  inch thick, on a core of tarred hemp. The speed was brought up by toothed gearing in two stages, so that the motor pulley made 19.04 turns for one of the water-wheel. For a speed of 96 turns per minute of the first intermediate shaft, the motor-pulley makes 145.85 turns, and the speed of its periphery is 50 feet per second, or 3000 feet per minute. At this speed, the loss by frictional resistance of the gearing and rope was 6.82 per cent.

### Transmission of Motive Power by Compressed Air.

The Paris Compressed Air Company supply air compressed by steam power, of 5 atmospheres pressure, to secondary engines of two types :—rotary engines for powers up to about

1 horse-power; and larger sized motors, up to double-cylinder engines having 12-inch cylinders with 14-inch stroke,—ordinary steam-engines employed for air. The secondary motor, when indicating 9.9 horse-power, and making 125 revolutions, according to Professor Kennedy, uses 890 cubic feet of air per indicator horse-power per hour. A small motor four miles distant from the central station, can indicate, in round numbers, 10 horse-power for 20 horse-power at the station, allowing for the value of the coke used in heating the air, or for 25 horse-power, if the air be not heated at all: making in the second instance an efficiency of 40 per cent.

### **Transmission of Domestic Motive Power by Atmospheric Exhaustion.**

The distribution of power in dwelling-houses in Paris is effected by means of the exhaustion of air from a system of pipes, laid in the sewers for the most part, from which the power is supplied in small quantities to work the tools or machines employed in small industries. A vacuum, averaging 67 per cent. or 20 inches of mercury,—occasionally reaching to 75 per cent. or 22½ inches—is maintained in a reservoir, 49 inches in diameter, 11½ feet in length, serving to regulate the pressure in the service pipes. These are 10 inches and 8 inches in diameter, from the pumping station to the sewer, and 8 inches and 4 inches in the sewer or trench. The conduits do not exceed from 1 mile to 1½ miles in length. The secondary motors are of the trunk type: supplying powers of from  $\frac{1}{25}$ th to 1 horse-power.

The air-cylinder utilises 93 per cent. of the engine-power transmitted. Of this the exhaust motors utilise a maximum of 60 per cent.; the loss of head in the main is 5 per cent.; lastly, the air yields only 85 per cent. of its total capacity for work. The resulting coefficient is 45 per cent.; and the actual work of 1 cubic foot of air is 1246 foot-pounds.

### **Transmission of Motive Power by Electricity.**

This is easily effected, where the power does not exceed 30 horse-power, nor the distance 1½ miles. In experiments by M. Fontaine, the dynamos made 1,200 revolutions per minute. The power delivered at the periphery of the fly-wheel of the steam engine was 95 horse-power; at the break, 50 horse-power; resistance of intermediate conductors ( $\frac{1}{4}$  inch copper wire, 77½ miles long), 100 ohms; 6,700 volts at origin of conducting line; intensity of current, 8 ampères; ultimate efficiency, 52.52 per cent.

In an experiment at the Munich Exhibition, in 1882, the generator was at Miesbach, and the electro-motor in the Exhibition palace, 35½ miles apart. The conductor was a

double line of iron telegraph wire,  $4\frac{1}{2}$  millimetres in diameter. The machines used were two similar Gramme dynamos, series wound. The resistance of each was 470 ohms, and that of the line 950 ohms, making the total resistance of circuit,  $(950 + (470 \times 2)) = 1890$  ohms.

Generator, 1611 revolutions per minute; electromotive force = 1343 volts; current intensity = 519 ampère.

Motor, 752 revolutions per minute; counter electromotive force = 850 volts.

$$\text{Theoretical efficiency} = \frac{850}{1343} = .63.$$

The power received at Munich was  $\frac{1}{2}$  horse-power; and the economical efficiency was about 25 per cent.

TABLE 242.—RESULTS OF TRIALS.

	First Trial.		Second Trial.	
	Generator.	Receiver.	Generator.	Receiver.
Speed in revolutions per minute . . .	190	248	120	277
Electromotive force (direct or inverse). Volts	5469	4242	5717	4441
Current . . . Ampères	7.21	7.21	7.20	7.20
Work in magnetic field . . . H. P.	9.20	3.75	10.30	3.80
Electrical work in armature . . . H. P.	53.59	41.44	55.90	43.40
Mechanical work measured in transmission dynamometer and at Prony break, H. P.	62.10	35.80	61.00	40.00
Efficiency.				
	First Trial.		Second Trial.	
	Per Cent.		Per Cent.	
Electric . . . . .	77.0		78.0	
Mechanical (commercial) . . . . .	47.7		53.4	

See also *Hydraulic Transmission of Motive Power*, post, p. 603

## HEAT.

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The British unit of heat, or thermal unit, is that which can raise the temperature of one pound of water 1 degree Fahrenheit, at or near  $39^{\circ}\cdot 1$  F., the temperature of maximum density of water.

The French thermal unit, or *calorie*, is that which can raise the temperature of one kilogramme of water, 1 degree centigrade, at or about  $4^{\circ}$  C. ( $=39^{\circ}\cdot 1$  F.).

1 calorie, or French unit of heat, is equal to 3·568 British heat-units.

1 British heat-unit is equal to ·252 calorie.

The mechanical equivalent of one British heat-unit (Joule's equivalent) is 772 foot-pounds, or 10·67 kilogrammetres.

The mechanical equivalent of one French heat-unit is 425 kilogrammetres, or 3074 foot-pounds. If calculated in terms of Joule's equivalent, the value would be 423·55 kilogrammetres, or 3063·5 foot-pounds.

1 calorie per square metre is equal to ·369 heat-unit per square foot.

1 heat-unit per square foot is equal to 2·713 calories per square metre.

1 calorie per kilogramme is equal to 1·800 heat-units per pound.

1 heat-unit per pound is equal to ·556 calorie per kilogramme.

### Thermometers.

	Freezing Point.	Boiling Point.
Fahrenheit thermometer	$32^{\circ}$	$212^{\circ}$
Centigrade            "	$0^{\circ}$	$100^{\circ}$
Réaumur               "	$0^{\circ}$	$80^{\circ}$

1 degree Fahr.  $=\frac{5}{9}$  Centigr. degree ; or  $\frac{4}{9}$  Réaumur degree.

1 degree Centigr.  $=\frac{9}{5}$  Fahr. degree ; or  $\frac{9}{4}$  Réaumur degree.

1 degree Réaumur  $=\frac{9}{4}$  Fahr. degree ; or  $\frac{5}{4}$  Centigr. degree.

Representing the thermometric scales by their initials.

Equivalent temperature by the }  
Centigrade scale }  $C. = \frac{5}{9} (F. - 32) = \frac{4}{9} R.$

do. by the Réaumur scale  $R. = \frac{4}{9} (F. - 32) = \frac{4}{9} C.$

do. by the Fahrenheit scale  $F. = \frac{9}{5} C. + 32 = \frac{9}{4} R. + 32.$

TABLE 243. —THERMOMETERS : FAHRENHEIT AND CENTI-  
GRADE SCALES.

Fahr.	Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.	Centigr.
°	°	°	°	°	°	°	°
15	—9·45	69	20·56	110	43·34	151	66·11
20	—6·67	70	21·11	111	43·90	152	66·67
25	—3·90	71	21·67	112	44·45	153	67·23
30	—1·11	72	22·23	113	45·00	154	67·78
32	0·00	73	22·78	114	45·56	155	68·34
33	+0·56	74	23·34	115	46·11	156	68·90
34	1·11	75	23·90	116	46·67	157	69·45
35	1·67	76	24·45	117	47·23	158	70·00
36	2·23	77	25·00	118	47·78	159	70·56
37	2·78	78	25·56	119	48·34	160	71·11
38	3·34	79	26·12	120	48·90	161	71·67
39	3·90	80	26·67	121	49·45	162	72·23
40	4·45	81	27·23	122	50·00	163	72·78
41	5·00	82	27·78	123	50·56	164	73·34
42	5·56	83	28·34	124	51·11	165	73·90
43	6·11	84	28·89	125	51·67	166	74·45
44	6·67	85	29·45	126	52·23	167	75·00
45	7·23	86	30·00	127	52·78	168	75·56
46	7·78	87	30·55	128	53·34	169	76·11
47	8·34	88	31·11	129	53·90	170	76·67
48	8·89	89	31·67	130	54·45	171	77·23
49	9·45	90	32·22	131	55·00	172	77·78
50	10·00	91	32·78	132	55·56	173	78·34
51	10·56	92	33·33	133	56·11	174	78·90
52	11·11	93	33·89	134	56·67	175	79·45
53	11·67	94	34·45	135	57·23	176	80·00
54	12·23	95	35·00	136	57·78	177	80·56
55	12·78	96	35·56	137	58·34	178	81·11
56	13·34	97	36·11	138	58·90	179	81·67
57	13·90	98	36·67	139	59·45	180	82·23
58	14·45	99	37·23	140	60·00	181	82·78
59	15·00	100	37·78	141	60·56	182	83·34
60	15·56	101	38·34	142	61·11	183	83·90
61	16·11	102	38·90	143	61·67	184	84·45
62	16·67	103	39·45	144	62·23	185	85·00
63	17·23	104	40·00	145	62·78	186	85·56
64	17·78	105	40·56	146	63·34	187	86·11
65	18·34	106	41·11	147	63·90	188	86·67
66	18·89	107	41·67	148	64·45	189	87·23
67	19·45	108	42·23	149	65·00	190	87·78
68	20·00	109	42·78	150	65·56	191	88·34

TABLE 243.—THERMOMETERS (*continued*).

Fahr.	Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.	Centigr.
°	°	°	°	°	°	°	°
192	88.90	222	105.56	310	154.45	460	237.78
193	89.45	223	106.11	315	157.23	465	240.56
194	90.00	224	106.67	320	160.00	470	243.34
195	90.56	225	107.23	325	162.78	475	246.11
196	91.11	226	107.78	330	165.56	480	248.90
197	91.67	227	108.83	335	168.34	485	251.67
198	92.23	228	108.90	340	171.11	490	254.45
199	92.78	229	109.45	345	173.90	495	257.23
200	93.34	230	110.00	350	176.67	500	260.00
201	93.90	232	111.11	355	179.45	505	262.78
202	94.45	234	112.23	360	182.23	510	265.56
203	95.00	236	113.34	365	185.00	515	268.34
204	95.56	238	114.45	370	187.78	520	271.11
205	96.11	240	115.56	375	190.56	525	273.90
206	96.27	242	116.67	380	193.34	530	276.67
207	97.23	244	117.78	385	196.11	535	279.45
208	97.78	246	118.90	390	198.90	540	282.23
209	98.34	248	120.00	395	201.67	545	285.00
210	98.90	250	121.11	400	204.45	550	287.78
211	99.45	255	123.90	405	207.23	555	290.56
212	100.00	260	126.67	410	210.00	560	293.34
213	100.56	265	129.45	415	212.78	565	296.11
214	101.11	270	132.23	420	215.56	570	298.90
215	101.67	275	135.00	425	218.34	575	301.67
216	102.23	280	137.78	430	221.11	580	304.45
217	102.78	285	140.56	435	223.90	585	307.23
218	103.34	290	143.34	440	226.67	590	310.00
219	103.90	295	146.11	445	229.45	595	312.78
220	104.45	300	148.90	450	232.23	600	315.56
221	105.00	305	151.67	455	235.00		

TABLE 244.—THERMOMETERS : CENTIGRADE AND FAHRENHEIT SCALES.

Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.
°	°	°	°	°	°	°	°
-10	14.0	3	37.4	8	46.4	13	55.4
-5	23.0	4	39.2	9	48.2	14	57.2
0	32.0	5	41.0	10	50.0	15	59.0
+1	33.8	6	42.8	11	51.8	16	60.8
2	35.6	7	44.6	12	53.6	17	62.6

TABLE 244.—THERMOMETERS (*continued*).

Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.
°	°	°	°	°	°	°	°
18	64·4	60	140·0	102	215·6	158	316·4
19	66·2	61	141·8	103	217·4	160	320·0
20	68·0	62	143·6	104	219·2	162	323·6
21	69·8	63	145·4	105	221·0	164	327·2
22	71·6	64	147·2	106	222·8	166	330·8
23	73·4	65	149·0	107	224·6	168	334·4
24	75·2	66	150·8	108	226·4	170	338·0
25	77·0	67	152·6	109	228·2	172	341·6
26	78·8	68	154·4	110	230·0	174	345·2
27	80·6	69	156·2	111	231·8	176	348·8
28	82·4	70	158·0	112	233·6	178	352·4
29	84·2	71	159·8	113	235·4	180	356·0
30	86·0	72	161·6	114	237·2	182	359·6
31	87·8	73	163·4	115	239·0	184	363·2
32	89·6	74	165·2	116	240·8	186	366·8
33	91·4	75	167·0	117	242·6	188	370·4
34	93·2	76	168·8	118	244·4	190	374·0
35	95·0	77	170·6	119	246·2	192	377·6
36	96·8	78	172·4	120	248·0	194	381·2
37	98·6	79	174·2	121	249·8	196	384·8
38	100·4	80	176·0	122	251·6	198	388·4
39	102·2	81	177·8	123	253·4	200	392·0
40	104·0	82	179·6	124	255·2	202	395·6
41	105·8	83	181·4	125	257·0	204	399·2
42	107·6	84	183·2	126	258·8	206	402·8
43	109·4	85	185·0	127	260·6	208	406·4
44	111·2	86	186·8	128	262·4	210	410·0
45	113·0	87	188·6	129	264·2	212	413·6
46	114·8	88	190·4	130	266·0	214	417·2
47	116·6	89	192·2	132	269·6	216	420·8
48	118·4	90	194·0	134	273·2	218	424·4
49	120·2	91	195·8	136	276·8	220	428·0
50	122·0	92	197·6	138	280·4	222	431·6
51	123·8	93	199·4	140	284·0	224	435·2
52	125·6	94	201·2	142	287·6	226	438·8
53	127·4	95	203·0	144	291·2	228	442·4
54	129·2	96	204·8	146	294·8	230	446·0
55	131·0	97	206·6	148	298·4	232	449·6
56	132·8	98	208·4	150	302·0	234	453·2
57	134·6	99	210·2	152	305·6	236	456·8
58	136·4	100	212·0	154	309·2	238	460·4
59	138·2	101	213·8	156	312·8	240	464·0

TABLE 244.—THERMOMETERS (*continued*).

Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.	Centigr.	Fahr.
°	°	°	°	°	°	°	°
242	467·6	262	503·6	282	539·6	302	575·6
244	471·2	264	507·2	284	543·2	304	579·2
246	474·8	266	510·8	286	546·8	306	582·8
248	478·4	268	514·4	288	550·4	308	586·4
250	482·0	270	518·0	290	554·0	310	590·0
252	485·6	272	521·6	292	557·6	312	593·6
254	489·2	274	525·2	294	561·2	314	597·2
256	492·8	276	528·8	296	564·8	316	600·8
258	496·4	278	532·4	298	568·4	318	604·4
260	500·0	280	536·0	300	572·0	320	608·0

TABLE 245.—HIGH TEMPERATURES AND CORRESPONDING LUMINOSITY. (Pouillet.)

## I. TEMPERATURE OF A FIRE.

	Centigrade.	Fahrenheit.
Nascent red . . . . .	525	977
Dark red . . . . .	700	1292
Nascent cherry red . . . . .	800	1472
Cherry red . . . . .	900	1652
Bright cherry red . . . . .	1000	1832
Very deep orange . . . . .	1100	2012
Bright orange . . . . .	1200	2192
White . . . . .	1300	2372
Dazzling white . . . . .	1500	2732

## II. TEMPERATURE BY FUSION OF METALS, &amp;c.

Substance.	Temperature.	Metal.	Temperature.	Metal.	Temperature.
	Fahr.		Fahr.		Fahr.
	°		°		°
Tallow . . . . .	92	Bismuth . . . . .	518	Silver, pure . . . . .	1880
Spermaceti . . . . .	120	Lead . . . . .	630	Gold coin . . . . .	2156
Wax, white . . . . .	154	Zinc . . . . .	793	Iron, cast, ( . . . . .	2010
Sulphur . . . . .	239	Antimony . . . . .	820	med. )	
Tin . . . . .	455	Brass . . . . .	1650	Steel . . . . .	2550
				Wrought ( . . . . .	2910
				iron )	



**Radiation of Heat.**

The heat radiated from incandescent coal or coke is expressed by the formula :—

$$R = 144 a^{\theta} (a^t - 1) \quad (1)$$

$R$  = quantity of heat radiated per square foot of surface per hour, in British units.

$\theta$  = temperature of the enclosure, in Fahrenheit degrees.

$t$  = excess temperature of surface of hot body above the temperature of the enclosure,  $\theta$ , in Fahrenheit degrees.

$a$  = constant, 1.00425.

According to the formula, the rate of radiation increases in a much more rapid ratio than the excess temperature, when the temperature of the enclosure is constant.

The heat radiated from a coal or a coke fire, is estimated to be about one-half of the whole heat generated. It increases almost as fast as the rate of combustion of the fuel per hour per square foot.

**Convection of Heat, from an External Surface (Hopkins).**

Surrounding Medium.

Air . . .  $C = .2849t^{1.233}$  . . . . . (2)

Hydrogen . . .  $C = .9827t^{1.233}$  . . . . . (3)

Carbonic acid: . .  $C = .2759t^{1.233}$  . . . . . (4)

Olefiant gas . .  $C = .3817t^{1.233}$  . . . . . (5)

$C$  = quantity of heat, in English units, conveyed away from a solid body by a gas external to it, per square foot of surface per hour, under one atmosphere of pressure.

$t$  = excess temperature of surface in Fahrenheit degrees.

**TABLE 246.—COMPARATIVE CONDUCTING POWER OF SOLIDS.**

Substance.	Comparative Power.	Substance.	Comparative Power.
	Gold = 1000.		Gold = 1000.
Brass . . . . .	749	Platinum . . . . .	981
Copper . . . . .	892	Porcelain . . . . .	12
Gold . . . . .	1000	Silver . . . . .	973
Iron, cast . . . . .	562	Terra Cotta . . . . .	11
„ wrought . . . . .	374	Tin . . . . .	304
Lead . . . . .	180	Zinc . . . . .	363
Marble . . . . .	24		

TABLE 247.—COMPARATIVE ABSORBING OR RADIATING AND REFLECTING PROPERTIES OF SOLIDS.

Substance.	Absorbing or Radiating Power.	Reflecting Power.
	Proportion per Cent.	Proportion per Cent.
Brass, bright polished . . .	7	93
„ dead polished . . .	11	89
Copper . . . . .	7	93
Glass . . . . .	90	10
Gold . . . . .	5	95
Ice . . . . .	85	15
Iron, cast, polished . . .	25	75
„ wrought, polished . . .	23	77
Marble . . . . .	93 to 98	7 to 2
Mercury . . . . .	23	77
Platinum, polished . . .	24	76
„ sheet . . . . .	17	83
Silverleaf on glass . . .	27	73
Silver, polished . . . . .	3	97
Steel, polished . . . . .	17	83
Tin . . . . .	15	85
Water . . . . .	100	0
Writing paper . . . . .	98	2
Zinc, polished . . . . .	19	81

**Condensation of Steam in Bare Pipes exposed to Air.**

Tredgold found that steam of  $17\frac{1}{2}$  lbs. absolute pressure per square was condensed in cast-iron pipes in a room at  $60^{\circ}$  F., at the rate of .352 pound per square foot of exposed surface per hour; or .0022 pound per degree of difference of temperature.

The following results were found by M. Clément. It is here assumed that the steam was of 20 lbs. absolute pressure per square inch. The pipes were exposed in a room at  $77^{\circ}$  F.

Bare Surface.		Steam Condensed per Square Foot per Hour.
Cast-iron pipe, horizontal	.	.328 lb.
Blackened „ „	.	.308 „
Copper „ „	.	.267 „
Blackened „ „	.	.308 „
„ „ upright	.	.359 „

M. Burnat found that for steam of 22 lbs. absolute pressure, with 196°·6 F. difference of temperature, 581 lb. was condensed per square foot of a cast-iron pipe, nearly horizontal, per hour.

Dr. William Anderson experimented with a tubular steam heater, of 2-inch wrought-iron tubes, in a temperature of 59° F., with steam of 51 lbs. total pressure per square inch 785 lb. was condensed per square foot per hour.

The foregoing results are collected in the following tablet :—

Observer.	Temperature of surrounding Air.	Difference of Temperature.	Steam consumed per Square Foot per Hour.		Heat emitted per 1° F. difference of Temperature.
			Total.	Per 1° F.	
	° Fahr.	° Fahr.	Pound.	Pound.	Units.
Clement .	77	151	328	00217	2·07
Tredgold. .	60	161	352	0022	2·10
Burnat .	36·5	196·6	581	0030	2·81
Anderson .	59	223	785	0035	3·22

From these data, the following approximate formulæ are deduced :—

*Condensation of steam in cast-iron pipes, in air, per square foot of surface per hour at ordinary temperatures :—*

$$s = \frac{t^2}{55000} - 12 \quad . \quad . \quad . \quad (6)$$

*Heat emitted from cast-iron pipes, in air, per square foot of surface per hour, at ordinary temperatures :—*

$$h = \frac{t^2}{58} - 114 \quad . \quad . \quad . \quad (7)$$

*Heat emitted from cast-iron pipes, in air, per square foot of surface per degree of difference of temperature of steam and air, per hour, at ordinary temperatures.*

$$h' = \frac{t}{58} - \frac{114}{t} \quad . \quad . \quad . \quad (8)$$

$s$  = quantity of steam condensed in pounds.

$h$  = quantity of heat emitted in units.

$h'$  = quantity of heat emitted, per degree of difference of temperature.

$t$  = difference of temperature, in Fahrenheit degrees.

The latent heat of steam of 22 lbs. total pressure per square inch, 950 units per pound, is employed as the heat-factor, as an average value.

The Table 248 has been calculated by means of these formulas.

**TABLE 248.—STEAM CONDENSED IN BARE CAST-IRON PIPES IN AIR, AND HEAT EMITTED, AT ORDINARY TEMPERATURES.**

Steam.		Difference or Excess of Temperature of Steam above 62° Fahr.	Steam Condensed per Square Foot per Hour.		Heat Emitted per Square Foot per Hour.	
Total Pressure per Square Inch.	Temperature.		Total.	Per 1° F. of Difference.	Total.	Per 1° F. of Difference.
Pounds.	° Fahr.	° Fahr.	Lbs.	Pounds.	Units.	Units.
14.7	212	150	.29	.00193	276	1.84
18	222	160	.346	.00216	329	2.05
21.5	232	170	.405	.00238	384	2.26
26	242	180	.47	.00261	446	2.48
31	252	190	.54	.00284	513	2.70
36.5	262	200	.607	.00303	577	2.89
43	272	210	.682	.00325	648	3.08
51	282	220	.76	.00345	722	3.28

For the increased rate of condensation induced by a draught of air, compared with that caused in the still air of a room, a bare steam boiler, in open air, was tested. Steam of 50 lbs. absolute pressure per square inch was condensed at the rate of 1.25 pounds per square foot of external surface per hour; or, for a difference of 236° of temperature, .0053 pound per degree of difference; showing that 4.79 units of heat per degree was emitted, or a half more than from a pipe in still air.

### Non-Conducting Coating for Steam Pipes.

M. Burnat's experiments were made with cast-iron steam pipes, 4.72 inches in diameter externally,  $\frac{1}{4}$  inch thick, in a large unbeated hall free from draughts. They were in five groups differently coated:—

1st group, coated with straw laid lengthwise, .60 inch thick, lined with straw rope.

2nd group, bare.

3rd group. Each pipe laid in a pottery pipe, enclosing an air-space, coated with a mixture of loamy earth and chopped straw, covered with tresses of straw.

4th group, coated with cotton-waste, 1 inch thick, wrapped in cloth bound with cord.

5th group, coated with a plaster of clay and cow's hair, 2·36 inches thick.

The results are given in Table 249.

TABLE 249.—CONDENSATION OF STEAM IN COATED PIPES.  
(Burnat.)

Absolute Pressure of Steam per Square Inch.	Temperatures.			Steam condensed per Square Foot of External Surface of Pipes per Hour.				
	Steam.	Air.	Difference.	Straw coat, 1st.	Bare, 2nd.	Pottery coat, 3rd.	Waste coat, 4th.	Plaster coat, 5th.
Lbs.	Fahr.	Fahr.	Fahr.	Lb.	Lb.	Lb.	Lb.	Lb.
16·5	218·0	46·4	171·6	·139	·496	·170	·217	·254
16·5	218·0	33·8	184·2	·152	·485	·163	·205	·262
18·4	223·4	33·7	189·7	·164	·555	·186	·229	·287
18·4	223·4	27·1	196·4	·182	·571	·264	·287	·344
22·0	233·2	41·5	191·7	·246	·576	·258	·244	·320
22·0	233·2	36·5	196·7	·164	...	·158	·250	...
22·0	233·2	36·1	197·1	·162	·557	·178	·260	...
22·0	233·2	28·9	204·3	·201	·586	·264	·328	·346
25·7	241·6	43·3	198·4	·244	·645	·301	·375	·389
25·7	241·6	36·5	205·1	·274	...	·285	·369	...
29·4	249·1	43·3	205·8	·252	·721	·270	·342	·379
29·4	249·1	30·6	218·4	·225	·621	·250	·328	·336
Averages, 22·0	233·1	36·5	196·6	·200	·581	·229	·286	·324

The plaster coat, fifth group, was afterwards painted white, when an average of ·307 pound of steam was condensed per square foot per hour, against ·324 pound previously.

The bare pipe was afterwards coated with old felt, which had been treated with caoutchouc; and it condensed an average of ·313 pound of steam per square foot per hour:

The rates of condensation and of emission of heat are summarised as follows :—

TABLE 250.—SUMMARY RESULTS.

Coating of Pipe.	Steam Condensed per Square Foot per Hour.		Heat Emitted per Square Foot per Hour.	
	Total.	Per 1° F. Difference.	Total.	Per 1° F. Difference.
	Pound.	Pound.	Units.	Units.
Bare pipe . . . . .	581	00300	552.8	2.812
Straw . . . . .	200	00102	190.3	0.968
Pottery pipes with air-space . . . . .	229	00115	224.8	1.108
Cotton waste . . . . .	286	00146	272.1	1.384
Felt . . . . .	313	00159	297.8	1.515
Plaster . . . . .	324	00165	308.3	1.568
The same, painted white . . . . .	307	00156	292.1	1.486

**Cooling of Water in Pipes exposed to Air.**

Dr. Anderson experimented with 2-inch wrought-iron pipes,  $\frac{3}{16}$  inch thick, galvanised, and 4-inch cast-iron pipes,  $\frac{5}{16}$  inch thick, through which hot water was passed. Results are given in Table 251. The ultimate results harmonise with those for the use of steam in pipes.

TABLE 251.—COOLING OF WATER IN PIPES EXPOSED TO AIR.

	Two-Inch Wrought-iron Pipes.				Four-Inch Cast-iron Pipes.			
	1	2	3	4	1	2	3	4
Number of experiment								
Temperature of the atmosphere Fahr.	53°	53°	52°·5	52°	60°	60°	60°	59°
Average difference of temperatures of the water and the air . Fahr.	103°·7	49°·4	25°·4	14°·3	62°·3	45°·8	33°·9	27°·3
Total heat emitted per square foot per hour. Units	233·7	104·4	46·45	19·7	99·5	63·9	49·5	38·2
Heat emitted per 1° F. difference of temperature Units.	2·25	2·11	1·88	1·39	1·59	1·53	1·46	1·40

Tredgold experimented with small vessels of different materials, in which water was cooled from a temperature of  $180^{\circ}$  to one of  $159^{\circ}$ , in a room at  $58^{\circ}$ . The heat emitted per square foot per hour per degree of mean difference of temperature was as follows :—

Tin-plate . . . . .	1.37 units.
Sheet-iron . . . . .	2.24 "
Glass . . . . .	2.18 "

Also, in a  $2\frac{1}{2}$  inch cast-iron pipe,  $\frac{1}{4}$  inch thick, water was cooled from  $152^{\circ}$  to  $140^{\circ}$  F., in a room at  $67^{\circ}$ . The heat emitted per square foot per hour per degree of difference of temperature was as follows :—

Ordinary rusty surface . . . . .	1.823 units.
Black, varnished . . . . .	1.900 "
White (two coats of lead paint). . . . .	1.778 "

### **Transmission of Heat through Metal Plates from Water to Water.**

In a metal tubular refrigerator, hot wort was cooled by water at such a rate that, taking averages, 80 units of heat passed from the wort, and was absorbed by the water per square foot of cooling surface per  $1^{\circ}$  F. per difference of temperature. The water and the wort were moved in opposite directions.

M. Pécelet proved experimentally that the rate of transmission of heat was directly as the difference of temperature at the two faces of metal plates.

### **Transmission of Heat through Metal Plates from Steam to Water.**

The rate of transmission of heat from steam through a metal plate to water at the other side is practically uniform per degree of difference of temperature. The following Table gives average results of performance, from which it appears that the transmission is much more effective for evaporating than for heating water, twice as much for flat copper plate, three times as much for copper pipe, one-fourth more for cast-iron plate. Also, that pipe surface is one-fifth more effective than flat plate surface for heating, and more than twice as much for evaporation—the result of better circulation, no doubt.

TABLE 252.—HEATING AND EVAPORATING WATER BY STEAM THROUGH METALS.

Metal Surface.	Per Square Foot per 1° F. difference of Temperature.			
	Steam Condensed.		Heat Transmitted.	
	Heating.	Evaporating.	Heating.	Evaporating.
	Pounds.	Pounds.	Units.	Units.
Copper plate . . . . .	248	483	276	534
Copper pipe . . . . .	291	1070	312	1034
Cast-iron boiler . . . . .	77	105	82	100

Mr. Isherwood experimented with cylindrical metal-pots, 10 inches in diameter, 21½ inches deep; ¼ inch, ½ inch, and ¾ inch thick; turned and bored. They were placed in a steam-bath of from 220° to 320° F. Water at 212° was supplied to the pots, and evaporated. The rate of evaporation per degree of difference of temperature was the same for all temperatures; and the rate was the same for the different thicknesses. The respective weights of water, and heats consumed per square foot of inside surface, per degree of difference, were as follows:—

	Water at 212°.	Heat.
Copper . . . . .	665 lb.	642.5 units.
Brass . . . . .	577 "	556.8 "
Wrought-iron . . . . .	387 "	373.6 "
Cast-iron . . . . .	327 "	315.7 "

The differences of results for the same metal evidently arise in part from the comparative activity of circulation, and in part from the condition and position of the heating surfaces.

### Condensation of Steam in Pipes or Tubes by Water externally.

From the results of experiments with surface-condensers, in which the steam was passed through the tubes, it appears that 500 units of heat by condensation were transmitted per square foot of tube surface per hour per 1° F. difference of temperature. The condensers were arranged in three groups of tubes successively traversed by the condensing water. In another case, where the condenser was arranged in two groups, from 220 to 240 units were transmitted.

Mr. B. G. Nichol experimented with an ordinary surface



condenser brass tube,  $\frac{3}{4}$  inch in diameter outside, No. 18 wire-gauge in thickness; encased in a  $3\frac{1}{4}$  inch iron pipe. Steam of  $32\frac{1}{2}$  lbs. total pressure per square inch occupied the interspace, whilst cold water at  $58^{\circ}$  F. initial temperature was run through the brass tube. Three experiments were made with the tubes in a vertical position, and three in a horizontal position.

Vertical Position.			Horizontal Position.		
1,	2,	3,	4,	5,	6,
Velocity of water through tube, in feet per minute,—					
81,	278,	390,	78,	307,	415 feet.

Steam condensed per square foot of surface per hour, for  $1^{\circ}$  F. difference of temperature,—

·335,	·436,	·457,	·480,	·603,	·699 lb.
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Heat absorbed by the water, per square foot per hour, per  $1^{\circ}$  F. difference of temperature,—

346,	449,	466,	479,	621,	696 units.
------	------	------	------	------	------------

The rate of condensation was greater in the horizontal position than in the vertical position. Also, the efficiency of the condensing surface was increased by an increase of velocity of the water through the tube, nearly in the ratio of the fourth root of the velocity for vertical tubes; and nearly as the 4·5 root for horizontal tubes.

#### Transmission of Heat through Metal Plates or Tubes, from Air or other Dry Gas to Water.

The rate of transmission of convected heat is probably from 2 to 5 units of heat per hour per square foot of surface per  $1^{\circ}$  F. of difference of temperature.

In a locomotive fire-box, where radiant heat co-operated with convected heat, the following results have been obtained in generating steam of 80 lbs. pressure per square inch. The temperature of the fire is taken at  $2000^{\circ}$  F.

	Water Evaporated per Square Foot per Hour.	Heat Transmitted per Square Foot per Hour per $1^{\circ}$ F. difference of Temperature.
Burning coke. 75 lbs. per square foot of grate	25½ lbs.	14½ units
Burning briquettes. 74½ lbs. per square foot of grate	35 "	20 "

There are in practice little or no differences between iron, copper, and lead in evaporative activity, when the surfaces are dimmed or coated, as under ordinary conditions.

TABLE 253.—LINEAL EXPANSION OF SOLIDS AT ORDINARY TEMPERATURES (Board of Trade).

	For 1° Fahr.	For 1° Cent.	Expansion between Freezing and Boiling Points.			Common Fraction.	
			Coefficient.	In length of Ten Feet.	Inch.		
	Length = 1.	Length = 1.		Foot.			
Aluminium (cast)	·00001234	·00002221	·002221	·02221	·2664	$\frac{1}{365}$	
Antimony (cryst.)	·00000627	·00001129	·001129	·01129	·1336	$\frac{1}{745}$	
Brass, cast	·00000957	·00001722	·001722	·01722	·2066	$\frac{1}{481}$	
" English plate	·00001052	·00001894	·001894	·01894	·2273	$\frac{1}{439}$	
" sheet	·00001040	·00001872	·001872	·01872	·2246	$\frac{1}{445}$	
Brick, best stock	·00000306	·00000550	·000550	·00550	·0660	$\frac{1}{1518}$	
Bronze (Baily's)							
Copper, 17	}	·00001774	·001774	·01774	·2129	$\frac{1}{465}$	
Tin, 2½							
Zinc, 1							
" Roman, dry	·00000975	·00001755	·001755	·01755	·2106	$\frac{1}{465}$	
Cement, Roman, dry	·00000797	·00001435	·001435	·01435	·1722	$\frac{1}{577}$	
" Portland (mixed), pure	·00000594	·00001070	·001070	·01070	·1284	$\frac{1}{785}$	
" mortar, with sand	·00000656	·00001180	·001180	·01180	·1416	$\frac{1}{707}$	
Concrete: cement mortar and pebbles	·00000795	·00001430	·001430	·01430	·1716	$\frac{1}{586}$	
Copper	·00000887	·00001596	·001596	·01596	·1915	$\frac{1}{525}$	
Ebonite	·00004278	·00007700	·007700	·07700	·9240	$\frac{1}{110}$	

TABLE 253.—LINEAL EXPANSION OF SOLIDS AT ORDINARY TEMPERATURES (*continued*).

	For 1° Fahr.	For 1° Cent.	Expansion between Freezing and Boiling Points.		Common Fraction.
			Coefficient.	In length of Ten Feet.	
Glass, English flint	Length=L. ·00000451	Length=L. ·00000812	·000812	Foot. ·00812	inch. ·0974
" French flint	·00000484	·00000872	·000892	·00892	·1070
" white, free from lead.	·00000492	·00000886	·000886	·00886	·1063
" blown	·00000498	·00000896	·000896	·00896	·1075
" thermometer	·00000499	·00000897	·000897	·00897	·1076
" hard	·00000397	·00000714	·000714	·00714	·0857
Granite, grey, dry	·00000438	·00000789	·000789	·00789	·0947
" red	·00000498	·00000897	·000897	·00897	·1076
Gold, pure	·00000786	·00001415	·001415	·01415	·1698
Iridium, pure	·00000356	·00000641	·000641	·00641	·0768
Iron, wrought	·00000648	·00001166	·001166	·01166	·1399
" Swedish	·00000636	·00001145	·001145	·01145	·1374
" cast	·00000556	·00001001	·001001	·01001	·1201
" soft	·00000626	·00001126	·001126	·01126	·1351
Lead	·00001571	·00002828	·002828	·02828	·3394
Marble, moist	·00000663	·00001193	·001193	·01193	·1432
" dry	·00000363	·00000654	·000654	·00654	·0785
" white Sicilian, dry	·00000786	·00001415	·001415	·01415	·1698

TABLE 253.—LINEAL EXPANSION OF SOLIDS AT ORDINARY TEMPERATURES (*continued*).

	Expansion between Freezing and Boiling Points.					Common Fraction.
	For 1° Fahr.	For 1° Cent.	Coefficient.	In length of Ten Feet.		
				Foot.	Inch.	
Marble, black (Galway).	Length = 1. ·00000308	Length = 1. ·00000554	·000554	·00554	·0665	$\frac{1}{1805}$
“ Carrara	·00000471	·00000848	·000848	·00848	·1018	$\frac{1}{1176}$
Masonry, of brick in cement- mortar: headers	·00000494	·00000890	·000890	·00890	·1068	$\frac{1}{1123}$
Do. do. stretchers	·00000256	·00000460	·000460	·00460	·0552	$\frac{1}{2174}$
Mercury (cubic expansion).	·00009984	·00017971	·017971	·17971	2·1565	$\frac{1}{46}$
Nickel	·00000695	·00001251	·001251	·01251	·1501	$\frac{1}{800}$
Osmium	·00000317	·00000570	·000570	·00570	·0684	$\frac{1}{1754}$
Palladium, pure	·00000556	·00001000	·001000	·01000	·1200	$\frac{1}{1000}$
Pewter	·00001129	·00002033	·002033	·02033	·2440	$\frac{1}{404}$
Plaster, white	·00000922	·00001660	·001660	·01660	·1992	$\frac{1}{602}$
Platinum	·00000479	·00000863	·000863	·00863	·1036	$\frac{1}{1156}$
Platinum, 90 per cent						
Iridium, 10 per cent.	·00000476	·00000857	·000857	·00857	·1028	$\frac{1}{1167}$
hammered and annealed						
Platinum, 85 per cent.	·00000453	·00000815	·000815	·00815	·0978	$\frac{1}{1227}$
Iridium, 15 per cent.						
Porcelain	·00000200	·00000360	·000360	·00360	·0432	$\frac{1}{2778}$

TABLE 253.—LINEAL EXPANSION OF SOLIDS AT ORDINARY TEMPERATURES (*continued*).

	For 1° Fabr.	For 1° Cent.	Expansion between Freezing and Boiling Points.		
			Coefficient.	In length of Ten Feet.	
				Foot.	Inch.
	Length = 1.	Length = 1.			Common Fraction.
Quartz, parallel to major axis, $t$ 0° to 40° C.	·00000434	·00000781	·000781	·00781	$\frac{1}{120}$
" perpendicular to major axis, $t$ 0° to 40° C.	·00000788	·00001419	·001419	·01419	$\frac{1}{60}$
" cubic expansion at 16° C.	·00001924	·00003463	·003463	·03463	$\frac{1}{240}$
Silver, pure	·00001079	·00001943	·001943	·01943	$\frac{1}{51}$
Slate	·00000577	·00001038	·001038	·01038	$\frac{1}{95}$
Steel, cast	·00000636	·00001144	·001144	·01144	$\frac{1}{72}$
" tempered	·00000689	·00001240	·001240	·01240	$\frac{1}{63}$
Stone (sandstone), dry	·00000652	·00001174	·001174	·01174	$\frac{1}{71}$
" " Rauville	·00000417	·00000750	·000750	·00750	$\frac{1}{133}$
" " Caen	·00000494	·00000890	·000890	·00890	$\frac{1}{112}$
Tin	·00001163	·00002094	·002094	·02094	$\frac{1}{47}$
Wedgwood ware	·00000489	·00000881	·000881	·00881	$\frac{1}{116}$
Wood, pine	·00000276	·00000496	·000496	·00496	$\frac{1}{200}$
Zinc	·00001407	·00002532	·002532	·02532	$\frac{1}{35}$
Zinc, S.					
Tin, I	·00001496	·00002692	·002692	·02692	$\frac{1}{37}$

### Comparative Rate of Emission of Heat from Steam Pipes in Air and in Water.

It appears that for equal total difference of temperature, the rate of emission of heat from steam pipes in water amounts, in round numbers, to from 150 to 250 times the rate in air, according as the pipes are vertical or horizontal.

### Comparative Rate of Emission of Heat from Water-Tubes in Air and in Water at Rest and in Motion.

It appears that the rate of emission from water-tubes in water was about twenty times the rate in air. Mr. Craddock proved it experimentally to be twenty-five times. When the water-tube was moved through the air at a speed of 59 feet per second, it was cooled in one-twelfth of the time occupied in still air. In water, moved at a speed of 3 feet per second, the water in the tube was cooled in half the time.

### Expansion of Liquids.

The cubical expansion, or expansion of volume, of water, from 32° F. to 212° F. and upwards, is given in Table 252. The rate of expansion increases with the temperature. The expansion for the range of temperature from 32° to 212° is .0466, or fully  $4\frac{1}{2}$  per cent. of the volume at 32°; or an average of .000259 per degree, or  $\frac{1}{3863}$  part of the volume at 32° F.

TABLE 254.—EXPANSION OF LIQUIDS, FROM 32° TO 212 F.  
Volume at 32° = 1.

Liquid.	Volume at 212°.	Expansion.	Liquid.	Volume at 212°.	Expansion.
Alcohol . .	1.1100	$\frac{1}{9}$	Sea water .	1.0500	$\frac{1}{20}$
Nitric acid .	1.1100	$\frac{1}{9}$	Water . .	1.0466	$\frac{1}{21}$
Olive oil . .	1.0800	$\frac{1}{12}$	Mercury .	1.018	$\frac{1}{54}$
Turpentine .	1.0700	$\frac{1}{11}$			

TABLE 255.—EXPANSION AND WEIGHT OF WATER AT VARIOUS TEMPERATURES.

Tempe- rature.	Relative Volume by Ex- pansion.	Weight of One Cubic Foot.	Weight of One Gallon.	Tempe- rature.	Relative Volume by Ex- pansion.	Weight of One Cubic Foot.	Weight of One Gallon.
Fahr.		Pounds.	Pounds.	° Fahr.		Pounds.	Pounds.
32	1·00000	62·418	10·0101	100	1·00639	62·022	9·947
35	·99993	62·422	10·0103	105	1·00739	61·960	9·937
		62·425		110	1·00889	61·868	9·922
39·1	·99989	maxi- mum density	10·0112	115	1·00989	61·807	9·913
				120	1·01139	61·715	9·897
40	·99989	62·425	10·0112	125	1·01239	61·654	9·887
45	·99993	62·422	10·0103	130	1·01390	61·563	9·873
46	1·00000	62·418	10·0101	135	1·01539	61·472	9·859
50	1·00015	62·409	10·0087	140	1·01690	61·381	9·844
		62·400		145	1·01839	61·291	9·829
		ordi- nary calcula- tions.		150	1·01989	61·201	9·815
52·3	1·00029		10·0072	155	1·02164	61·096	9·799
				160	1·02340	60·991	9·781
55	1·00038	62·394	10·0063	165	1·02589	60·843	9·757
60	1·00074	62·372	10·0053	170	1·02690	60·783	9·748
62				175	1·02906	60·665	9·728
mean				180	1·03100	60·548	9·711
tem- pera- ture	1·00101	62·355	10·0000	185	1·03300	60·430	9·691
				190	1·03500	60·314	9·672
65	1·00119	62·344	9·9982	195	1·03700	60·198	9·654
70	1·00160	62·313	9·9933	200	1·03889	60·081	9·635
75	1·00239	62·275	9·9871	205	1·0414	59·93	9·611
80	1·00299	62·232	9·980	210	1·0434	59·82	9·594
85	1·00379	62·182	9·972	212	1·0466	59·64	9·565
90	1·00459	62·133	9·964	250	1·06243	58·75	9·422
95	1·00554	62·074	9·955	300	1·09563	56·97	9·136
				400	1·15056	54·25	8·700
				500	1·22005	51·16	8·204

**Expansion of Gases.**

The volume of atmospheric air is increased in the ratio of 1 to 1·365, in rising in temperature from 32° to 212° F., under constant pressure; and when the volume is constant, the pressure is increased in the ratio of 1 to 1·3665.

The expansion under constant pressure is uniform, and is at the rate of  $\frac{1}{103\frac{2}{3}}$  part of the volume at 32° F., for each degree of rise of temperature: say the fraction  $\frac{1}{103}$ . At this rate of

contraction the absolute zero of the Fahrenheit scale, or point of no heat, is  $(493 - 32) = -461^{\circ}$  F., or  $461^{\circ}$  below  $0^{\circ}$  on the scale. On the Centigrade scale, the absolute zero is  $-274^{\circ}$ . The absolute temperature by the Fahrenheit scale is found by adding 461 to the temperature indicated on the thermometrical scale. For a given volume of air or other gases at a given temperature, the volume for any other temperature under a constant pressure is,—

$$V' = V \frac{t' + 461}{t + 461} \quad . \quad . \quad . \quad . \quad . \quad (9)$$

When the initial temperature is  $62^{\circ}$  F., the formula becomes

$$V' = V \frac{t' + 461}{523} \quad . \quad . \quad . \quad . \quad . \quad (10)$$

When the temperature is constant, the volume varies as the pressure, or

$$V' = V \frac{p}{p'} \quad . \quad . \quad . \quad . \quad . \quad (11)$$

When the temperature and pressure change,—

$$V' = V \frac{p(t' + 461)}{p'(t + 461)} \quad . \quad . \quad . \quad . \quad . \quad (12)$$

When the initial temperature is  $62^{\circ}$  F., and the initial pressure is 14.7 lbs. per square inch, the formula becomes

$$p' = \frac{V(t' + 461)}{35.58 V'} \quad . \quad . \quad . \quad . \quad . \quad (13)$$

When in addition the volume is constant, this formula becomes

$$p' = \frac{t' + 461}{35.58} \quad . \quad . \quad . \quad . \quad . \quad (14)$$

The product of the volume and pressure of a constant weight of a gas varies as the absolute temperature.

$$(1 \text{ pound of air}) Vp = \frac{(t + 461)}{2.7074} \quad . \quad . \quad . \quad . \quad . \quad (15)$$

And the volume of one pound of air at any pressure and any temperature, is

$$V = \frac{(t + 461)}{2.7074 p} \quad . \quad . \quad . \quad . \quad . \quad (16)$$

$V$  = initial volume of gas.

$V'$  = final volume of gas.

$t$  = initial temperature.

$t'$  = final temperature.

$p$  = initial pressure.

$p'$  = final pressure.



**Specific Heat.**

The specific heat of a body is its capacity for heat relative to that of water as a standard; of which the specific heat is that required to raise the temperature of 1 pound of water at 32° F., one degree Fahrenheit: in short, the British unit of heat. The specific heat of water is not constant; but increases slightly with the temperature, in so much that the heat required to raise the temperature from 32° to 212° F., through 180 degrees, is 180·9 units; and the average specific heat is 1·005, or one-half per cent. more than that at 32° F.

The specific heat of all solids and liquids is variable, gradually augmenting with the temperature. For temperatures under 212°, they are nearly constant.

The specific heat of perfect gases is constant.

TABLE 256.—SPECIFIC HEAT OF METALS.

Antimony . . . . .	·0507	Manganese . . . . .	·1441
Bismuth . . . . .	·0308	Mercury, solid . . . .	·0319
Brass . . . . .	·0939	„ liquid . . . . .	·0333
Copper . . . . .	·0951	Nickel . . . . .	·1086
Cymbal metal . . . .	·086	Platinum, sheet . . .	·0324
Gold . . . . .	·0324	„ spongy . . . . .	·0329
Iridium . . . . .	·1887	Silver . . . . .	·0570
Iron, cast . . . . .	·1298	Steel . . . . .	·1165
„ wrought . . . . .	·1138	Tin . . . . .	·0569
Lead . . . . .	·0314	Zinc . . . . .	·0955

TABLE 257.—SPECIFIC HEAT OF OTHER MINERAL SUBSTANCES.

STONES.		CARBONACEOUS— <i>con.</i>	
Brickwork and ma- / sonry . . . . .	·20	Graphite, natural . .	·2019
Marble . . . . .	·2129	„ of blast / furnaces . . . . .	·497
Chalk . . . . .	·2148		
Quicklime . . . . .	·2169	SUNDRY.	
Magnesian limestone	·2174	Glass . . . . .	·1977
CARBONACEOUS.		Ice . . . . .	·504
Coal . . . . .	·2411	Phosphorus . . . . .	·2503
Charcoal . . . . .	·2415	Soda . . . . .	·2311
Cannel coke . . . . .	·2031	Sulphate of lead . . .	·0872
Coke of pit coal . . .	·2008	„ lime . . . . .	·1966
Anthracite . . . . .	·2017	Sulphur . . . . .	·2026

TABLE 258.—SPECIFIC HEAT OF LIQUIDS.

Alcohol . . . . .	·6588	Turpentine . . . . .	·4160
Benzine . . . . .	·3932	Vinegar . . . . .	·9200
Mercury . . . . .	·0333	Water, at 32° F. . . . .	1·0000
Olive oil . . . . .	·3096	"    212° F. . . . .	1·0130
Sulphuric acid :—		"    32° to 212° F. . . . .	1·0050
Density, 1·87 . . . . .	·3346	Wood spirit . . . . .	·6009
"    1·30 . . . . .	·6514		

TABLE 259.—SPECIFIC HEAT OF GASES.

For Equal Weights.	At Constant Pressure.	At Constant Volume.
Air . . . . .	·2377	·1688
Carbonic acid (CO <sub>2</sub> ) . . . . .	·2164	·1714
"    oxide (CO) . . . . .	·2479	·1768
Hydrogen . . . . .	3·4046	2·4096
Light carburetted hydrogen . . . . .	·5929	·4683
Nitrogen . . . . .	·2440	·1740
Oxygen . . . . .	·2182	·1559
Steam, saturated . . . . .	...	·3050
Steam gas . . . . .	·4750	·3700
Sulphurous acid . . . . .	·1553	·1246

TABLE 260.—SPECIFIC HEAT OF WATER AT VARIOUS TEMPERATURES.

Temperature.	Specific Heat.	Heat to raise 1lb. of Water from 32° F. to given Temperature.	Temperature.	Specific Heat.	Heat to raise 1lb. of Water from 32° F. to given Temperature.
° Fahr.		Units.	° Fahr.		Units.
32	1·0000	0·000	248	1·0177	217·449
50	1·0005	18·004	266	1·0204	235·791
68	1·0012	36·018	284	1·0232	254·187
86	1·0020	54·047	302	1·0262	272·628
104	1·0030	72·090	320	1·0294	291·132
122	1·0042	90·157	338	1·0328	309·690
140	1·0056	108·247	356	1·0364	328·320
158	1·0072	126·378	374	1·0401	347·004
176	1·0089	144·508	392	1·0440	365·760
194	1·0109	162·686	410	1·0481	384·588
212	1·0130	180·900	428	1·0524	403·488
230	1·0153	199·152	446	1·0568	422·478

TABLE 261.—SPECIFIC HEAT OF WOODS.

Turpentine . . .	·467	Oak . . . . .	·570
Pear tree . . .	·500	Fir . . . . .	·650

TABLE 262.—VOLUME OF 1 POUND OF AIR AT ATMOSPHERIC PRESSURE, 14·7 LBS. PER SQUARE INCH.

Tem- perature.	Volume of One Pound.	Tem- perature.	Volume of One Pound.	Tem- perature.	Volume of One Pound.
° Fahr.	Cubic Feet.	° Fahr.	Cubic Feet.	° Fahr.	Cubic Feet.
0	11·583	230	17·362	525	24·775
32	12·387	240	17·612	550	25·403
40	12·586	250	17·865	575	26·031
50	12·840	260	18·116	600	26·659
62	13·141	270	18·367	650	27·915
70	13·342	280	18·621	700	29·172
80	13·593	290	18·870	750	30·428
90	13·845	300	19·121	800	31·685
100	14·096	320	19·624	850	32·941
120	14·592	340	20·126	900	34·197
140	15·100	360	20·630	950	35·453
160	15·603	380	21·131	1000	36·710
180	16·106	400	21·634	1250	42·990
200	16·605	425	22·262	1500	49·274
210	16·860	450	22·890	2000	61·836
212	16·910	475	23·518	2500	74·400
220	17·111	500	24·146	3000	86·962

TABLE 263.—MELTING POINTS OF ALLOYS OF LEAD, TIN, AND BISMUTH.

	° Fahr.		° Fahr.
1 tin, 5 lead . . .	511	6 tin, 1 lead . . .	381
1 " 3 " . . . . .	482	4 " 4 " 1 bismuth	320
1 " 2 " . . . . .	441	2 " 2 " 1 "	292
1 " 1 " . . . . .	370	1 " 1 " 1 "	254
2 " 1 " . . . . .	340	5 " 3 " 8 "	202
4 " 1 " . . . . .	365		
Fusible Plugs.		Soften at	Melt at
		° Fahr.	° Fahr.
2 tin, 2 lead . . . . .		365	372
2 " 6 " . . . . .		372	383
2 " 7 " . . . . .		377½	388
2 " 8 " . . . . .		395½	408

TABLE 264.—MELTING POINTS OF METALS.

	° Fahr.		° Fahr.
Aluminium	Full red heat	Iron, cast, white	1922 to 2012
Antimony	1150	„ wrought	2912
Bismuth	507	Lead	617
Bronze	1690	Mercury	—39
Copper	1996	Silver	1873
Gold, standard	2156	Steel	2372 to 2552
„ pure	2282	Tin	442
Iron, cast, gray	2012	Zinc	773

TABLE 265.—MELTING POINTS OF SUNDRY SOLIDS.

	° Fahr.		° Fahr.
Carbonic acid	—108	Spermaceti	120
Ice	32	Sulphur	239
Nitro-glycerine	45	Tallow	92
Phosphorus	112	Turpentine	14
Stearine	109 to 120	Wax, rough	142
		„ bleached	154

TABLE 266.—BOILING POINTS OF LIQUIDS, AND HEAT OF EVAPORATION.

Liquid.	Boiling Point.	Latent Heat of Evaporation of One Pound.	Total Heat from 32° F. of One Pound.
	° Fahr.	Units.	Units.
Alcohol	173	374	461·7
Ammonia	140	...	...
Benzine	176	...	...
Linseed oil	597	...	...
Mercury	648	...	...
Sulphuric ether	100	175	210·4
Turpentine.	315	124	256·6
Water	212	965·2	1146·1
„ sea	213·2	...	...
„ saturated brine	226	...	...
Wood spirit	150	475	545·9

TABLE 267. —HEAT CONDUCTING POWER OF METALS.  
SILVER = 1000.

(F. Crace-Calvert &amp; R. Johnson.)

METALS.	Relative Con- ducting Power. Silver = 1000.
Silver . . . . .	1000
Gold . . . . .	981
Gold, with 1 per cent. of silver . . . . .	840
Copper, rolled . . . . .	845
Copper, cast . . . . .	811
Mercury . . . . .	677
Mercury, with 1·25 per cent. of tin . . . . .	412
Aluminium . . . . .	665
Zinc, rolled . . . . .	641
Zinc, cast vertically . . . . .	628
Zinc, cast horizontally . . . . .	608
Cadmium . . . . .	577
Wrought iron . . . . .	436
Tin . . . . .	422
Steel . . . . .	397
Platinum . . . . .	380
Sodium . . . . .	365
Cast iron . . . . .	359
Lead . . . . .	287
Antimony, cast horizontally . . . . .	215
Antimony, cast vertically . . . . .	192
Bismuth . . . . .	61
<i>Influence of a non-metallic substance in combination on the conducting power of a metal.</i>	
<i>Influence of carbon on iron :—</i>	
Wrought iron . . . . .	436
Steel . . . . .	397
Cast iron . . . . .	359
<i>Influence of arsenic on copper :—</i>	
Cast copper . . . . .	811
Copper with 1 per cent. of arsenic . . . . .	570
" " " " . . . . .	669
" " " " . . . . .	771

TABLE 268. — FRIGORIFIC MIXTURES.  
(Selection.)

Mixture.		Fall of Temperature.		Degrees of Cold Produced.
		Fahr.	Fahr.	
Nitrate of ammonia	1	From + 50° to + 4°	46°	
Water	1			
Phosphate of soda	9	From + 50° to — 21°	71°	
Nitrate of ammonia	6			
Dilute nitric acid	4			
Muriate of soda (common salt)	1	From any temperature to — 5°	...	
Snow, or pounded ice	2			
Muriate of soda	5	From any temperature to — 25°	...	
Nitrate of ammonia	5			
Snow, or pounded ice	12			
Dilute sulphuric acid	2	From + 32° to — 23°	55°	
Snow	3			
Potash	4	From + 32° to — 51°	83°	
Snow	3			
Muriate of lime		From + 20° to — 48°	68°	
Snow				

### Conduction of Heat by Metals, Alloys, and Amalgams.

Messrs. F. Crace-Calvert and R. Johnson investigated the conducting powers of metals, alloys, and amalgams. Of the solid metals square bars 1 centimetre square ( $\frac{39}{64}$  inch), and 6 centimetres long (2.36 inches), were employed. Mercury and sodium were deposited in a box of the given dimensions to hold them. The metals and alloys were of pure metals, excepting platinum, aluminium, iron, and sodium, which were only commercially pure. Tables 264 and 266 give the results of the trials. The alloys of tin and lead, and tin and zinc, there is reason to believe, are only mixtures. The alloys of copper and tin appear to be definite chemical compounds; the observed conducting powers being widely different from the powers calculated from those of the elements. In one instance, an alloy of 68 per cent. of copper and 32 per cent. of tin has less than one-fourth of the calculated power. The low conducting powers of the commercial alloys, No. 7, are due to impurities.

Mercury, when so situated that circulation is prevented, is the worst heat-conducting metal known. The conducting

power of silver, the best conductor, being 1000, that of mercury is only 54 when the column is vertical, and the source of heat is applied at the upper part of the column. When the column is horizontal, the power is 679. Water, like mercury, presents a complete barrier to conduction of heat applied at the upper end of a vertical column.

TABLE 269.—HEAT-CONDUCTING POWER OF ALLOYS AND AMALGAMS : SILVER = 1000.

(F. Crace-Calvert & R. Johnson.)

*I. Alloys by which Heat is Conducted in the Ratio of the Calculated Mean Conducting Power of the Metals composing them.*

ALLOY.	Proportions per Cent., by Weight.	Actual Relative Conducting Power, Silver = 1000.	Calculated Conducting Power.
<i>1. Tin and Lead.</i>			
Pb Sn <sup>5</sup> . . .	{ T 73.97 L 26.03 }	385	386
Pb Sn . . .	{ T 36.22 L 63.78 }	230	236
Sn Pb <sup>5</sup> . . .	{ T 10.20 L 89.80 }	299	301
<i>2. Tin and Zinc.</i>			
Zn <sup>5</sup> Sn . . .	{ Z 73.43 T 26.57 }	541	572
Zn Sn . . .	{ Z 35.61 T 64.39 }	501	495
Zn Sn <sup>5</sup> . . .	{ Z 9.95 T 90.05 }	456	442
<i>II. Alloys containing an Excess of the Worse-Conducting Metal.</i>			
<i>3. Lead and Anti- mony.</i>			
Pb Sb . . .	{ L 61.61 A 38.39 }	190	251
Pb Sb <sup>5</sup> . . .	{ L 24.30 A 75.70 }	179	215

TABLE 269.—HEAT-CONDUCTING POWER OF ALLOYS (*cont.*).

ALLOY.	Proportions per Cent., by Weight.	Actual Relative Conducting Power. Silver = 1000.	Calculated Conducting Power.
4. <i>Antimony and Bismuth.</i>			
Sb Bi. . . .	{ A 37.74 B 62.26 }	62	110
Sb Bi <sup>s</sup> . . . .	{ A 10.82 B 89.18 }	48	75
5. <i>Copper and Tin.</i>			
Cu Sn . . . .	{ C 34.98 T 65.02 }	415	558
Cu Sn <sup>2</sup> . . . .	{ C 21.21 T 78.79 }	431	504
Cu Sn <sup>3</sup> . . . .	{ C 15.21 T 84.79 }	423	481
Cu Sn <sup>4</sup> . . . .	{ C 11.86 T 88.14 }	406	468
Cu Sn <sup>5</sup> . . . .	{ C 9.73 T 90.27 }	396	459
The following have excess of copper :—			
Sn Cu <sup>3</sup> . . . .	{ T 38.21 C 61.79 }	494	670
Sn Cu <sup>4</sup> . . . .	{ T 31.73 C 68.27 }	155	686
Sn Cu <sup>5</sup> . . . .	{ T 27.10 C 72.90 }	207	705
6. <i>Zinc and Copper.</i>			
Cu Zn . . . .	{ C 49.32 Z 50.68 }	688	718
Cu Zn <sup>2</sup> . . . .	{ C 32.74 Z 67.26 }	428	687
Cu Zn <sup>3</sup> . . . .	{ C 24.64 Z 75.36 }	531	672
Cu Zn <sup>4</sup> . . . .	{ C 19.57 Z 80.43 }	589	663
Cu Zn <sup>5</sup> . . . .	{ C 16.30 Z 83.70 }	595	657



TABLE 269.—HEAT-CONDUCTING POWER OF ALLOYS (*cont.*).

ALLOY.	Proportions per Cent., by Weight.	Actual Relative Conducting Power. Silver = 1000.	Calculated Conducting Power.
6. <i>Zinc and Copper</i> ( <i>continued</i> ). The following have excess of copper:—			
Zn Cu <sup>2</sup> . . .	Z 33.94 C 66.06	621	748
Zn Cu <sup>3</sup> . . .	Z 25.52 C 74.48	638	764
Zn Cu <sup>4</sup> . . .	Z 20.44 C 79.56	665	770
Zn Cu <sup>5</sup> . . .	Z 17.05 C 82.95	715	780
7. <i>Commercial Alloys.</i>			
"Yellow brass"	Copper 64.0 Zinc 36.0	558	712
"Pumps and pipes" . . .	Copper 80 Tin 5 Zinc 7.5 Lead 7.5	426	707
"Mud plugs" .	Copper 80 Tin 10 Zinc 10	394	754
"Large bear- ings" . . .	Copper 84.05 Tin 12.82 Zinc 5.13	345	751
III. <i>Amalgams (Compounds of Mercury), Solid and Semi-Solid, in which there is an Excess of the Amalgamated Metal.</i>			
8. <i>Amalgams of Tin.</i>			
Hg Sn <sup>2</sup> . . .	M 45.88 T 54.12	8.65	8.11
Hg Sn <sup>3</sup> . . .	M 36.18 T 63.82	9.45	9.2
Hg Sn <sup>4</sup> . . .	M 29.84 T 70.16	9.65	9.95
Hg Sn <sup>5</sup> . . .	M 25.38 T 74.62	10.6	10.5

TABLE 269.—HEAT-CONDUCTING POWER OF ALLOYS (*cont.*).

ALLOY.	Proportions per Cent., by Weight.	Actual Relative Conducting Power. Silver = 1000.	Calculated Conducting Power.
9. <i>Amalgams of Zinc.</i>			
Hg Zn <sup>2</sup> . . .	( M 60.63 ) ( Z 39.37 )	9.7	8.97
Hg Zn <sup>3</sup> . . .	( M 54.70 ) ( Z 45.30 )	10.45	10.05
Hg Zn <sup>4</sup> . . .	( M 43.50 ) ( Z 56.50 )	11.00	12.08
Hg Zn <sup>5</sup> . . .	( M 38.11 ) ( Z 61.89 )	13.95	13.05
10. <i>Amalgams of Bismuth.</i>			
Hg Bi <sup>2</sup> . . .	( M 31.82 ) ( B 68.18 )	2.15	1.87
Hg Bi <sup>3</sup> . . .	( M 23.86 ) ( B 76.14 )	2.6	1.89
Hg Bi <sup>4</sup> . . .	( M 19.03 ) ( B 80.97 )	2.55	1.90
Hg Bi <sup>5</sup> . . .	( M 15.82 ) ( B 84.18 )	2.35	1.91

## COMBUSTION.—FUELS.

## Combustion.

The volume of air consumed chemically in the combustion of fuel is expressed by the formula :—

$$A = 1.52 (C + 3H - .4O) \quad . \quad . \quad . \quad (1)$$

A = volume of air as at 62° F., and under one atmosphere of pressure, in cubic feet, per pound of fuel.

A' = weight of air as at 62° F., per pound of fuel.

C = percentage of constituent carbon.

H = percentage of constituent hydrogen.

O = percentage of constituent oxygen.

The weight of the air thus found by volume is equal to the volume divided by 13·14. Or it is found directly by the formula :—

$$A' = \cdot 116 (C + 3H - \cdot 4O) . . . . . (2)$$

In these formulas the heat evolved by the combustion of the sulphur constituent is not noticed, as it is trifling in proportion.

The volume of the volatile or gaseous products of the complete combustion of one pound of a fuel, as at 62° F., at atmospheric pressure, is, by formula,—

$$V = 1\cdot 52C + 5\cdot 52H . . . . . (3)$$

The weight of the gaseous products is, by formula,—

$$w = \cdot 126C + \cdot 358H . . . . . (4)$$

$V$  = volume of gaseous products, in cubic feet.

$w$  = weight of gaseous products, in pounds.

$C$  = percentage of constituent carbon.

$H$  = percentage of constituent hydrogen.

The volume at any other temperature is found by the formula for expansion of volume of gases, p. 474.

The proportion of free or unconsumed air usually present in the gaseous products is determined by multiplying the percentage of oxygen, found by analysis, by 4·35. The product is the percentage of free air in parts of the whole mixture.

The heat generated by combustion is as follows :—

Carbon . . . . .	14,500 heat-units per pound.
Hydrogen . . . . .	62,000                   "
Sulphur . . . . .	4,000                   "

The heating power of fuels containing carbon and hydrogen is approximately expressed by the formula :

$$h = 145 (C + 4\cdot 28H) . . . . . (5)$$

in which  $h$  is the total heat of combustion.

The evaporative efficiency for one pound of fuel is

$$e = \cdot 15 (C + 4\cdot 28H) . . . . . (6)$$

$$\text{or, } e = \frac{h}{966} . . . . . (7)$$

$e$  = weight of water evaporable from and at 212°, in pounds, per pound of fuel.

The maximum temperature of combustion of carbon is about 5000° F. ; and that of hydrogen is about 5800° F.

**Fuels.**

*Coal* consists mainly of carbon, which varies from 50 per cent. to 80 per cent., by weight, of the fuel. Lignite or brown coal contains from 56 to 76 per cent. of carbon. The average composition of British coal is, say, 80 per cent. of carbon, 5 per cent. of hydrogen,  $1\frac{1}{4}$  per cent. of sulphur,  $1\frac{1}{2}$  per cent. of nitrogen, 8 per cent. of oxygen, and 4 per cent. of ash. The fixed carbon or coke averages 61 per cent. The average specific gravity is 1.279; average weight of a solid cubic foot, 80 pounds; and of a cubic foot heaped, 50 pounds; average bulk of one ton heaped,  $44\frac{1}{2}$  cubic feet; equivalent evaporative efficiency, 15.40 pounds of water per pound of coal, from and at 212° F.

Bituminous coals hold from 6 per cent. to 10 per cent. of water hygroscopically; Welsh coals from  $\frac{8}{9}$  per cent. to  $2\frac{1}{2}$  per cent.

*Coke* contains from 85 to  $97\frac{1}{2}$  per cent. of carbon; from  $\frac{3}{4}$  to 2 per cent. of sulphur, and from  $1\frac{1}{2}$  to  $14\frac{1}{2}$  per cent. of ash. The average composition may be taken as  $93\frac{1}{2}$  per cent. of carbon,  $1\frac{1}{4}$  per cent. of sulphur;  $5\frac{1}{2}$  per cent. of ash. It weighs from 40lbs. to 50lbs per cubic foot solid, and about 30lbs. broken and heaped. The volume of 1 ton heaped is from 70 to 80 cubic feet; average, 75 cubic feet. Coke is capable of absorbing from 15 to 20 per cent. of moisture. There is ordinarily from 5 per cent. to 10 per cent. of hygrometric moisture in coke.

*Lignite* or *brown coal* consists chiefly of carbon, oxygen, and nitrogen; averaging in perfect lignite, 69 per cent. of carbon, 5 per cent. of hydrogen, 20 per cent. of oxygen and nitrogen, and 6 per cent. of ash. The weight is about 80 pounds per cubic foot. Imperfect lignite weighs about 72 pounds per cubic foot.

*Asphalte* consists, in round numbers, of 79 per cent. of carbon, 9 per cent. of hydrogen, 9 per cent. of oxygen and nitrogen, and 3 per cent. of ash. It weighs about 66 pounds per cubic foot.

*Woods* of various kinds are approximately the same in composition, averaging, when perfectly dry, 50 per cent. of carbon, 6 per cent. of hydrogen, 41 per cent. of oxygen, 1 per cent. of nitrogen, and 2 per cent. of ash. Green wood when cut down contains moisture to the extent of 45 per cent. of its weight. Wood kept in a dry place holds from 15 per cent. to 20 per cent. of water. In a closely packed pile of wood, consisting of uncloven stems, the interstitial space is about 30 per cent. of the gross bulk. A cord of pine-wood, in the United States of America, is 4 feet by 4 feet by 8 feet, and has a volume of

128 cubic feet. Its weight averages 2,700 pounds, or 21 pounds per cubic foot. A "corde" of wood, in France, has a volume of 4 cubic feet metres or 141 cubic feet. Ordinarily dry wood, in France, averages 20 pounds weight per cubic foot heaped, or 114 cubic feet per ton heaped.

*Wood charcoal*, as manufactured in the forests, consists of 79 per cent. of carbon, 2 per cent. of free hydrogen, 11 per cent. of hydrogen, oxygen, and nitrogen, and 8 per cent. of ash :— average composition. The yield of charcoal varies from 17 to 21 per cent. in weight of the wood, which is a mixture of oak, beech, poplar, willow, and elm. The weight of charcoal as manufactured, heaped, is 14 pounds per cubic foot; in small pieces, heaped, 25 pounds per cubic foot. The bulk of 1 ton heaped is 160 cubic feet and 88.5 cubic feet respectively. Charcoal holds generally 10 or 12 per cent. of moisture.

*Peat*, cut and dried, has a specific gravity varying from .22 to 1.06. Ordinary air-dried peat holds from 20 per cent. to 30 per cent. of its gross weight of moisture. Perfectly dry peat contains, on an average, 59 per cent. of carbon, 6 per cent. of hydrogen, 30 per cent. of oxygen,  $1\frac{1}{4}$  per cent. of nitrogen, and 4 per cent. of ash. The weight of one cubic foot, heaped or stalked, is from 6 pounds to  $22\frac{1}{2}$  pounds per cubic foot; or the volume of one ton is from 370 cubic feet to 100 cubic feet; Condensed peat, such as is macerated and mixed, weighs from 44 to 57 pounds per cubic foot stalked, or the volume is from 51 to 40 cubic feet per ton.

*Peat charcoal* is yielded at the rate of from 30 per cent. to 40 per cent. by weight of good peat. It contains from 85 to 90 per cent. of carbon, and from 10 to 15 per cent. of ash.

*Straw*, in its ordinary state, consists of about 16 per cent. of water, 36 per cent. of carbon, 5 per cent. of hydrogen, 38 per cent. of oxygen,  $\frac{1}{4}$  per cent. of nitrogen, and  $4\frac{1}{2}$  per cent. of ash. Pressed straw weighs from 6 pounds to 8 pounds per cubic foot.

*Petroleum* consists of about 85 per cent. of carbon, 13 per cent. of hydrogen, and 2 per cent. of oxygen; having .87 specific gravity, and weighing 8.70 pounds per gallon. *Petroleum oils* consist of about 73 per cent. of carbon, and 27 per cent. of hydrogen; having .71 specific gravity, and weighing 7.10 pounds per gallon.

*Coal Gas*, which will be noticed in detail, consists, in round numbers, of 12 per cent. of olefiant gas, 53 per cent. of marsh gas, 14 per cent. of carbonic oxide, 8 per cent. of hydrogen, 6 per cent. of nitrogen, and a small fraction of oxygen.

For the above-named fuels, the Heat of Combustion is recorded in Table 267, with the quantity of air chemically consumed.

TABLE 270.—HEAT OF COMBUSTION OF FUELS.

Fuel.	Air Chemically Consumed per Pound of Fuel.		Total Heat of Combustion of One Pound of Fuel.	Equivalent Evaporative Power, from and at 212° F., Water per Pound of Fuel.
	Pounds.	Cub. Ft. at 62° F.	Units.	Pounds.
Coal of average composition . . . . .	10.7	140	14,700	15.22
Coke . . . . .	10.81	142	13,548	14.02
Lignite . . . . .	8.85	116	13,108	13.57
Asphalte . . . . .	11.85	156	17,040	17.64
Wood, desiccated . . . . .	6.09	80	10,974	11.36
Wood, 25 per cent. moisture . . . . .	4.57	60	7,951	8.20
Wood charcoal, desiccated . . . . .	9.51	125	13,006	13.46
Peat, desiccated . . . . .	7.52	99	12,279	12.71
Peat, 30 per cent. moisture . . . . .	5.24	69	8,260	9.53
Peat charcoal, desiccated . . . . .	9.9	130	12,325	12.76
Straw . . . . .	4.26	56	8,144	8.43
Petroleum . . . . .	14.33	188	20,411	21.13
Petroleum oils . . . . .	17.93	235	27,531	28.50
Coal gas, per cubic foot at 62° F. . . . .	...	...	630	.70

**WARMING AND VENTILATION.—COOKING-STOVES.****Warming and Ventilation.**

The quantity of air required for ventilation of buildings is variously estimated at from  $3\frac{1}{2}$  cubic feet to 20 cubic feet per minute, or from 210 to 1,200 cubic feet per hour per head of inmates in ordinary good health. In public schools, 1,800 cubic feet per hour per head is recommended; for

theatres and concert-halls, from 1,500 to 3,000 cubic feet ; for hospitals, from 4,000 to 6,000 cubic feet. For each lamp or gas-burner employed, from 30 to 60 cubic feet per hour should be provided.

In warming dwelling-rooms by open coal fires and by close stoves, the results of the tests made by Mr. D. K. Clark for the Smoke Abatement Committee, showed that the heat of combustion was distributed as follows :—

	Open Grates.	Close Stoves.
Heat carried up the chimney . . . . .	43	24
Radiated and conducted heat absorbed by the walls . . . . .	42	54
Heat lost by radiation and conduction externally, and heat lost by imperfection of combustion . . . . .	15	22
	<hr/> 100	<hr/> 100

The grates and stoves were tested in rooms 15 feet square, 17 feet total height ; having 3,600 cubic feet of capacity.

	Open Grates.	Close Stoves.
Average weight of Wallsend coal consumed per hour . . . . .	3·65 lbs.	3·87 lbs.
Average rise of temperature maintained in the room . . . . .	10·83° F.	17·74° F.
Average rise of temperature maintained per lb. of coal consumed per hour . . . . .	3·22° F.	4·48° F.

It was shown that, of the open grates, those constructed on the principle of drawing the combustible gases through the incandescent fuel, were the most efficient ; and that, of these, the best were those in which the fresh fuel was supplied below the fire, the combustible gases rising upwards through it. Ordinary open fires, having either bottom grids or solid floors, were the least effective for warming relatively to the quantity of coal consumed per hour.

The efficiency generally varied inversely as the depth of the smoke-shade at the top of the chimney.

The velocity and temperature of draught in the chimney, which was 8½ inches in diameter, were as follows :—

	Open Grates.	Close Stoves.
Velocity of draught in feet per minute . . . . .	376 ft.	275 ft.

	Open Grates. 197° F.	Close Stoves. 200° F.
Temperature in chimney. . . .		
Actual volume of gases passed up the chimney in cubic feet per hour . . . . .	9,400 ft.	6,880 ft.
Equivalent volume, as for 62° F. in cubic feet . . . . .	7,471 "	5,443 "
Equivalent volume, per lb. of coal, in cubic feet . . . . .	2,099 "	1,158 "
Percentage volume of burnt gases in chimney . . . . .	7 per cent.	12½ per cent.
Percentage volume of atmospheric air in chimney . . . . .	93 "	87½ "

### Heating by Steam ("Steam").

In heating buildings by steam, the boiler power and pipe surface depend much upon the kind of building and the situation. If heating be done by indirect radiation, from 50 to 100 per cent. more heat is required than for direct radiation.

**RULE.**—*For direct radiating surface.* Add together the area of glass in the windows in square feet, the volume of air in cubic feet required to be changed per minute, and one-twentieth of the surface of external wall and roof. Multiply the sum by the difference between the required temperature of the room and the minimum temperature of the external air; divide the product by the difference between the temperature of the steam in the pipes and the required temperature of the room. The quotient is the required radiating surface in square feet.

Each square foot of radiating surface gives off, in average practice, three heat-units per hour for each degree of difference of temperature between the steam inside and the air outside; varying 50 per cent. more or less.

In *indirect heating*, the efficiency of the radiating surface increases, and the temperature of the air diminishes, when the quantity of air passed through the coil increases. Thus, one square foot of radiating surface, with steam at 212° F., will heat 100 cubic feet of air per hour from 32° to 150°; or 300 cubic feet from 32° to 100°, in the same time. Small pipes are more effective than large pipes. When the diameter is doubled, 20 per cent. additional surface should be allowed; for three times the diameter, 30 per cent.

One square foot of boiler surface can supply to from 7 to 10 square feet of radiating surface. Each horse-power of boiler,



—measured by the evaporation of 30 pounds of water under 75 lbs. pressure, per hour—will supply to from 240 to 360 feet of 1-inch steam pipe, or from 80 to 120 square feet of radiating surface.

Under ordinary conditions, one horse-power will heat various buildings as follows :—

	Cubic feet.
Brick dwellings, in blocks, as in cities . . . . .	15,000 to 20,000
„ stores . . . . .	10,000 to 15,000
„ dwellings, exposed on all sides . . . . .	10,000 to 15,000
„ mills, shops, factories, &c. . . . .	7,000 to 10,000
Wooden dwellings, exposed . . . . .	7,000 to 10,000
Foundries and wooden shops . . . . .	6,000 to 10,000
Exhibition buildings, largely of glass . . . . .	4,000 to 15,000

### Heating Rooms by Hot Water.

Mr. Hood allows one square foot of direct heating surface of boilers, or three square feet of flue-surface for every 40 feet of 4-inch pipe containing hot water for heating buildings ; and, allowing about 10 pounds of good coal consumed per hour per square foot of fire-grate, 20 square inches area of grate suffice for heating 40 feet of 4-inch pipe.

Mr. Jones makes the following allowance of fire-grate per 100 feet of 4-inch pipe, for different kinds of boiler :—

	Grate-area.
Plain saddle . . . . .	50 square inches.
Cheek-end saddle . . . . .	45 „ „
Chambered saddle . . . . .	40 „ „
Double-chambered saddle . . . . .	35 „ „
Trentham vertical cylindrical . . . . .	35 „ „

Mr. Hood gives the following rule for the length of 4-inch pipe required to heat 1,000 cubic feet of air per minute :—

Multiply the volume of air in cubic feet to be warmed per minute, by the difference of the temperature in the room and the external temperature, and by 0.56, and divide the product by the difference of the internal temperature and that of the pipes. The quotient is the length of 4-inch pipe in feet.

The following, in Table 268, are a selection of values calculated by this rule :—

TABLE 271.—LENGTH OF 4-INCH PIPE TO HEAT 1,000  
CUBIC FEET OF AIR PER MINUTE.  
Temperature of the Pipe, 200° F.

		Temperature of the Room (Fahr.).						
External Tempera- ture		50°	55°	60°	65°	70°	75°	80°
° Fahr.	Feet.	Feet.	Feet.	Feet.	Feet.	Feet.	Feet.	Feet.
10	150	174	200	229	259	292	328	
16	127	151	176	204	233	265	300	
20	112	135	160	187	216	247	281	
24	97	120	144	170	199	229	262	
32	67	89	112	137	164	193	225	
40	37	58	80	104	129	157	187	
44	22	42	64	87	112	139	168	
50	...	19	40	62	85	112	140	
52	...	11	32	54	77	103	131	

Mr. Jones gives the following Table 269, for approximate lengths of 4-inch pipe required for every 1,000 cubic feet. The required lengths may be varied to suit special conditions.

TABLE 272.—LENGTH OF 4-INCH PIPE REQUIRED FOR EVERY 1,000 CUBIC FEET.

Building.	Temperature Required.	Length of Pipe.
Public buildings . . . . .	° Fahr. 55	Feet. 6 to 7
Workshops, warehouses, &c. . . . .	55	6 to 7
Schools, churches, offices, bed-rooms, &c. . . . .	60	7 to 8
Shops, waiting rooms, &c. . . . .	60	10 to 11
Living rooms . . . . .	65	10 to 11
Drying stoves (closed rooms) . . . . .	100	100
" " . . . . .	110	120
" " . . . . .	120	170
" " . . . . .	130	240
Conservatories, greenhouses, &c. . . . .	45 to 50	35
Ferneries, &c. . . . .	50 to 55	40
Vineries, stoves . . . . .	55 to 60	45
" " . . . . .	60 to 65	50
Orchids, stoves . . . . .	65 to 70	55
" " . . . . .	70 to 75	60
"eries, forcing houses . . . . .	75 to 80	70

**Distribution of Heat in Furnaces.**

In melting pig-iron in an ordinary cupola by the combustion of 30 per cent. of its weight of coke, Peccet estimated that 14 per cent. only of the heat of combustion was actually utilised.

In an ordinary metallurgical re-heating furnace, one ton of coal is consumed in heating  $1\frac{3}{4}$  tons of wrought-iron to the welding point,  $2,700^{\circ}$  F.; showing that only  $4\frac{1}{4}$  per cent. of the whole heat generated is appropriated by the metal.

Barely  $1\frac{1}{2}$  per cent. of the whole heat generated is absorbed in melting pot steel in ordinary furnaces. In the Siemens regenerative furnace, a ton of steel is melted for the combustion of 12 cwts. of small coal, showing that 6 per cent. of the heat produced is utilised.

Sir I. Lowthian Bell's estimate of the distribution of heat in a blast furnace from Durham coke, which contains 92.5 per cent. of carbon, for the production of 1 ton of pig-iron is as follows:—He assumes that 30.4 per cent. of the carbon of the fuel—Durham coke—which escapes in a gaseous form, is carbonic acid; and that, therefore, only 51.27 per cent. of the heating power of the fuel is developed, and the remaining 48.73 per cent. leaves the tunnel head undeveloped. He adopts as a unit of heat, the heat required to raise the temperature of 112 pounds of water  $1^{\circ}$  centigrade. To produce 1 ton of pig-iron there are required 11 cwts. of limestone and 49 cwts. of calcined ironstone. The ironstone consists of 18.6 cwts. of iron, 9 cwts. of oxygen, and 21.4 cwts. of earths.

*For 1 ton of Pig-Iron.*

	Units.	Per cent.
Evaporation of water in coke and chemical action in smelting . . . . .	48,354	54.1
Fusion of pig-iron . . . . .	6,600	7.4
Fusion of slag . . . . .	15,356	17.2
Expansion of blast . . . . .	3,700	4.1
	<hr/>	<hr/>
For direct work of furnace . . . . .	74,010	82.8
Loss by radiation through the walls . . . . .	3,600	
Carried away by tuyere water . . . . .	1,800	
Sensible heat of gaseous products . . . . .	10,000	
	<hr/>	<hr/>
Waste . . . . .	15,400	17.2
	<hr/>	<hr/>
Total heat generated in the furnace . . . . .	89,410	100.0

**Gas-Heating Stoves and Fires.**

The results of Mr. D. K. Clark's test-trials of Gas-Heating Stoves and Fires of various classes, are summarised in Table 273.

TABLE 273.—AVERAGE RESULTS OF TEST-TRIALS OF GAS-HEATING STOVES AND FIRES.

Classes of Stoves.	Ex- ternal Tem- pera- ture.	Tem- pera- ture in the Test- ing Room.	Diffe- rence, or Ele- vation of Tem- pera- ture.	Gas Con- sumed per Hour.	Gas per Hour per Degree of Ele- vation of Tem- pera- ture.	Room Space per Cubic Foot of Gas per Hour per Degree of Eleva- tion of Tem- pera- ture.
	° Fahr.	° Fahr.	° Fahr.	Cub. Ft.	Cub. Ft.	Cub. Ft.
I. Close stoves . . . .	57.1	61.3	7.2	10.9	1.35	218
II. Open stoves:—						
Asbestos fuel stoves . .	57.4	72.1	14.7	28.7	2.05	175
Tile stoves . . . .	59.7	69.2	9.5	16.9	1.84	195
III. Gas baskets or gas fires:						
Reflector stoves . . . .	58.7	66.5	7.8	11.1	1.55	232
Gas fires . . . .	55.8	63.7	7.9	12.2	1.57	229

The volume of the testing-room was about 3,600 cubic feet. The consumption of gas per hour per degree of elevation of temperature is the measure of relative effectiveness: showing that the reflector stoves were the most effective; consuming about  $1\frac{1}{2}$  cubic feet of gas per hour per degree. Gas baskets, or gas fires, were practically of equal efficiency with the reflector stoves. Next in order, are close stoves, then tile stoves; and, lastly, asbestos fuel stoves, consuming 2 cubic feet of gas per hour per degree.

The ventilation of the room, as dependent on draught in the chimney, averaged from 6,000 to 10,000 cubic feet of air, as at 62° F., per hour: showing that a volume of air of from twice to thrice the capacity of the room, was passed up the chimney per hour. By the natural draught in the chimney independent of the augmentation of draught by the stove heat, 2,400 cubic feet of air passed up the chimney per hour.

The average efficiency of the stoves was upwards of 90 per cent.; or, less than 10 per cent. of the heat generated was wasted up the chimney.

**Cooking Ranges.**

From the average results of tests of Cooking Ranges at the Smoke Abatement Exhibition, it appears that a joint from the sirloin weighing  $12\frac{1}{2}$  lbs., and a sample of puff pastry following

the joint, were roasted and baked in two hours, with a consumption of 17 pounds of hard steam coal.

### Cooking with Gas.\*

From the average results of numerous test-trials of gas-cooking stoves, having burners inside, in roasting legs of mutton weighing from 8 lbs. to 9 lbs. each, the loss of weight and net weight were as follows:—

#### *Average distribution of Joints when very well done.*

Joint as cooked . . . . .	6 lbs. 7 ozs.	or	77 per cent.
Dripping . . . . .	1 " 0 "	"	12 " "
Loss by evaporation . . . . .	0 " 15 "	"	11 " "

8 lbs. 6 ozs. or 100 per cent.

The bone of a leg of mutton weighed 1 pound.

The average temperature in the oven was 378° F. The average length of time roasting was 2 hours 16 minutes; or at the rate of a quarter of an hour per pound weight of the joint, with 16 minutes for the odd 6 ounces. The average quantity of gas consumed while roasting was 22·6 cubic feet of the average temperature 56° F., or at the rate of 2·70 cubic feet per pound of fresh joint, and of 10 cubic feet per hour. Adding the gas consumed in heating up the stoves, which was an average of 3·40 cubic feet, the sum is 26 cubic feet of gas; the total average consumption being at the rate of 3·1 cubic feet per pound of the fresh joint. The average capacity of the ovens was 2·54 cubic feet, represented nearly by that of Davis's No. 9 Stove, which is 22 inches high above the burners, and 14½ inches square. The flavour of the meat roasted by plain gas was decidedly better than that of the meat roasted by atmospheric gas.

Externally heated stoves consumed about one-third more gas than internally heated stoves.

The distribution of the heat of combustion of the 22 cubic feet of gas consumed in roasting the joint, averaging for 25 trials, was as follows:—

	Heat Units.	Gas.—Cubic Feet at 62° F.	Per cent.
Roasting the joint . . . . .	2,203	or 3·54	or 16·1
Carried off in the burnt gases . . . . .	585	" 0·94	" 4·3
Dispersed by external radiation } and conduction . . . . . }	10,896	" 17·52	" 79·6
	13,684	" 22·0	" 100·0

Showing that barely one-sixth of the whole of the heat generated was utilised in roasting; that the proportion of heat carried off in the burnt gases was comparatively insignificant, and that four-fifths of the total heat was dispersed wastefully.

\* See *International Electric and Gas Exhibition, 1882* S3: *Report on Gas Section*, by D. K. Clark.

## STEAM.

The leading properties of saturated steam are stated in Table 274 (p. 508). The specific heat of saturated steam is .305 at constant volume. That of steam gas is .3643 at constant volume, and .475 at constant pressure.

Steam of from 25 lbs. to 215 lbs. absolute pressure flows into the atmosphere, at a velocity averaging about 900 feet per second, as calculated for constant density,—that is to say, on the assumption that the steam does not expand in the course of the outflow. It actually expands and attains a velocity by expansion averaging 1450 feet per second.

*Equivalent Weight of Steam formed from and at 212° F.*—Let  $w$  = the weight of water evaporated per pound of a fuel, from water supplied at the temperature  $t$ , into steam of the total heat  $H$ , measured from 32° F. Let  $w'$ ,  $t'$ , and  $H'$ , be the corresponding values for steam of any other pressure. Then the total heat expended in evaporating 1 pound of water is  $H + 32 - t$ , or  $H' + 32 - t'$ ; and

$$w' = w \frac{H + 32 - t}{H' + 32 - t'} \quad (1)$$

Let  $H'$  be the total heat of steam generated at 212° F., or 1146 units; and  $t' = 212°$  E. By substitution and reduction,

$$w' = w \frac{H + 32 - t}{966} \quad (2)$$

in which  $w'$  is the equivalent weight of water evaporated from and at 212° F.

**RULE.**—To find the equivalent weight of water evaporated from and at 212° F., when a given weight of water is supplied at a given temperature, and evaporated under a given pressure.—Find in Table 271, the total heat of the steam generated at the given absolute pressure; add 32 to it, and from the sum subtract the temperature of the feed-water; divide the remainder by 966, and multiply the quotient by the given weight of water. The product is the equivalent weight of water as evaporated from and at 212° F.

### Moisture or Priming in Steam.

Blow a quantity of the so-called steam into a vessel holding a given weight of cold water: noting the pressure and the

weight of the steam blown in, and the initial and final temperatures of the mixture. An addition is to be made to the initial weight of water, to represent the weight of water equivalent to that of the vessel containing the water, in terms of their respective specific heats. A corresponding addition is to be made for such portion of the apparatus as is immersed in the water.

Let  $W$  = weight of condensing water, plus the equivalent weight of the receiver and apparatus immersed in the water.

$w$  = weight of nominal steam discharged into the vessel under water.

$W + w$  = gross weight of mixture of nominal steam and condensing water.

$H$  = total heat of one pound of the steam, reckoned from the temperature of the condensing water.

$Hw$  = total heat delivered by the gross weight of nominal steam discharged, taken as dry steam.

$t$  = initial temperature of condensing water.

$t'$  = final do. do. do.

$s$  = augmentation of specific heat of water due to rise of temperature.

$L$  = latent heat of one pound of steam of the given initial pressure.

$Lw$  = latent heat of steam discharged into the vessel, taking it as dry steam.

$P$  = weight of priming or moisture in percentage of the gross weight of nominal steam.

$$P = 100 \frac{Hw - [(W + w) \times (t' - t + s)]}{Lw} \quad . \quad . \quad . \quad (3)$$

**RULE.**—*To determine the proportion of moisture or priming in steam.*—To the rise of temperature add the augmentation of specific heat of the water. Multiply the gross weight of nominal steam and condensing water by this sum, and deduct the product from the constituent or total heat of the weight discharged into the vessel, taken as dry steam; and reckoned from the temperature of the condensing water. Multiply the remainder by 100, and divide by the latent heat of the steam taken as dry. The quotient is the proportion of water in percentage of the gross weight of nominal steam.

If there be no remainder, the steam is taken as dry. If, on the contrary, the product be greater than the constituent heat, the difference is evidence of superheated steam, the percentage quantity of which is found by multiplying it by 100, and dividing by the given constituent heat.

TABLE 274.—SATURATED STEAM.

Absolute Pressure per Square Inch.	Temperatures.	Total Latent Heat of Steam from Water supplied at 32° F.	Water-heat of Steam (to raise Temperature of Water from 32° F.).	Total Heat of One Pound of Steam from Water supplied at 32° F.	Density, or Weight of One Cubic Foot of Steam.	Volume of One Pound of Steam.	Relative Volume, or Cubic Feet of Steam from One Cubic Foot of Water.
1.	2.	6.	7.	3.	8.	9.	10.
Lbs.	° Fahr.	Units.	Units.	Units.	Lbs.	Cub. Ft.	Rel. Vol.
0.5	80.2	1058.4	47.1	1105.5	.001376	726.608	45307.5
1	102.1	1042.9	69.6	1112.5	.003027	330.360	20599.1
1.5	115.9	1033.2	83.5	1116.7	.004433	225.580	14066.1
2	126.3	1025.8	93.9	1119.7	.005811	172.080	10730.0
2.5	134.6	1019.9	102.6	1122.5	.007169	139.488	8697.8
3	141.6	1015.0	109.6	1124.6	.008511	117.500	7326.5
3.5	147.7	1010.6	115.8	1126.4	.009839	101.632	6337.3
4	153.1	1006.8	121.3	1128.1	.01116	89.632	5589.0
4.5	157.9	1003.4	126.2	1129.6	.01246	80.231	5002.6
5	162.3	1000.3	130.6	1130.9	.01370	72.991	4551.3
5.5	166.4	997.4	134.7	1132.1	.01505	66.428	4142.1
6	170.2	994.7	138.6	1133.3	.01634	61.201	3816.2
6.5	173.6	992.3	142.0	1134.3	.01762	56.761	3539.3
7	176.9	990.0	145.3	1135.3	.01889	52.936	3300.9
7.5	180.0	987.8	148.5	1136.3	.02016	49.610	3093.4
8	182.9	985.7	151.5	1137.2	.02142	46.686	2911.1
8.5	185.7	983.8	154.2	1138.0	.02268	44.097	2749.7
9	188.3	981.9	156.9	1138.8	.02394	41.777	2605.0
9.5	190.8	980.1	159.4	1139.5	.02517	39.261	2448.1
10	193.3	978.4	161.9	1140.3	.02642	37.845	2359.8
10.5	195.6	976.7	164.3	1141.0	.02767	36.145	2253.8
11	197.8	975.2	166.5	1141.7	.02890	34.599	2157.4
11.5	200.1	973.6	168.8	1142.4	.03026	33.045	2060.5
12	202.0	972.2	170.8	1143.0	.03137	31.879	1987.7
12.5	204.0	970.8	172.8	1143.6	.03260	30.678	1913.0
13	205.9	969.4	174.8	1144.2	.03382	29.573	1844.0
13.5	207.8	968.1	176.7	1144.8	.03504	28.536	1779.4
14	209.6	966.8	178.5	1145.3	.03627	27.573	1719.1
14.7	212.0	965.2	180.9	1146.1	.03797	26.360	1642.0
15	213.1	964.3	182.1	1146.4	.03870	25.843	1611.6
16	216.3	962.1	185.3	1147.4	.04112	24.320	1516.3
17	219.6	959.8	188.5	1148.3	.04253	23.513	1466.1
18	222.4	957.7	191.5	1149.2	.04594	21.766	1357.4
-	225.3	955.7	194.4	1150.1	.04834	20.687	1290.0



TABLE 274.—SATURATED STEAM (*continued*).

Absolute Pressure per Square Inch.	Temperatures.	Total Latent Heat of Steam from Water supplied at 32° F.	Water-heat of Steam (to raise Temperature of Water from 32° F.).	Total Heat of One Pound of Steam from Water supplied at 32° F.	Density, or Weight of One Cubic Foot of Steam.	Volume of One Pound of Steam.	Relative Volume, or Cubic Feet of Steam from One Cubic Foot of Water.
1.	2.	6.	7.	3.	8.	9.	10.
Lbs.	° Fahr.	Units.	Units.	Units.	Lbs.	Cub. Ft.	Rel. Vol.
20	228.0	953.8	197.1	1150.9	.05074	19.710	1229.0
21	230.6	951.9	199.8	1151.7	.05311	18.828	1174.0
22	233.1	950.2	202.3	1152.5	.05549	18.022	1123.8
23	235.5	948.5	204.7	1153.2	.05786	17.282	1077.6
24	237.8	946.9	207.0	1153.9	.06023	16.603	1035.2
25	240.1	945.3	209.3	1154.6	.06259	15.977	996.2
26	242.3	943.7	211.6	1155.3	.06495	15.401	960.2
27	244.4	942.2	213.6	1155.8	.06728	14.863	926.8
28	246.4	940.8	215.6	1156.4	.06971	14.345	894.5
29	248.4	939.4	217.7	1157.1	.07196	13.896	866.5
30	250.4	937.9	219.9	1157.8	.07430	13.459	839.2
31	252.2	936.7	221.7	1158.4	.07663	13.050	813.7
32	254.1	935.3	223.6	1158.9	.07894	12.666	789.8
33	255.9	934.0	225.5	1159.5	.08128	12.300	767.1
34	257.6	932.8	227.2	1160.0	.08358	11.964	746.0
35	259.3	931.6	228.9	1160.5	.08590	11.640	725.9
36	260.9	930.5	230.5	1161.0	.08821	11.337	706.9
37	262.6	929.3	232.2	1161.5	.09050	11.050	689.0
38	264.2	928.2	233.8	1162.0	.09282	10.773	671.7
39	265.8	927.1	235.4	1162.5	.09510	10.515	655.6
40	267.3	926.0	236.9	1162.9	.09740	10.267	640.2
41	268.7	924.9	238.5	1163.4	.09946	10.054	626.9
42	270.2	923.9	239.9	1163.8	.1020	9.806	611.4
43	271.6	922.9	241.3	1164.2	.1042	9.592	598.1
44	273.0	921.9	242.7	1164.6	.1065	9.386	585.3
45	274.4	920.9	244.2	1165.1	.1088	9.191	573.1
46	275.8	919.9	245.6	1165.5	.1111	9.003	561.4
47	277.1	919.0	246.9	1165.9	.1134	8.821	550.0
48	278.4	918.1	248.2	1166.3	.1156	8.650	539.3
49	279.7	917.2	249.5	1166.7	.1179	8.482	528.9
50	281.0	916.3	250.8	1167.1	.1202	8.322	518.9
51	282.3	915.4	252.1	1167.5	.1224	8.170	509.4
52	283.5	914.5	253.4	1167.9	.1247	8.021	500.2
53	284.7	913.6	254.7	1168.3	.1269	7.880	491.1

TABLE 274.—SATURATED STEAM (*continued*).

Absolute Pressure per Square Inch.	Temperatures.	Total Latent Heat of Steam from Water supplied at 32° F.	Water-heat of Steam (to raise Temperature of Water from 32° F.).	Total Heat of One Pound of Steam from Water supplied at 32° F.	Density, or Weight of One Cubic Foot of Steam.	Volume of One Pound of Steam.	Relative Volume, or Cubic Feet of Steam from One Cubic Foot of Water.
1.	2.	6.	7.	3.	8.	9.	10.
Lbs.	° Fahr.	Units.	Units.	Units.	Lbs.	Cub. Ft.	Rel. Vol.
54	285.9	912.8	255.8	1168.6	.1292	7.741	482.7
55	287.1	912.0	257.0	1169.0	.1314	7.610	474.5
56	288.2	911.2	258.1	1169.3	.1337	7.482	466.5
57	289.3	910.4	259.3	1169.7	.1357	7.370	459.5
58	290.4	909.6	260.4	1170.0	.1382	7.238	451.3
59	291.6	908.8	261.6	1170.4	.1404	7.123	444.2
60	292.7	908.0	262.7	1170.7	.1426	7.011	437.2
61	293.8	907.2	263.9	1171.1	.1449	6.902	430.4
62	294.8	906.4	265.0	1171.4	.1471	6.798	423.9
63	295.9	905.6	266.1	1171.7	.1493	6.696	417.5
64	296.9	904.9	267.1	1172.0	.1516	6.596	411.3
65	298.0	904.2	268.1	1172.3	.1538	6.502	405.4
66	299.0	903.5	269.1	1172.6	.1560	6.410	399.7
67	300.0	902.8	270.1	1172.9	.1583	6.318	394.0
68	300.9	902.1	271.1	1173.2	.1604	6.233	388.7
69	301.9	901.4	272.1	1173.5	.1627	6.147	383.3
70	302.9	900.8	273.0	1173.8	.1650	6.059	377.8
71	303.9	900.3	273.8	1174.1	.1671	5.984	373.1
72	304.8	899.6	274.7	1174.3	.1693	5.905	368.2
73	305.7	898.9	275.7	1174.6	.1716	5.829	363.5
74	306.5	898.2	276.7	1174.9	.1738	5.754	358.8
75	307.5	897.5	277.7	1175.2	.1760	5.683	354.4
76	308.4	896.8	278.6	1175.4	.1782	5.610	349.8
77	309.3	896.1	279.6	1175.7	.1803	5.544	345.7
78	310.2	895.5	280.5	1176.0	.1826	5.476	341.5
79	311.1	894.9	281.4	1176.3	.1848	5.411	337.4
80	312.0	894.3	282.2	1176.5	.1870	5.348	333.5
81	312.8	893.7	283.1	1176.8	.1892	5.286	329.6
82	313.6	893.1	284.0	1177.1	.1912	5.230	326.1
83	314.5	892.5	284.9	1177.4	.1936	5.167	322.2
84	315.3	892.0	285.6	1177.6	.1957	5.109	318.5
85	316.1	891.4	286.5	1177.9	.1980	5.052	315.0
86	316.9	890.8	287.3	1178.1	.2001	4.996	311.5
	317.8	890.2	288.2	1178.4	.2023	4.942	308.2

TABLE 274.—SATURATED STEAM (*continued*).

Absolute Pressure per Square Inch.	Temperatures.	Total Latent Heat of Steam from Water supplied at 32° F.	Water-heat of Steam (to raise Temperature of Water from 33° F.).	Total Heat of One Pound of Steam from Water supplied at 32° F.	Density, or Weight of One Cubic Foot of Steam.	Volume of One Pound of Steam.	Relative Volume, or Cubic Feet of Steam from One Cubic Foot of Water.
1	2.	6.	7.	3.	8.	9.	10.
Lbs.	° Fahr.	Units.	Units.	Units.	Lbs.	Cub. Ft.	Rel. Vol.
88	318.6	889.6	289.0	1178.6	.2046	4.889	304.8
89	319.4	889.0	289.9	1178.9	.2067	4.837	301.6
90	320.2	888.5	290.6	1179.1	.2088	4.790	298.6
91	321.0	887.9	291.4	1179.3	.2111	4.737	295.4
92	321.7	887.3	292.2	1179.5	.2133	4.688	292.3
93	322.5	886.8	293.0	1179.8	.2154	4.642	289.4
94	323.3	886.3	293.7	1180.0	.2176	4.595	286.5
95	324.1	885.8	294.5	1180.3	.2198	4.549	283.7
96	324.8	885.2	295.3	1180.5	.2220	4.505	280.9
97	325.6	884.6	296.2	1180.8	.2241	4.462	278.2
98	326.3	884.1	296.9	1181.0	.2263	4.419	275.5
99	327.1	883.6	297.6	1181.2	.2286	4.375	272.8
100	327.9	883.1	298.3	1181.4	.2307	4.335	270.3
101	328.5	882.6	299.0	1181.6	.2329	4.305	267.8
102	329.1	882.1	299.7	1181.8	.2350	4.256	265.4
103	329.9	881.6	300.4	1182.0	.2372	4.216	262.9
104	330.6	881.1	301.1	1182.2	.2393	4.178	260.5
105	331.3	880.7	301.7	1182.4	.2415	4.140	258.2
106	331.9	880.2	302.4	1182.6	.2437	4.104	255.9
107	332.6	879.7	303.1	1182.8	.2458	4.068	253.6
108	333.3	879.2	303.8	1183.0	.2480	4.033	251.4
109	334.0	878.7	304.6	1183.3	.2502	3.998	249.3
110	334.6	878.3	305.2	1183.5	.2523	3.963	247.1
111	335.3	877.8	305.9	1183.7	.2545	3.930	245.0
112	336.0	877.3	306.6	1183.9	.2566	3.897	243.0
113	336.7	876.8	307.3	1184.1	.2588	3.865	241.0
114	337.4	876.3	308.0	1184.3	.2610	3.832	238.9
115	338.0	875.9	308.6	1184.5	.2631	3.801	237.0
116	338.6	875.5	309.2	1184.7	.2653	3.770	235.0
117	339.3	875.0	309.9	1184.9	.2674	3.740	233.2
118	339.9	874.5	310.6	1185.1	.2696	3.710	231.3
119	340.5	874.1	311.2	1185.3	.2717	3.681	229.5
120	341.1	873.7	311.7	1185.4	.2738	3.652	227.7
121	341.8	873.2	312.4	1185.6	.2760	3.623	225.9

TABLE 274.—SATURATED STEAM (*continued*).

Absolute Pressure per Square Inch.	Temperatures.	Total Latent Heat of Steam from Water supplied at 32° F.	Water-heat of Steam (to raise Temperature of Water from 32° F.).	Total Heat of One Pound of Steam from Water supplied at 32° F.	Density, or Weight of One Cubic Foot of Steam.	Volume of One Pound of Steam.	Relative Volume, or Cubic Feet of Steam from One Cubic Foot of Water.
1.	2.	6.	7.	3.	8.	9.	10.
Lbs.	° Fahr.	Units.	Units.	Units.	Lbs.	Cub. Ft.	Rel. Vol.
122	342.4	872.8	313.0	1185.8	2781	3.595	224.2
123	343.0	872.3	313.7	1186.0	2803	3.567	222.4
124	343.6	871.9	314.3	1186.2	2824	3.541	220.8
125	344.2	871.5	314.9	1186.4	2846	3.514	219.1
126	344.8	871.1	315.5	1186.6	2867	3.488	217.5
127	345.4	870.7	316.1	1186.8	2889	3.462	215.8
128	346.0	870.2	316.7	1186.9	2910	3.436	214.3
129	346.6	869.8	317.3	1187.1	2931	3.411	212.7
130	347.2	869.4	317.9	1187.3	2951	3.388	211.3
131	347.8	869.0	318.5	1187.5	2974	3.362	209.7
132	348.3	868.6	319.0	1187.6	2996	3.338	208.1
133	348.9	868.2	319.6	1187.8	3017	3.315	206.7
134	349.5	867.8	320.2	1188.0	3038	3.291	205.2
135	350.1	867.4	320.8	1188.2	3060	3.268	203.8
136	350.6	867.0	321.3	1188.3	3080	3.246	202.4
137	351.2	866.6	321.9	1188.5	3102	3.224	201.0
138	351.8	866.2	322.5	1188.7	3123	3.201	199.6
139	352.4	865.8	323.1	1188.9	3145	3.180	198.3
140	352.9	865.4	323.6	1189.0	3166	3.159	197.0
141	353.5	865.0	324.2	1189.2	3187	3.138	195.6
142	354.0	864.6	324.8	1189.4	3209	3.117	194.3
143	354.5	864.2	325.4	1189.6	3230	3.096	193.1
144	355.0	863.9	325.8	1189.7	3251	3.076	191.8
145	355.6	863.5	326.4	1189.9	3272	3.056	190.6
146	356.1	863.1	326.9	1190.0	3293	3.037	189.4
147	356.7	862.7	327.5	1190.2	3315	3.017	188.1
148	357.2	862.3	328.0	1190.3	3336	2.998	186.9
149	357.8	861.9	328.6	1190.5	3357	2.979	185.7
150	358.3	861.5	329.2	1190.7	3378	2.960	184.6
151	359.0	861.1	329.8	1190.9	3400	2.941	183.4
152	359.5	860.7	330.3	1191.0	3421	2.923	182.2
153	360.0	860.4	330.8	1191.2	3442	2.905	181.2
154	360.5	860.0	331.4	1191.4	3463	2.887	180.0
155	361.1	859.6	331.9	1191.5	3484	2.870	179.0

TABLE 274.—SATURATED STEAM (*continued*).

Absolute Pressure per Square Inch.	Temperatures.	Total Latent Heat of Steam from Water supplied at 32° F.	Water-heat of Steam (to raise Temperature of Water from 32° F.).	Total Heat of One Pound of Steam from Water supplied at 32° F.	Density, or Weight of One Cubic Foot of Steam.	Volume of One Pound of Steam.	Relative Volume, or Cubic Feet of Steam from One Cubic Foot of Water.
1.	2.	6.	7.	3.	8.	9.	10.
Lbs.	° Fahr.	Units.	Units.	Units.	Lbs.	Cub. Ft.	Rel. Vol.
156	361.6	859.2	332.5	1191.7	.3505	2.853	177.9
157	362.1	858.9	332.9	1191.8	.3527	2.836	176.8
158	362.6	858.5	333.5	1192.0	.3548	2.818	175.7
159	363.1	858.1	334.0	1192.1	.3569	2.802	174.7
160	363.6	857.8	334.5	1192.3	.3590	2.785	173.7
165	366.0	856.2	336.7	1192.9	.3696	2.706	168.7
170	368.2	854.5	339.2	1193.7	.3801	2.631	164.1
175	370.8	852.9	341.5	1194.4	.3905	2.559	159.7
180	372.9	851.3	343.8	1195.1	.4011	2.493	155.5
185	375.3	849.6	346.2	1195.8	.4115	2.430	151.5
190	377.5	848.0	348.5	1196.5	.4220	2.370	147.8
195	379.7	846.5	350.7	1197.2	.4324	2.313	144.2
200	381.7	845.0	352.8	1197.8	.4419	2.263	141.1

## STEAM ENGINES AND BOILERS.

## Steam Engines.

The work of steam in the cylinder is in two parts :—the work during admission, and the work done during expansion after the steam is cut off.

The absolute work done during admission is,

$$aPl, \text{ or a } P(l' - c) \quad (1)$$

The absolute work done during expansion to the end of the stroke, is,

$$aPl + \text{hyp. log. } R' \quad (2)$$

Here, for purposes of calculation, the hyperbolic law of expansion is assumed; according to which the pressure varies inversely as the volume.

The sum for these two quantities gives the total absolute work for one stroke : or, by reduction,

$$w = aP[l'(1 + \text{hyp. log. } R') - c] \quad (')$$



In practice, the value ( $p-p'$ ) may be taken by direct measurements of the net area of pressure circumscribed by the diagram.

TABLE 275.—WORK OF ONE POUND OF STEAM IN THE CYLINDER.

Point of Admission, or Cut-off.		Total Absolute Work done.	Steam per Total Absolute Horse- Power per Hour.	Average Total Pres- sure, that for 100 per cent. Admission being 1·000.	Net Capacity of Cylinder per lb. of 100 lbs. Steam (absolute pressure) ad- mitted in one Stroke.
Per cent.	Fraction.	Ft. Lbs.	Pounds.		Cubic Feet.
90	or $\frac{9}{10}$	63,850	31·0	·996	4·45
80	" $\frac{4}{5}$	70,246	28·2	·980	4·98
75	" $\frac{3}{4}$	73,513	26·9	·969	5·26
70	" $\frac{2}{3}$	77,242	25·6	·953	5·63
66·6	" $\frac{2}{3}$	79,555	24·9	·942	5·87
62·5	" $\frac{5}{8}$	83,055	23·8	·925	6·23
60	" $\frac{1}{2}$	85,125	23·3	·913	6·47
55	" $\frac{1}{2}$	89,357	22·2	·888	6·98
50	" $\frac{1}{2}$	94,200	21·0	·860	7·61
45	" $\frac{1}{2}$	98,849	20·0	·827	8·30
40	" $\frac{2}{5}$	104,406	19·0	·787	9·23
37·6	" $\frac{2}{5}$	107,050	18·5	·766	9·71
33·3	" $\frac{1}{3}$	112,220	17·7	·726	10·72
30	" $\frac{3}{10}$	116,885	16·9	·692	11·74
25	" $\frac{1}{4}$	124,066	16·0	·637	13·56
20	" $\frac{1}{5}$	132,770	14·9	·567	16·19
16·7	" $\frac{1}{6}$	138,130	14·34	·526	18·21
14·3	" $\frac{1}{7}$	142,180	13·92	·488	20·23
12·5	" $\frac{1}{8}$	146,325	13·53	·457	22·25
11·1	" $\frac{1}{9}$	148,940	13·29	·432	23·87
10·0	" $\frac{1}{10}$	151,370	13·08	·413	25·49
9·0	" $\frac{1}{11}$	152,595	12·98	·398	26·71
8·3	" $\frac{1}{12}$	155,200	12·75	·381	28·33
7·7	" $\frac{1}{13}$	156,960	12·61	·369	29·54
7·1	" $\frac{1}{14}$	157,975	12·53	·357	30·76
6·7	" $\frac{1}{15}$	158,414	12·25	·348	31·57
6·4	" $\frac{1}{16}$	159,433	11·83	·342	32·38

The absolute work done by one pound of steam of absolute pressure varying from 65 lbs. to 160 lbs., worked expansively, with the consumption per absolute horse-power are given approximately in the Table 275. No correction need be made

for clearance space, nor for the resistance of compression, as the period of compression can be so adjusted that the loss by resistance is compensated by the gain of exhaust steam shut into the cylinder. But, for the back pressure of exhaust, whether from the condenser or from the atmosphere, suitable allowance is to be made. The pressure during admission into the cylinder is supposed to be uniform; and the steam is supposed to be expanded to the end of the stroke.

The values in the last column.—net capacity per pound of steam of 100 lbs. absolute pressure per square inch—are to be modified for steam of other pressures in the ratio of the volume of 100 lbs. steam to that of steam of other pressures. The multipliers are here given for absolute pressures of from 65 lbs. to 160 lbs. :—

Pressures.	Multipliers.	Pressures.	Multipliers.	Pressures.	Multipliers.
Lbs.		Lbs.		Lbs.	
65	1.50	90	1.11	130	.781
70	1.40	95	1.05	140	.730
75	1.31	100	1.00	150	.683
80	1.24	110	.917	160	.644
85	1.17	120	.843		

The effective mean pressure in ordinary non-condensing cylinders, with ordinary slide-valve and excentric motion, or a like motion, working at average speeds, is given approximately by the equation :—

$$p = 13.5 \sqrt{a} - 28 \quad . \quad . \quad . \quad (9)$$

$p$  = effective mean pressure, in per cent. of the maximum pressure of admission.

$a$  = period of admission, in per cent. of the length of stroke.

For a speed of 560 feet of piston per minute, the formula is applicable without material error. For lower speeds, the values of the effective mean pressures are slightly too small; and for higher speeds slightly too great. The rule applies without material error to periods of admission of from 10 per cent. to 75 per cent., and to maximum pressures in the cylinder of from 60 lbs. to 100 lbs. or even 150 lbs. per square inch.

The Table 276 has been calculated by means of the above formula :—



TABLE 276.—EFFECTIVE MEAN PRESSURES IN NON-CONDENSING CYLINDER, FOR VARIOUS PERIODS OF ADMISSION, FROM PRACTICE.

("Railway Machinery.")

Period of Admission, in per cent. of the Stroke.	Effective Mean Pressure, in per cent. of Maximum Pressure.	Period of Admission, in parts of the Stroke.	Effective Mean Pressure, in parts of Maximum Pressure.
Per Cent.	Per Cent.	Fraction.	Fraction.
10	15	1-10th	1-7th fully
12.5	20	1-8th	1-5th
15	24	...	...
17.5	28	1-6th	1-4th
20	32	1-5th	1-3rd
25	40	1-4th	1-2.5th part
30	46	...	...
35	52	1-3rd	1-2nd
40	57	...	...
45	62	...	...
50	67	1-2nd	2-3rds
55	72	...	...
60	77	...	...
65	81	2-3rds	4-5ths
70	85	...	...
75	89	3-4ths	9-10ths

When gaseous steam is expanded in the cylinder, it follows approximately the adiabatic law, the essential condition of which is that the cylinder should be non-conductive. The formula for gaseous steam is as follows:—

$$P' = P \times \left(\frac{r'}{r}\right)^{1.284} \quad . \quad . \quad . \quad . \quad . \quad . \quad (10)$$

$P$  = absolute pressure, say in pounds per square inch, for the given volume  $V$ .

$P'$  = absolute pressure, in pounds per square inch, for any other volume  $V'$ .

$V$  = initial volume, say in cubic feet.

$V'$  = volume by expansion, in cubic feet.

Any number of pressures with expansion may be calculated by the formula, and thus the expansion-curve may be determined; for comparison with expansive curves of ordinary practice, using saturated steam.

**Valve Motions.**

In slide-valves for the distribution of the steam in the cylinder—taking an ordinary valve for a three-port cylinder—the lap, or cover, is the length by which the valve when in its middle position, overlaps the steam port at each end; the lead is the length of opening of each steam port for steam at the beginning of the stroke; and the linear advance of the valve is the sum of the lap and the lead. Inside lap is

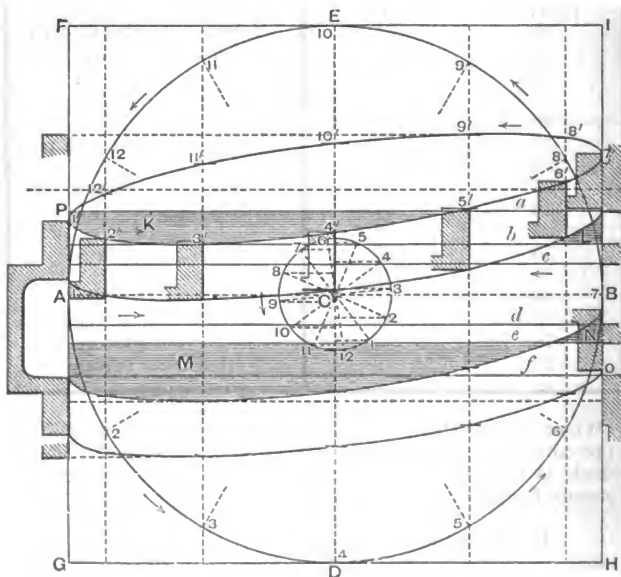


FIG. 79.—Valve-diagram.

occasionally applied to slide-valves; it is the width by which the inner edge of the valve, when the valve is in its middle position, overlaps the inner edge of the steam port. The angular advance is the angle formed by the excentric with its position at its half-stroke, when the piston is at the commencement of its stroke.

The movements of sliding valves worked by an excentric or by an equivalent motion—as that of ordinary expansion link-

motions—may be established by means of diagrams, exemplified by figure 79.

To construct this diagram, draw  $AB$  equal to the length of stroke of the piston, and bisect it at  $C$ . On  $C$  as a centre, with  $CA$  or  $CB$  as a radius, describe a circle representing the path of the crank-pin; and describe also the circle  $DE$  for that of the centre of the excentric. Through  $C$  draw the perpendicular  $DE$ , and construct a square on the large circle. Let the side  $HI$  be taken to represent the ordinary three-ported valve-face of the cylinder, and set off the ports and bars above and below the centre-line  $AB$ , and through the points draw the parallels  $a, b, c, d, e, f$ . The movement of the excentric is taken as horizontal, in the direction  $AB$ , and is directly determined by the position of the centre of the excentric; and that of the valve is for convenience taken as in the direction of  $DE$ . The middle position of the valve is represented by the dot-lines across the diagram parallel to  $AB$ ; which represent its total length, and they overlie the outer edges  $a$  and  $f$  of the steam ports, by a length representing the lap. For the first position of the valve—at the beginning of the stroke—it is placed at a length equal to the linear advance, or the lap plus the lead, from its middle position, as measured on the perpendicular drawn from the corresponding first position of the excentric, No. 1. to the vertical centre-line  $ED$ . Divide both circles into 12 parts, numbered in succession from point No. 1 to point No. 12, and draw radial lines through the points of division, to represent the successive simultaneous positions of the crank and the excentric. The transverse lines drawn through the points of division on the larger circle parallel to  $DE$ , represent the corresponding positions of the piston during the inward and outward strokes; and the perpendiculars drawn to the line  $DE$  from the points of division of the smaller circle, measure the simultaneous longitudinal movements of the excentric, or the distances of the valve-edges above or below their middle positions. These are set off on the ordinates parallel to  $DE$ , and they range in elliptic curves as inscribed on the diagram, representing the whole movements of the valve for a double stroke of the piston, or one revolution of the crank.

Zeuner's valve-diagram fig. 80, affords a simple means of settling the points of the distribution of steam. Draw two lines,  $AB$  and  $CD$ , at right angles, intersecting at  $O$ ; and with the radius  $AO$ , equal to half the travel of the valve, describe the circle  $AB$ , taken to represent the path of the crank-pin. Set off the diameter  $AOa'$ , at the angle  $aOC$ , equal to the angular advance of the excentric; and on the radii  $aO$  and  $Oa'$  describe the circles  $aQ$  and  $Oa'$ . On the

centre  $O$ , with the radius  $O b$ , equal to the outside lap of the valve, describe a circle cutting the circle  $a O$  at  $b$  and  $c$ ; and from these points of intersection, draw the radii  $O f$  and  $O g$ . Draw the diameter  $d O e$  at right angles to the diameter  $a O a'$ . Taking  $A B$  for the stroke of the piston, the point  $f$ , is the position of the crank-pin when the valve opens for lead at

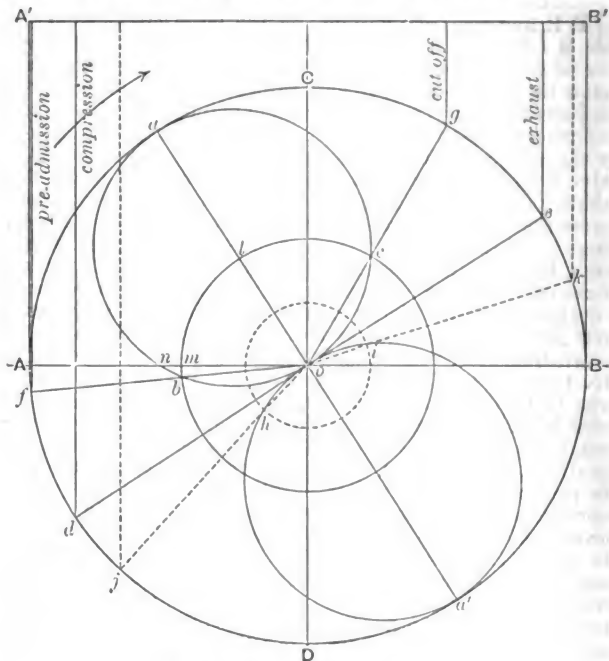


FIG. 80.—Zeuner's Valve-diagram.

$A$ , the beginning of the stroke;  $g$  is the position when the steam is cut off;  $e$  is the position when the valve is opened for exhaust; and  $d$  is the position when the exhaust side of the valve is closed for compression. In this case, there is no inside lap.

For a case of inside lap on the valve, describe the circle  $h i$ , with a radius equal to the inside lap, cutting the circle  $O a'$  at  $h$  and  $i$ , and through these points draw the radii  $O j$ , and  $O k$ . The point  $k$ , in the outer circle, is the position of the crank-

pin when the exhaust is opened, and the point *j* is the position when it is closed for compression.

Draw a parallel *A' B'* to the base-line *A B*, and draw ordinates to it from the several points of the distribution in

TABLE 277.—CORRECTIONS FOR THE POSITION OF THE PISTON, DUE TO THE OBLIQUITY OF THE CONNECTING-ROD.

Distance of Piston from Commencement of Stroke, as represented by the progress longitudinally of the Crank, in percentage of the Stroke.		Corrections for Connecting-Rods of Several Lengths related to the Length of the Crank, in percentages of the Whole Stroke.		
		Four Lengths of Crank.	Six Lengths of Crank.	Eight Lengths of Crank.
Per Cent.	Per Cent.	Per Cent.	Per Cent.	Per Cent.
0	100	0	0	0
2	98	0 $\frac{1}{2}$	0 $\frac{1}{4}$	0 $\frac{1}{4}$
4	96	1	0 $\frac{1}{2}$	0 $\frac{1}{2}$
6	94	1 $\frac{1}{2}$	1	0 $\frac{3}{4}$
8	92	2	1 $\frac{1}{4}$	1
10	90	2 $\frac{1}{4}$	1 $\frac{1}{2}$	1
12	88	2 $\frac{3}{4}$	1 $\frac{3}{4}$	1 $\frac{1}{2}$
14	86	3	2	1 $\frac{1}{2}$
16	84	3 $\frac{1}{2}$	2 $\frac{1}{4}$	1 $\frac{3}{4}$
18	82	3 $\frac{3}{4}$	2 $\frac{1}{2}$	2
20	80	4	2 $\frac{3}{4}$	2
22	78	4 $\frac{1}{2}$	3	2 $\frac{1}{4}$
24	76	4 $\frac{1}{2}$	3	2 $\frac{1}{4}$
26	74	5	3 $\frac{1}{4}$	2 $\frac{1}{2}$
28	72	5	3 $\frac{1}{4}$	2 $\frac{1}{2}$
30	70	5 $\frac{1}{4}$	3 $\frac{1}{2}$	2 $\frac{1}{2}$
32	68	5 $\frac{1}{2}$	3 $\frac{3}{4}$	2 $\frac{3}{4}$
34	66	5 $\frac{3}{4}$	3 $\frac{3}{4}$	3
36	64	6	4	3
38	62	6	4	3
40	60	6	4	3
42	58	6 $\frac{1}{4}$	4	3
44	56	6 $\frac{1}{4}$	4 $\frac{1}{4}$	3
46	54	6 $\frac{1}{4}$	4 $\frac{1}{4}$	3
48	52	6 $\frac{1}{2}$	4 $\frac{1}{4}$	3 $\frac{1}{4}$
50	50	6 $\frac{1}{2}$	4 $\frac{1}{4}$	3 $\frac{1}{4}$

the circle *A B*. The intersections of these ordinates with the parallel *A' B'* give the points of the distribution for the double stroke of the piston.

The distribution is affected by the obliquity of the connect-

ing-rod, insomuch that during the front stroke—that is the stroke made towards the crank—the piston is in advance of its normal position, as represented by the progress longitudinally of the crank-pin ; and during the back stroke, it is behind its normal position. The corrections in per cent. of the stroke are given in Table 277, for three different lengths of connecting-rod, in proportion to the length of the crank. They are additive for front strokes, and subtractive for back strokes. They have been calculated by means of the formula (11) (*Railway Machinery*).

$$x = a r - \sqrt{(a^2 - 1)r^2 + b^2} \quad . \quad . \quad . \quad (11)$$

$a$  = length of connecting-rod in parts of that of the crank.

$b$  = distance of piston from the middle of the stroke as represented by the progress longitudinally of the crank.

$r$  = length of crank.

$x$  = the correction.

### Rules for Valves.

1. *For the angular advance of the excentric.* Divide the linear advance by the half-travel ; the quotient is the sine of the angle of advance ; and the angle, which is acute, may be found in a table of sines.

2. *For the period of admission or point of cut-off.* Divide the lap by the half-travel of the valve ; the quotient is the sine of the angle of the excentric at the instant of cut-off ; the angle is obtuse and is found in a table of sines. From this angle subtract the angle of advance as found by Rule I. ; the difference is the angle of the crank. If this angle is obtuse, add 1 to its cosine ; if acute, subtract it from 1. The product of the sum or the difference by 50, is the percentage of admission.

3. *For the period of compression.* Subtract the cosine of the angle of advance from 1, and multiply by 50, to find the percentage of the period of compression.

These rules may be employed for link-motions ; and generally for all valve-motions based on the motion of excentrics.

By means of the first and second rules, the following table 276, has been calculated with a constant lead,  $\frac{1}{16}$  inch.

When it is desired that the lap, lead, and travel of the slide-valve should bear constant ratios to each other, the following general rule is useful :—

4. Given the travel, to find the lap and lead suitable for an admission of about 75 per cent. of the stroke.

1st for lap, multiply the travel by 22, and divide by 100.

2nd for lead, multiply the travel by 7, and divide by 100.

By this rule, the Table 278, has been calculated.

TABLE 278.—LAP AND LEAD OF SLIDE-VALVES, PROPORTIONED FOR VARIOUS TRAVELS, FOR AN ADMISSION OF ABOUT 75 PER CENT. OF THE STROKE.

Travel of Valve.	Lap.	Lead.	Travel of Valve.	Lap.	Lead.
Inches.	Inches.	Inch.	Inches.	Inches.	Inch.
$1\frac{1}{2}$	33 or $\frac{5}{16}$ $\frac{1}{64}$	10 or $\frac{3}{32}$	$3\frac{1}{4}$	71 or $\frac{11}{16}$ $\frac{1}{64}$	22 or $\frac{3}{16}$ $\frac{1}{32}$
$1\frac{5}{8}$	36 " $\frac{5}{16}$ $\frac{3}{64}$	11 " $\frac{1}{16}$ $\frac{3}{64}$	$3\frac{1}{2}$	77 " $\frac{12}{16}$ $\frac{1}{64}$	24 " $\frac{3}{16}$ $\frac{3}{64}$
$1\frac{3}{4}$	38 " $\frac{6}{16}$	12 " $\frac{1}{8}$	$3\frac{3}{4}$	82 " $\frac{13}{16}$	26 " $\frac{1}{4}$
$1\frac{7}{8}$	41 " $\frac{6}{16}$ $\frac{1}{32}$	13 " $\frac{1}{8}$	4	88 " $\frac{14}{16}$	28 " $\frac{1}{4}$ $\frac{1}{32}$
2	44 " $\frac{7}{16}$	14 " $\frac{1}{8}$ $\frac{1}{64}$	$4\frac{1}{4}$	93 " $\frac{15}{16}$	30 " $\frac{1}{4}$ $\frac{3}{64}$
$2\frac{1}{8}$	47 " $\frac{7}{16}$ $\frac{1}{32}$	15 " $\frac{1}{8}$ $\frac{1}{32}$	$4\frac{1}{2}$	99 " 1.00	31 " $\frac{5}{16}$
$2\frac{1}{4}$	50 " $\frac{8}{16}$	16 " $\frac{1}{8}$ $\frac{1}{32}$	$4\frac{3}{4}$	1.04 " $\frac{1}{16}$ $\frac{3}{64}$	33 " $\frac{5}{16}$ $\frac{1}{64}$
$2\frac{3}{8}$	52 " $\frac{8}{16}$ $\frac{1}{64}$	17 " $\frac{1}{8}$ $\frac{3}{64}$	5	1.10 " $\frac{1}{16}$ $\frac{1}{32}$	35 " $\frac{5}{16}$ $\frac{1}{32}$
$2\frac{1}{2}$	55 " $\frac{9}{16}$ $\frac{1}{64}$	17 " $\frac{1}{8}$ $\frac{3}{64}$	$5\frac{1}{4}$	1.15 " $\frac{1}{8}$ $\frac{1}{32}$	37 " $\frac{3}{8}$
$2\frac{5}{8}$	58 " $\frac{9}{16}$ $\frac{1}{64}$	18 " $\frac{3}{16}$	$5\frac{1}{2}$	1.21 " $\frac{1}{16}$ $\frac{1}{64}$	38 " $\frac{3}{8}$
$2\frac{3}{4}$	60 " $\frac{9}{16}$ $\frac{1}{32}$	19 " $\frac{3}{16}$	$5\frac{3}{4}$	1.26 " $\frac{1}{4}$	40 " $\frac{3}{8}$ $\frac{1}{32}$
$2\frac{7}{8}$	63 " $\frac{10}{16}$	20 " $\frac{3}{16}$ $\frac{1}{64}$	6	1.32 " $\frac{1}{5}$ $\frac{1}{16}$	42 " $\frac{3}{8}$ $\frac{3}{64}$
3	66 " $\frac{10}{16}$ $\frac{1}{32}$	21 " $\frac{3}{16}$ $\frac{1}{64}$	$6\frac{1}{4}$	1.50 " $\frac{1}{2}$	47 " $\frac{7}{16}$ $\frac{1}{32}$

In the Table 279, following, is shown the relative distribution for a slide-valve of the proportions assumed in rule 4, above; with admissions varied from 73.5 per cent. (say 75) to 12 per cent., for the corresponding travels given in the last two columns.

TABLE 279.—DISTRIBUTION FOR VARIOUS TRAVELS OF A VALVE OF STANDARD PROPORTIONS.

Steam Cut-off.	Steam Exhausted.	Point of Compression.	Point of Admission.	Travel of the Valve. Lap 1 Inch. Lead $\frac{1}{16}$ Inch.	
Per Cent.	Per Cent.	Per Cent.	Per Cent.	Inches.	Per Cent. of Maximum Travel.
75	91	9	62	$4\frac{1}{2}$	100
60	86	14	1.10	$3\frac{3}{4}$	83
50	80	20	1.90	$3\frac{3}{8}$	75
40	75	25	2.50	$3\frac{1}{32}$	67
30	68	32	4.35	$2\frac{13}{16}$	62
20	57	43	7.60	$2\frac{11}{16}$	60
12	50	50	12.25	$2\frac{5}{8}$	58.3

TABLE 280. PERIODS OF ADMISSION FOR VARYING TRAVELS AND LAPS OF THE SLIDE-VALVE.

Lead  $\frac{5}{16}$  inch.

Travel.	Lap in Inches.								
	$\frac{1}{2}$	$\frac{5}{8}$	$\frac{3}{4}$	$\frac{7}{8}$	1	$1\frac{1}{8}$	$1\frac{1}{4}$	$1\frac{3}{8}$	$1\frac{1}{2}$
Periods of Admission in Percentages of Stroke.									
Inches.	%.	%.	%.	%.	%.	%.	%.	%.	%.
$1\frac{5}{8}$	19	...	...	...	...	...	...	...	...
$1\frac{3}{4}$	39	...	...	...	...	...	...	...	...
$1\frac{7}{8}$	47	17	...	...	...	...	...	...	...
2	55	34	...	...	...	...	...	...	...
$2\frac{1}{8}$	61	42	14	...	...	...	...	...	...
$2\frac{1}{4}$	65	50	30	...	...	...	...	...	...
$2\frac{3}{8}$	68	55	38	13	...	...	...	...	...
$2\frac{1}{2}$	71	59	45	27	...	...	...	...	...
$2\frac{5}{8}$	74	63	49	36	12	...	...	...	...
$2\frac{3}{4}$	76	67	56	43	26	...	...	...	...
$2\frac{7}{8}$	78	70	59	47	32	11	...	...	...
3	80	73	62	50	38	23	...	...	...
$3\frac{1}{8}$	81	74	65	55	44	30	10	...	...
$3\frac{1}{4}$	83	76	68	59	48	34	22	...	...
$3\frac{3}{8}$	84	78	71	62	51	40	29	9	...
$3\frac{1}{2}$	85	80	73	64	53	45	34	20	...
$3\frac{5}{8}$	86	81	75	66	57	49	38	26	9
$3\frac{3}{4}$	87	82	76	68	60	52	42	32	19
$3\frac{7}{8}$	87	83	78	70	63	55	46	36	25
4	88	84	79	72	66	58	49	40	29
$4\frac{1}{4}$	89	86	81	76	70	63	56	47	37
$4\frac{1}{2}$	90	87	83	79	73	67	61	54	45
$4\frac{3}{4}$	92	89	85	81	76	70	65	58	51
5	93	90	87	83	78	73	67	62	56
$5\frac{1}{2}$	94	92	89	86	82	78	73	68	63
6	95	93	91	88	85	82	78	74	69



TABLE 281.—PERIODS OF ADMISSION, OR POINTS OF CUT-OFF, FOR GIVEN TRAVELS AND LAPS OF SLIDE-VALVES.

Travel of Valve.	Lead of Value.	Periods of Admission, or Points of Cut-off, for the following Laps of Valve, in Inches, in Percentages of Stroke.									
		2	1½	1½	1¼	1	¾	¾	⅝	½	⅜
Inches.	Inch.	%	%	%	%	%	%	%	%	%	%
12	¼	88	90	93	95	96	97	98	98	99	99
10	¼	82	87	89	92	95	96	97	98	98	99
8	¼	72	78	84	88	92	94	95	96	98	98
6	¼	50	62	71	79	86	89	91	94	96	97
5½	⅛	43	56	68	77	85	88	91	94	96	97
5	⅛	32	47	61	72	82	86	89	92	95	97
4½	⅛	14	35	51	66	78	83	87	90	94	96
4	⅛	...	17	39	57	72	78	83	88	92	95
3½	⅛	...	...	20	44	63	71	79	84	90	94
3	⅛	...	...	...	23	50	61	71	79	86	91
2½	⅛	...	...	...	...	27	43	57	70	80	88
2	⅛	...	...	...	...	...	...	33	52	70	81

**Woolf Engine:—Continuous Expansion in two Cylinders.**

The total work for one stroke of the two pistons, may be calculated by the formula (5), page 514, for the work of a single cylinder.

**Receiver Engine:—Successive Expansions in two Cylinders.**

The total work for one stroke of the two pistons, may be calculated by the formula:—

$$w = a P \left[ l' (1 \times \text{hyp. log. } R'') - e \left( 1 \times \frac{r-1}{R'} \right) \right] \quad (12)$$

In the construction of the foregoing formulæ, it is assumed that the line of pressure during admission of steam is straight and parallel to the datum-line; that the expansion curves are hyperbolic to the end of the strokes; that the exhaust is open to the end of the return stroke of the second piston; and that there is no back pressure on it.

The work of back pressure is most directly measured from the indicator diagram, in which the other modifications of performance due to compression, and wiredrawing may also be measured.

**RULE.**—*To find the indicator horse-power of a single-cylinder steam engine, from the indicator diagram.* Multiply the area of the piston in square inches by the effective mean pressure on the piston in pounds per square inch, and by twice the length of the stroke, and by the number of revolutions per minute; and divide the product by 33,000. The quotient is the indicator horse-power.

For compound and multiple-expansion engines, the indicator power in each cylinder is calculated separately; and the sum of the powers thus obtained is the total indicator horse-power. When strokes of the pistons are equal, and if the horse-powers of the cylinders are not required separately, it will suffice to multiply the area of each piston by the effective mean pressure; and to complete the calculation with the sum of these products.

The best performance of steam engines under various conditions, may be accepted approximately to be as follows:—

*Single Cylinders, not steam-jacketed, non-condensing.*—Steam cut off at one-third of the stroke, and consumed at the rate of 26 pounds per indicator horse-power per hour; the effective pressure during admission being 60 lbs. per square inch.

*Single Cylinders, using superheated steam, non-condensing.*—With 80 lbs. effective pressure of steam during admission, cutting off at one-fifth; 18½ pounds of steam consumed per indicator horse-power per hour. For a lower effective mean pressure of 34 lbs. per square inch, cutting off at about 30 per cent. with 130 degrees of superheat, about 30½ pounds of steam are consumed per indicator horse-power per hour.

*Single Cylinders, steam-jacketed, non-condensing.*—With 75 lbs. effective pressure during admission, cutting off at one-fifth, 25 pounds of steam are consumed per indicator horse-power per hour.

*Single Cylinders, with superheated steam, condensing.*—With 65 lbs. effective pressure during admission, and 150 degrees of superheat, cutting off at 22½ per cent. of the stroke, 15½ pounds of steam are consumed per indicator horse-power per hour.

*Single Cylinders, not steam-jacketed, condensing.*—The economical results are affected by the length of the stroke relatively to the diameter. In strokes considerably longer than the diameters, an admission of from 15 per cent. to 20 per cent. is most efficient for economy. With initial steam of 80 lbs. total pressure per square inch, approximately 20 pounds of steam are consumed per indicator horse-power per hour.

For short-stroke cylinders—having strokes considerably shorter than two diameters—with initial steam of 73 lbs. total pressure, approximately 25 pounds of steam are consumed per horse-power.

*Single Cylinders, steam-jacketed, condensing.*—The period of admission most favourable for economy, is from 15 per cent. to 25 per cent. of the stroke. For thoroughly steam-jacketed cylinders, of long strokes, the longer periods of admission are preferable; and for those of short strokes, the shorter periods. For cylinders jacketed only at the sides or barrel, the longer ranges are preferable. With thoroughly steam-jacketed cylinders of long stroke, and steam of 80 lbs. total initial pressure, about  $18\frac{1}{2}$  pounds of steam are consumed per indicator horse-power per hour; and for cylinders of short stroke, 21 pounds.

### **Woolf Compound Steam Engines.**

Proportionally long strokes, compared with proportionally short strokes, are conducive to economy. With a stroke of five diameters, and a total initial pressure of 100 lbs. per square inch, and worked with 12 actual expansions, the work is done for about 14 pounds of steam per indicator horse-power per hour. With a stroke equal to twice the diameter,  $17\frac{1}{2}$  pounds are consumed.

### **Receiver Compound Steam Engines.**

With a stroke equal to from two to three diameters of the first cylinder, for a total initial pressure of from 80 lbs. to 90 lbs. per square inch, cutting off at one-fifth, and ten actual expansions, with thorough jacketing and intermediate heating of steam, the work may be done with a consumption of 15 pounds of steam per indicator horse-power per hour. With shorter strokes—from  $1\frac{1}{4}$  to  $1\frac{1}{2}$  diameters— $18\frac{1}{2}$  pounds are consumed. Without steam-jacketing, the consumption of steam is from 2 pounds to 3 pounds more.

### **Capacity-ratio of Multiple-Expansion Cylinders.**

For speed of piston of from 750 feet to 1000 feet per minute, the capacity-ratios of triple-expansion steam engines, given in the following Table, are recommended. They are based upon a wide range of practice. The terminal absolute pressure of steam in the third cylinder, is supposed to be about 10 lbs. per square inch.

TABLE 282.—TRIPLE - EXPANSION STEAM ENGINES :—  
CAPACITY-RATIOS OF CYLINDERS RECOMMENDED.

(Jay M. Whitham.)

Gauge Pressure per Square Inch in the Boiler.	Capacity-Ratios of Cylinders.		
	1st (Small).	2nd (Intermediate).	3rd (Large).
Pounds.	Ratio.	Ratio.	Ratio.
130	1	2.25	5.00
140	1	2.40	5.85
150	1	2.55	6.90
160	1	2.70	7.25
170 and upwards }	Quadruple expansion to be adopted.		

For quadruple expansion, with steam of, say, 180 lbs. per square inch, capacity-ratios of four cylinders, taken as 1, 2, 4, 8, are very suitable.

### Efficiency and Frictional Resistance of Steam Engines.

The frictional resistance of steam engines varies inversely as their leading dimensions. A direct-action engine having a 4-inch cylinder, yielded at the main shaft only 43 per cent. of the indicator power, with a frictional resistance of 57 per cent.

Eight horse-power portable engines, having 9-inch cylinders, yield from 78 per cent. to 87 per cent., with from 13 per cent. to 22 per cent. of resistance.

Corliss engines having 18-inch and 24-inch cylinders, yield about 90 per cent. of the indicator power at the main shaft ; with about 10 per cent. of resistance.

Compound engines having first cylinders of from 12 inches to 21 inches in diameter, with or without a beam, yield from 80 per cent. to 89 per cent. of the indicator power.

Rotative pumping steam engines yield from 80 per cent. to 86 per cent. of duty ; Worthington's large pumping engines for waterworks, yield 91 per cent. So also do Cornish pumping engines.

From the results of experiments made by Dr. Thurston, on the distribution of friction in direct-acting non-condensing steam engines having balanced valves, it appears that from 40 per cent. to 47 per cent. of the resistance arises at the main bearings ; about 33 per cent. at the piston and its rod, 7 per cent. at the crank-pin,  $5\frac{1}{2}$  per cent. at the crosshead and

gudgeon,  $2\frac{1}{2}$  per cent. at the valve and its rod,  $5\frac{1}{4}$  per cent. at the excentric-strap. An unbalanced valve absorbed  $26\frac{1}{2}$  per cent. of the whole resistance. In a condensing engine, the air-pump caused 12 per cent. of the resistance.

The frictional resistance of a steam engine increases very slowly with the load. In some cases, the load may be doubled whilst the resistance is increased by only one-fifth.

### Lancashire Steam Boiler—Standard Data.

*Boiler of Wrought-iron.*—Shell 7 feet in diameter, 27 feet long; two furnace-tubes, 2 feet 9 inches in diameter. Shell plates  $\frac{7}{16}$  inch thick for a working steam pressure of 75 lbs. per square inch;  $\frac{9}{16}$  inch thick for 100 lbs. pressure. Plates of furnace-tubes,  $\frac{3}{8}$  inch and  $\frac{7}{16}$  inch respectively.

Fire-grates 6 feet long; fire-bars  $\frac{3}{4}$  inch thick; air-spaces between fire-bars,  $\frac{3}{8}$  inch wide.

Height of flue-way over each bridge, 14 inches; side flues 6 inches wide at the top; width of bottom flue equal to the semi-diameter of the boiler, or  $3\frac{1}{4}$  feet. The draught passes from the furnace-tubes to the bottom flue, thence by the sides to the back.

The grate-area is  $16\frac{1}{2}$  square feet for one furnace, or 33 square feet for both furnaces. The air-space through each grate is  $5\frac{1}{2}$  square feet, or one-third of the grate-area.

The flue-way over each bridge is 1.88 square feet, or  $11\frac{1}{2}$  per cent. of the grate-area—about  $\frac{1}{4}$ th.

Each furnace-tube has 5.94 square feet of sectional area beyond the bridge=nearly one-third of the grate-area.

The bottom flue has 7 square feet of sectional area, or fully one-fifth of the whole grate-area.

The side flues have a united area of  $12\frac{1}{2}$  square feet, or nearly two-fifths of the whole grate-area.

The weight of the boiler is about 12 tons; with fittings,  $15\frac{1}{2}$  tons. The cost is about £425, or about £27 8s. per ton, or £16 per lineal foot.

The heating surface is 850 square feet, or 26 times the grate-area. The heating surface is augmented by feed-water heaters, occasionally to the extent of three-fourths. In such a boiler, from 15 tons to 20 tons of coal may, without undue stress, be consumed per week of 60 hours, or from 5 cwt. to  $6\frac{1}{4}$  cwt. per hour, or from 17 lbs. to 23 lbs. per square foot of fire-grate per hour. At the rate of 8 pounds of water per pound of coal, this corresponds to an evaporation of from 70 to 90 cubic feet of water per hour.

In the best practice, iron boiler-plates have a tensile strength of from 24 to 25 tons per square inch, with an elongation



The side of a square chimney equal in sectional area to a given round chimney, is equal to the product of the diameter by  $\cdot 886$ ; and the equivalent fraction of the height for the side of a square chimney is one thirty-fourth.

Conversely, the diameter of a round chimney equal in sectional area to a given square chimney, is equal to the product of the side of the square by  $1\cdot13$ .

In Table 283, are given the quantity of coals that may be consumed per hour, at the assumed rate of 15 pounds per square foot per hour, and the corresponding total area of fire-grate, for chimneys of various heights, and corresponding diameters one-thirtieth of the respective heights.

TABLE 283.—FACTORY CHIMNEYS.—COAL CONSUMPTION.

Chimney.				Chimney.			
Height.	Dia- meter.	Coal Con- sumable per Hour.	Grate Area.	Height.	Dia- meter.	Coal Con- sumable per Hour.	Grate Area.
Feet.	Ft. Ins.	Pounds.	Sq. Ft.	Feet.	Ft. Ins.	Pounds.	Sq. Ft.
40	1 4	142	9·5	110	3 8	1777	118·4
50	1 8	248	16·5	120	4 0	2208	147·2
60	2 0	390	26·0	135	4 6	2964	197·6
70	2 4	574	38·3	150	5 0	3858	257·2
80	2 8	801	53·4	165	5 6	4896	326·4
90	3 0	1076	71·7	180	6 0	6086	405·7
100	3 4	1394	93·0	200	6 8	7920	526·6

TABLE 284.—HORSE-POWER IN VARIOUS COUNTRIES IN  
FOOT-POUNDS PER SECOND.

("Steam.")

Country.	Kilogra- meters per sec.	Baden per sec.	Saxony per sec.	Würtem- berg per sec.
		Foot-lbs.	Foot-lbs.	Foot-lbs.
France and Baden	<b>75</b>	<b>500</b>	529·68	521·58
Saxony . . .	75·045	500·30	<b>530</b>	523·89
Württemberg . .	75·240	501·36	531·12	<b>525</b>
Prussia . . .	75·325	502·17	531·97	525·85
Hanover . . .	75·361	502·41	532·23	526·10
England . . .	76·041	506·94	537·03	530·84
Austria . . .	76·119	507·46	537·58	531·39

TABLE 284.—HORSE-POWER IN VARIOUS COUNTRIES (*con.*).

Country.	Prussian per sec.	Hanoverian per sec.	English per sec.	Austrian per sec.
	Foot-lbs.	Foot-lbs.	Foot-lbs.	Foot-lbs.
France and Baden	477·93	513·53	542·47	423·68
Saxony . . .	478·22	513·84	542·80	423·93
Württemberg . .	479·23	514·92	543·95	424·83
Prussia . . .	<b>480</b>	515·75	544·82	425·51
Hanover . . .	480·23	<b>516</b>	545·08	425·72
England . . .	484·56	520·65	<b>550</b>	429·56
Austria . . .	485·06	521·19	550·57	<b>430</b>

TABLE 285.—ECONOMY OF FUEL BY HEATING THE FEED-WATER.

(For Steam of 60 lbs. per square inch Working Pressure.)

Initial Temperature of Water.	Final Temperature of Feed-Water (Fahrenheit).						
	120°	140°	160°	180°	200°	250°	300°
° Fahr.	%	%	%	%	%	%	%
32	7·50	9·20	10·90	12·36	14·30	19·03	22·90
35	7·25	8·96	10·66	12·09	14·09	18·34	22·60
40	6·85	8·57	10·28	12·00	13·71	17·99	22·27
45	6·45	8·17	9·90	11·61	13·34	17·64	21·94
50	6·05	7·71	9·50	11·23	13·00	17·28	21·61
55	5·64	7·37	9·06	10·85	12·60	16·93	21·27
60	5·23	6·97	8·72	10·46	12·20	16·58	20·92
65	4·82	6·56	8·32	10·07	11·82	16·20	20·58
70	4·40	6·15	7·91	9·08	11·43	15·83	20·23
75	3·98	5·74	7·50	9·28	11·04	15·46	19·88
80	3·55	5·32	7·09	8·87	10·65	15·08	19·52
85	3·12	4·90	6·63	8·46	10·25	14·70	19·17
90	2·68	4·47	6·26	8·06	9·85	14·32	18·81
95	2·24	4·04	5·84	7·65	9·44	13·94	18·44
100	1·80	3·61	5·42	7·23	9·03	13·55	18·07
110	·90	2·73	4·55	3·38	8·20	12·76	17·28
120	0	1·84	3·67	5·52	7·36	11·95	16·49
130	...	·92	2·77	4·64	6·99	11·14	15·24
140	...	0	1·87	3·75	5·62	10·31	14·99
150	...	...	·94	2·83	4·72	9·46	14·18
160	...	...	0	1·91	3·82	8·59	13·37
170	...	...	...	·96	2·89	7·71	12·54
180	...	...	...	0	1·96	6·81	11·70
190	...	...	...	...	·90	5·90	10·82
(20)	...	...	...	...	0	4·85	9·93



TABLE 286.—RELATIVE ECONOMY OF FEED-APPARATUS.  
(Jacobus.)

Feed Water: how Supplied.	Relative Consumption of Coal.	Relative Economy Effected.
Direct-acting pump, feeding water at 60°, without a heater . . . . .	1.000	0.0
Injector feeding water at 150° without a heater . . . . .	.985	1.5 per cent.
Injector feeding through a heater in which the water is heated from 150° to 200° . . . . .	.938	6.2    "
Direct-acting pump, feeding water through a heater, in which it is heated from 60° to 200° . . . . .	.879	12.1    "
Geared pump, run from the engine, feeding water through a heater, in which it is heated from 60° to 200° . . . . .	.808	13.2    "

TABLE 287.—WEIGHT OF SEDIMENT COLLECTED IN A STEAM-BOILER, FROM HARD WATER, EVAPORATED AT THE RATE OF 1000 GALLONS PER DAY.

Solid Matter per Gallon Evaporated.	Solid Matter Collected per Day, from 1000 Gallons of Water Evaporated.	Solid Matter Collected per Week of Six Days, from 6000 Gallons of Water Evaporated.	Solid Matter per Gallon Evaporated.	Solid Matter Collected per Day, from 1000 Gallons of Water Evaporated.	Solid Matter Collected per Week of Six Days, from 6000 Gallons of Water Evaporated.
Grains.	Lbs. Ozs.	Lbs. Ozs.	Grains.	Lbs. Ozs.	Lbs. Ozs.
1	0 2.3	0 13.7	15	2 2.3	12 13.7
2	0 4.6	1 11.4	20	2 13.7	17 2.3
3	0 6.9	2 9.1	25	3 9.1	21 6.9
4	0 9.1	3 6.9	30	4 4.6	25 11.4
5	0 11.4	4 4.6	35	5 0	30 0
6	0 13.7	5 2.3	40	5 11.4	34 4.6
7	1 0	6 0	45	6 6.9	38 9.1
8	1 2.3	6 13.7	50	7 2.3	42 13.7
9	1 4.6	7 11.4	55	7 13.7	47 2.3
10	1 6.9	8 9.1			

TABLE 288.—MULTIPLIERS FOR FINDING THE EQUIVALENT  
FOR GIVEN PRESSURES OF STEAM AND

Temperature of Feed Water.	Boiler Pressures in Pounds per									
	0	5	10	15	20	25	30	35	40	45
° Fahr.										
32	1.187	1.192	1.195	1.199	1.201	1.204	1.206	1.209	1.211	1.212
35	1.184	1.189	1.192	1.196	1.198	1.201	1.203	1.206	1.208	1.209
40	1.179	1.184	1.187	1.191	1.193	1.196	1.198	1.201	1.203	1.204
45	1.173	1.178	1.181	1.185	1.187	1.190	1.192	1.195	1.197	1.198
50	1.168	1.173	1.177	1.180	1.182	1.185	1.187	1.190	1.192	1.193
55	1.163	1.168	1.171	1.175	1.177	1.180	1.182	1.185	1.187	1.188
60	1.158	1.163	1.166	1.170	1.172	1.175	1.177	1.180	1.182	1.183
65	1.153	1.158	1.161	1.165	1.167	1.170	1.172	1.175	1.177	1.178
70	1.148	1.153	1.156	1.160	1.162	1.165	1.167	1.170	1.172	1.173
75	1.143	1.148	1.151	1.155	1.157	1.160	1.162	1.165	1.167	1.168
80	1.137	1.143	1.146	1.149	1.151	1.154	1.156	1.159	1.161	1.162
85	1.132	1.137	1.140	1.144	1.146	1.149	1.151	1.154	1.156	1.157
90	1.127	1.132	1.135	1.139	1.141	1.144	1.146	1.149	1.151	1.152
95	1.122	1.127	1.130	1.134	1.136	1.139	1.141	1.144	1.146	1.147
100	1.117	1.122	1.125	1.129	1.131	1.134	1.136	1.139	1.141	1.142
105	1.111	1.117	1.120	1.123	1.125	1.128	1.130	1.133	1.135	1.136
110	1.106	1.111	1.114	1.118	1.120	1.123	1.125	1.128	1.130	1.131
115	1.101	1.106	1.109	1.113	1.115	1.118	1.120	1.123	1.125	1.126
120	1.096	1.101	1.104	1.108	1.110	1.113	1.115	1.118	1.120	1.121
125	1.091	1.096	1.099	1.103	1.105	1.108	1.110	1.113	1.115	1.116
130	1.085	1.091	1.094	1.097	1.099	1.102	1.104	1.107	1.109	1.110
135	1.080	1.085	1.088	1.092	1.094	1.097	1.099	1.102	1.104	1.105
140	1.075	1.080	1.083	1.087	1.089	1.092	1.094	1.097	1.099	1.100
145	1.070	1.075	1.078	1.082	1.084	1.087	1.089	1.092	1.094	1.095
150	1.065	1.070	1.073	1.077	1.079	1.082	1.084	1.087	1.089	1.090
155	1.059	1.065	1.068	1.071	1.073	1.076	1.078	1.081	1.083	1.084
160	1.054	1.059	1.062	1.066	1.068	1.071	1.073	1.076	1.078	1.079
165	1.049	1.054	1.057	1.061	1.063	1.066	1.068	1.071	1.073	1.074
170	1.044	1.049	1.052	1.056	1.058	1.061	1.063	1.066	1.068	1.069
175	1.039	1.044	1.047	1.051	1.053	1.056	1.058	1.061	1.063	1.064
180	1.033	1.039	1.042	1.045	1.047	1.050	1.052	1.055	1.057	1.058
185	1.028	1.033	1.036	1.040	1.042	1.045	1.047	1.050	1.052	1.053
190	1.023	1.028	1.031	1.035	1.037	1.040	1.042	1.045	1.047	1.048
195	1.018	1.023	1.025	1.030	1.032	1.035	1.037	1.040	1.042	1.043
200	1.013	1.018	1.021	1.025	1.027	1.030	1.032	1.035	1.037	1.038
205	1.008	1.013	1.015	1.020	1.022	1.025	1.027	1.030	1.032	1.033
210	1.008	1.008	1.011	1.015	1.017	1.020	1.022	1.025	1.027	1.028
212	1.002	1.002	...	...	...	...	...	...	...	...

RATE OF EVAPORATION OF WATER FROM AND AT 212° F.,  
TEMPERATURES OF FEED-WATER.

Square Inch above the Atmosphere.

50	60	70	80	90	100	120	140	160	180	200
1.214	1.217	1.219	1.222	1.224	1.227	1.231	1.234	1.237	1.239	1.241
1.211	1.214	1.216	1.219	1.221	1.224	1.228	1.231	1.234	1.236	1.238
1.206	1.209	1.211	1.214	1.216	1.219	1.223	1.226	1.229	1.231	1.233
1.200	1.203	1.205	1.208	1.210	1.213	1.217	1.220	1.223	1.225	1.227
1.195	1.198	1.200	1.203	1.205	1.208	1.212	1.215	1.218	1.220	1.222
1.190	1.193	1.195	1.198	1.200	1.203	1.207	1.210	1.213	1.215	1.217
1.185	1.188	1.190	1.193	1.195	1.198	1.202	1.205	1.208	1.210	1.212
1.180	1.183	1.185	1.188	1.190	1.193	1.197	1.200	1.203	1.205	1.207
1.175	1.178	1.180	1.183	1.185	1.188	1.192	1.195	1.198	1.200	1.202
1.170	1.173	1.175	1.178	1.180	1.183	1.187	1.190	1.193	1.195	1.197
1.164	1.167	1.169	1.172	1.174	1.177	1.181	1.184	1.187	1.189	1.191
1.159	1.162	1.164	1.167	1.169	1.172	1.176	1.179	1.182	1.184	1.186
1.154	1.157	1.159	1.162	1.164	1.167	1.171	1.174	1.177	1.179	1.181
1.149	1.152	1.154	1.157	1.159	1.162	1.166	1.169	1.172	1.174	1.176
1.144	1.147	1.149	1.152	1.154	1.157	1.161	1.164	1.167	1.169	1.171
1.133	1.141	1.143	1.146	1.148	1.151	1.155	1.158	1.161	1.163	1.165
1.133	1.136	1.138	1.141	1.143	1.146	1.150	1.153	1.156	1.158	1.160
1.128	1.131	1.133	1.136	1.138	1.141	1.145	1.148	1.151	1.153	1.155
1.123	1.126	1.128	1.131	1.133	1.136	1.140	1.143	1.146	1.148	1.150
1.118	1.121	1.123	1.126	1.128	1.131	1.135	1.138	1.141	1.143	1.145
1.112	1.115	1.117	1.120	1.122	1.125	1.129	1.132	1.135	1.137	1.139
1.107	1.110	1.112	1.115	1.117	1.120	1.124	1.127	1.130	1.132	1.134
1.102	1.105	1.107	1.110	1.112	1.115	1.119	1.122	1.125	1.127	1.129
1.097	1.100	1.102	1.105	1.107	1.110	1.114	1.117	1.120	1.122	1.124
1.092	1.095	1.097	1.100	1.102	1.105	1.109	1.112	1.115	1.117	1.119
1.086	1.089	1.091	1.094	1.096	1.099	1.103	1.106	1.109	1.111	1.113
1.081	1.084	1.086	1.089	1.091	1.094	1.098	1.101	1.104	1.106	1.108
1.076	1.079	1.081	1.084	1.086	1.089	1.093	1.096	1.099	1.101	1.103
1.071	1.074	1.076	1.079	1.081	1.084	1.088	1.091	1.094	1.096	1.098
1.066	1.069	1.071	1.074	1.076	1.079	1.083	1.086	1.089	1.091	1.093
1.060	1.063	1.065	1.068	1.070	1.073	1.077	1.080	1.083	1.085	1.087
1.055	1.058	1.060	1.063	1.065	1.068	1.072	1.075	1.078	1.080	1.082
1.050	1.053	1.055	1.058	1.060	1.063	1.067	1.070	1.073	1.075	1.077
1.045	1.048	1.050	1.053	1.055	1.058	1.062	1.065	1.068	1.070	1.072
1.040	1.043	1.045	1.048	1.050	1.053	1.057	1.060	1.063	1.065	1.067
1.035	1.038	1.040	1.043	1.045	1.048	1.052	1.055	1.058	1.060	1.062
1.030	1.033	1.035	1.038	1.040	1.043	1.047	1.050	1.053	1.055	1.057
...	...	...	...	...	...	...	...	...	...	...

## Flow of Steam through Pipes.

TABLE 2-9.—FLOW OF STEAM THROUGH PIPES.  
(“Steam.”)

Initial Pressure per Square Inch.	Diameter of Pipe in Inches. Length of each Pipe, 740 Diameters.						
	$\frac{3}{4}$	1	1 $\frac{1}{2}$	2	2 $\frac{1}{2}$	3	4
	Weight of Steam per Minute in Pounds, with One Pound Fall of Pressure.						
Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
1	1.16	2.07	3.7	10.27	15.45	25.38	46.85
10	1.44	2.57	7.1	12.72	19.15	31.45	48.05
20	1.70	3.02	8.3	14.94	22.49	36.94	68.20
30	1.91	3.40	9.4	16.84	25.35	41.63	76.84
40	2.10	3.74	10.3	18.51	27.87	45.77	84.49
50	2.27	4.04	11.2	20.01	30.13	49.48	91.34
60	2.43	4.32	11.9	21.38	32.19	52.87	97.60
70	2.57	4.58	12.6	22.65	34.10	56.00	103.37
80	2.71	4.82	13.3	23.82	35.87	58.91	108.74
90	2.83	5.04	13.9	24.92	37.52	61.62	113.74
100	2.95	5.25	14.5	25.96	39.07	64.18	118.47
120	3.16	5.63	15.5	27.85	41.93	68.87	127.12
150	3.45	6.14	17.0	30.37	45.72	75.09	138.61

Initial Pressure per Square Inch.	Diameter of Pipe in Inches. Length of each Pipe, 240 Diameters.						
	5	6	8	10	12	15	18
	Weight of Steam per Minute in Pounds, with One Pound Fall of Pressure.						
Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
1	77.3	115.9	211.4	341.1	502.4	804	1177
10	95.8	143.6	262.0	422.7	622.5	996	1458
20	112.6	168.7	307.8	496.5	731.3	1170	1713
30	126.9	190.1	346.8	559.5	824.1	1318	1930
40	139.5	209.0	381.3	615.3	906.0	1450	2122
50	150.8	226.0	412.2	665.0	979.5	1567	2294
60	161.1	241.5	440.5	710.6	1046.7	1675	2451
70	170.7	255.8	466.5	752.7	1108.5	1774	2596
80	179.5	269.0	490.7	791.7	1166.1	1866	2731
90	187.8	281.4	513.3	828.1	1219.8	1951	2856
100	195.6	293.1	534.6	862.6	1270.1	2032	2975
120	209.9	314.5	573.7	925.6	1363.3	2181	3193
150	228.8	343.0	625.5	1009.2	1486.5	2378	3481

Mr. Babcock gives the following formula for the flow of steam through pipes :—

$$W = 300 \sqrt{\frac{D (p_1 - p_2) a^3}{L \left(1 + \frac{3.6}{d}\right)}} \quad (19)$$

$W$  = weight of steam in pounds.

$d$  = diameter of pipe in inches.

$D$  = density or weight per cubic foot of the steam.

$p_1$  = initial pressure.

$p_2$  = pressure at end of pipe.

$L$  = length of pipe in feet.

Table 289 gives, approximately, the weight of steam which would flow through a straight smooth pipe, of which the length is equal to 240 diameters, with one pound fall of pressure.

For any other given fall of pressure, multiply the tabular weight by the square root of the given fall of pressure.

For any other given length of pipe, divide 240 by the given length in diameters, and multiply the tabular values by the square root of the quotient, to give the flow for one pound fall of pressure.

Conversely, divide the given length by 240, to find the fall of pressure for the flow given in the Table.

The loss of head due to generation of the velocity of flow, and the friction of the steam entering the pipe, is about equal to the resistance of a length of pipe equal to the quotient of 114 diameters, divided by  $\left(1 + \frac{3.6}{d}\right)$ , in which  $d$  is the diameter in inches. For the sizes given in the Table, the corresponding lengths are as follows :—

Diameter in Inches.	Length in Diameters.	Diameter in Inches.	Length in Diameters.	Diameter in Inches.	Length in Diameters.
$\frac{3}{4}$	20	3	52	10	84
1	25	4	60	12	88
$1\frac{1}{2}$	34	5	66	15	92
2	41	6	71	18	95
$2\frac{1}{2}$	47	8	79		

The resistance of a globe-valve is equal to that at the entrance of the pipe; and that at an elbow is equal to two-thirds of that of a globe-valve. The equivalent lengths respectively are to be added to the actual length of the pipe. For instance, a 4-inch pipe 120 diameters, or 40 feet, long, with a globe-valve and three elbows, would be equivalent to  $(120 + 60 \text{ (entrance)} + 60 \text{ (globe-valve)} + (40 \times 3) = )$  360 diameters in.

length. By the rule above given,  $(360 \div 240 =) 1\frac{1}{2}$  lbs. is the fall or loss of pressure for the tabulated flow. Or, it would deliver  $(1 \div \sqrt{1\frac{1}{2}} =) \cdot 816$ , or 81·6 per cent. of the steam with the same loss (1 lb.) of pressure.

### Coverings for Steam-Boilers and Steam-Pipes.

The efficiency of different substances for the prevention of radiation of heat, varies generally in the inverse ratio of their conducting power for heat. From the results of experiments, it appears that the rates of condensations of steam in a naked pipe, a pipe coated with a cement, and a pipe coated with hair-felt, were proportionally as 100, 67, and 27. According to Dr. Emery, the relative efficiency of various substances as coatings, is as given in Table 290.

TABLE 290.—RELATIVE EFFICIENCY OF NON-CONDUCTORS.  
(Emery.)

Substance.	Relative Efficiency.	Substance.	Relative Efficiency.
Wood felt . . . . .	1·000	Loam, dry and open	·550
Mineral wool, No. 2 .	·832	Slacked lime . . .	·480
„ „ with tax	·715	Gas-house carbon .	·470
Sawdust . . . . .	·680	Asbestos . . . . .	·363
Mineral wool, No. 1 .	·676	Coal ashes . . . .	·345
Charcoal . . . . .	·632	Coke in lumps . . .	·277
Pine wood, across fibre	·553	Air space undivided	·136

### Green's Economiser.

Green's Economiser for heating the feedwater for steam-boilers, consists of a set of 4-inch cast-iron pipes 9 feet long, vertically placed in the flueway. In two extreme cases in ordinary working, the economy effected by the Economiser varied from  $12\frac{1}{2}$  per cent. to 29 per cent. The burnt gases were cooled to the extent of  $156^{\circ}$  F. and  $253^{\circ}$  F. respectively.

### Loss of Steam by Condensation in Pipes.

The relative loss of heat from steam-pipes naked and clothed with wool or hair-felt, in several thicknesses, is given in Table 291. The steam pressure is taken at 75 lbs. per square inch; and the temperature of the air at  $60^{\circ}$  F. The horse-power mentioned in the Table is the standard for steam-boilers favourably received in America, according to which one horse-power is measured by the evaporation of 30 pounds of water per hour, at a working pressure of 70 lbs. per square inch from  $100^{\circ}$  F. temperature.

TABLE 291.—LOSS OF STEAM BY CONDENSATION IN PIPES.  
("Steam.")

Thickness of Covering.	Two Inches.			Four Inches.			Six Inches.			Eight Inches.			Twelve Inches.		
	Loss per Lineal Foot per Hour.	Ratio of Loss.	Length of Pipe per H. P. Lost.	Loss per Lineal Foot per Hour.	Ratio of Loss.	Length of Pipe per H. P. Lost.	Loss per Lineal Foot per Hour.	Ratio of Loss.	Length of Pipe per H. P. Lost.	Loss per Lineal Foot per Hour.	Ratio of Loss.	Length of Pipe per H. P. Lost.	Loss per Lineal Foot per Hour.	Ratio of Loss.	Length of Pipe per H. P. Lost.
Inches.	Units.	Feet.	Feet.	Units.	Feet.	Feet.	Units.	Feet.	Feet.	Units.	Feet.	Feet.	Units.	Feet.	Feet.
Naked.	219·0	1·00	132	390·8	1·00	75	624·1	1·000	46	729·8	1·000	40	1077·4	1·000	26
4	100·7	·46	288	189·9	·46	160	...	...	...	...	...	...	...	...	...
½	65·7	·30	441	117·2	·30	247	187·2	·300	154	219·6	·301	132	301·7	·280	92
1	43·8	·20	662	73·9	·18	392	111·0	·178	261	128·3	·176	225	185·3	·172	157
2	28·4	13	1020	44·7	·11	648	66·2	·106	438	75·2	·103	385	98·0	·091	294
4	19·8	·09	1464	28·1	·07	1031	41·2	·046	703	46·0	·063	630	60·3	·056	486
6	...	...	...	23·4	·06	1238	33·7	·054	800	34·3	·047	845	45·2	·042	642

## TUCK'S STEAM PACKING.

Diameter.	Weight per foot.	Diameter.	Weight per foot.
inches.	lbs.	inches.	lbs.
$\frac{3}{16}$	·013	$\frac{1}{8}$	·255
$\frac{1}{4}$	·024	$\frac{7}{8}$	·311
$\frac{5}{16}$	·041	1	·400
$\frac{3}{8}$	·050	$1\frac{1}{8}$	·519
$\frac{7}{16}$	·074	$1\frac{1}{4}$	·608
$\frac{1}{2}$	·106	$1\frac{3}{8}$	·728
$\frac{9}{16}$	·131	$1\frac{1}{2}$	·859
$\frac{5}{8}$	·158	$1\frac{5}{8}$	·958
$\frac{11}{16}$	·220	$1\frac{3}{4}$	1·08
$\frac{3}{4}$	·234	2	1·48

## RAILWAYS.

THE lengths of lines in the United Kingdom open for traffic on the 31st December, 1889, were in—

	Miles Open.
England and Wales . . . . .	14,034
Scotland . . . . .	3,118
Ireland . . . . .	2,791
	<hr/> 19,943

as a round number, say, 20,000 miles.

The total paid-up capital, including loans and debenture stock, was £876,595,166, or £43,960 per mile open.

The number of passengers conveyed in the year 1889, were :—

1st class . . . . .	30,074,810 or	3·88 per cent.
2nd „ . . . . .	62,687,927 „	8·07 „
3rd „ . . . . .	682,420,336 „	88·05 „
Total . . . . .	775,183,073	100·00

In goods traffic there were conveyed—

211,810,551 tons of minerals, or	71·20 per cent.
85,695,947 „ „ general merchandise . }	28·80 „
	<hr/> 100·00



The number of miles travelled by trains were as follows :—

	Miles.
Passenger trains . . . . .	161,082,875
Goods and mineral trains . . . . .	138,941,233
Total . . . . .	303,116,953

The total includes 3,092,845 miles travelled by mixed trains.

The receipts were as follows :—

Gross receipts from } passenger traffic }	£32,630,724	or 42·4 per cent.
Do. Goods „ .	41,086,333	„ 53·3 „
Miscellaneous receipts .	3,307,960	„ 4·3 „
	£77,025,017	100·0

or about £3,851 per mile open, or 5s. 1d. per train-mile run.

The total working expenditure was £40,094,116, or 52 per cent. of the receipts.

The rolling stock, on December 31, 1889, was as follows :—

Locomotives (fully three-fourths of a locomotive per mile open) . . . . .	15,924
Passenger carriages . . . . .	36,137
Other passenger train stock . . . . .	13,501
Waggons . . . . .	503,260
Sundry carriages and waggons . . . . .	14,335
Passenger and goods trains carrying stock } (or about 35½ vehicles per locomotive; } or about 28½ vehicles per mile open) }	567,233

The average number of train-miles run per locomotive was 19,000.

The standard forms of rails are the bull-headed, the double-headed, and the flange or flat-foot rails. Of the rails used on British and Irish railways, the following are the principal dimensions :—

TABLE 292.—RAILWAY RAILS AND SLEEPERS.

	Bull-headed Rails.	Double-headed Rails.	Flange Rails.
Weight of rail per yard }	80 lb. to 86 lb.	82 lbs.	74 lbs., 79 lbs.
Height . .	$5\frac{3}{4}$ ins. to $5\frac{5}{8}$ ins.	$5\frac{1}{4}$ ins., $5\frac{3}{8}$ ins.	$4\frac{9}{16}$ ins. to $4\frac{11}{16}$ ins.
Width of head .	$2\frac{1}{4}$ ins. to $2\frac{3}{4}$ ins.	$2\frac{1}{2}$ ins.	$2\frac{1}{2}$ ins., $2\frac{3}{4}$ ins.
Width of flange	...	...	5 ins.
Thickness of web	$\frac{1}{4}$ in. to $\frac{1}{2}$ in.	$\frac{1}{4}$ in. to $\frac{7}{8}$ in.	$\frac{7}{16}$ in. to 1 in.
Length of bars .	24 ft. to 32 ft.	24 ft. to 30 ft.	24 ft. to $26\frac{1}{2}$ ft.
Section of sleepers }	10×5 ft. to 12×6 ft.	10×5 ft.	10×5 ft.
Distance of sleepers apart }	2 ft. 6 ins. to 3 ft. 1 in.	2 ft. 8 in. to 2 ft. 10 in.	3 ft.
Weight of chair	39 lbs. to 55 lbs.	31 lbs. to 40 lbs.	...

### Locomotives and Speed of Trains.

Large express locomotives weigh in working order from 40 tons to 50 tons. The latest Midland Railway express engine weighs, in working order, 43 tons, of which the driving weight, on a single pair of wheels, is  $17\frac{1}{2}$  tons. The area of fire-grate is 19·6 square feet; the heating surface is  $1,240\frac{1}{2}$  square feet. The tender weighs, empty, 12 tons; and 30 tons when loaded with  $3\frac{1}{2}$  tons of coal, and 3,250 gallons of water. The working steam pressure in the boiler is 160 lbs. per square inch. The cylinders are  $18\frac{1}{2}$  inches in diameter, with a stroke of 26 inches. The driving wheels, single, are  $7\frac{1}{2}$  feet in diameter, with a bogie in front. The total wheel-base of the engine and tender together is about 43 feet on the rails. On the London and Nottingham traffic, the average gross load weighs from 170 to 215 tons, or from 9 to 12 carriages. The time-bill speed is  $53\frac{1}{2}$  miles per hour; the longest continuous run is 124 miles, and from 20 lbs. to 23 lbs. of Derbyshire coal is consumed per mile-run.

Parliamentary trains, calling at all the stations, run at an average speed of from 19 to 28 miles per hour. Express goods trains make a speed of from 20 to 25 miles per hour. The speed of coal trains is limited, as far as is practicable, to 15 miles per hour.

Coal trains generally consist of from 30 to 35 waggons, weighing from 5 tons to  $5\frac{1}{2}$  tons each, and carrying 8 tons of coal. At this rate, the total load of coal for 35 waggons weighs 280 tons; add the weight of the break van at the end of the train, 10 tons, 17 cwt., and the maximum gross weight of the train is 483 tons, 7 cwt.

A 6-coupled locomotive, suited for taking this train on the

Great Northern Railway, has  $5\frac{1}{2}$  feet wheels,  $17\frac{1}{2}$  inch cylinders with a 26 inch stroke, with 140 lbs. pressure in the boiler; weighing, in working order, 37 tons, and with the tender full of water and coal, 68 tons. The engine, tender, and train together weigh 551 tons. Such trains are taken at a speed of 18 miles per hour; ascending inclines of 1 in 178 at a speed of 10 miles per hour; consuming 45 lbs. of coal per mile. With more powerful engines, having 19 inch cylinders, trains of 45 loaded coal waggons are taken.

Six-coupled goods engines, working at full power, exert a tractive force of from 5 tons to 6 tons at the rails. With a tractive force of 10 lbs. or 12 lbs., 1 ton of gross weight can be drawn on a level straight line at a speed of 10 miles per hour. At 60 miles per hour, the tractive force, with sharp curves and high winds, may amount to 45 lbs. for 1 ton.

### Railway Gauges.

The standard gauge of railways in Great Britain is 4 feet  $8\frac{1}{2}$  inches. The same gauge is adopted in some other countries. See Table 293.

TABLE 293.—GAUGES OF THE PRINCIPAL RAILWAY SYSTEMS IN THE WORLD.

	Ft. Ins.		Ft. Ins.
Great Britain, standard gauge . . . . .	4 8 $\frac{1}{2}$	Mexico . . . . .	4 8 $\frac{1}{2}$
Ireland, stand. gauge . . . . .	5 3	United States { prevailing gauges . . . . .	3 0
Central Europe, prevailing gauge . . . . .	4 8 $\frac{1}{2}$	of . . . . .	4 8 $\frac{1}{2}$
Russia, standard gauge . . . . .	5 0	America . . . . .	4 9
Norway . . . . .	4 8 $\frac{1}{2}$		6 0
	3 6		5 0
Spain and Portugal, standard gauge . . . . .	5 6		3 0
Antwerp and Ghent . . . . .	2 3		2 0
India, prevailing gauge . . . . .	5 6	Chili . . . . .	5 6
„ metre gauge . . . . .	3 3 $\frac{3}{8}$		4 8 $\frac{1}{2}$
„ Arconum and Conjeveram . . . . .	3 6		4 2
Japan . . . . .	3 6	Brazil . . . . .	3 6
Egypt . . . . .	4 8 $\frac{1}{2}$		5 6
	5 6	South Australia . . . . .	5 3
Canada . . . . .	4 8 $\frac{1}{2}$		3 6
	3 6	New South Wales . . . . .	4 8 $\frac{1}{2}$
		Victoria . . . . .	5 3
		New Zealand . . . . .	5 3
			3 6

In the United Kingdom there are a few local railways of less than the national gauge :—

	Feet	Inches.
Festiniog . . . . .	1	11½
Talyllyn . . . . .	2	6
Dinas and Snowdon, Ballymena and Larne, and others . . . . .	3	0

### The Way: Rails, Chairs, and Sleepers.

The bull-headed rail is laid on most of the railways in Great Britain. The double-headed rail, reversible, is also in use. In Ireland, both are in use. They weigh from 82 lbs. to 86 lbs. per lineal yard. The heads are from 2½ to 2¾ inches wide; and the height of rail is from 5¼ to 5½ inches. The rails are of steel, rolled in bars mostly 30 feet in length. They are carried in cast-iron chairs weighing from 31 lbs. to 55 lbs. each, spiked to transverse sleepers of Baltic red wood generally 10 inches wide, 5 inches deep, and 9 feet long.

#### *Cost of 1 Mile of Single Line of Way on a first class Railway.*

	£	s.	d.
Steel rails, bull-headed, 30 feet long, 85 lbs. per yard; 133½ tons at £5 . . . . .	667	10	0
Chairs, 3,872, at 50 lbs.; 86½ tons at £3 . . . . .	259	10	0
Fish-plates, steel clip, 352 pairs at 40 lbs. = 6½ tons, at £8 . . . . .	50	0	0
Bolts and nuts, 1,408 at 1½ lbs.; 1 ton at £9 10s. . . . .	9	10	0
Spikes, 7,744 at 1¼ lbs.; 4½ tons at £7 10s. . . . .	31	17	6
Trenails, solid oak, 7,744 at £2 10s. per 1,000 . . . . .	19	7	2
Keys, oak, 3,872 at £4 per 1,000 . . . . .	15	9	9
Sleepers, creosoted, 1,936 at 4s. . . . .	387	4	0
Labour, 1,760 yards at 1s. 6d. . . . .	132	0	0
Total cost of laying . . . . .	£1,572	8	5
Taking credit for old materials in case of relaying, the net cost of relaying is, say . . . . .	£858	0	2

### Centre of Gravity of Locomotives.

To find the position of the centre of gravity of a locomotive in the horizontal sense, when the loads on the rails at the axle, and their distances apart are given.

1. *Four-wheeled locomotive.* Multiply the load at the driving axle in tons by the length of the wheel-base in feet;

and divide by the total weight in tons. The quotient is the horizontal distance, in feet, of the centre of gravity from the other axle.

When the loads at the axles are equal, the centre of gravity lies half-way between them.

2. *Six-wheeled locomotive.* Multiply the loads at the leading and trailing axles, in tons, by their respective distances from the middle axle in feet; divide the difference of the products so found by the total weight in tons. The quotient is the horizontal distance, in feet, of the centre of gravity from the middle axle, measured towards the axle for which the greater product was found.

When the products are equal, the centre of gravity lies exactly over the middle axle.

3. *Locomotives having more than six wheels.* Select a middle axle. Multiply the loads at the axles in front of the selected axle by their distances respectively from this axle; do likewise with the axles behind the selected axle. Find the difference of the sums of the products in front and behind the selected axle; and divide it by the total weight in tons. The quotient is the distance horizontally, in feet, of the centre of gravity from the selected axle, measured in the direction for which the greater sum of the products was found.

### Tractive Power and Resistance on Railways.

For two cylinders of equal diameters, the equivalent tractive force, as at the rails for a given effective mean pressure in the cylinders, may be calculated by means of the formula—

$$T = \frac{d^2 L p}{D} \quad . \quad . \quad . \quad . \quad . \quad (1)$$

The equivalent effective mean pressure in the cylinders required for a given tractive force as at the rails is by formula—

$$p = \frac{DT}{d^2 L} \quad . \quad . \quad . \quad . \quad . \quad (2)$$

$d$  = diameter of cylinder, in inches.

$L$  = length of stroke, in inches.

$D$  = diameter of driving wheels, in inches.

$p$  = effective mean pressure, in pounds per square inch.

$T$  = equivalent tractive force, as at the rails, in pounds.

If it be assumed that the work done in the second cylinder of a compound locomotive is equal to that done in the first

cylinder, the formula (1) becomes available for calculating the tractive force at the rails in terms of the sizes and pressure of the first cylinder.

The proportion of the adhesion weight, or driving weight, varies from one-fifth in dry weather to one-ninth in damp weather. A fraction of from one-sixth to one-seventh may be adopted in calculation, as it can be maintained by the use of sand on the rails or other expedients. The fraction 1-6-4th gives an adhesion of 350 pounds per ton; and adopting this unit, the adhesions for various driving weights are as follows :—

Driving Weight in tons.	Adhesion or available tractive force as at the rails.
10 . . . . .	3,500 pounds, or 1·56 tons.
20 . . . . .	7,000     "     " 3·12     "
30 . . . . .	10,500   "     " 4·68     "
40 . . . . .	14,000   "     " 6·25     "
50 . . . . .	17,500   "     " 7·81     "
60 . . . . .	21,000   "     " 9·37     "

The resistance of engines and trains on railways is expressed by the formula (3), quoted from *Railway Machinery*. It applies under the following conditions :—

1. The permanent way in good order.
2. The engine, tender, and train in good order; lubricated with grease.
3. A straight and level line of rails.
4. Fair weather, and dry and clean rails.
5. An average side-wind, of average force, varying during the experiment between *slight* and *very strong*.

#### Resistance of Engine, Tender, and Train.

$$R = 8 + \frac{V^2}{171} \quad . \quad . \quad . \quad (3)$$

V = speed in miles per hour.

R = total resistance in pounds per ton.

In cases of frequent sharp curves, in connection with strong side and head winds, the resistance may be augmented by one-half the given resistance on a level.

The annexed Table 294, gives the resistance per ton of engine, tender, and train, for various speeds and gradients.

TABLE 294.—RESISTANCE OF PASSENGER TRAINS.

Ascending Gradients.	CONDITIONS.— <div style="display: flex; align-items: center;"> <div style="font-size: 3em; margin-right: 10px;">{</div> <div> A good sound road.  A straight line.  An average side-wind.  Engine, tender, and train in  good working order, with  grease lubrication. </div> </div>						
	Speed, in Miles per Hour.						
	10	20	30	40	50	60	70
Total Resistance as at the Rails, in Pounds per Ton.							
Level	Lbs. 8·6	Lbs. 10·3	Lbs. 13·2	Lbs. 17·3	Lbs. 22·6	Lbs. 29	Lbs. 36·6
1 in 40	64	66	69	73	79	85	93
1 „ 60	46	48	50	55	60	66	74
1 „ 80	36	38	41	45	51	57	65
1 „ 100	31	33	36	40	45	51	59
1 „ 150	24	26	28	32	38	44	51
1 „ 200	20	22	25	29	34	40	48
1 „ 250	18	20	22	26	32	38	46
1 „ 300	16	18	21	25	30	36	44
1 „ 500	13	15	18	22	27	33	41
1 „ 800	11	13	16	20	25	32	39
1 „ 1000	11	12	15	19	25	30	39
Level	8·6	10·3	13·2	17·3	22·6	29	36·6

*Note.*—Fifty per cent. of the resistance as on a straight level way may be added for cases of frequent curves, of or under one mile in radius, in connection with strong side and head winds.

The general dimensions, weights, and capacity of the standard carriage stock and waggon stock of the Midland Railway, are given in Tables 298 and 299, page 553.

Supposing an engine and tender, weighing together 40 tons, and exerting a given tractive force, takes 40 loaded carriages, weighing 360 tons, at 20 miles per hour on a level, the loads which it could take if it exerted the same tractive force at higher speeds, would be proportionately as follows:—

At 20 miles per hour, 40 carriages weighing 360 tons.

„ 30	„	„	30	„	„	200	„
„ 40	„	„	21	„	„	144	„
„ 50	„	„	15	„	„	106	„
„ 60	„	„	11	„	„	75	„

N N 2

The influence of rising inclines is exemplified as follows :—

If an engine and tender, weighing together 40 tons, can draw a maximum train of 42 loaded carriages, weighing 420 tons, at 20 miles per hour on a level, it would draw only the following loads at the same speed up the annexed inclines :—

Level	.	.	42 carriages, weighing 420 tons.
Incline, 1 in 600	.	34	340 "
" " 300	.	27	270 "
" " 150	.	20	200 "
" " 100	.	15	150 "
" " 75	.	12	120 "
" " 50	.	9	90 "
" " 40	.	6	65 "
" " 30	.	5	45 "
" " 20	.	3	24 "
" " 10	.	nil	nil.

### Speed of Railway Trains.

The speed of railway trains may be calculated in terms of the number of revolutions of the driving wheels of the locomotive in a given number of seconds. Let,—

$r$  = number of revolutions in the given time.

$t$  = time in seconds.

$d$  = diameter of driving wheels, in feet.

$v$  = velocity or speed in miles per hour.

The number of turns per hour is  $\left( r \times \frac{60}{t} \times 60 \text{ minutes,} = \right)$

$$\frac{3,600 r}{t} \quad \dots \quad (a)$$

The number of turns per mile is  $\left( \frac{5,280 \text{ feet}}{3.1416 d} = \right)$

$$\frac{1680.7}{d} \quad \dots \quad (b)$$

The speed in miles per hour is equal to  $(a)$  divided by  $(b)$  ; or, by reduction,—

$$v = \frac{2.142 d r}{t} \quad \dots \quad (4)$$

The Table 295 gives multipliers in the 3rd column, by the use of which the speed of a train may be calculated in terms of the diameter of the driving wheel, column 1, for any given number of revolutions of the wheels in a given number of seconds. The speeds in the 3rd column are those due to one revolution in one second ; and the speed due to the given diameter of wheel is to be multiplied by the observed number



of turns, and the product divided by the time of observation in seconds. Or, thus,—

Speed for 1 turn in 1 second  $\times \frac{\text{number of turns observed}}{\text{time of observation in seconds}}$

For example, a 5 feet driving wheel makes 20 revolutions in 10 seconds. The multiplier in col. 3 for a 5 feet wheel is 10.71; and the speed is  $\left(10.71 \times \frac{20}{10} = \right) 21.42$  miles per hour.

TABLE 295.—MULTIPLIERS FOR SPEED OF RAILWAY TRAINS.

Diameter of Driving Wheels. 1.		Number of Revolutions in One Mile. 2.	Speed for One Revolution in One Second. 3.	Diameter of Driving Wheels. 1.		Number of Revolutions in One Mile. 2.	Speed for One Revolution in One Second. 3.
Ft.	Ins.	Revolutions.	Miles per Hour.	Ft.	Ins.	Revolutions.	Miles per Hour.
3	0	560.2	6.42	6	9	249.0	14.46
3	3	517.1	6.96	7	0	240.1	14.99
3	6	480.2	7.50	7	3	231.8	15.53
3	9	448.2	8.03	7	6	224.1	16.06
4	0	420.2	8.57	7	9	216.9	16.60
4	3	395.4	9.10	8	0	210.1	17.14
4	6	373.5	9.64	8	3	203.7	17.67
4	9	353.8	10.17	8	6	197.7	18.21
5	0	336.1	10.71	8	9	192.7	18.74
5	3	320.1	11.25	9	0	186.7	19.28
5	6	305.6	11.78	9	3	181.7	19.81
5	9	292.3	12.32	9	6	176.9	20.35
6	0	280.1	12.85	9	9	172.4	20.88
6	3	268.9	13.39	10	0	168.1	21.42
6	6	258.6	13.92				

The relations of the speed in miles per hour and the corresponding time running one mile, are expressed by the formulas (5) and (6). There are  $(60 \times 60 =)$  3,600 seconds in an hour, and the time of running one mile is equal to the quotient of 3,600 divided by the speed in miles per hour. Also the speed is equal to the quotient of 3,600 divided by the time of running one mile. Or,

$$t = \frac{3,600}{v} \quad . \quad . \quad . \quad . \quad (5)$$

$$v = \frac{3,600}{t} \quad . \quad . \quad . \quad . \quad (6)$$

$t$  = time running one mile, in seconds.

$v$  = speed in miles per hour.

By means of formula (5), the Table 296 has been calculated.

TABLE 296.—SPEED IN MILES PER HOUR, AND  
CORRESPONDING TIME RUNNING ONE MILE.

Speed in Miles per Hour.			Time Running One Mile.		
Speed in Miles per Hour.			Time Running One Mile.		
Miles.	Seconds.	Mins. Secs.	Miles.	Seconds.	Mins. Secs.
1	3600	60 0	29	124	2 4
1½	2400	40 0	30	120	2 0
2	1800	30 0	31	116	1 56
2½	1440	24 0	32	112	1 52
3	1200	20 0	33	109	1 49
3½	1028	17 8	34	106	1 46
4	900	15 0	35	103	1 43
4½	800	13 20	36	100	1 40
5	720	12 0	37	97	1 37
6	600	10 0	38	95	1 35
7	514	8 34	39	92	1 32
8	450	7 30	40	90	1 30
9	400	6 40	41	88	1 28
10	360	6 0	42	86	1 26
11	327	5 27	43	84	1 24
12	300	5 0	44	82	1 22
13	277	4 37	45	80	1 20
14	257	4 17	46	79	1 19
15	240	4 0	47	77	1 17
16	225	3 45	48	75	1 15
17	212	3 32	49	73	1 13
18	200	3 20	50	72	1 12
19	190	3 10	51	71	1 11
20	180	3 0	52	70	1 10
21	171	2 51	53	68	1 8
22	164	2 44	54	67	1 7
23	157	2 37	55	65	1 5
24	150	2 30	56	64	1 4
25	144	2 24	57	63	1 3
26	138	2 18	58	62	1 2
27	133	2 13	59	61	1 1
28	129	2 9	60	60	1 0

(Continued on next page.)

TABLE 296.—SPEED IN MILES PER HOUR (*continued*).

Speed in Miles per Hour.	Time Running One Mile.	Speed in Miles per Hour.	Time Running One Mile.	Speed in Miles per Hour.	Time Running One Mile.
Miles.	Seconds.	Miles.	Seconds.	Miles.	Seconds.
61	59	75	48	88	41
62	58	76	47·4	89	40·4
63	57	77	47	90	40
64	56	78	46	91	39·6
65	55	79	45·6	92	39·1
66	54·5	80	45	93	38·7
67	54	81	44·4	94	38·3
68	53	82	44	95	37·9
69	52	83	43·4	96	37·5
70	51·4	84	43	97	37·1
71	51	85	42	98	36·7
72	50	86	41·9	99	36·4
73	49	87	41·4	100	36
74	48·6				

TABLE 297.—BULK AND WEIGHT OF GOODS, AS CONVEYED BY RAILWAY.

(Col. Kennedy.)

Number of Kind of Goods.	Description of Goods carried.	Cubic Feet per Ton.	Weight per Cubic Foot.
No.		Cubic Feet.	Pounds.
CLASS 1.			
1	Unpressed Cotton . . . . .	224	10
2	Furniture . . . . .	200	11
3	Half-pressed cotton . . . . .	186	12
4	Cotton seeds . . . . .	186	12
5	Wool . . . . .	140	16
6	Fruit and vegetables . . . . .	100	22
7	Eggs . . . . .	90	25
CLASS 2.			
8	Grass . . . . .	80	28
9	Sundries . . . . .	80	28
10	Bagging . . . . .	70	32
11	Commissariat stores . . . . .	70	32

TABLE 257.—BULK AND WEIGHT OF GOODS (*continued*).

Number of Kind of Goods.	Description of Goods carried.	Cubic Feet per Ton.	Weight per Cubic Foot.
No.		Cubic Feet.	Pounds.
	CLASS 2 ( <i>continued</i> ).		
12	Full-pressed cotton . . . . .	70	32
13	Flax and hemp . . . . .	70	32
14	Groceries . . . . .	60	37
15	Grains and seed . . . . .	60	37
16	Twist . . . . .	60	37
17	Sugar . . . . .	56	40
18	Soap . . . . .	56	40
19	Firewood . . . . .	56	40
20	Salt . . . . .	51	44
21	Lime . . . . .	51	44
22	Dry fruits . . . . .	50	45
	CLASS 3.		
23	Molasses . . . . .	45	50
24	Seed cotton . . . . .	45	50
25	{ Mowra (flowers which pro- duce spirit) . . . . . }	45	50
26	Timber . . . . .	45	50
27	Ghee (clarified butter) . . . . .	40	56
28	Oil . . . . .	40	56
29	Piece goods . . . . .	40	56
30	Rape . . . . .	40	56
31	Beer and spirits . . . . .	36	62
32	Coal . . . . .	28	80
33	Paper . . . . .	28	80
34	Tobacco . . . . .	28	80
35	Opium . . . . .	26	86
36	Machinery . . . . .	25	90
	CLASS 4.		
37	Cutlery . . . . .	20	112
38	Potash . . . . .	20	112
39	Sand . . . . .	20	112
40	Colours . . . . .	18	124
41	Bricks . . . . .	17	132
42	Stone . . . . .	15	148
43	Metal . . . . .	5	448

TABLE 298.—CARRIAGE STOCK, MIDLAND RAILWAY.

Carriage.	Length of Body.	Compartments.	No. of Passengers.	Weight of Vehicle.		Price.
				Tons. Cwts.	£	
6-wheel bogie composite .	54	{ 3 first class, 4 third class, 1 luggage = 8 }	58	23 0	1007	
4-wheel bogie composite .	45	{ 3 first class, 3 third class, 1 luggage = 6 }	48	18 10	768	
4-wheel bogie third class .	43	7 third class . . . .	70	17 15	620	
4-wheel bogie composite .	40	{ 2 first class, 3 third class, 1 luggage = 6 }	42	17 5	654	
6-wheel first class . . . .	30	4 first class . . . .	24	10 13	516	
6-wheel composite . . . .	31	{ 2 first class, 2 third class, 1 luggage = 5 }	32	11 10	450	
6-wheel third class . . . .	31	5 third class . . . .	50	10 7	390	

TABLE 299.—WAGON STOCK, MIDLAND RAILWAY.

Wagon.	External Dimensions over Corner Pillars.		Internal Dimensions.			Load to Carry.	Weight of Wagon.	Price.
	Length.	Width.	Length.	Width.	Height above Floor.			
	Ft. Ins.	Ft. Ins.	Ft. Ins.	Ft. Ins.	Ft. Ins.	Tons.	Tns. Cwts.	£
Covered goods	14 11	7 5	14 2	6 10	5 10½	8	5 3	72
High-sided, for goods or coal .	14 11	7 5	14 6	7 0	2 10	8	5 2	65
Low-sided . . . .	14 11	7 5	14 6	7 0	1 9	8	4 14	61
Cattle wagon . . . .	18 6	8 0	17 9	7 4	7 0½	8	6 0	86

### Electrical Propulsion on Railways.

In consequence of the number of stages between the generation of steam in the stationary boilers and the hauling of the train, the efficiency of electric propulsion is relatively small. There is, first, the power consumed in driving the engine and dynamo; then, the dynamo cannot give in electrical power all the mechanical power applied to it; then there is the loss by line resistance and leakage; and the loss in the motor. These losses were such, in one case, that the efficiency of the entire plant was only 15·1 per cent. In another case, the efficiency averaged 25 per cent. The cost for power by electric agency is considered to be about four times that of direct steam power.

**TRAMWAYS.****Length Open and Costs of Working.**

The total length of tramway lines in the United Kingdom open for public traffic on the 30th June, 1889, was 949 miles, distributed as follows :—

	Miles open.
England . . . . .	758
Scotland . . . . .	81
Ireland . . . . .	110
	<hr/>
	949

Of this length, 407½ miles were double line, and 541½ miles were single line : respectively 42 per cent. and 58 per cent.

The total capital expended at June 30, 1889, amounted to £13,664,591 ; or £14,400 per mile open.

The gross receipts for the year were £2,980,224 ; or £3,140 per mile open ; or 11½d. per car mile run.

The working expenses were £2,266,681, or 76 per cent. of the receipts ; or 8¾d. per mile run.

**Working Stock.**

The working stock was as follows :—

27,060 horses, or . . . . .	28½ horses per mile open.
539 locomotives . . . . .	57 locomotives „
3,645 cars, or . . . . .	3·84 cars „
62,041,013 miles were run by cars.	

Flat foot girder rails of steel, weighing from 80 lbs. to 90 lbs. per yard, are now most commonly laid. They are about 6 inches in height, and from 5 inches to 6 inches wide at the flange-base.

Cars capable of holding 20 passengers inside, and 22 outside, weigh about 2½ tons each. The gross weight, fully loaded, is 5½ tons. The body of the car is 15¼ feet in length, 6 feet 8 inches wide, outside measurement. The total length of the car is 21¼ feet, allowing 3 feet at each end for the platform.

The average resistance to traction is about 30 lbs. per ton of car and its load. When the rails are wet and clean, straight and new, a minimum of 15 lbs. per ton may be reached. An occasional maximum resistance of 60 lbs. per ton may be reached ; the augmentation being due mostly to the clogging of the grooves of the rails.

**Cost per Mile.**

(Single line, of sample of Tramway: girder rail 80 lbs. per yard, 7 inches high.)

	£	s.	d.
Steel rails, 80 lbs. per yard, 125 $\frac{3}{4}$ tons, @ £8 14s.	1,094	0	6
Wrought-iron fish-plates, 4 $\frac{3}{4}$ tons, @ £8	38	0	0
" " bolts and nuts, 9 cwt., at 11s.	4	19	0
Lifting and carting away, 522 cubic yards, @ 1s. 9d.	45	13	6
Excavation, &c., 1,108 cubic yards, @ 2s.	110	16	0
Portland cement concrete, 6 inches thick, 782 cubic yards, @ 17s.	664	14	0
Laying tramway, 1,760 yards, @ 1s. 8d.	146	13	4
Total for the way	2,104	16	4
Paving, &c., 2,836 square yards, @ 7s. 3d.	1,028	1	0
Paving in cement and sand, next rails, 1,564 square yards, @ 7s. 7d.	593	0	4
Grouting joints of sets with bitumen, 4,400 square yards, @ 1s. 3 $\frac{1}{2}$ d.	284	3	4
Total for paving	1,905	4	8
Total for way and paving	4,010	1	0

**Steam Power on Tramways.**

Kitson & Co.'s engines on the Birmingham Central Tramways weigh, with water and coal, from 9 to 10 tons. They draw a car holding 60 passengers. On the same line, the engines of the Falcon Company have 8-inch cylinders, with 14 inches of stroke, and 2 $\frac{1}{2}$  feet wheels. In drawing two loaded cars weighing together 18 $\frac{1}{2}$  tons, at a speed of 6 miles per hour, on a gradient of 1 in 25, they indicated 40 horsepower, consuming from 8 to 9 pounds of coke per mile.

**Compressed-Air Tramway Engines.**

Mekarski's system of employing compressed air, heated by an admixture of steam, is in operation on the Nantes tramways. The efficiency of the air-compressors is 76 per cent. in volume of air delivered: one kilogramme, or 2.205 pounds of air, compressed to a pressure of 426 lbs. per square inch, supplies energy equivalent to 90,375 foot-pounds, and 100 kilogrammes, or 220 pounds of compressed air, is sufficient to propel a car of 8 tons loaded weight for a distance of from 7 $\frac{1}{2}$  to 8 or 9 miles. The cars have seats for 19 persons, a platform for 15 or 16 at one end, and the heater and the driver's cab at the other end. The total length is 23 $\frac{1}{4}$  feet, and the

width is  $7\frac{1}{4}$  feet. The weight of the car is 6 tons empty, 8 tons full, of which the adhesion weight is  $4\frac{1}{2}$  tons. The compressed air is contained in 10 cylindrical reservoirs, placed transversely underneath the platform, connected by pipes, in two sets, to form a working and a reserve battery, having respectively 70 and 28 cubic feet of capacity; together, 98 cubic feet, and holding, when charged, 220 pounds of compressed-air. The working cylinders are outside,  $5\frac{1}{4}$  inches in diameter, with a stroke of  $10\frac{1}{4}$  inches; the compressed air is cut off at one-third. The driving wheels are  $27\frac{1}{2}$  inches in diameter. The heater has a capacity of 28 gallons, and the water is heated to  $300^{\circ}$  F. by the injection of steam before starting. The consumption of compressed air varies from 23 pounds to  $28\frac{1}{2}$  pounds per mile. The working cost is at the rate of about *6d.* per mile-run.

From the results of trials made by D. K. Clark of one of Hughes & Lancaster's low-pressure compressed-air tramcars, propelled by means of four single-acting 5-inch cylinders, of 3 inches stroke, it appears that the consumption of compressed air was at the rate of  $30\frac{1}{2}$  pounds per mile-run for a level. The car, with passengers, weighed  $4\frac{1}{2}$  tons; and the work done was at the rate of 22,070 foot-pounds per pound of air. The maximum working pressure of compressed air was 132 lbs. per square inch.

### Electrical Propulsion on Tramways.

The Bessbrook and Newry Tramway, 3 miles long, has an average gradient of 1 in 86, and a maximum gradient of 1 in 50; and is to a 3 feet gauge. It is worked by electric power. Two passenger cars, 33 feet and 21 feet 8 inches long, are each provided with a motor. The longer car weighs  $8\frac{1}{4}$  tons, comprising 2 tons, 1 cwt., 1 quarter, the weight of the dynamo, bed-plate, armature, and accessories. The shorter car is similar to the longer; and there is a third passenger car 33 feet long, weighing  $5\frac{1}{2}$  tons. The generator is worked by a fall of water, 28 feet high. There are two generating dynamos for a normal output of 250 volts, 72 ampères, at a speed of 1,000 revolutions per minute, for which the electrical efficiency is 92.2 per cent., and the commercial efficiency 90.4 per cent. The conductor is of channel steel, laid midway between the rails or under insulators. The circuit is completed by the rails of the permanent way, which are uninsulated. Each locomotive car is fitted with an Edison-Hopkinson dynamo-motor. A speed of one mile per hour corresponds to 100 revolutions of the dynamo-axle per minute. Three trains, having six trucks, four trucks, and no trucks respectively,



and weighing 28·64 tons, 21·9 tons, and 8·8 tons, including the weight of the locomotive, were tried for efficiency. The leading results are given in Table 300, and the percentages in Table 301.

**TABLE 300.—BESSBROOK AND NEWRY TRAMWAYS :  
RESULTS OF ELECTRICAL TRACTION.**

Items.	First Journey.	Second Journey.	Third Journey.
	Tns. Cwts. Qrs.	Tns. Cwts. Qrs.	Tns. Cwts. Qrs.
Gross load . . . . .	28 12 3	21 18 0	8 16 0
Average speed, in miles per hour . . . . .	5·7	7·2	11·3
Total energy of water, in foot-pounds . . . . .	60,291,000	40,860,600	27,522,000
Total electrical energy developed by generator, in foot-pounds . . . . .	35,871,000	21,516,000	9,332,400
Total mechanical energy developed by motor, in foot-pounds . . . . .	24,928,200	15,493,500	7,170,900
Sum of electrical losses, in foot-pounds . . . . .	12,493,800	5,841,000	2,174,700
Loss in generator, in foot-pounds . . . . .	3,343,000	1,735,800	801,900
" leakage . . . . .	1,420,300	1,029,600	775,500
" resistance of line, " in foot pounds . . . . .	3,613,500	1,296,900	287,100
" motor, in foot-pounds . . . . .	4,098,600	1,791,900	326,700
Total work done against gravity . . . . .	11,867,400	7,356,800	2,858,300
" friction . . . . .	13,060,800	8,136,700	4,312,600
Average tractive " forces, exclusive of gravity, in pounds per ton . . . . .	28·9	27·4	37·1

**TABLE 301.—BESSBROOK AND NEWRY TRAMWAYS :  
PERCENTAGE DISTRIBUTION OF POWER.**

Items.	1st Journey.		2nd Journey.		3rd Journey.	
	Water Power.	Total Power of Generator.	Water Power.	Total Power of Generator.	Water Power.	Total Power of Generator.
	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.
Water power . . . . .	100·0	...	100·0	...	100·0	...
Generator power . . . . .	59·5	100·0	52·6	100·0	33·9	100·0
Net motor power . . . . .	41·3	69·4	37·9	72·0	26·1	76·8
Loss in generator . . . . .	5·5	9·3	4·2	8·0	2·9	8·6
" leakage . . . . .	2·3	3·9	2·5	4·8	2·8	8·3
" line resistance . . . . .	6·0	10·6	3·2	6·0	1·0	3·1
" in motor . . . . .	6·8	11·4	4·4	8·3	1·2	3·1

The Barking Road section of the North Metropolitan Tramways is worked by electrical power by contract, charged for at the rate of about  $4\frac{1}{2}d.$  per car mile run, including the wages of the driver.

### Resistance to Traction on Common Roads.

(F. V. Greene.)

WAY.	Pounds per ton.
Iron . . . . .	10 lbs.
Asphalte . . . . .	15 „
Wood . . . . .	21 „
Best stone blocks . . . . .	33 „
Inferior stone blocks . . . . .	50 „
Average cobble stone . . . . .	90 „
Macadam . . . . .	100 „
Earth . . . . .	200 „

### STEAM-SHIPS.

The gross register tonnage of a ship is reckoned at the rate of 100 cubic feet of capacity per ton, by the formula :—

$$\text{Register tonnage} = C \frac{L B D}{100} \quad (1)$$

L = inside length on the upper deck from the plank at the stem to the plank at the stern, in feet.

B = inside main breadth from ceiling to ceiling, in feet.

D = inside midship depth from the upper deck to the ceiling at the limber strake, in feet.

C = a constant, the values of which are as follows :—

Sailing ships . . . . .	C	70
Steam vessels and clippers	{ Ships of 2 decks . . . . .	65
	{ Ships of 3 decks . . . . .	68
Yachts . . . . .	{ Above 60 tons . . . . .	50
	{ Under 60 tons . . . . .	45

The values thus obtained express the entire cubical capacity of the ship. Deductions are allowed for buildings erected for the shelter of passengers only, for crew space at the rate of 72 cubic feet per man, and propelling space. This third item, for screw steamers, is taken as 32 per cent. if the cubic content is 13 per cent. and under 20 per cent. of the gross tonnage ; if the space is smaller than 13 per cent. and larger

than 20 per cent., deduct 32 per cent., or  $1\frac{1}{4}$  times the content. For paddle-steamers, deduct 37 per cent., if the content is 20 per cent. and under 30 per cent.; if the space is smaller than 20 per cent. or larger than 30 per cent., deduct 37 per cent., or  $1\frac{1}{2}$  times the content.

Builder's measurement is computed in terms of the length and the breadth by the formula :—

$$\text{Tonnage} = \frac{(L - .60 B) 1.5 B}{94} \quad (2)$$

L = length measured from the back of the main stern post to a vertical from the fore part of the main stem under the bowsprit, in feet.

B = the extreme breadth to the outside planking, exclusive of doubling planks, in feet.

### Resistance of Ships.

The thrust on the collars of the propeller shaft is a measure of the power actually exerted for the propulsion of the vessel. Let P = the thrust or pressure of the propeller against the thrust bearing in pounds; and S = the speed of the ship in feet per minute; the effective horse-power is,—

$$\frac{S \times P}{33,000}$$

Taking it as two-thirds of the indicator power, which is a usual proportion,  $\frac{2}{3}$  I. H. P. =  $\frac{S \times P}{33,000}$ ; and

$$P = \text{I. H. P} \times \frac{22,000}{S} \quad (3)$$

The effective indicator horse-power required to propel a steam-ship is given by the following formulæ :—

$$\text{Eff. I. H. P.} = \frac{D^3 \times S^3}{C} \quad (4)$$

$$\text{Eff. I. H. P.} = \frac{A \times S^3}{K} \quad (5)$$

I. H. P. = effective indicator horse-power, or the net indicator power for propulsion.

D = displacement, in tons.

S = speed in knots per hour.

A = immersed mid ship section, in square feet.

C = a constant.

K = a constant.

The results obtained by means of these formulæ are to be taken as only approximate. The first is the more trustworthy. The following are a few values of the constants C and K :—

Length.	Speed.	C.	K.
Less than 200 feet .	About 10 knots	210	600
200 to 250 feet . .	11 "	220	600
250 to 300 " . .	12 "	240	620
300 to 400 " . .	15 "	250	650
Over 400 " . .	17 "	240	620

The effective indicator horse-power may also be calculated in terms of the area of wetted surface, by the formula :—

$$\text{Eff. I. H. P.} = \frac{W \times S^3}{20,000} \quad . \quad . \quad . \quad (6)$$

W = area of wetted surface, in square feet.

S = speed in knots per hour.

### Forced Draught in Marine Boilers.

A blast of compressed air was applied in the chimney of the "Résolue," with the results given in Table 302.

TABLE 302.—COMPRESSED-AIR EXHAUSTING BLAST ON THE S.S. "RÉSOLUE."

Horse-power of the Blowing Engine.	Horse-Power of the Main Engine.	Coal Consumed per Hour (Anzin briquettes).	Coal per Indicator Horse-Power per Hour.	Water Evaporated per Pound of Coal.
I. H.-P.	I. H.-P.	Pounds.	Pounds.	Pounds.
0.00 natural draught	57.5	213	3.72	10.77
0.96				
2.00	88.8	289	3.26	8.82
3.00	100.5	315	3.12	8.00
4.20	106.1	321	3.04	7.82
5.00	118.8	348	2.93	7.82
6.00	119.8	374	3.12	7.53
7.40	127.9	400	3.12	7.00
	135.7	420	3.10	7.03

The fuel consumed and the power were doubled, but the evaporative efficiency was reduced.

From the results of trials on ships of the Navy, it appears that with open stokeholds and natural draught versus closed stokeholds and forced draught, the indicator power of the engines was increased by  $52\frac{1}{2}$  per cent.; and 65 per ton of boiler.

By Mr. Fothergill's system of closed ashpits and forced draught, there is an economy of 20 per cent. of coal for steaming.

With a combined forced and induced draught by compressed air into the ashpit, the speed of a steam launch was increased from 3 knots to 6 knots per hour. The quantity of water evaporated per hour was trebled.

By an induced draught caused by an exhausting fan at the base of the chimney of a marine boiler, nearly three times as much water was evaporated as by natural draught; about 6 per cent. less water was evaporated per pound of coal.

**Average Weight of Steam-Engines with Boilers, Water, and all Fittings per Indicator Horse-power.**

(F. C. Marshall.)

	Per I. H. P.
Merchant steamer . . . . .	180 lbs.
Royal Navy . . . . .	360 "
Engines specially designed for light-draught vessels . . . . .	280 "
Royal Navy, Polyphemus Class . . . . .	180 "
Locomotive . . . . .	140 "
Torpedo vessels . . . . .	60 "
Ordinary Marine boilers, with water . . . . .	196 "
Locomotive boilers, with water . . . . .	60 "

**Average Proportions and Results of Performance of Compound Engines.**

(F. C. Marshall.)

	Average.
Speed of piston, in feet per minute . . . . .	from 350 to 550 . . . . . 467 ft.
Working pressure of steam above the atmosphere . . . . .	" 70 lbs. to 100 lbs. . . . . 77.4 lbs.
Condensing surface . . . . .	" 1,518 to 7,427 sq. ft.
Heating surface . . . . .	" 2,379 to 11,045 "
" I. H. P. " per horse-power . . . . .	" 2.77 to 6.30 " . . . . . 3.92 sq. ft.
Indicator horse-power . . . . .	" 560 to 2,745 I. H. P.
Coal consumption in 24 hours . . . . .	" 11 to 51.9 tons.

		Average.
Coal consumption	} from 1½ to 2 lbs. . . .	1·83 lbs.
per I. H. P. per hour . . . .		
Heating surface per	} „ 1·65 to 3·12 sq. ft. . .	2·18 sq. ft.
pound of coal per hour . . . .		

The above proportions apply with sufficient nearness to the multiple compound practice of to-day, excepting that higher pressures are employed, up to 160 lbs. per square inch in the boiler; and that the consumption of coal may, under good conditions, be reduced as low as 1·44 lbs. per I. H. P. per hour.

### Horse-power of Marine Engines.

The North East Coast Institution of Engineers and Ship-builders have framed a general rule for what they designate the Normal Indicator Horse-power on loaded trial trip of surface-condensing marine screw engines working at any boiler pressure between 50 lbs. and 250 lbs. per square inch.

$$\text{(For screw engines) N. I. H. P.} = \frac{(D^2 \sqrt[3]{S} + 3H) \sqrt[3]{P}}{100} \quad (7)$$

D = diameter of low-pressure cylinder, in inches.

S = stroke of piston, in inches.

P = working boiler pressure, in lbs. per square inch above the atmosphere.

H = heating surface of boilers, in square feet.

P<sub>m</sub> = mean pressure in lbs. per square inch, reduced to low-pressure cylinder.

R = revolutions per minute.

N. I. H. P. = maximum normal indicator horse-power, or loaded trial trip, of surface-condensing marine screw engines.

The conditions assumed as normal are: 1. That the steam, whatever its initial pressure, is expanded in the engines to the same pressure. 2. That the expansion is effected in the engines with the same degree of efficiency for all pressures between 50 lbs. and 250 lbs. per square inch. On this condition, for the higher pressures, engines of triple, quadruple, or more expansions, must be employed, the number of expansions depending on the initial pressure. From conditions 1 and 2, it follows that the mean pressure reduced to the low-pressure cylinder, P<sub>m</sub>, may be assumed as proportional to the cube root of the boiler pressure,  $\sqrt[3]{P}$ ; and that its actual

loaded trial-trip value may be taken without sensible error as  $5.6 \sqrt[3]{P}$ . 3. That the piston speeds of engines of different lengths of stroke, are proportional to the cube roots of their respective strokes; and that the actual loaded trial-trip value of piston speed may be taken as  $144 \sqrt[3]{S}$ . 4. That in all cases where the engines and boilers bear to each other such proportions as to prevent condition 1 from being fulfilled, without thereby violating condition 3, the coal consumption per indicator horse-power will not be affected, but will be constant for the same boiler pressure. 5. That the boilers are constructed in accordance with the fair average practice of the present day; that if forced draught be employed, it does not exceed the average chimney draught; that the horse-power is proportional to the heating surface,  $H$ , and to the cube root of the pressure,  $\sqrt[3]{P}$ ; and that the actual loaded trial-trip horse-power may be taken as  $\frac{H \sqrt[3]{P}}{16}$ . 6. That the efficiency of the engine mechanism is constant, and that the propeller is such that the engines may utilise the boiler power in the manner prescribed in conditions 3 and 4.

### Deductions from the Rule.

$$\text{I. H. P. of engines} = D^2 \sqrt[3]{P S} \quad . \quad . \quad . \quad (8)$$

$$\text{I. H. P. of boilers} = \frac{H \sqrt[3]{P}}{16} \quad . \quad . \quad . \quad (9)$$

These values (8) and (9) are equal; and, reducing.—

$$(\text{For screw engines}) H = \frac{D^2 \sqrt[3]{S}}{3.25} \quad . \quad . \quad (10)$$

Assuming that half the sum of the powers calculated for the engines and boilers taken together, or the mean of the powers, represents the effective power of the system,—

N. I. H. P. of screw engines and boilers jointly =

$$\frac{(D^2 \sqrt[3]{S} + 3 H) \sqrt[3]{P}}{100} \quad . \quad . \quad . \quad (11)$$

For paddle engines, the same formula is available, with a suitable co-efficient. Taking the piston speed at  $90 \sqrt[3]{S}$  :—

$$(\text{For paddle engines}) \text{N. I. H. P.} = \frac{(D^2 \sqrt[3]{S} + 5 H) \sqrt[3]{P}}{160} \quad (12)$$

$$H = \frac{D^2 \sqrt[3]{S}}{5.2} \quad . \quad . \quad . \quad (13)$$

What is known as nominal horse-power may be valued at one-sixth of the normal indicator horse-power.

In America, a standard of horse-power has come into practice, measured by 30 pounds of water evaporated per hour, at a pressure of 70 lbs. per square inch above the atmosphere, from 100° F. per horse-power.

### PUMPING STEAM-ENGINES AND PUMPS.

The net work done, or duty effected by a pump, is equal to the product of the weight in pounds of water lifted by the height in feet through which it is raised. The efficiency of the pump is the ratio of the effective work done to the whole work expended in driving the pump. The efficiency increases generally with the height of the lift, as shown in Table 303.

TABLE 303.—EFFICIENCY, OR RATIO OF DUTY TO ENGINE-POWER, OF LARGE PUMPING ENGINES.

	Head, in Feet.	Efficiency per Cent.
Cornish pumping engines . . . . .	140	90·8
Rotative beam engine . . . . .	20·5	86
Rotative Woolf beam . . . . .	210	85 to 88
Rotative receiver beam . . . . .	35	77·4
Rotative compound beam . . . . .	169	83·7
Worthington pump . . . . .	60·6	85
" " . . . . .	148·5	91·5

The duty of a pumping engine is defined as the number of pounds of water lifted one foot high, by the consumption of 1 cwt. of coal (112 pounds). The duty may be deduced from the performance of a pumping engine expressed in pounds of coal consumed per indicator horse-power, by dividing 1,980,000 by the given pounds of coal, and multiplying the quotient by 112.

Conversely, the fuel consumed per net horse-power of the pump may be calculated from the duty expressed in foot-pounds per cwt. of coal, by dividing the duty by 112, to give the duty per pound of fuel; and dividing the quotient into



1,980,000. The final quotient is the quantity of coal in pounds consumed per horse-power per hour.

Or, divide 222 by the duty in millions of pounds lifted one foot per cwt. of fuel. The quotient is the quantity of coal consumed in pounds per horse-power per hour.

The duty or effective horse-power of pumping engines, varies from 75 per cent. to 85 per cent. of the indicator power, for vertical direct-acting and beam-rotative engines. For horizontal pumping engines, the duty horse-power is about 85 per cent. of the indicator power. The Worthington horizontal compound direct-action pumping engine, tested by Mr. J. G. Mair, realised a duty power  $91\frac{1}{2}$  per cent. of the indicator power; or, deducting  $3\frac{1}{2}$  per cent. for the aid of an auxiliary engine to work the air-pump and the feed-pump, a net efficiency of 88 per cent. is obtained.

The slip of large reciprocating pumps varies from 5 per cent. to  $1\frac{1}{2}$  per cent., or occasionally less: showing that from 95 per cent. to  $98\frac{1}{2}$  per cent. of the working capacity of the pump is utilised. An average of  $2\frac{1}{2}$  per cent. of slip may be taken. It is customary to include an allowance of 5 per cent. for slip. In rare instances there is no slip.

Of the four values, the area and stroke of the pump, and the area and stroke of the steam cylinder, or of the second cylinder of a compound engine, to find the value of one, when those of the three others are known. The product of the area of the steam cylinder by the effective average pressure per square inch is equal to the product of the area of the pump barrel by the load in pounds per square inch, plus an allowance, say, of 25 per cent. to overcome frictional resistance. Whence the following rules, in which the areas of the cylinder and the pump-barrel are expressed in square inches, and the pressures and loads in pounds per square inch:—

1. *To find the required area of the cylinder.* Multiply the area of the air-pump by the load on the pump, and divide by the effective average pressure of steam available in the cylinder. Add 25 per cent. of the area for friction.

2. *To find the average effective steam pressure required in the cylinder.* Multiply the area of the pump by the load on the pump, and divide by the area of the cylinder. The quotient is the effective average pressure required to balance the load. Add 25 per cent. of the pressure for friction.

3. *To find the load against which the pump will deliver water.* Multiply the area of the cylinder by the effective average steam pressure, and divide by the area of the pump. From the quotient deduct 20 per cent. for friction; the remainder is the pressure or load under which water will be delivered.

4. *To find the area of the pump-barrel.* Multiply the area of the cylinder by the effective average steam pressure, and divide by the load. Deduct 20 per cent. for friction; the remainder is the area of pump-barrel required to balance the load.

In the case of compound engines, the area of the second cylinder is to be taken into the calculation; and the effective average pressure in the first cylinder is to be reduced in the ratio of the area of the second cylinder to that of the first cylinder; and, thus reduced, added to the effective average pressure in the second cylinder. The sum is to be adopted for calculation as in the case of a single cylinder.

### Speed of Pistons.

The speed of steam-pistons may be from 100 feet to 200 feet per minute. The water may pass through the service-pipes at speeds of from 150 feet to 350 feet.

Six-inch three-throw pumps, raising water, performed the following duties for corresponding lifts, in parts of the indicator power:—

Water per Hour.	Lift.	Efficiency.
120 barrels	165 feet	77 per cent.
160 "	140 "	65.6 "
80 "	54 "	78.5 "
250 "	48 "	45.0 "

### Centrifugal Pumps.

TABLE 304.—RAISING WATER FROM DEEP WELLS.  
(Appleby.)

Quantity of Water lifted per Hour.	Lift for One Man on Crank.	Lift for One Donkey Engine.	Lift for One Horse Engine.	Lift for One Horse-Power Steam-Engine.
Gallons.	Feet.	Feet.	Feet.	Feet.
200	90	180	630	990
350	52	102	357	561
500	36	72	252	396
650	28	56	196	308
800	22	45	154	242
1000	18	36	126	198

The maximum duty of a centrifugal pump worked by a steam-engine, according to the late Mr. David Thomson, varies from 55 per cent. for smaller pumps to 70 per cent. for larger pumps. For lifts of from 15 to 20 feet, they are as economical of power as ordinary pumps; for lifts of 4 or 5 feet they are more efficient.

The height to which water would ascend in a pipe by the action of centrifugal force, would, if there were no other resistances, be that due to the velocity of the circumference of the revolving wheel, or to  $\frac{v^2}{2g}$  or  $\frac{v^2}{64}$ .

### Chain Pumps.

An endless chain, fitted with floats, circulating continuously, and drawing up an inclined plane, utilises in duty, 40 per cent. of the power applied. Lifting water through a vertical pipe, the efficiency is 65 per cent. The slip is about 17 per cent.

### Hydraulic Rams.

The efficiency of the hydraulic ram is expressed by Dautbuisson's formula:—

$$\frac{d'h'}{dh} = 1.42 - .28 \sqrt{\frac{h'}{h}} \quad (1)$$

$d$  = quantity of water used, in gallons per minute.

$d'$  = quantity of water raised, in gallons per minute.

$h$  = head used, in feet.

$h'$  = lift, in feet.

TABLE 305.—EFFICIENCY OF HYDRAULIC RAMS.

Ratio of Lift to Fall. Fall = 1.		Ratio of Lift to Fall. Fall = 1.		Ratio of Lift to Fall. Fall = 1.		Ratio of Lift to Fall. Fall = 1.	
Ratio.	Efficiency. Per cent.	Ratio.	Efficiency. Per cent.	Ratio.	Efficiency. Per cent.	Ratio.	Efficiency. Per cent.
4	72	10	44	16	25	22	9
5	66	11	41	17	22	23	7
6	61	12	37	18	19	24	4
7	57	13	34	19	17	25	2
8	52	14	31	20	14	26	0
9	48	15	28	21	12		

The Table 305 of efficiencies was calculated by means of

this formula, only five-sixths of the calculated values being taken, in order to cover contingencies.

According to Eytelwein's formula, the proper diameter of the driving-pipe, in inches, is equal to the square root of the quantity of water in gallons per minute:

### Cast-Iron Water-Pipes.

The suitable thickness of cast-iron water-pipes is given by the formulæ,—

$$t = .25 + \frac{Hd}{9600} \quad . \quad . \quad . \quad . \quad . \quad (2)$$

$$t = .25 + \frac{pd}{4250} \quad . \quad . \quad . \quad . \quad . \quad (3)$$

$t$  = thickness of pipe, in inches.

$H$  = head of pressure, in feet of water.

$d$  = inside diameter of pipe, in inches.

$p$  = the interior pressure, in pounds per square inch.

For the usual head, 300 feet of water, the formula (2) becomes,—

$$t = .25 + .031 d \quad . \quad . \quad . \quad . \quad . \quad (4)$$

For socket ends, the equivalent length of pipe, equal in weight to that of the socket, is given by the formula,—

$$\text{Equivalent length in inches} = 7 + \frac{d}{15} \quad . \quad . \quad . \quad . \quad (5)$$

$$\text{“ “ feet} = 7 + \frac{d}{180} \quad . \quad . \quad . \quad . \quad (6)$$

The additional weight for a pair of joint-flanges is equivalent to that of a lineal foot of pipe.

### COAL GAS, &c.

TABLE 306.—PRODUCTS OF DISTILLATION OF COAL,  
PER TON.

	Wigan Cannel.	Wigan Coal.	Newcastle Coal.
Gas . . . . .	10,900 cub. ft.	9980 cub. ft.	9700 cub. ft.
Coke . . . . .	1436 pounds.	1517 pounds	1540 pounds
Tar . . . . .	17 gallons	11 gallons	9 gallons
Ammoniacal liquor .	18 “	20 “	10 “
Illuminating power of gas . . . . .	24 sperm candles	15 caudles	15 candles
Percentage of coke .	64 per cent.	68 per cent.	70 per cent.

**Average Yield of Bituminous Coal, by Weight.**

(Newbigging.)

	Per cent.
Gas . . . . .	18
Coke and breeze . . . . .	68
Tar . . . . .	5
Ammoniacal liquor . . . . .	9
	<hr/> 100

**TABLE 307.—RESULTS OF DISTILLATION OF ONE TON OF NEWCASTLE CANNEL COAL, FOR GAS AND FOR OIL.**

(Gesner.)

Distilled for Gas, at from 1000° to 1200° F.		Distilled for Oil, at from 750° to 800° F.	
Gas . . . . .	7450 cub. ft.	Gas . . . . .	1400 cub. ft.
Tar . . . . .	18½ gallons	Crude oil . . . . .	68 gallons
Coke . . . . .	1200 pounds	Coke . . . . .	1280 pounds
<i>Products of the Tar.</i>		<i>Products of the Crude Oil.</i>	
Benzole . . . . .	3 pints	Eupion . . . . .	2 gallons
Coal-tar naphtha . . . . .	3 gallons	Lamp Oil . . . . .	22½ "
Heavy oil and } naphthaline . }	9 "	Heavy oil and } paraffin . }	24 "
	12½ "		48½ "

**TABLE 308.—AVERAGE COMPOSITION OF LONDON GAS, BY VOLUME.**

(Dr. Letheby, 1866.)

Description of Gas.	Common Gas.	Cannel Gas.
	Per cent.	Per cent.
Hydrogen . . . . .	46·0	27·7
Light carburetted hydrogen . . . . .	39·5	50·0
Olefiant gas . . . . .	3·8	13·0
Carbonic oxide . . . . .	7·5	6·8
Carbonic acid . . . . .	0·7	0·1
Aqueous vapour . . . . .	2·0	2·0
Nitrogen . . . . .	0·5	0·4
	100·0	100·0



**Weight of Coal.**

	Per Cubic Foot, Solid.	Per Cubic Foot, Heaped.	Cubic Feet in One Ton, Heaped.
Anthracite	85.4 lbs.	58.3 lbs.	38.4 cubic feet.
Bituminous	78.3 „	49.8 „	45.3 „
Cannel	76.8 „	48.3 „	43.1 „

TABLE 310.—CALORIFIC VALUE OF COAL GAS.  
(T. L. Miller.)

Place of Manufacture.	Heating Power per Cubic Foot.
	Heat-Units.
Glasgow . . . . .	813
Liverpool . . . . .	770
Kilmarnock . . . . .	680
Manchester . . . . .	654
Birmingham . . . . .	639
London . . . . .	624
Hoboken . . . . .	617
Berlin . . . . .	549

**Weight of Lime.**

1 bushel of quicklime weighs about	70 lbs.
1 cubic foot „ „ „	54 „
1 cubic yard „ „ „	1460 „
1 ton „ „ „	measures about 32 bushels.

Area of pipe-surface required for condensation of gas—  
10 square feet per 1000 cubic feet of maximum production per  
day of 24 hours (*Newbigging*).

**Illuminating Power of Gas.**

The standard for comparison of gases for illuminating power is the sperm candle, weighing six to the pound, each burning off at the rate of 120 grains of sperm per hour. The gas for comparison is burned at the rate of 5 cubic feet per hour.

The gas supplied in London averages more than 16 candles for illuminating power. In fact, the larger companies are required, by Acts of Parliament, to supply gas of such a quality, that when burned through the Government standard Argand burner at the rate of 5 cubic feet per hour, it shall be capable of giving a light equal to that of 16 spermaceti candles, of six to the pound, when each candle is burning.

the rate of 120 grains of material per hour. This is called common gas. The London companies, and most provincial companies, are required to maintain in all their street mains a pressure equal to a column of water 1 inch in height, between sunset and midnight; and a pressure of  $\frac{9}{10}$  inch between midnight and sunset.

### Main Pipes.

Main pipes should be tested to 150 feet of water pressure.

Cast-iron pipes below 3 inches bore, are made in lengths of 6 feet; from 3 inches to 11 inches, 9 feet long; 12 inches and upwards, 6 feet or 9 feet long.

The weight of cast-iron pipes is given by the formula, —

$$W = 2.45 (D^2 - d^2) \quad (1)$$

$D$  = diameter, outside, in inches.

$d$  = diameter inside, in inches.

$W$  = weight in pounds per lineal foot.

The weight of a socket is equal to  $\frac{9}{10}$ ths of that of a lineal foot of the pipe.

TABLE 311.—THICKNESS OF CAST-IRON GAS MAIN PIPES.

Diameters.	Thick- ness.	Diameters.	Thick- ness.	Diameters.	Thick- ness.
Inches.	Inches.	Inches.	Inches.	Inches.	Inches.
1, 1½, 2	$\frac{5}{16}$	12, 13, 14, 15	$\frac{8}{8}$	30	1
2½, 3, 4	$\frac{3}{8}$	16, 17, 18	$\frac{11}{16}$	36	1½
5, 6	$\frac{7}{16}$	19, 20, 21	$\frac{3}{4}$	42	1¾
7, 8, 9	$\frac{1}{2}$	22, 23	$\frac{13}{16}$	48	1½
10, 11	$\frac{9}{16}$	24	$\frac{7}{8}$		

TABLE 312.—THICKNESS AND WEIGHT OF WROUGHT-IRON GAS PIPES.

Diameter.	Thickness.	Weight per Lineal Foot.
Inches.	Inch.	Pounds.
3, 3½	$\frac{5}{32}$ full	6, 7
4, 5, 6	$\frac{3}{16}$	9, 10½, 13
7, 8, 9	$\frac{1}{4}$ bare	16, 20, 24½
10, 12	$\frac{1}{4}$	28, 33
14, 16	$\frac{5}{16}$	43, 50



TABLE 313.—SMALL GAS-TUBES.

Diameter Inside.	Light.		Heavy.	
	Weight per Yard.	Length of Bundles.	Weight per Yard.	Length of Bundles.
Inches.	Lbs. Oz.	Yards.	Lbs. Oz.	Yards.
$\frac{1}{4}$	0 11 $\frac{1}{2}$	80	0 15	67
$\frac{3}{8}$	1 2	60	1 6 $\frac{1}{2}$	46
$\frac{1}{2}$	2 0	32	2 10	16
$\frac{5}{8}$	2 4	25	3 0	20
$\frac{3}{4}$	3 3	23	3 12	19
1	4 8	26	6 0	20
1 $\frac{1}{4}$	8 0	16	10 0	12
1 $\frac{1}{2}$	12 0	10	14 0	9
2	18 1	5	21 0	5

TABLE 314.—SMALL BRASS TUBES.

Diameter Outside.	Weight per Foot.	Diameter Outside.	Weight per Foot.
Inches.	Pounds or Ounces.	Inches.	Pounds or Ounces.
$\frac{1}{4}$	·08 or 1·28	$\frac{7}{8}$	·50 or 8·00
$\frac{5}{16}$	·15 „ 2·40	1	·59 „ 9·44
$\frac{3}{8}$	·19 „ 3·04	1 $\frac{1}{4}$	·81 „ 12·96
$\frac{7}{16}$	·21 „ 3·36	1 $\frac{1}{2}$	1·00 „ 16·00
$\frac{1}{2}$	·25 „ 4·00	1 $\frac{3}{4}$	1·12 „ 17·92
$\frac{9}{16}$	·31 „ 4·96	2	1·25 „ 20·00
$\frac{5}{8}$	·37 „ 5·92	2 $\frac{1}{2}$	1·50 „ 24·00
$\frac{3}{4}$	·43 „ 6·88	3	1·87 „ 29·92

**Flow of Gas through Pipes.**

Dr. Pole's formula for the volume of gas delivered through large pipes is as follows,—

$$Q = 1350 d^2 \sqrt{\frac{hd}{sl}} \quad . \quad . \quad . \quad . \quad . \quad . \quad (2)$$

Conversely, the diameter of pipes required for a given rate of delivery, is,—

$$d = \sqrt[3]{\frac{Qsl}{(1350)^2 h}} \quad . \quad . \quad . \quad . \quad . \quad . \quad (3)$$

$Q$  = quantity of gas delivered, in cubic feet per hour.

$l$  = length of pipe, in yards.

$d$  = diameter of pipe, in inches.

$h$  = pressure in inches of water.

$s$  = specific gravity of gas = 40 ; that of air being = 1.

For any other specific gravity, multiply the value of  $Q$  given by formula (2), by  $\cdot 6325$  (or  $\sqrt{0\cdot 40}$ ), and divide the product by  $\sqrt{\text{specific gravity}}$ .

The discharge for small pipes is less than the calculated quantity. The value of  $d$  by formula (3) is to be augmented one-third for lead service pipes; and one-half for wrought-iron service pipes.

### Dowson Gas.

The Dowson gas is a cheap gas, generated by passing a mixture of superheated steam and air through a mass of red-hot carbonaceous fuel—anthracite by preference. The composition of the gas, generated with Garnant anthracite, as analysed by Professor William Foster, is as follows,—

	Volume per cent.
Hydrogen . . . . .	18·73
Marsh gas . . . . .	·31
Olefiant gas . . . . .	·31
Carbonic oxide . . . . .	25·07
Carbonic acid . . . . .	6·57
Oxygen . . . . .	·03
Nitrogen . . . . .	48·98
	<hr/>
	100·00

The calorific power of Dowson gas is about one-fourth of that of London gas. The anthracite fuel consumed per 1000 cubic feet is 13·2 pounds. Tested by D. K. Clark, in working an Otto gas engine developing 4·41 indicator horse-power, and 3·26 break horse-power, at a speed of 156 revolutions per minute, the following results were yielded:—

Gas consumed per indicator horse-power				110·34 cubic feet.
	"	"	break	149·30 "
Fuel	"	"	indicator	1·45 lbs. "
"	"	"	break	1·97 "

The cost of Dowson gas is 50 per cent. less than that of coal-gas at 3s. per 1000 cubic feet. Whilst coal-gas of average composition requires chemically 5·3 volumes of air for combustion, each volume of Dowson gas requires only 1·1 volume of air.

More recently, Mr. Dowson has produced his gas from ordinary gas-coke. From the results of thirteen Otto engines, using Dowson gas, indicating from 150 to 16 horse-power, it appears that from 1·5 pounds to 1·2 pounds of fuel was consumed per indicator horse-power per hour.

TABLE 315.—OIL GAS, FROM BLUE PARAFFIN OIL.  
(Macadam.)

Items.	Pintsch's Apparatus.			Keith's Apparatus.		
	1	2	Mean	1	2	Mean
Specific gravity of oil . . . . .	'878	'878	'878	'874	'878	'876
Flashing point . . . . .	296°	294°	295°	292°	286°	289°
Firing point . . . . .	356°	352°	354°	348°	346°	347°
Gas per gallon, cubic feet . . . . .	90·7	103·4	97	85	84·8	84·9
Illuminating power . . . . .	62·5	59·1	60·8	63·2	59·5	61·4
Volume of oil in gallons, flowing in to each retort, per hour	1·4	1·18	1·29	2·3	1·3	1·8
Gas per retort, per hour, cubic feet	126·8	122·5	124·6	197·5	111·9	154·7
Heavy hydrocarbons, per cent.	39·2	37·1	38·2	39·9	38·2	39·0
Gas per ton, cubic feet . . . . .	23,138	26,356	24,742	21,772	21,671	21,721

TABLE 316.—PRODUCER GAS: COMPOSITION, BY WEIGHT.

Elementary Gases.	H. Hydro- gen.	CO. Carbonic Oxide.	CO <sub>2</sub> . Carbonic Acid.	CH <sub>4</sub> . Marsh Gas.	C <sub>2</sub> H <sub>4</sub> . Olefiant Gas.	N.
	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.
Siemens Producer	·00	24·92	6·95	·89	2·73	64·50
" "	·65	25·97	8·71	1·45	...	63·22
Wilson Producer .	·90	29·58	6·91	·91	...	61·70
" "	1·11	26·33	8·29	1·43	...	62·84

### Gas Engines.

The Crossley gas engine, horizontal, is constructed with a single cylinder, of nominal powers of from  $\frac{1}{2}$  H.P. to 30 H.P., indicating from 2 H.P. to 85 H.P.; and with double cylinders of from  $\frac{1}{4}$  H.P. nominal to 30 H.P., indicating from 16 H.P. to 170 H.P. The over-all dimensions of the engine only, single cylinder, vary from 6 feet by 3 feet 7 inches, to 12 feet by 8 feet 2 inches. The speed of the engines is at the rate of 160 revolutions per minute, except for the  $\frac{1}{2}$  H.P. and the 1 H.P. engines, which make 180 per minute.

The 12 H.P. engine has developed 28 indicator H.P., and 23 H.P. at the break, or 82 per cent. of the indicator power; consuming 20 cubic feet of gas per indicator horse-power per hour, or 24·3 cubic feet per break horse-power. In a 4 H.P. engine, 23·3 cubic feet was consumed per break horse-power

The following Table 317, gives some results of trials of a Crossley gas engine.\* The cylinder was 9½ inches in diameter, with a stroke of 18 inches; single-acting. The gas used was of the composition shown in Table 309.

TABLE 317.—CROSSLEY GAS ENGINE: RESULTS OF TRIALS.

Trial.	A	B	C
Power . . . . .	Full	Half	Empty
Revolutions per minute . . . . .	160·1	158·8	161·6
Explosions per minute . . . . .	78·4	41·1	10·2
Mean initial pressure . . . Lbs.	196·9	196·2	148·0
Mean effective pressure . . . ..	67·9	73·4	66·7
Indicator horse-power . . . H.-P.	17·12	9·73	2·19
Break horse-power . . . . .	14·74	7·41	...
Mechanical efficiency . . . Per cent.	86·1	76·2	...
Gas per hour, main . . . Cub. ft.	351·8	202·6	49·0
" " for ignition . . . "	3·5	3·2	...
" " total . . . . .	355·3	205·8	...
Gas per indicator H.P. per hour, ) main, Cub. ft. )	20·55	20·8	22·38
" " " total " " )	20·76	21·2	...
Gas per break H.P. per hour, main " .	23·87	27·34	...
" " " total " " .	24·10	27·77	...
Water for cooling per hour . . Lbs.	713	480	...
Rise of temperature . . . Fahr.	128°·0	102°·3	...
Power to drive engine only . . H.P.	2·38	2·31	2·19
Mean pressure during working stroke, ) equivalent to work done in pump- ) ing strokes . . . . . Lbs. )	2·19	...	...
Corresponding indicator . . . H.P.	·55	...	...

The distribution of the heat of combustion of the gas in working the Crossley engine, was as follows,—

Trial.	A. Per cent.	B. Per cent.	C. Per cent.
Heat turned into work	22·1	20·9	19·4
Heat rejected in jacket water	43·2	41·1	...
Heat rejected in exhaust	35·5	38·0	...
	100·8	100·0	...

\* See *Report of the Judges on Trials of Motors for Electric Lighting, 1889*, for the Society of Arts.

TABLE 318.—RESULTS OF TRIALS OF GAS ENGINES. (T. L. Miller.)

Type of Engine.	Tested by	Indicator Horse-Power.	Break Horse-Power.	Gas per I. H. P.	Gas per B.H. P.	Heat Converted into Work.	Revolutions per Minute.	Speed of Piston per Minute.
Otto	Adams	I. H. P. 3.42	B. H. P. 2.87	Cub. Feet. 30.9	Cub. Feet. 33.4	Per cent. 14.46	Turns. 160.3	Feet. 320.6
"	"	22.56	18.31	23.6	24.1	17.5	158.7	423.2
"	"	33.6	27.75	25.04	30.3	16.15	151.37	529.7
Clerk	Society of Arts	17.12	14.75	20.55	23.87	21.2	160.1	480.3
"	Garrett	3.62	2.70	29.8	40	10.5	212	308
"	"	9.05	7.23	24.3	30.42	12.9	146	292
"	"	27.46	23.21	20.39	24.12	15.5	132	440
Beck	Kennedy	7.35	5.71	21.18	27.27	20.7	212	530
"	"	6.12	4.84	20.67	26.14	21.1	168.9	422.8
Griffin	Jamieson	17.28	13.6	19.27	24.48	20.8	183	427
"	Kennedy	17.46	14.94	18.92	23.58	21.2	223.8	522
"	Society of Arts	15.47	12.51	22.64	28	19.2	198.1	420.5
Simplex	Witz	...	6.70	...	21.55	19.4	160	420
"	"	...	8.67	...	20.12	20.9	160	420
Forward	R. H. Smith	5.54	4.807	20.79	23.97	19.2	...	...
Ajax	Jamieson	10.04	8.84	18.9	21.5	...	...	...
Fawcett	Miller	11.49	8.52	18.4	24.74	19.6	...	...
Atkinson	Unwin	5.536	4.889	19.78	22.51	21.9	...	...
"	Society of Arts	11.15	9.48	19.22	22.61	22.8	...	...
Hargreaves	Bird	40	tar or creosote	tar or creosote	...	31.4	...	...
"	"	5.17	...	"	...	14.4	...	...

A Griffin gas engine, double-acting, was similarly tested. The cylinder was 9·02 inches in diameter, with a stroke of 14 inches. Three trials were made at full power, half power, and empty.

Trial.	A. Per cent.	B. Per cent.	C. Per cent.
Heat turned into work . . . .	21·1	19·4	17·5
Heat rejected in jacket water . .	35·2	32·5	...
Heat rejected in exhaust . . . .	39·8	48·1	...
Unaccounted for, including heat rejected in blank charge of air . }	3·9		

### Oil Engines.

Oil engines are in considerable employment as oil motors. In the Priestman oil engine, mineral oil or petroleum is used, having a specific gravity of '800 or upwards, with a flashing point from 75° to 150°. The oil is mixed with air under pressure, is drawn into the cylinder, and ignited by an electric spark from a small ordinary battery. The consumption of oil varies from about 1·25 pints or 1½ pounds per break horse-power per hour for the larger engines, to 1·60 pints or 1·60 pounds for the smaller engines. An engine having an 8½-inch cylinder, with a 12-inch stroke, made 180 revolutions per minute, and developed 4·60 break horse-power, with a consumption of 1·20 pints or 1·20 pounds of oil per horse-power per hour. In a half-power trial, 2·36 break horse-power was developed on a consumption of 1·20 pints or 1·20 pounds of oil.

The Hargreaves motor is designed for burning coal-tar or creosote as fuel. It consists of an air-compressing pump and motor cylinder, to the latter of which a regenerator is adapted, which absorbs a portion of the heat of the exhaust gases, and yields it up to the incoming charge. The compressed-air is delivered through the regenerator into the motor cylinder, where it meets a jet of coal-tar or creosote, and, being heated to redness, ignites the fuel. Results of trials are given in Table 318 (p. 577), by Mr. Miller, who gives results of other trials, in one of which, a net power of 40 indicator H.P. was generated, by the consumption of 512 pounds of coal-tar per indicator horse-power per hour. In another trial, with a smaller engine, for a net indicator power of 5·17 H.P., 1·2 pounds of creosote were consumed per indicator horse-power per hour.

## AIR IN MOTION.

DR. HUTTON's statement of the law of resistance of air to bodies in motion, has been corroborated. It is that in the case of slow motion, the resistance is nearly as the square of the velocity; gradually increasing more and more above that proportion as the velocity increases.

TABLE 319.—RESISTANCE OF AIR TO FLAT VANES,  
SQUARE AND ROUND.  
(Fairweather.)

Size.	Area.	Speed in Feet per Second.					
		5	10	15	20	25	30
Inches.	Sq. Ft.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.
<b>SQUARE.</b>							
7.41	.38	.55	1.4	3.25	5.7	9.4	14.0
12.9	1.155	1.30	5.5	13.60	...	...	...
15.58	2.40	3.25	15.0	...	...	...	...
<b>CIRCLE.</b>							
7.24	.286	.30	1.15	2.6	4.6	7.4	10.9
12.65	.875	.85	3.85	9.1	16.4	...	...
18.36	1.840	2.40	10.00	...	...	...	...

## High Winds.

Empirical formula for the velocity and pressure of high winds :—

$$P = \frac{V^2}{10} \quad . \quad . \quad . \quad . \quad . \quad . \quad . \quad (1)$$

$$V = \sqrt{10P} \quad . \quad . \quad . \quad . \quad . \quad . \quad . \quad (2)$$

V = maximum run of wind in any one hour.

P = maximum pressure, in pounds per square foot, at any time during the storm, to which V refers.

The formula (1) represents very fairly the greatest pressure as deduced from the mean velocity for an hour. The following are the greatest recorded pressures of wind per square foot at various places :—

	Per Square Foot.		Per Square Foot.
Aberdeen . . .	41 Lbs.	Liverpool . . .	90 Lbs.
Armagh . . .	27 "	London . . .	20·2 "
Birmingham . . .	27 "	Valentia . . .	65·6 "
Edinburgh . . .	35 "	Yarmouth . . .	42·2 "
Falmouth . . .	53·7 "	Brussels . . .	22 "
Glasgow . . .	47 "	Paris . . .	17 "
Greenwich . . .	42 "	Bombay . . .	38 "
Halifax . . .	30·2 "	Calcutta . . .	40 "
Holyhead . . .	64 "	Madras . . .	34 "
Kew . . .	27 "		

The Committee appointed to investigate the question, recommended that a maximum wind-pressure of 56 lbs. per square foot, should be employed in calculations for railway bridges and viaducts.

### Flow of Air in Pipes.

Mr. Hawksley's formulæ for the flow of air through pipes, under small differences of pressure, are as follows :—

$$v = 396 \sqrt{\frac{h d}{l}} \quad . \quad . \quad . \quad (3)$$

$$h = \frac{l v^2}{156,800 d} \quad . \quad . \quad . \quad (4)$$

$v$  = velocity in feet per second.

$h$  = head, or drag, in inches of water.

$d$  = diameter of pipe, in feet.

$l$  = length of pipe, or other passage, in feet.

$c$  = perimeter, in feet.

$a$  = sectional area of pipe, or other passage, in square feet.

$Q$  = Quantity of air discharged, in cubic feet per second.

$H$  = effective horse-power required for net work of discharge of air.

### Flow of Air through Passages of any form of Section, as Shafts, Air-ways, and Tunnels.

$$v = 796 \sqrt{\frac{a h}{c l}} \quad . \quad . \quad . \quad (5)$$

$$h = \frac{v^2 c l}{633,000 a} \quad . \quad . \quad . \quad (6)$$



*Quantity of Air delivered per Second.*

$$\text{From a pipe, } Q = 311 \sqrt{\frac{h d^5}{l}} \quad (7)$$

$$\text{From a passage of any section, } Q = 796 \sqrt{\frac{a^3 h}{c l}} \quad (8)$$

The density of dry air at 62° F., is taken at  $\frac{1}{813}$  part of the density of water at 62.4 pounds per cubic foot; and 1 inch of water as equivalent to a pressure of 5.20 lbs. per square foot.

**Effective Horse-power for net work of Discharge of Air.**

$$\text{From a pipe, } H = \frac{r d^2 h}{135} \quad (9)$$

$$\text{" } H = \frac{r^3 d^2 l}{21,200,000} \quad (10)$$

$$\text{from a passage of any section, } H = \frac{r a h}{105} = \frac{Q h}{105} \quad (11)$$

$$\text{" } H = \frac{r^3 c l}{67,000,000} \quad (12)$$

**Natural Flow of Air in Shafts of Mines.**

Mr. Hawksley's formula for the velocity of air in the up-cast shaft of a mine, due to difference of temperature is :—

$$v = 96 \sqrt{\frac{(T-t)}{(T+448)} \frac{D s}{m l + 368 s}} \quad (13)$$

T = temperature of air in up-cast shaft (Fahr.).

t = temperature of air in down-cast shaft.

D = depth of shaft, in feet.

m = periphery of air course, in feet.

s = section of air-course, in square feet.

l = length traversed by the current, in feet.

v = velocity of current, in feet per second.

**Fans.—Ventilators.**

The following Table 320, of the most suitable dimensions of fans, is based on the results of Mr. Buckle's experiments. The case is of the form of an arithmetical spiral, widening the clear space between the case and the revolving blades, circumferentially, from the origin to the opening for discharge.

TABLE 320.—DIMENSIONS OF FANS.

Pressure from 3 ounces to 6 ounces per square inch ; or  
5·2 inches to 10·4 inches of water.

Dia- meter of Fan.	Vanes.		Dia- meter of Inlet Open- ings.	Dia- meter of Fan.	Vanes.		Dia- meter of Inlet Open- ings.
	Width.	Length.			Width.	Length.	
Ft. Ins.	Ft. Ins.	Ft. Ins.	Ft. Ins.	Ft. Ins.	Ft. Ins.	Ft. Ins.	Ft. Ins.
3 0	0 9	0 9	1 6	4 6	1 1½	1 1½	2 3
3 6	0 10½	0 10½	1 9	5 0	1 3	1 3	2 6
4 0	1 0	1 0	2 0	6 0	1 6	1 6	3 0

Pressure, from 6 ounces to 9 ounces per square inch, and  
upwards, or 10·4 inches to 15·6 inches of water.

3 0	0 7	1 0	1 0	4 6	0 10½	1 4½	1 9
3 6	0 8½	1 1½	1 3	5 0	1 0	1 6	2 0
4 0	0 9½	1 3½	1 6	6 0	1 2	1 10	2 4

Guibal's fan, for mine ventilation, has blades which are straight, except at the outer ends, which curve forwards. The blades are fixed at a back inclination,—usually 45°—to the radius. The wheel is closely surrounded, for about two-thirds of the circumference, by a casing of brickwork. For the remaining third, the casing gradually opens out into the discharge vent, which expands upwards as an inverted frustum of a cone. A Guibal fan working at Staveley colliery, is 30 feet in diameter, 10 feet wide, it makes 60 revolutions per minute, with the following results of performance :—

Speed in Turns per Minute.	Draft in Inches of Water.	Volume of Air Discharged per Minute.	Efficiency, in parts of the Gross Indicator Power of the Engine.
Turns.	Inches.	Cubic Feet.	Per cent.
32	·70	43,852	40·4
51	1·70	86,283	43·1
64	2·77	101,773	53·3
68	3·10	110,005	53·8

## COMPRESSED AIR.

### Compressed or Expanded Isothermally.

Air when compressed or expanded under a uniform temperature, or isothermally, follows the hyperbolic law, according to which the pressure varies inversely as the volume.

The total net work for one stroke of the compressor of dry atmospheric air, isothermally, is found by the formula :—

$$W = P (V + v) \text{ hyp. log. } \frac{V + v}{V' + v} - (P' - P) v \quad (1)$$

The total net work of dry air for one stroke of a compressed air engine isothermally expanded in the cylinder down to atmospheric pressure, is given by formula :—

$$W = P (V + v) \text{ hyp. log. } \frac{V' + v}{V + v} - (P - P') v \quad (2)$$

The formulas (1) and (2) are identical in construction.

In cases where the back pressure  $P''$  is less than  $P'$ , the terminal positive pressure, the total net work is given by formula :—

$$W = P (V + v) \text{ hyp. log. } \frac{V' + v}{V + v} - P'' V' + P V \quad (3)$$

$P$  = total pressure of air, in pounds per square foot.

$V$  = volume of air, in cubic feet.

$v$  = volume of clearance at each end of cylinder, in cubic feet.

$W$  = work done, in foot pounds.

In practice, the temperature is not uniform, but rises with compression, and falls with expansion : requiring more work for compression, and less work by expansion, than are provided in the above formulas. But these differences are minimised by the application of cooling agents, as cold water surrounding the working cylinder.

In compressing dry air at 62° F. in a non-conducting vessel, adiabatically, to two atmospheres of pressure, the temperature is raised to 178° F. ; and the fall to 62°, in a reservoir, involves a loss of 116°, which is a loss of 18 per cent. of the maximum absolute temperature, or 18 per cent. of efficiency for work.

TABLE 321.—PRESSURE AND VOLUME OF COMPRESSED AIR.  
(Adapted from Mr. Shone's Table.)

Pressure above Atmosphere.			Comparative Volume of Air after Compression. Initial Volume=1.		Temperature by Adiabatic Com- pression, that of the Free Air being 60° F.	Rate of Compression Isothermally.	Average Load against Compress- ing Piston, per Square Inch.	
			Isother- mally.	Adiabati- cally.			Isother- mally.	Adiabati- cally.
Lbs. per Sq. In.	Inches of Mercury.	Feet of Water.	Volume.	Volume.	Fahr.	Com- pression.	Load.	Load.
1	2.041	2.31	0.936	0.954	70.04	1.0680	0.967	0.976
2	4.082	4.61	0.880	0.913	79.64	1.1361	1.876	1.910
3	6.123	6.92	0.831	0.876	88.84	1.2041	2.730	2.805
4	8.164	9.23	0.786	0.843	97.68	1.2721	3.538	3.664
5	10.205	11.54	0.746	0.812	106.18	1.3401	5.303	4.491
6	12.246	13.84	0.710	0.784	114.39	1.4081	5.031	5.288
7	14.287	16.15	0.677	0.758	122.32	1.4762	5.725	6.060
8	16.328	18.46	0.648	0.735	129.99	1.5442	6.387	6.806
9	18.369	20.76	0.620	0.713	137.43	1.6122	7.021	7.529
10	20.410	23.07	0.595	0.692	144.65	1.6803	7.629	8.232
11	22.451	25.38	0.572	0.673	151.66	1.7483	8.212	8.914
12	24.492	27.68	0.551	0.655	158.48	1.8164	8.774	9.578
13	26.533	29.99	0.531	0.638	165.13	1.8844	9.315	10.224
14	28.574	32.30	0.512	0.622	171.60	1.9524	9.836	10.854
15	30.615	34.61	0.495	0.607	177.92	2.0204	10.338	11.468
16	32.656	36.91	0.479	0.593	184.09	2.0884	10.825	12.068
17	34.697	39.22	0.464	0.579	190.11	2.1565	11.297	12.654
18	36.738	41.53	0.450	0.567	196.01	2.2245	11.753	13.227
19	38.779	43.83	0.436	0.555	201.77	2.2925	12.193	13.788
20	40.820	46.14	0.424	0.544	207.42	2.3605	12.623	14.337
21	42.861	48.45	0.412	0.533	212.95	2.4286	13.044	14.875
22	44.902	50.75	0.401	0.522	218.37	2.4966	13.450	15.403
23	46.943	53.06	0.390	0.512	223.69	2.5646	13.844	15.921
24	48.984	55.37	0.380	0.503	228.91	2.6327	14.230	16.429
25	51.025	57.68	0.370	0.494	234.03	2.7007	14.604	16.927
26	53.066	59.98	0.361	0.485	239.07	2.7687	14.970	17.419
27	55.107	62.29	0.353	0.477	244.02	2.8367	15.327	17.898
28	57.148	64.60	0.344	0.469	248.88	2.9048	15.676	18.371
29	59.189	66.90	0.336	0.461	253.66	2.9728	16.016	18.837
30	61.230	69.21	0.329	0.454	258.37	3.0408	16.348	19.294
31	63.271	71.52	0.322	0.447	263.00	3.1088	16.673	19.745
32	65.312	73.82	0.315	0.440	267.56	3.1769	16.992	20.190
33	67.353	76.13	0.308	0.434	272.05	3.2449	17.303	20.626
34	69.394	78.44	0.302	0.427	276.48	3.3129	17.608	21.056
35	71.435	80.75	0.296	0.421	280.84	3.3810	17.907	21.480
36	73.476	83.05	0.290	0.415	285.14	3.4490	18.200	21.899
37	75.517	85.36	0.284	0.409	289.38	3.5170	18.487	22.312
38	77.558	87.67	0.279	0.404	293.56	3.5850	18.768	22.718
39	79.599	89.97	0.274	0.399	297.68	3.6531	19.045	23.121
40	81.640	92.28	0.269	0.393	301.75	3.7211	19.316	23.516
41	83.681	94.59	0.264	0.388	305.77	3.7891	19.581	23.908
42	85.722	96.89	0.259	0.383	309.74	3.8571	19.844	24.293
43	87.763	99.20	0.255	0.379	313.66	3.9252	20.101	24.675
44	89.804	101.51	0.250	0.374	317.53	3.9932	20.358	25.052
45	91.845	103.82	0.246	0.370	321.36	4.0612	20.602	25.424
46	93.886	106.12	0.242	0.365	325.13	4.1293	20.846	25.729
47	95.927	108.43	0.238	0.361	328.87	4.1973	21.086	26.155
48	97.968	110.74	0.234	0.357	332.56	4.2653	21.323	26.515
49	100.009	113.04	0.231	0.353	336.21	4.3333	21.555	26.870
50	102.050	115.35	0.227	0.349	339.82	4.4014	21.784	27.221

The following table shows the corresponding loss of efficiency for several pressures :—

TABLE 322.—LOSS OF EFFICIENCY OF COMPRESSED AIR.

Pressure.	Final Temperature for Compression.	Reduced Efficiency, Initial Temperature for Work, 62° F.	Loss of Efficiency.
Atmospheres.	° Fahr.	Per cent.	Per cent.
2	178	82	18
3	258	73	27
4	321	67	33
5	373	63	37
10	559	51	49

Taking the efficiency of the compressor, and also that of the power-engine, at 80 per cent., the resultant efficiency of the combined compressor and engine, working to 10 atmospheres is  $\left( \frac{80 \times 80}{100} \times 51 = \right)$  33 per cent. Working to two atmospheres,

the resultant efficiency is 52 per cent. In general practice, the resultant efficiency rarely exceeds 30 per cent.

Table 321 shows the relation of pressure, volume, and temperature, with the load against a compressing piston.

Table 323 shows the net horse-power required for compressing atmospheric air, under pressures of from 2 to 20 atmospheres, calculated by means of formula (1); on the assumption that the temperature is maintained uniformly at 62° F.

The same table shows, reversely, the horse-power developed by compressed air introduced into the cylinder at the various pressures; on the assumption that the temperature is uniformly 62° F., and that the air is expanded down to atmospheric pressure at the end of the stroke. But, when the air is exhausted, at a pressure higher than that of the atmosphere, the difference of the initial work  $PV$  and the work of back pressure,  $P''V'$ , is to be added to the work as calculated by formula (3).

### Flow of Compressed Air through Pipes.

The head, or difference of the pressures at the beginning and end of a long pipe, through which compressed air is forced, may be taken to vary as the length of the pipe, as the square of the velocity, and inversely as the diameter. According to some authorities, it varies also with the density of the air; according to others it does not so vary. In Table 324 are given the results of observations made on the flow of compressed air in pipes at the St. Gothard tunnel.

TABLE 323.—NET POWER REQUIRED TO COMPRESS AIR AT THE UNIFORM TEMPERATURE 62° F.

Atmospheres of Pressure, and Ratio of Expansion. 1 Atmosphere = 1.	Pressure per Square Inch (approximate).	Horse Power per Cubic Foot of Compressed Air per Minute.	Volume of Compressed Air per Minute per Horse Power, at 62° F.	Equivalent Volume of Free Air, under one Atmosphere, at 62° F.	
Hyperbolic Logarithm of Ratio of Expansion.	Lbs.	H. P.	Cubic Feet.	Cubic Feet.	
2	·6931	30	·0889	11·25	22·50
3	1·0986	45	·2114	4·73	14·19
4	1·3863	60	·3556	2·88	11·52
5	1·6094	75	·516	1·94	9·70
6	1·7918	90	·690	1·450	8·70
7	1·9459	105	·874	1·145	8·01
8	2·0794	120	1·067	·938	7·50
9	2·1972	135	1·268	·788	7·09
10	2·3026	150	1·477	·667	6·67
11	2·3979	165	1·692	·591	6·50
12	2·4849	180	1·913	·523	6·28
13	2·5649	195	2·139	·468	6·08
14	2·6391	210	2·369	·422	5·91
15	2·7084	225	2·606	·384	5·76
16	2·7726	240	2·845	·352	5·63
17	2·8332	255	3·089	·324	5·51
18	2·8904	270	3·336	·300	5·40
19	2·9444	285	3·587	·279	5·30
20	2·9957	300	3·843	·260	5·20

At the Mont Cenis tunnel, compressed air of 5·70 atmospheres of pressure was reduced to 5·50 atmospheres, or by  $3\frac{1}{2}$  per cent. of the head, in a  $7\frac{1}{2}$  inch cast-iron pipe 1775 yards in length, comprising leakage and frictional resistance; whilst 64 cubic feet of compressed air was delivered per minute. In a length of 6,666 yards of pipe, the loss was 5 per cent. of the initial pressure.

The Table 325 of loss of pressure by friction in pipes, has been issued by the Rand Drill Company. The calculated quantities are those for straight pipes. To make ample allowance for heads, elbows, and tees, one size of pipe larger than the tabular size may be taken.

TABLE 324.—LOSS OF PRESSURE IN COMPRESSED-AIR PIPE-MAIN, AT ST. GOTHARD TUNNEL.  
(E. Stockalper.)

Expe- riment.	Air Main.		Volume per Second of Free Air, or Equivalent Volume at Atmospheric Pressure and 32° F.		Mean Density of Com- pressed Air. (Water = 1)	Weight of Air Flow- ing per Second.	Mean Velo- city in Feet per Second.	Mean Tempe- rature in Main.	Observed Pressures.			
	Dia- meter.	Length. Feet.	Cubic Feet. ( )	Cub. Ft. ( )					Pres- sure at Begin- ning of Pipe.	Pres- sure at End of Pipe.	Atmos. Atmos.	Per Cent.
1	7·87	15,092	( 6·534 )	( 6·534 )	·00650	2·669	19·32	70	5·60	5·24	0·36	6·4
	5·91	1,712·6	( 33·056 )	( 7·063 )	·00603	2·669	37·14	80	5·24	5·00	0·24	4·6
2	7·87	15,092	( 22·002 )	( 5·509 )	·00514	1·776	16·30	70	4·35	4·13	0·22	5·1
	5·91	1,712·6	( )	( 5·863 )	·00482	1·776	...	80	4·13	...	...	...
3	7·87	15,042	( 18·364 )	( 5·262 )	·00449	1·483	15·58	70	3·84	3·65	0·19	5·0
	5·91	1,712·6	( )	( 5·580 )	·00423	1·483	29·34	80	3·65	3·54	0·11	3·0

TABLE 325.—LOSS OF PRESSURE BY FRICTION OF COMPRESSED AIR IN PIPES.

(F. A. Halsey.)

Cubic Feet of Free Air compressed to a Gauge Pressure of 60 lbs. per Square Inch, and passing through the Pipe per Minute.																					
50	75	100	125	150	200	250	300	400	600	800	1000	1200	1500	1800	2000	2500	3000	4000	5000		
Loss of Pressure in Pounds per Square Inch for each 1,000 Feet of Straight Pipe.																					
Ins.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	Lbs.	
1	10.40	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	
1 1/4	2.63	5.90	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	
1 1/2	1.22	2.75	1.89	7.65	11.00	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	
2	.35	.79	1.41	2.20	3.17	5.64	8.78	...	...	...	...	...	...	...	...	...	...	...	...	...	
2 1/4	.14	.32	.57	.90	1.29	2.30	3.58	5.18	9.20	...	...	...	...	...	...	...	...	...	...	...	
3	...	.11	.20	.31	.44	.78	1.23	1.77	3.14	7.05	...	...	...	...	...	...	...	...	...	...	
3 1/4	...	...	...	.15	.21	.38	.59	.85	1.51	3.40	6.03	...	...	...	...	...	...	...	...	...	
4	...	...	...	...	...	.20	.31	.45	.80	1.81	3.22	5.02	7.23	11.30	...	...	...	...	...	...	
5	...	...	...	...	...	...	.10	.15	.26	.59	1.04	1.63	2.35	3.66	5.28	6.50	10.20	...	...	...	
6	...	...	...	...	...	...	...	...	.23	.41	.64	.93	1.46	2.09	2.59	4.06	5.81	10.30	...	...	
8	...	...	...	...	...	...	...	...	...	.10	.16	.23	.37	.53	.65	1.02	1.47	2.61	4.08	...	
10	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	.33	.47	.84	1.30	...	
12	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	.13	.19	.34	.53	...	
14	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	...	.16	.24	...	



## REFRIGERATING MACHINERY.

For the cooling of brine and other liquids by the alternate compression and expansion of air, Mr. David Thomson gives the following formulæ, in which the machine is supposed to be perfect :—

$$P = 772 C \times \frac{T - T_1}{T} \quad . \quad . \quad . \quad (1)$$

$$C = \frac{P}{772} \times \frac{T}{T - T_1} \quad . \quad . \quad . \quad (2)$$

$P$  = power required to do the cooling work  $C$ , in foot-pounds.

$C$  = cooling work done, in thermal units.

$T$  = Absolute maximum temperature, Fahrt., of the air in the hot or compression end of the cooling machine.

$T_1$  = absolute minimum temperature, Fahrt., of the air in the cold or expansion end of the machine.

These formulæ indicate that the most economical results, as regards consumption of power, are obtained when the machine is worked within a small range of temperature, as in breweries, where the temperature of water is frequently to be lowered only 10° F.

These formulæ are applicable to all cooling machines, whether they operate by means of air, ether, ammonia, or any other fluid.

In the ammonia machine, or other machine working on the same principle, in which no mechanical power is applied, the value of  $P$ , it is understood, is the heat theoretically required, at the rate of 1 heat-unit for 772 foot-pounds of power; and the formula (1) becomes :—

$$(\text{Ammonia}). \text{ Heat required to do the work } C = C \frac{T - T_1}{T_1} \quad . \quad (3)$$

The ammonia machine has, theoretically, a great economical superiority, as heat is so much less expensive than its equivalent of mechanical power.

The nature of the vapour employed affects the size of the machine; the relative capacity of cylinder required being :—

Ammonia . . . . 1	Methyl ether . . . . 1.8
Carbonic acid . . . . 0.16	Sulphurous acid . . . . 2.6
Methyl chloride . . . . 1.8	Ether . . . . 15.1



parts of the theoretical velocity  $v$ , as above, the velocity varies thus :—

	Per cent.
With internal tube . . . . .	50
Thin plate only . . . . .	62
Nozzle, 2 diameters in length . . . . .	82
Converging cone, length $2\frac{1}{2}$ diameters. . . . .	95
Vena contracta, length $\frac{1}{2}$ diameter of orifice . . . . .	160
Smallest diameter $\cdot 785$ diameter of orifice } . . . . .	
Diverging cone, length 9 diameters . . . . .	146

The velocity of flow of water in a full smooth cast-iron pipe of uniform diameter, is given by the formula :—  
(Hawksley).

$$v = 48 \sqrt{\frac{h}{l} \times d} \quad . \quad . \quad . \quad (2)$$

Mr. Downing employs the same formula with the co-efficient 50 instead of 48. His formula for the quantity of water discharged from a channel or pipe is,—

$$Q = 100a \sqrt{\frac{h}{l} \times D} \quad . \quad . \quad . \quad (3)$$

$v$  = velocity, in feet per second.

$h$  = head, in feet.

$l$  = length, in feet.

$d$  = diameter, in feet.

$c$  = wetted perimeter, in feet.

$a$  = sectional area of current, in square feet.

$Q$  = quantity of water discharged, in cubic feet per second.

$D = \frac{a}{c}$  = hydraulic mean depth.

By the aid of Table 326, based on formula (3), the discharge, the diameter of pipe, and the fall are readily calculable.

1. *To find the rate of discharge*, when the length, fall, and diameter of pipe in feet are given. Divide the tabular number next the diameter by the square root of the rate of inclination. The quotient is the rate of discharge in cubic feet per minute.

2. *To find the required diameter*, when the length and fall in feet, and the rate of discharge in cubic feet per minute, are given. Multiply the rate of discharge by the square root of the rate of inclination ; find the product or the nearest value to it in the table. The diameter next to it is the diameter required, in feet.

3. *To find the required fall*, when the length and diameter

in feet, and the rate of discharge in cubic feet per minute are given. Divide the tabular number next the given diameter by the rate of discharge ; square the quotient, and multiply it by the length of pipe. The final quotient is the fall in feet.

*Note.*—The rate of inclination is the quotient of the length by the vertical height.

Half the tabular number may be taken to find approximately the discharge for pipes half-full. The calculation is also available for sewers and the like.

TABLE 326.—DISCHARGE OF WATER IN PIPES.

(Turnbull.)

Diameter of Pipes.	Tabular Number.	Diameter of Pipes.	Tabular Number	Diameter of Pipes.	Tabular Number.
Inches.		Inches.		Inches.	
1	4.7	21	9544	42	53994
1½	13.0	22	10717	43	57250
2	26.4	23	11971	44	60625
3	73.6	24	13327	45	64142
4	150.7	25	14753	46	67770
5	262.9	26	16267	47	71494
6	416.5	27	17881	48	75391
7	611.4	28	19523	51	87713
8	852.8	29	21375	54	101190
9	1147.7	30	23282	57	115844
10	1492.1	31	25263	60	131700
11	1892	32	27335	66	167134
12	2356	33	29545	72	207752
13	2875	34	31826	78	253764
14	3459	35	34208	84	305384
15	4115	36	36726	90	362871
16	4806	37	39319	96	426436
17	5621	38	42018	102	496220
18	6492	39	44861	108	572343
19	7259	40	47674	114	655124
20	8439	41	58811	120	745014

#### Discharge of Water through Fire-hose and Nozzles.

In Tables 329 and 330, are given the actual discharge of water through small nozzles and ring-nozzles connected to 2½-inch hose, 50 feet and 100 feet long.

In Table 331, are given the loss of head by friction in fire-hose, of rubber and of leather, under given heads and rates of discharge.

TABLE 327.—PRESSURE OF WATER FOR GIVEN HEADS.

Head.	Pressure per Square Inch.	Head.	Pressure per Square Inch.	Head.	Pressure per Square Inch.	Head.	Pressure per Square Inch.
Feet.	Pounds.	Feet.	Pounds.	Feet.	Pounds.	Feet.	Pounds.
1	0.43	41	17.75	81	35.08	121	52.41
2	0.86	42	18.19	82	35.52	122	52.84
3	1.30	43	18.62	83	35.95	123	53.28
4	1.73	44	19.05	84	36.39	124	53.71
5	2.16	45	19.49	85	36.82	125	54.15
6	2.59	46	19.92	86	37.25	126	54.58
7	3.03	47	20.35	87	37.68	127	55.01
8	3.46	48	20.79	88	38.12	128	55.44
9	3.89	49	21.22	89	38.55	129	55.88
10	4.33	50	21.65	90	38.98	130	56.31
11	4.76	51	22.09	91	39.42	131	56.74
12	5.20	52	22.52	92	39.85	132	57.18
13	5.63	53	22.95	93	40.28	133	57.61
14	6.06	54	23.39	94	40.72	134	58.04
15	6.49	55	23.82	95	41.15	135	58.48
16	6.93	56	24.26	96	41.58	136	58.91
17	7.36	57	24.69	97	42.01	137	59.34
18	7.79	58	25.12	98	42.45	138	59.77
19	8.22	59	25.55	99	42.88	139	60.21
20	8.66	60	25.99	100	43.31	140	60.64
21	9.09	61	26.42	101	43.75	141	61.07
22	9.53	62	26.85	102	44.18	142	61.51
23	9.96	63	27.29	103	44.61	143	61.94
24	10.39	64	27.72	104	45.05	144	62.37
25	10.82	65	28.15	105	45.48	145	62.81
26	11.26	66	28.58	106	45.91	146	63.24
27	11.69	67	29.02	107	46.34	147	63.67
28	12.12	68	29.45	108	46.78	148	64.10
29	12.55	69	29.88	109	47.21	149	64.54
30	12.99	70	30.32	110	47.64	150	64.97
31	13.42	71	30.75	111	48.08	151	65.40
32	13.86	72	31.18	112	48.51	152	65.84
33	14.29	73	31.62	113	48.94	153	66.27
34	14.72	74	32.05	114	49.38	154	66.70
35	15.16	75	32.48	115	49.81	155	67.14
36	15.59	76	32.92	116	50.24	156	67.57
37	16.02	77	33.35	117	50.68	157	68.00
38	16.45	78	33.78	118	51.11	158	68.43
39	16.89	79	34.21	119	51.54	159	68.87
40	17.32	80	34.65	120	51.98	160	69.31

TABLE 327.—PRESSURE OF WATER FOR GIVEN HEADS  
(continued).

Head.	Pressure per Square Inch.	Head.	Pressure per Square Inch.	Head.	Pressure per Square Inch.	Head.	Pressure per Square Inch.
Feet.	Pounds.	Feet.	Pounds.	Feet.	Pounds.	Feet.	Pounds.
161	69·74	200	86·63	239	103·53	278	120·42
162	70·17	201	87·07	240	103·96	279	120·85
163	70·61	202	87·50	241	104·39	280	121·29
164	71·04	203	87·93	242	104·83	281	121·72
165	71·47	204	88·36	243	105·26	282	122·15
166	71·91	205	88·80	244	105·69	283	122·59
167	72·34	206	89·23	245	106·13	284	123·02
168	72·77	207	89·66	246	106·56	285	123·45
169	73·20	208	90·10	247	106·99	286	123·89
170	73·64	209	90·53	248	107·43	287	124·32
171	74·07	210	90·96	249	107·86	288	124·75
172	74·50	211	91·39	250	108·29	289	125·18
173	74·94	212	91·83	251	108·73	290	125·62
174	75·37	213	92·26	252	109·16	291	126·05
175	75·80	214	92·69	253	109·59	292	126·48
176	76·23	215	93·13	254	110·03	293	126·92
177	76·67	216	93·56	255	110·46	294	127·35
178	77·10	217	93·99	256	110·89	295	127·78
179	77·53	218	94·43	257	111·32	296	128·22
180	77·97	219	94·86	258	111·76	297	128·65
181	78·40	220	95·30	259	112·19	298	129·08
182	78·84	221	95·73	260	112·62	299	129·51
183	79·27	222	96·16	261	113·06	300	129·95
184	79·70	223	96·60	262	113·49	310	134·28
185	80·14	224	97·03	263	113·92	320	134·62
186	80·57	225	97·46	264	114·36	330	142·95
187	81·00	226	97·90	265	114·79	340	147·28
188	81·43	227	98·33	266	115·22	350	151·61
189	81·87	228	98·76	267	115·66	360	155·94
190	82·30	229	99·20	268	116·09	370	160·27
191	82·73	230	99·63	269	116·52	380	164·61
192	83·17	231	100·06	270	116·96	390	168·94
193	83·60	232	100·49	271	117·39	400	173·27
194	84·03	233	100·93	272	117·82	500	216·58
195	84·47	234	101·36	273	118·26	600	259·90
196	84·90	235	101·79	274	118·69	700	302·22
197	85·33	236	102·23	275	119·12	800	346·54
198	85·76	237	102·66	276	119·56	900	389·86
199	86·20	238	103·09	277	119·99	1000	433·18

TABLE 328.—FLOW OF WATER THROUGH CLEAN CAST-IRON PIPES, AND RELATIVE LOSS OF HEAD BY FRICTION, FOR EACH 100 FEET LENGTH OF PIPE. (Based on Ellis and Howland's experiments.)

Velocity in Feet per Second.		DIAMETER OF PIPES, IN INCHES.														
		3	4	5	6	7	8	9	10	12	14					
		Discharge per Minute in Cubic Feet, and Loss of Head in Feet, per 100 Feet long.														
Feet.		Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.
2	2	5.9	9.7	10.5	5.5	16.4	41	23.6	32	27	42	23	53	19	65	128
2.5	3	7.3	1.49	13	1.2	20.4	64	29.3	50	43	52	36	66	30	82	177
3	3	8.8	1.9	15.7	1.2	24.5	82	35.2	72	48	61	51	79	44	98	219
3.5	3.5	10.3	2.6	18.3	1.6	28.6	1.2	41.2	1.0	56	7	73	93	61	115	252
4	4	11.8	3.3	21	2.2	32.7	1.7	47	1.3	64	9	84	106	79	131	297
4.5	4.5	...	...	...	...	...	...	53	1.6	72	1.2	94	1.2	119	1.01	257
5	5	...	...	...	...	...	...	...	...	...	...	...	...	...	...	288
5.5	5.5	...	...	...	...	...	...	...	...	...	...	...	...	...	...	320
6	6	...	...	...	...	...	...	...	...	...	...	...	...	...	...	352
		15	18	21	24	27	30	33	36	42	48					48
Feet.		Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.	Cubic Feet. Head.
2	2	1.48	1.1	212	405	288	475	377	605	580	710	749	850	1000	1500	2300
2.5	3	1.84	1.7	264	1.47	300	1.17	470	1.09	730	1.085	890	1000	1067	1880	2846
3	3	2.20	2.5	317	2.1	430	1.7	565	1.5	715	1.13	880	1270	10	2250	3667
3.5	3.5	2.58	3.4	372	2.9	505	2.3	660	2.0	835	1.8	1030	15	1480	2630	4092
4	4	2.95	4.4	425	3.6	575	3.1	755	2.7	955	2.3	1180	22	2020	3000	4616
4.5	4.5	3.31	5.5	475	4.6	650	3.9	845	3.4	1070	3.0	1320	28	2500	3380	5115
5	5	3.68	7.0	530	5.8	720	4.8	940	4.1	1190	3.7	1470	34	2880	3750	5612
5.5	5.5	4.05	8.4	580	7.0	790	5.9	1030	5.0	1310	4.4	1610	39	3330	4130	6120
6	6	...	...	...	...	...	...	1130	5.9	1430	5.3	1760	49	2140	2430	3500

TABLE 325.—WATER DISCHARGED FROM NOZZLES ATTACHED TO 50 FEET OF 2½-INCH HOSE. (Freeman.)

Hy- dant Pres- sure.	1½-Inch Smooth Nozzle.	1½-Inch Smooth Nozzle.	1½-Inch Smooth Nozzle.	1-Inch Smooth Nozzle.	¾-Inch Smooth Nozzle or Nozzle or ¾-Inch Ring Nozzle.	12-Inch Ring Nozzle.	14-Inch Ring Nozzle.	14-Inch Ring Nozzle.	Hy- dant Pres- sure.
Lbs. per Sq. Inch.	Unlined Linen Hose.	Unlined Linen Hose.	Unlined Linen Hose.	Unlined Linen Hose.	Unlined Linen Hose.	Unlined Linen Hose.	Unlined Linen Hose.	Unlined Linen Hose.	Lbs. per Sq. Inch.
5	73	86	67	68	75	88	80	83	5
10	103	109	122	125	106	103	84	88	10
15	129	133	149	151	127	121	118	121	15
20	150	154	167	169	149	141	136	139	20
25	168	173	186	187	167	156	152	155	25
30	183	188	202	204	183	171	166	169	30
35	198	204	217	218	197	185	180	183	35
40	212	218	231	232	214	201	196	199	40
45	225	232	245	246	224	211	206	209	45
50	237	244	257	258	237	224	219	222	50
55	248	256	269	270	248	236	231	234	55
60	259	267	280	281	259	247	242	245	60
65	270	278	291	292	270	258	253	256	65
70	280	289	302	303	280	268	263	266	70
75	290	299	313	314	290	278	273	276	75
80	299	308	324	325	299	288	283	286	80
85	309	318	334	335	309	298	293	296	85
90	318	328	344	345	318	308	303	306	90
95	327	337	354	355	327	318	313	316	95
100	335	345	362	363	335	327	322	325	100
	343	353	370	371	343	335	330	333	
	351	361	378	379	351	343	338	341	
	359	369	386	387	359	351	346	349	
	367	377	394	395	367	359	354	357	
	375	385	402	403	375	367	362	365	
	383	393	410	411	383	375	370	373	
	391	401	418	419	391	383	378	381	
	399	409	426	427	399	391	386	389	
	407	417	434	435	407	399	394	397	
	415	425	442	443	415	407	402	405	
	423	433	450	451	423	415	410	413	
	431	441	458	459	431	423	418	421	
	439	449	466	467	439	431	426	429	
	447	457	474	475	447	439	434	437	
	455	465	482	483	455	447	442	445	
	463	473	490	491	463	455	450	453	
	471	481	498	499	471	463	458	461	
	479	489	506	507	479	471	466	469	
	487	497	514	515	487	479	474	477	
	495	505	522	523	495	487	482	485	
	503	513	530	531	503	495	490	493	
	511	521	538	539	511	503	500	503	
	519	529	546	547	519	511	506	509	
	527	537	554	555	527	519	514	517	
	535	545	562	563	535	527	522	525	
	543	553	570	571	543	535	530	533	
	551	561	578	579	551	543	538	541	
	559	569	586	587	559	551	546	549	
	567	577	594	595	567	559	554	557	
	575	585	602	603	575	567	562	565	
	583	593	610	611	583	575	570	573	
	591	601	618	619	591	583	578	581	
	599	609	626	627	599	591	586	589	
	607	617	634	635	607	599	594	597	
	615	625	642	643	615	607	602	605	
	623	633	650	651	623	615	610	613	
	631	641	658	659	631	623	618	621	
	639	649	666	667	639	631	626	629	
	647	657	674	675	647	639	634	637	
	655	665	682	683	655	647	642	645	
	663	673	690	691	663	655	650	653	
	671	681	700	701	671	663	658	661	
	679	689	708	709	679	671	666	669	
	687	697	716	717	687	679	674	677	
	695	705	724	725	695	687	682	685	
	703	713	732	733	703	695	690	693	
	711	721	740	741	711	703	698	701	
	719	729	748	749	719	711	706	709	
	727	737	756	757	727	719	714	717	
	735	745	764	765	735	727	722	725	
	743	753	772	773	743	735	730	733	
	751	761	780	781	751	743	738	741	
	759	769	788	789	759	751	746	749	
	767	777	796	797	767	759	754	757	
	775	785	804	805	775	767	762	765	
	783	793	812	813	783	775	770	773	
	791	801	820	821	791	783	778	781	
	799	809	828	829	799	791	786	789	
	807	817	836	837	807	799	794	797	
	815	825	844	845	815	807	802	805	
	823	833	852	853	823	815	810	813	
	831	841	860	861	831	823	818	821	
	839	849	868	869	839	831	826	829	
	847	857	876	877	847	839	834	837	
	855	865	884	885	855	847	842	845	
	863	873	892	893	863	855	850	853	
	871	881	900	901	871	863	858	861	
	879	889	908	909	879	871	866	869	
	887	897	916	917	887	879	874	877	
	895	905	924	925	895	887	882	885	
	903	913	932	933	903	895	890	893	
	911	921	940	941	911	903	898	901	
	919	929	948	949	919	911	906	909	
	927	937	956	957	927	919	914	917	
	935	945	964	965	935	927	922	925	
	943	953	972	973	943	935	930	933	
	951	961	980	981	951	943	938	941	
	959	969	988	989	959	951	946	949	
	967	977	996	997	967	959	954	957	
	975	985	1004	1005	975	967	962	965	
	983	993	1012	1013	983	975	970	973	
	991	1001	1020	1021	991	983	978	981	
	999	1009	1028	1029	999	991	986	989	
	1007	1017	1036	1037	1007	999	994	997	
	1015	1025	1044	1045	1015	1007	1002	1005	
	1023	1033	1052	1053	1023	1015	1010	1013	
	1031	1041	1060	1061	1031	1023	1018	1021	
	1039	1049	1068	1069	1039	1031	1026	1029	
	1047	1057	1076	1077	1047	1039	1034	1037	
	1055	1065	1084	1085	1055	1047	1042	1045	
	1063	1073	1092	1093	1063	1055	1050	1053	
	1071	1081	1100	1101	1071	1063	1058	1061	
	1079	1089	1108	1109	1079	1071	1066	1069	
	1087	1097	1116	1117	1087	1079	1074	1077	
	1095	1105	1124	1125	1095	1087	1082	1085	
	1103	1113	1132	1133	1103	1095	1090	1093	
	1111	1121	1140	1141	1111	1103	1098	1101	
	1119	1129	1148	1149	1119	1111	1106	1109	
	1127	1137	1156	1157	1127	1119	1114	1117	
	1135	1145	1164	1165	1135	1127	1122	1125	
	1143	1153	1172	1173	1143	1135	1130	1133	
	1151	1161	1180	1181	1151	1143	1138	1141	
	1159	1169	1188	1189	1159	1151	1146	1149	
	1167	1177	1196	1197	1167	1159	1154	1157	
	1175	1185	1204	1205	1175	1167	1162	1165	
	1183	1193	1212	1213	1183	1175	1170	1173	
	1191	1201	1220	1221	1191	1183	1178	1181	
	1199	1209	1228	1229	1199	1191	1186	1189	
	1207	1217	1236	1237	1207	1199	1194	1197	
	1215	1225	1244	1245	1215	1207	1202	1205	
	1223	1233	1252	1253	1223	1215	1210	1213	
	1231	1241	1260	1261	1231	1223	1218	1221	
	1239	1249	1268	1269	1239	1231	1226	1229	
	1247	1257	1276	1277	1247	1239	1234	1237	
	1255	1265	1284	1285	1255	1247	1242	1245	
	1263	1273	1292	1293	1263	1255	1250	1253	
	1271	1281	1300	1301	1271	1263	1258	1261	
	1279	1289	1308	1309	1279	1271	1266	1269	
	1287	1297	1316	1317	1287	1279	1274	1277	
	1295	1305	1324	1325	1295	1287	1282	1285	
	1303	1313	1332	1333	1303	1295	1290	1293	
	1311	1321	1340	1341	1311	1303	1298	1301	
	1319	1329	1348	1349	1319	1311	1306	1309	
	1327	1337	1356	1357	1327	1319	1314	1317	
	1335	1345	1364	1365	1335	1327	1322	1325	
	1343	1353	1372	1373	1343	1335	1330	1333	
	1351	1361	1380	1381	1351	1343	1338		





TABLE 331.—LOSS OF PRESSURE BY FRICTION PER 100 FEET OF 2½-INCH FIRE-HOSE, FOR GIVEN HEADS AND RATES OF DISCHARGE. (Fanning.)

Head.		DIAMETER OF NOZZLE IN INCHES.									
		1 Inch.					1½ Inches.				
		Loss of Head by Friction.		Distances reached by Jet.		Discharge per Minute.	Loss of Head by Friction.		Distances reached by Jet.		Discharge per Minute.
		Rubber Hose.	Leather Hose.	Horizontal.	Vertical.		Rubber Hose.	Leather Hose.	Horizontal.	Vertical.	
Lbs. per Sq. In.	Feet.	Gallons.	Lbs.	Feet.	Feet.	Gallons.	Lbs.	Lbs.	Feet.	Feet.	Gallons.
20	46.2	91.7	4.35	70	43	115.8	6.79	9.05	71	43	115.8
30	69.3	103.3	6.40	90	62	141.7	10.16	21.71	93	63	141.7
40	92.4	129.2	8.40	109	79	163.3	13.00	36.38	113	81	163.3
50	115.5	144.2	10.20	126	94	182.5	17.05	50.11	132	97	182.5
60	138.6	157.5	12.80	142	108	200.0	20.59	23.88	148	112	200.0
70	161.7	170.9	14.80	156	121	215.8	24.00	37.61	163	125	215.8
80	184.8	182.5	17.00	168	131	230.8	27.00	31.41	175	137	230.8
90	207.9	193.3	19.20	178	140	245.0	30.00	55.24	186	148	245.0
100	231.0	204.2	20.50	186	148	259.3	33.00	39.07	193	157	259.3

Head.		1½ Inches.									
		1½ Inches.					1½ Inches.				
		Loss of Head by Friction.		Distances reached by Jet.		Discharge per Minute.	Loss of Head by Friction.		Distances reached by Jet.		Discharge per Minute.
		Rubber Hose.	Leather Hose.	Horizontal.	Vertical.		Rubber Hose.	Leather Hose.	Horizontal.	Vertical.	
Lbs. per Sq. In.	Feet.	Gallons.	Lbs.	Feet.	Feet.	Gallons.	Lbs.	Lbs.	Feet.	Feet.	Gallons.
20	46.2	142.5	10.28	73	43	172.5	15.00	18.81	75	44	172.5
30	69.3	175.0	15.04	96	63	210.8	22.96	26.39	100	65	210.8
40	92.4	201.7	20.85	118	82	244.2	29.40	35.01	124	85	244.2
50	115.5	225.8	25.46	138	99	273.3	40.50	43.38	146	102	273.3
60	138.6	247.5	29.50	156	115	290.8	48.20	52.00	166	118	290.8
70	161.7	266.7	33.00	172	129	322.5	55.70	60.40	184	133	322.5
80	184.8	285.0	43.81	186	142	344.2	64.70	68.59	200	146	344.2
90	207.9	302.5	49.42	198	154	374.2	73.00	70.73	213	158	374.2
100	231.0	319.2	55.00	207	164	385.0	79.26	84.87	224	169	385.0

TABLE 332.—DISCHARGE OF WATER OVER WEIRS IN STREAMS, FOR EACH INCH OF WIDTH.

Depth on Weir.	Dis-charge per Minute per Inch Wide.	Depth on Weir.	Dis-charge per Minute per Inch Wide.	Depth on Weir.	Dis-charge per Minute per Inch Wide.	Depth on Weir.	Dis-charge per Minute per Inch Wide.
Inches.	Cub. Ft.	Inches.	Cub. Ft.	Inches.	Cub. Ft.	Inches.	Cub. Ft.
1	.40	5 $\frac{1}{2}$	5.18	10	12.71	14 $\frac{1}{2}$	22.22
1 $\frac{1}{8}$	.43	5 $\frac{5}{8}$	5.36	10 $\frac{1}{8}$	12.83	14 $\frac{5}{8}$	22.51
1 $\frac{1}{4}$	.55	5 $\frac{3}{4}$	5.54	10 $\frac{1}{4}$	13.19	14 $\frac{3}{4}$	22.79
1 $\frac{3}{8}$	.65	5 $\frac{7}{8}$	5.72	10 $\frac{3}{8}$	13.43	14 $\frac{7}{8}$	23.08
1 $\frac{1}{2}$	.74	6	5.90	10 $\frac{1}{2}$	13.67	15	23.38
1 $\frac{5}{8}$	.83	6 $\frac{1}{8}$	6.00	10 $\frac{5}{8}$	13.93	15 $\frac{1}{8}$	23.53
1 $\frac{3}{4}$	.93	6 $\frac{1}{4}$	6.28	10 $\frac{3}{4}$	14.16	15 $\frac{1}{4}$	23.97
1 $\frac{7}{8}$	1.03	6 $\frac{3}{8}$	6.47	10 $\frac{7}{8}$	14.42	15 $\frac{3}{8}$	24.26
2	1.14	6 $\frac{1}{2}$	6.65	11	14.67	15 $\frac{1}{2}$	24.56
2 $\frac{1}{8}$	1.19	6 $\frac{5}{8}$	6.85	11 $\frac{1}{8}$	14.79	15 $\frac{5}{8}$	24.86
2 $\frac{1}{4}$	1.36	6 $\frac{3}{4}$	7.05	11 $\frac{1}{4}$	15.18	15 $\frac{3}{4}$	25.16
2 $\frac{3}{8}$	1.47	6 $\frac{7}{8}$	7.25	11 $\frac{3}{8}$	15.43	15 $\frac{7}{8}$	25.46
2 $\frac{1}{2}$	1.59	7	7.44	11 $\frac{1}{2}$	15.67	16	25.76
2 $\frac{5}{8}$	1.71	7 $\frac{1}{8}$	7.54	11 $\frac{5}{8}$	15.96	16 $\frac{1}{8}$	25.91
2 $\frac{3}{4}$	1.83	7 $\frac{1}{4}$	7.84	11 $\frac{3}{4}$	16.20	16 $\frac{1}{4}$	26.36
2 $\frac{7}{8}$	1.96	7 $\frac{3}{8}$	8.05	11 $\frac{7}{8}$	16.46	16 $\frac{3}{8}$	26.66
3	2.09	7 $\frac{1}{2}$	8.25	12	16.73	16 $\frac{1}{2}$	26.97
3 $\frac{1}{8}$	2.16	7 $\frac{5}{8}$	8.45	12 $\frac{1}{8}$	16.86	16 $\frac{5}{8}$	27.27
3 $\frac{1}{4}$	2.36	7 $\frac{3}{4}$	8.66	12 $\frac{1}{4}$	17.26	16 $\frac{3}{4}$	27.58
3 $\frac{3}{8}$	2.50	7 $\frac{7}{8}$	8.86	12 $\frac{3}{8}$	17.52	16 $\frac{7}{8}$	27.89
3 $\frac{1}{2}$	2.63	8	9.10	12 $\frac{1}{2}$	17.78	17	28.20
3 $\frac{5}{8}$	2.78	8 $\frac{1}{8}$	9.20	12 $\frac{5}{8}$	18.05	17 $\frac{1}{8}$	28.35
3 $\frac{3}{4}$	2.92	8 $\frac{1}{4}$	9.52	12 $\frac{3}{4}$	18.32	17 $\frac{1}{4}$	28.82
3 $\frac{7}{8}$	3.07	8 $\frac{3}{8}$	9.74	12 $\frac{7}{8}$	18.58	17 $\frac{3}{8}$	29.14
4	3.22	8 $\frac{1}{2}$	9.96	13	18.87	17 $\frac{1}{2}$	29.45
4 $\frac{1}{8}$	3.29	8 $\frac{5}{8}$	10.18	13 $\frac{1}{8}$	19.01	17 $\frac{5}{8}$	29.76
4 $\frac{1}{4}$	3.52	8 $\frac{3}{4}$	10.40	13 $\frac{1}{4}$	19.42	17 $\frac{3}{4}$	30.08
4 $\frac{3}{8}$	3.68	8 $\frac{7}{8}$	10.62	13 $\frac{3}{8}$	19.69	17 $\frac{7}{8}$	30.39
4 $\frac{1}{2}$	3.83	9	10.86	13 $\frac{1}{2}$	19.97	18	30.70
4 $\frac{5}{8}$	3.99	9 $\frac{1}{8}$	10.97	13 $\frac{5}{8}$	20.24	18 $\frac{1}{8}$	30.86
4 $\frac{3}{4}$	4.16	9 $\frac{1}{4}$	11.31	13 $\frac{3}{4}$	20.52	18 $\frac{1}{4}$	31.34
4 $\frac{7}{8}$	4.32	9 $\frac{3}{8}$	11.54	13 $\frac{7}{8}$	20.80	18 $\frac{3}{8}$	31.66
5	4.50	9 $\frac{1}{2}$	11.77	14	21.09	18 $\frac{1}{2}$	31.98
5 $\frac{1}{8}$	4.58	9 $\frac{5}{8}$	12.00	14 $\frac{1}{8}$	21.23	18 $\frac{5}{8}$	32.31
5 $\frac{1}{4}$	4.84	9 $\frac{3}{4}$	12.23	14 $\frac{1}{4}$	21.65	18 $\frac{3}{4}$	32.63
5 $\frac{3}{8}$	5.01	9 $\frac{7}{8}$	12.47	14 $\frac{3}{8}$	21.94	18 $\frac{7}{8}$	32.96

### Measurement of Water in a Stream.

To measure the volume of water flowing past a given point in a stream per minute, select a portion of the stream, uniform or nearly uniform in width, throw into the middle of the stream, a floating body sufficiently heavy to be almost totally immersed, as a bottle partly filled with water, and note the time taken to float from one mark to another; or, note the distance traversed by the float in one minute. The observation should be repeated several times to give an average result. Measure several sections of the stream within the measured distance, and multiply the average area in square feet by the distance in feet. From the volume thus calculated, one-fifth is deducted, as an allowance for retardation by frictional resistance at the bottom and sides, to give the volume of flow in cubic feet per minute.

Another method of measurement, admitting of more nearly exact results, is to cause the water to flow over a weir, by fixing a board across the stream where it flows slowly, having a notch cut into it broad enough and deep enough for all the water to pass over and fall freely. At the distance of a yard or two from the notch, up-stream, fix a rod, and mark on it the level of the crest of the notch, measure the height of the water surface above this mark, to give the depth of the crest below the surface of the water. Find in the Table 332, calculated according to Du Buat's formula, the observed depth in inches, and multiply it by the corresponding value in the next column, which expresses the volume discharged for each inch in width of the crest. The product is the whole volume of water discharged in cubic feet per minute.

For example, if the depth over a weir 50 inches wide be  $6\frac{1}{2}$  inches, find  $6\frac{1}{2}$  inches in the columns of depths, and note in the next column the quantity of water, 6.65 cubic feet per inch wide per minute. Multiply 6.65 by 50; the product is 332.5 cubic feet, the volume discharged per minute.

### Discharge of Water from a Tank over a Tumbling Bay.

Messrs. B. Donkin & Co. have made observations of the quantity of water discharged from a tank, over a rectangular notch, tumbling bay or weir, cut into a brass or copper sheet,  $\frac{1}{8}$  inch thick, fastened to the inside of the tank. The bay was 6 inches wide. The levels of water were observed on the same system as already described for the measurement of streams.

The width of the bay should not in any case be greater than one-third of the width of the tank. Table 333 gives the weight and volume of water falling over a bay 6 inches wide, in one minute, for depths of from  $1\frac{1}{4}$  in. to  $4\frac{1}{8}$  ins. over the bay.

For bays of greater width than 6 inches, the rate of discharge is increased in the same proportion.

TABLE 333.—QUANTITY OF WATER DISCHARGED OVER A TUMBLING BAY, 6 INCHES WIDE. (Donkin.)

Depth over Tumbling Bay.			Depth over Tumbling Bay.		
Inches.	Pounds.	Cub. Ft.	Inches.	Pounds.	Cub. Ft.
1½	274	4.39	3¼	874	14.00
1⅞	292	4.67	3⅝	900	14.43
1⅚	310	4.96	3⅞	926	14.83
1⅓	327	5.24	3⅞	951	15.24
1¼	345	5.52	3½	977	15.65
1⅓	365	5.84	3⅞	1003	16.08
1⅞	383	6.13	3⅞	1030	16.44
1⅝	402	6.44	3⅞	1056	16.84
2	421	6.74	3¾	1083	17.35
2⅓	442	7.08	3⅞	1112	17.82
2⅞	462	7.40	3⅞	1139	18.25
2⅓	483	7.74	3⅞	1166	18.68
2¼	503	8.06	4	1193	19.11
2⅝	525	8.41	4⅓	1221	19.56
2⅞	547	8.76	4⅓	1250	20.01
2⅞	568	9.10	4⅓	1279	20.49
2½	589	9.43	4¼	1306	20.93
2⅞	612	9.80	4⅝	1336	21.41
2⅞	634	10.16	4⅞	1365	21.87
2⅓	657	10.36	4⅞	1394	22.34
2¾	680	10.89	4½	1424	22.82
2⅓	704	11.28	4⅞	1454	23.30
2⅞	727	11.65	4⅞	1483	23.76
2⅝	751	12.05	4⅞	1514	24.26
3	775	12.41	4¾	1544	24.74
3⅓	800	12.82	4⅞	1575	25.24
3⅓	825	13.22	4⅞	1605	25.72
3⅓	850	13.62	4⅞	1635	26.22

Messrs. Donkin and Salter made more recent measurements of the flow of water over a bay of rectangular form, 1½ inches wide cut square out of sheet brass ⅓ inch thick. They give the general formula for theoretical discharge, reduced for pounds and inches, as follows:—

$$Q = L \cdot 40.032 \sqrt{h^3} \quad (4)$$

$L$  = length of bay, in inches.  $h$  = head, or height over bay in inches.  $Q$  = pounds of water discharged, per minute.

The co-efficients of actual discharge vary from 64 to 62 per cent. of the theoretical discharge, for heads of from  $\frac{1}{2}$  inch to 3 inches.

### **Flow of Water through a Submerged Weir.**

A horizontal rectangular opening, 6 inches deep, 6 feet wide, was made in a board 5 inches thick, the upper and lower surfaces being rounded to a semicircular section,  $2\frac{1}{2}$  inches radius. The opening was entirely submerged at the inner side, under heads of from 6 inches to 4 feet. The efficiency of discharge varied from 73 per cent. to 78 per cent.

### **Water Power.**

The power of a fall of water for work, is measured by the product of the weight of water falling in a given time, by the height of the fall. The fall is measured from the surface of the head-water to the surface of the tail-water when the mill is at work. In calculations of water power, the weight of a cubic foot of water is commonly taken at  $62\frac{1}{2}$  pounds.

The potential horse-power of a stream is measured in the same way in terms of the fall or difference of level of the upper and lower gauge points.

The proportion of the horse-power of the fall that can be utilised depends upon the efficiency of the motor.

### **Water-Wheels.**

Under-shot wheels, having radial floats, are from 10 feet to 25 feet in diameter, and have an efficiency of from 27 per cent. to 30 per cent. Poncelet's under-shot wheels have curved floats. The efficiency is about 65 per cent. for falls of 4 feet or less; and from 55 per cent. to 50 per cent. for falls of from 6 feet to  $6\frac{1}{2}$  feet. The velocity of the floats should be 55 per cent. of that of the water.

Breast wheels have an efficiency of 70 per cent. when the height of the fall is about 8 feet; 50 per cent. for 4 feet of fall. The most suitable velocity of the floats is  $4\frac{1}{2}$  feet per second. The diameter should be at least  $11\frac{1}{2}$  feet; it is seldom more than double this.

Over-shot wheels are employed for heads of from 13 feet to 20 feet. The velocity of the floats should be at least 3 feet per second: say  $6\frac{1}{2}$  feet for the smaller diameters; 10 feet for the larger diameters. The efficiency is from 70 to 75 per cent.

Whitelaw's water-mill—a development of Barker's mill—has been proved experimentally to show 76 per cent. of efficiency. In ordinary, the efficiency is about 55 per cent.

The Fourneson turbine, having an outward flow, has an efficiency of from 60 per cent. to 70 per cent. The Jonval turbine, having a downward flow, has usually 72 per cent.

efficiency, under a full charge. It varies from 68 per cent. to 80 per cent. The vortex wheel, or inward-flow turbine, designed by Mr. James Thomson, has realised an efficiency of 77½ per cent. The Swain turbine, in which an inward and a downward discharge are combined, when tested by Mr. J. B. Francis, realised a maximum efficiency of 84 per cent. At half gate the maximum efficiency was 78 per cent.

The Girard turbine, or tangential wheel, has yielded an efficiency of 87 per cent. ; at moderate speeds, in ordinary practice, from 75 per cent. to 80 per cent.

### Hydraulic Power.

The Armstrong hydraulic machines work with efficiency varying with the multiplying gear, as follows :—

Efficiency per cent.		Efficiency per cent.		Efficiency per cent.	
Direct-acting . . . . .	93	6 to 1 . . . . .	72	12 to 1 . . . . .	59
2 to 1 . . . . .	89	8 to 1 . . . . .	67	14 to 1 . . . . .	54
4 to 1 . . . . .	76	10 to 1 . . . . .	63	16 to 1 . . . . .	50

Conditions :—Ordinary pump packing, with sheaves and wrought-iron pins. With special precautions, comprising large sheaves, and small hard pins, the efficiency of a machine multiplying 20 to 1 was as high as 66 per cent. With the accumulator rising or falling, at 700 lbs. pressure per square inch, the friction of the ram is about 2½ per cent.

The loss by friction in a steam-engine pumping into an accumulator, has been taken at 8·3 per cent. The ultimate efficiency is given by compounding the engine efficiency with the efficiency of the machine.

The ram of the hydraulic press is packed with a leather collar, the friction of which is 1 per cent. of the pressure for a 4-in. ram ; ½ per cent. for 8-in. ram ; ¼ per cent. for 16-in ram.

### Hydraulic Transmission of Motive Power.

At the Central Pumping Station, Falcon Wharf, Blackfriars, of the London Hydraulic Power Company, there are two accumulators having 20-inch rams of 23-feet stroke, loaded for a pressure of 750 lbs. per square inch. At the Philip Lane Pumping Station, the accumulator is 13 feet above those, and is loaded to 710 lbs. per square inch. The delivery of power-water from Falcon Wharf is through four 6-inch mains ; and, at 200 yards distance, through five 6-inch mains. The delivery is 1040 gallons per minute, at a velocity averaging 2·83 feet per second, or 170 feet per minute. The loss of head due to this velocity is 22·896 feet per 1000 yards, by the formula :—

$$\frac{(\text{Gallons per minute})^2 \times \text{length of pipe in yards}}{(3 \times \text{diameter of pipe in inches})}$$

The most distant point of the main is 5320 yards, or just over 3 miles, from the accumulators. In a circuit of 5 miles, the normal difference of pressure, or loss of head, was 20 feet head. To allow for such losses, as well as for valve passages and bends, the stated pressure supplied is 700 lbs. per square inch. At the end of 1887, the total length of mains laid was nearly 27 miles. There were then about 600 machines working from the mains in London, when the largest quantity of power delivered in one week was a little over 2,000,000 gallons, or 3,333 gallons per machine. The maximum consumption in any one hour was 35,000 gallons; the minimum, 1500 gallons. The practical efficiency—brake horse-power of hydraulic motors—may be fixed, says Mr. E. B. Ellington, the engineer of the company, at from 50 to 60 per cent. of the indicator power developed at the central station.

By the results of special trials, when 178½ indicator horse-power was developed, 4558 gallons of water were pumped per cwt. of coal consumed, with the Vicars stoker; 2·19 pounds of rough small coal being consumed per indicator horse-power per hour. In a trial for one week, under ordinary conditions, 3399 gallons of water were pumped per cwt. of coal consumed.

### **Hydraulic Machine Tools (Tweddell's System).**

Hydraulic pressure is used with great economy instead of the heavy gearing otherwise required to obtain the enormous power now used for riveting, punching, shearing and forging machines.

It is the cheapest and most efficient mode of transmitting power from the prime mover, especially in cases where the machines are spread over a large area of ground.

The efficiency of the pumps themselves is about 96, and that of the accumulator 99 per cent., and as the working parts of each tool practically only consist of a direct-acting ram, the loss by friction in the machine is equally small, and is at a minimum when doing useful work.

The pressure used by Mr. Tweddell (and almost invariably adopted as the standard one) is 1,500 lbs. per square inch. At this pressure, a pipe of ½-inch bore, at a speed of 5 feet per second, transmits 2·67 actual horse-power, a 1-inch pipe 10·7 horse-power, and a 1½-inch pipe 24, without any appreciable loss of efficiency.

The Tweddell Stationary Riveting Machines frequently put a pressure of 150 tons on rivet heads, closing them at the rate of from 3 to 5 per minute; but they are also made to exert pressures of 5 to 10 tons only for small rivets. Tweddell's Portable Riveters are used in all large bridge contracts for



TABLE 334.—SPEEDS OF CUTTING TOOLS. (J. Rose.)

Work Diameter. Inches.	Roughing Cuts. Feet per Minute.	Roughing Cuts. Lathe Revolutions per Minute.	Feed or Lathe Revolutions per Inch of Tool Travel.	Finishing Cuts. Lathe Revolutions per Minute.	Finishing Cuts. Lathe Revolutions per Inch Tool Travel.
WROUGHT IRON.					
$\frac{1}{2}$	40	305	30	305	60
1	35	133	30	133	60
$1\frac{1}{2}$	30	76	30	76	60
2	28	53	25	53	60
$2\frac{1}{2}$	28	42	25	42	50
3	28	35	25	35	50
$3\frac{1}{2}$	26	28	25	30	50
4	26	24	20	26	50
5	25	18	20	21	50
6	25	15	20	16	50
CAST IRON.					
1	45	163	30	163	40
$1\frac{1}{2}$	45	135	25	135	30
2	40	76	25	76	25
$2\frac{1}{2}$	40	61	20	61	20
3	35	44	20	50	16
$3\frac{1}{2}$	35	38	18	43	16
4	35	33	18	38	16
$4\frac{1}{2}$	30	25	16	28	14
5	30	22	16	26	14
$5\frac{1}{2}$	30	20	14	24	12
6	30	19	14	22	12
BRASS.					
$\frac{1}{2}$	120	910	25	910	40
$\frac{3}{4}$	110	556	25	556	40
1	100	382	25	382	40
$1\frac{1}{4}$	90	275	25	275	40
$1\frac{1}{2}$	80	203	25	203	40
$1\frac{3}{4}$	80	174	25	174	40
2	75	143	25	143	40
$2\frac{1}{2}$	75	114	25	114	40
3	70	89	25	80	40
$3\frac{1}{2}$	70	76	25	76	40
4	70	66	25	66	40
$4\frac{1}{2}$	65	55	25	55	40
5	65	50	25	50	40
$5\frac{1}{2}$	65	45	25	45	40
6	65	41	25	41	40
TOOL STEEL.					
$\frac{1}{2}$	24	245	60	245	60
$\frac{3}{4}$	24	184	60	184	60
1	24	147	50	147	60
$1\frac{1}{4}$	24	122	40	122	60
$1\frac{1}{2}$	20	87	30	87	60
$1\frac{3}{4}$	20	76	30	76	60
2	20	61	25	61	50
$2\frac{1}{4}$	18	45	25	45	50
$2\frac{1}{2}$	18	34	25	34	50
3	18	27	25	27	50
$3\frac{1}{2}$	18	22	25	22	40
4	18	19	25	19	40
$4\frac{1}{2}$	18	17	25	17	40
5	18	15	25	15	40

riveting up the bridges *in situ*, as was first done by Mr. Tweddell on the Primrose Street bridge, London, in 1873.

As many as 5,000  $\frac{7}{8}$ -inch rivets have been put in per day of 9½ hours by Messrs. Sellers at their Edgemoor Works in the U.S.A. by these machines, and for a time they put in from 17 to 20 rivets per minute.

Many of the Flanging Presses exert 650 tons of pressure. This system is also largely employed for cranes, placed over the machine tools, whether hydraulic or geared.

At the present time about 2,000 of these hydraulic machine tools of various types are at work.

### Speed of Cutting Tools.

For cast-iron, 150 to 190 inches per minute; boring, 80 inches per minute.

For wrought-iron, 260 to 280 inches per minute.

For yellow brass, 300 inches per minute.

### Wood-Working Machinery.

	Feet per Minute.
Teeth of circular saws . . . . .	9,000
Cutter blocks for planing and moulding (cutting edge) . . . . .	6,000
Irregular moulding and shaping machines (ditto) . . . . .	5,000
Band-saw for cutting metals . . . . .	250
Band-saw blades . . . . .	4,000
Saw and cutter sharpening machine . . . . .	5,000
Shafting . . . . .	250 revolutions.

### COLOURS.

TABLE 335.—COLOURS USED IN MECHANICAL AND ARCHITECTURAL DRAWING, TO REPRESENT VARIOUS MATERIALS.

Materials.	Colours used.
Brass . . . . .	Gamboge.
Brickwork (in section) . . . . .	Crimson lake.
Brickwork (in elevation) . . . . .	Crimson lake, mixed with burnt sienna.
Cement . . . . .	Sepia.
Concrete . . . . .	Sepia, mottled, with burnt umber.
Copper . . . . .	Crimson lake, mixed with gamboge.
Glass . . . . .	Cobalt (blue), mottled.
Iron (wrought) . . . . .	Prussian blue.
Iron (cast) . . . . .	Payne's grey.
Lead . . . . .	Indigo, or light Indian ink.
Leather . . . . .	Vandyke brown.
Plaster . . . . .	Sepia.
Stone . . . . .	Indigo, mixed with crimson lake.
Steel . . . . .	Crimson lake, mixed with Prussian blue.
Wood . . . . .	Burnt umber.
. . . . .	Indian red.
. . . . .	Burnt sienna

## ELECTRICAL ENGINEERING.

## Electrical Units.

Unit.	Name.	Derivation.	Dimensions in C. G. S. Units.
Electromotive Force . . .	Volt . . .	Ampère $\times$ Ohm .	$10^8$
Resistance . . .	Ohm . . .	Volt $\div$ Ampère .	$10^9$
" . . .	Megohm . . .	1 million Ohms .	$10^{12}$
Current . . .	Ampère . . .	Volt $\div$ Ohm .	$10^{-1}$
" . . .	Milliampère {	1 thousandth Ampère . . .	{ $10^{-4}$
Quantity . . .	Coulomb . . .	Ampère $\times$ Second	$10^{-1}$
Capacity . . .	Farad . . .	Coulomb $\div$ Volt	$10^{-9}$
" . . .	Microfarad . {	1 millionth Farad . . .	{ $10^{-15}$
* C. G. S. = Centimètre-Gramme-Second.			

For electric light and power purposes the Ampère is the practical unit of current.

For telegraph purposes the Milliampère is the practical unit of current.

The B.A. (British Association) Ohm, the unit of resistance in general use = resistance of column of pure mercury 1.0482 mètres long, 1 sq. mm. section at  $0^\circ$  C.; it is less in value than the true Ohm, which according to most recent determinations is  $\frac{1.0627}{1.0482}$  of the B.A. Ohm.

The Siemens Mercury Unit. = .9540 B.A. Unit.

Insulation resistances are usually measured in Megohms (1,000,000 ohms).

When a current of 1 Ampère flows, electricity is passing at the rate of 1 Coulomb per second.

A capacity of 1 Farad charged to a potential of 1 Volt contains 1 Coulomb of electricity.

The Microfarad is the practical unit of capacity ; it is the capacity of about  $\frac{1}{3}$ rd of a mile of submarine cable.

A Daniell Cell has roughly an Electromotive Force of 1.07 Volts.

### Electro-Mechanical Units.

Rate at which work is being done or energy expended in a resistance,  $R$ , through which a current,  $C$ , is flowing, there being an electromotive force or potential difference,  $E$ , between the ends of the resistance is

$$EC, C^2 R, \text{ or } \frac{E^2}{R}, \text{ Watts.}$$

1 Watt =  $\frac{1}{746}$ th of a horse-power, *i.e.*, 1 horse-power = 746 Watts.

1 Kilowatt = 1000 Watts = 1.34 horse-power.

1 Watt = 1 Joule per sec.

A current of 1 Ampère flowing through a resistance of 1 Ohm for 1 sec. does 1 Joule of work.

1 Joule will raise .238 grammes of water  $1^\circ$  C. in temperature.

1 Calorie is the amount of heat required to raise 1 gramme of water  $1^\circ$  C.

1 Joule = .238 calories.

1 Joule = .7373 foot-lbs. = 10,000,000 Ergs.

1 Erg (the absolute unit of *work*) = 1 Centimètre-dyne.

1 Dyne (the absolute unit of *force*) is that force which, acting for 1 sec. on a weight of 1 gramme on a smooth horizontal plane, will give it a velocity of 1 centimètre per sec.

Board of Trade unit = 1000 Watt-hours = work done by 1.34 horse-power during 1 hour.

### Measurement of Resistances.

For general purposes, the measurement of resistances is most conveniently effected by the Post Office pattern of Wheatstone bridge, the plan of connections of which is shown in Fig. 81.

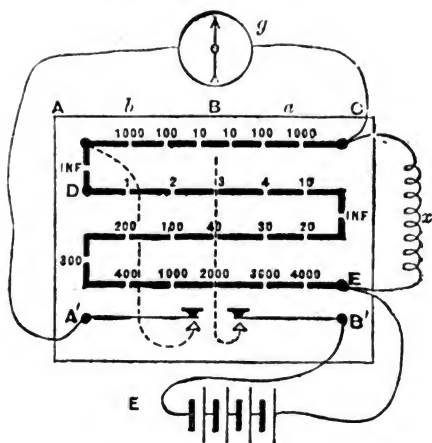
**Wheatstone Bridge.***Post Office Pattern.*

FIG. 81.

$x$  is the resistance to be measured,  $g$  a galvanometer of about 1000 ohms resistance, and  $E$  a battery (which for ordinary purposes may be about 10 Leclanché cells). In making a measurement plugs must be removed from  $a$  and  $b$ , and the right hand key pressed and kept down, then the left hand key must be alternately depressed and raised, plugs being removed from between  $D$  and  $E$  until no movement of the galvanometer needle is observed to take place on the depression and raising of the key. When balance is thus obtained

$$x = \frac{a}{b} r$$

$r$  being the resistance unplugged between  $D$  and  $E$  (the greatest value of this resistance is 10,000 ohms). By making  $a$  greater than  $b$  resistances greater than the whole of the resistance between  $D$  and  $E$ , i.e., 10,000 ohms, can be measured, the greatest value being 1,000,000 ohms, which is obtained by making  $a=1000$  and  $b=10$ , for when  $r=10,000$  ohms, then

$$x = \frac{1000}{10} \times 10,000 = 1,000,000 \text{ ohms.}$$

By making  $a$  less than  $b$  resistances less than 1 ohm can be measured, the least value being .01 ohm, which is obtained by making  $a=10$  and  $b=1000$ , for when  $r=1$  ohm, then

$$x = \frac{10}{1000} \times 1 = .01 \text{ ohms.}$$

**Individual Resistance of Three or more Telegraph Wires.**

In order to avoid errors due to earth currents or an imperfect earth when measuring the conductor resistance of 3 or more telegraph wires,

Loop wires 1 and 2 and let measured resistance be  $r_1$

" " 1 " 3 " " " "  $r_2$

" " 2 " 3 " " " "  $r_3$

then

$$\text{Resistance of No. 1 Wire} = \frac{r_1 + r_2 - r_3}{2}$$

$$\text{" " 2 " } = r_1 - \text{Resistance of No. 1 Wire}$$

$$\text{" " 3 " } = r_2 - \text{" " 2 " }$$

As the resistance of No. 1 wire is thus known we can loop it with any number of other wires, and having ascertained the resistances of the loops, the resistance of any one of the wires is given by subtracting the resistance of No. 1 wire from the resistance of the loop.

**Measurement of Low Resistances.**

For measuring low resistances—*i.e.* resistances of less than 1 ohm—with accuracy, the measurements are usually made by means of the "Metre" bridge:—

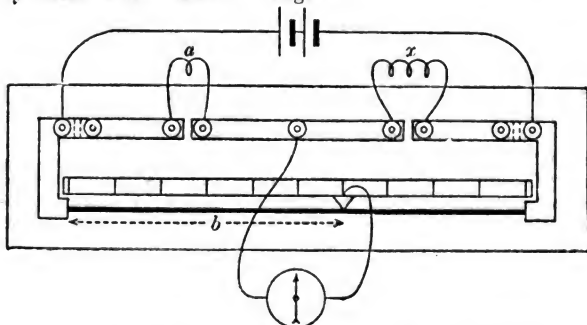


FIG. 82.

$a$  is a standard resistance of 1 ohm,  $x$  is the low resistance to be measured. A slider connected to one end of the galvanometer is moved until no movement of the needle takes place on depressing the slider contact, then

$$x = \frac{1000}{b} - 1$$

The galvanometer should have a resistance of about  $\frac{1}{10}$ th ohm, and the battery should be about 2 large size Leclanché cells. Great care should be taken that all the connections to the terminals are well made, and that the surfaces in contact are scraped bright.

**Measurement of High Resistances.**

For measuring high resistances, *i.e.* resistances exceeding 1 megohm, such as the *Insulation resistance* of a well insulated wire, the bridge method cannot be adopted with accuracy; in these cases the "deflection" method must be used, and a galvanometer of high resistance and one in which the deflections are directly proportional to the current, be employed. The galvanometer most suitable for the purpose is the "Thomson Reflecting."

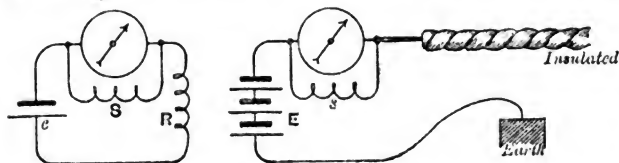


FIG. 83.

A small battery *c* (usually 1 cell) is first connected up with the galvanometer and with a resistance *R* of 10,000 ohms (the resistance between *D* and *E* of the Post Office Wheatstone bridge may be used for the purpose), the galvanometer being shunted by a shunt *S* (usually the  $\frac{1}{1000}$ th shunt) so that a convenient deflection *D* is obtained; this is called taking the *constant*. The connections are then altered as shown by the second fig., a large battery *E* (about 100 or more cells) being used, and the wire whose insulation is to be measured being joined up as shown. Let the deflection be *d*, and the shunt, *s*, on the galvanometer be the  $\frac{1}{n}$ th (usually  $\frac{1}{10}$ th,  $\frac{1}{100}$ th or  $\frac{1}{1000}$ th, *i.e.* *n* = 10, 100, or 1000); also let the shunt used when the *constant* is taken be the  $\frac{1}{N}$ th shunt, then

$$\text{Insulation resistance of wire} = \frac{D \times N}{n} \times K \div d$$

where *K* is the ratio between the number of cells used in taking *D* and in taking the constant; thus if *d* is given by 100 cells and *D* by 1 cell, then *K* = 100. When great accuracy is required, the exact ratio of the force of the large to the small battery has to be determined, for it is seldom that 100 cells have exactly 100 times the force of 1 cell, though in a large number of cases it is sufficient to consider it as such, care being taken that the cells are all in good condition. If a megohm resistance (1,000,000 ohms) is available, the *constant* may be taken with the same battery as is used for testing the insulated wire, the megohm being used in the place of the 10,000 ohms - in this case *K* = 1.

Care should be taken that the ends of the insulated wire being tested are well trimmed and quite dry; preferably the ends should be painted over with, or dipped for a moment in, hot paraffin *war*, *not* paraffin oil.

### Combined Resistances.

The joint resistance of any number of resistances joined in parallel or multiple arc, is equal to the reciprocal of the sum of the reciprocals of their respective resistances; thus the joint resistance in parallel of wires whose resistances are  $r_1, r_2, r_3, r_4$ , &c., is

$$\frac{1}{\frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3} + \frac{1}{r_4} + \dots}$$

If there are only *two* resistances, then their joint resistance in parallel is equal to the product of their values divided by their sum, or

$$\frac{r_1 r_2}{r_1 + r_2}$$

### Shunts.

If  $C$  = total current flowing through a galvanometer of resistance  $G$  shunted by a resistance  $S$ , and  $c$  the portion of this current flowing through the galvanometer, then

$$C = c \frac{G + S}{S}.$$

$\frac{G + S}{S}$  is called the *multiplying power* of the shunt.

The joint resistance of the galvanometer and shunt is

$$\frac{GS}{G + S}.$$

The shunt required to give a certain multiplying power  $n$  is

$$\frac{G}{n - 1}.$$

The joint resistance of the shunt and galvanometer in this case is

$$\frac{G}{n}.$$

If it is required to make up for the reduction of resistance in the circuit caused by the addition of the shunt, a *compensating* resistance,

$$\frac{G^2}{G + S}, \text{ or } G \frac{n - 1}{n}.$$

must be added in the circuit.



**Ratio of Current to Resistance and Potential Difference.**

C = current flowing through a wire,

V = potential difference between its ends,

R = resistance of wire,

$$C = \frac{V}{R}, \quad R = \frac{V}{C}, \quad V = C R.$$

**Corrections for Temperature.**

For general Telegraphic and Electric Light purposes, the resistances of copper conductors are reduced or corrected from the measured results at the observed temperature to the values at 60° F., this being the normal temperature of the air; this reduction can be effected by the following Table :—

**TABLE 336.—MULTIPLYING COEFFICIENTS FOR REDUCING THE OBSERVED RESISTANCE OF ORDINARY COPPER WIRE AT ANY TEMPERATURE TO 60° F.**

Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.
90	·9392	79	·9610	68	·9834	57	1·006	46·5	1·029
89·5	·9402	78·5	·9621	67·5	·9844	56·5	1·007	46	1·030
89	·9412	78	·9631	67	·9855	56	1·008	45·5	1·031
88·5	·9421	77·5	·9641	66·5	·9865	55·5	1·009	45	1·032
88	·9431	77	·9651	66	·9875	55	1·010	44·5	1·033
87·5	·9441	76·5	·9661	65·5	·9886	54·5	1·012	44	1·034
87	·9451	76	·9671	65	·9896	54	1·013	43·5	1·035
86·5	·9461	75·5	·9681	64·5	·9906	53·5	1·014	43	1·036
86	·9471	75	·9691	64	·9917	53	1·015	42·5	1·037
85·5	·9481	74·5	·9701	63·5	·9927	52·5	1·016	42	1·038
85	·9491	74	·9711	63	·9937	52	1·017	41·5	1·039
84·5	·9501	73·5	·9722	62·5	·9948	51·5	1·018	41	1·041
84	·9510	73	·9732	62	·9958	51	1·019	40·5	1·042
83·5	·9520	72·5	·9742	61·5	·9969	50·5	1·020	40	1·043
83	·9530	72	·9752	61	·9979	50	1·021	39·5	1·044
82·5	·9540	71·5	·9762	60·5	·9990	49·5	1·022	39	1·045
82	·9550	71	·9772	<b>60</b>	1·000	49	1·023	38·5	1·046
81·5	·9560	70·5	·9783	59·5	1·001	48·5	1·024	38	1·047
81	·9570	70	·9793	59	1·002	48	1·025	37·5	1·048
80·5	·9580	69·5	·9803	58·5	1·003	47·5	1·026	37	1·049
80	·9590	69	·9814	58	1·004	47	1·027	36·5	1·050
79·5	·9600	68·5	·9824	57·5	1·005				

*Example.*—The resistance of a copper wire at 48° F. is 200 ohms; what is its resistance at 60° F.?

Resistance at 60° F. =  $200 \times 1·025 = 205·0$  ohms.

For Submarine Cable tests the results are reduced to 75° F. by the following table:—

TABLE 337.—MULTIPLYING COEFFICIENTS (k) FOR REDUCING THE OBSERVED RESISTANCE OF ORDINARY COPPER WIRE AT ANY TEMPERATURE TO 75° F.

Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.
90	·9691	79	·9917	68	1·015	57	1·038	46·5	1·061
89·5	·9701	78·5	·9927	67·5	1·016	56·5	1·039	46	1·062
89	·9711	78	·9937	67	1·017	56	1·041	45·5	1·064
88·5	·9722	77·5	·9948	66·5	1·018	55·5	1·042	45	1·065
88	·9732	77	·9958	66	1·019	55	1·043	44·5	1·066
87·5	·9742	76·5	·9969	65·5	1·020	54·5	1·044	44	1·067
87	·9752	76	·9979	65	1·021	54	1·045	43·5	1·068
86·5	·9762	75·5	·9990	64·5	1·022	53·5	1·046	43	1·069
86	·9772	75	1·000	64	1·023	53	1·047	42·5	1·070
85·5	·9783	74·5	1·001	63·5	1·024	52·5	1·048	42	1·071
85	·9793	74	1·002	63	1·025	52	1·049	41·5	1·072
84·5	·9803	73·5	1·003	62·5	1·026	51·5	1·050	41	1·074
84	·9814	73	1·004	62	1·027	51	1·051	40·5	1·075
83·5	·9824	72·5	1·005	61·5	1·029	50·5	1·053	40	1·076
83	·9834	72	1·006	61	1·030	50	1·054	39·5	1·077
82·5	·9844	71·5	1·007	60·5	1·031	49·5	1·055	39	1·078
82	·9855	71	1·008	60	1·032	49	1·056	38·5	1·079
81·5	·9865	70·5	1·009	59·5	1·033	48·5	1·057	38	1·080
81	·9875	70	1·010	59	1·034	48	1·058	37·5	1·082
80·5	·9886	69·5	1·012	58·5	1·035	47·5	1·059	37	1·083
80	·9896	69	1·013	58	1·036	47	1·060	36·5	1·084
79·5	·9906	68·5	1·014	57·5	1·037				

*Example.*—The resistance of a copper wire at 57° F. is 300 ohms; what is its resistance at 75° F.?

Resistance at 75° F. =  $300 \times 1·038 = 311·4$  ohms.

By means of the foregoing Table the temperature of the Sea in which a Submarine Cable is laid can be determined, provided the resistance of the conductor of the Cable at 75° was ascertained during the course of manufacture. The measured resistance of the Cable when the latter is laid, divided into the resistance at 75° gives a coefficient which in the above Table corresponds to the temperature of the conductor, that is of the Sea.

The reduction to 75° of the Insulation (dielectric) tests is effected by the following Table:—

TABLE 338.—DIVIDING COEFFICIENTS FOR CORRECTING THE OBSERVED RESISTANCE OF GUTTA-PERCHA AT ANY TEMPERATURE TO 75° F

Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.	Temp. ° F.	Coeff.
90	3197	80	6837	70	1463	60	3128	50	6692
89.5	3320	79.5	7102	69.5	1519	59.5	3250	49.5	6951
89	3449	79	7378	69	1578	59	3376	49	7220
88.5	3583	78.5	7663	68.5	1639	58.5	3506	48.5	7500
88	3722	78	7960	68	1703	58	3642	48	7791
87.5	3866	77.5	8269	67.5	1769	57.5	3783	47.5	8093
87	4016	77	8589	67	1837	57	3930	47	8406
86.5	4171	76.5	8922	66.5	1908	56.5	4082	46.5	8732
86	4343	76	9267	66	1982	56	4240	46	9070
85.5	4501	75.5	9627	65.5	2059	55.5	4405	45.5	9422
85	4675	75	1000	65	2139	55	4575	45	9787
84.5	4856	74.5	1039	64.5	2222	54.5	4753	44.5	1017
84	5044	74	1079	64	2308	54	4937	44	1056
83.5	5240	73.5	1121	63.5	2397	53.5	5128	43.5	1097
83	5443	73	1164	63	2490	53	5327	43	1139
82.5	5654	72.5	1209	62.5	2587	52.5	5533	42.5	1184
82	5873	72	1256	62	2687	52	5748	42	1229
81.5	6100	71.5	1305	61.5	2792	51.5	5970	41.5	1277
81	6337	71	1355	61	2899	51	6202	41	1327
80.5	6582	70.5	1408	60.5	3012	50.5	6442	40.5	1378

*Example.*—The insulation resistance at 62° F. of a wire insulated with gutta-percha is 500 megohms; what is the resistance at 75° F.?

$$\text{Resistance} = 500 \div 2.687 = 186.1 \text{ megohms.}$$

### Fault Testing.

#### Blavier's Method.

Insulate further end of line and measure resistance  $l$ .

Put further end of line to earth, and measure resistance  $l_1$ .

Resistance of line when good =  $L$ .

$$\text{Resistance up to fault} = l_1 - \sqrt{(l - l_1)(L - l_1)}.$$

*Overlap Method.*

Measure resistance  $l$  from station A, station B insulating.

Measure resistance  $l_2$  from station B, station A insulating.

Resistance of line when good =  $L$ .

Resistance up to fault from station A =  $\frac{L + l - l_2}{2}$ .

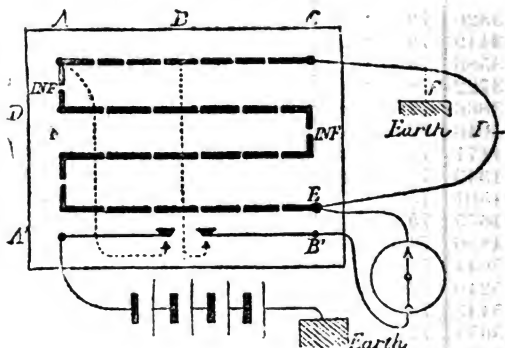
*Murray's Loop Method.*

FIG. 84.

C P faulty line.

E P good line.

All plugs to be inserted between B and C, also plug between A and D.

10, 100, or 1000 plugs (according to length of loop) to be taken out between A and C.

*Left-hand* key to be held permanently down, and *right-hand* key to be manipulated.

D E to be adjusted till equilibrium is produced.

Resistance from C up to fault =  $L \frac{b}{b+d}$ .

$L$  = total resistance of entire loop (measured by bridge, page 609).

$b$  = resistance unplugged in A B.

" " " " D E.

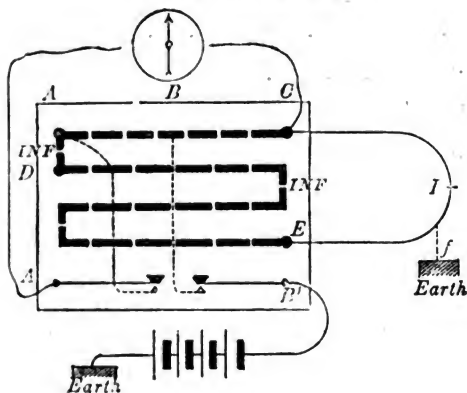
*Varley's Loop Method.*

FIG. 85

E P. faulty line.      C P good line.

10, 100, or 1000 plugs (according to length of loop) to be taken out between A and B and between B and C.

*Right-hand key* to be held permanently down, and *left-hand key* to be manipulated.

D E to be adjusted till equilibrium is produced.

Resistance from E up to fault =  $\frac{bL - ad}{b + a}$ .

L = total resistance of entire loop (measured by bridge, page 609).

a = resistance unplugged in B C.

b =     "             "             " A B.

d =     "             "             " D E.

**Inductive or Electrostatic Capacity.**

Inductive capacities are measured by comparing the discharge from a standard condenser with the discharge from the

insulated wire whose capacity is required ; the capacities will be in direct proportion to the discharges if the latter are measured on a Thomson reflecting galvanometer.

Inductive capacity of a wire insulated with gutta-percha

$$= \frac{.170}{\log. \frac{D}{d}} \text{ m. farads per knot, approximately}$$

$$= \frac{.147}{\log. \frac{D}{d}} \quad \text{,,} \quad \text{,, statute mile ,,}$$

where  $D$  = diameter of insulating material,

$d$  = ,, conductor.

For india-rubber the values are about 10 to 15 per cent. less.

Inductive capacity of an aerial line

$$= \frac{.061637}{\log. \frac{4h}{d}} \text{ m. farads per statute mile, approx.}$$

where  $d$  = diameter of wire in mils (1 mil. =  $\frac{1}{1000}$  in.)

$h$  = height of wire above ground, also in mils.

If there are a large number of wires on the poles the inductive capacity of each wire will be increased to a small extent.

### ELECTRO-CHEMISTRY.

One ampère of current decomposes .00009324 gramme of water per second, liberating .000010384 gramme of hydrogen, and .00008286 gramme of oxygen.

$C$  ampères of current in  $T$  seconds will throw down or deposit from a solution of any salt of a metal

$CTa$  grammes, or  $CTb$  grains,

where  $a$  and  $b$  are the values given in the following Table :—

TABLE 339.—VALUES OF *a* AND *b*, ELECTRO-CHEMICAL DEPOSITS.

Metal.	<i>a</i> (grammes).	<i>b</i> (grains).
Hydrogen . . . . .	·000010384	·00016025
Aluminium . . . . .	·00009449	·0014582
Magnesium . . . . .	·00012430	·0019182
Iron (Ferric) . . . . .	·00019356	·0029869
„ ( <i>Ferrous</i> ) . . . . .	·00029035	·0044808
Sodium . . . . .	·00023873	·0036842
Nickel . . . . .	·00030425	·0046953
Tin (Stannic) . . . . .	·00030581	·0047085
„ ( <i>Stannous</i> ) . . . . .	·00061162	·0094387
Copper (Cupric) . . . . .	·00032709	·0050478
„ ( <i>Cuprous</i> ) . . . . .	·00065419	·0100960
Zinc . . . . .	·00033696	·0052001
Potassium . . . . .	·00040539	·0062561
Gold . . . . .	·00067911	·0104800
Mercury (Mercuric) . . . . .	·00103740	·0160100
„ ( <i>Mercurous</i> ) . . . . .	·00207470	·0320170
Lead . . . . .	·00107160	·0165370
Silver . . . . .	·00111800	·0172540

**Primary Batteries.**

A current of 1 ampère for 1 hour in a primary battery will dissolve 1·213 grammes = 18·72 grains of zinc in each cell, provided there is no local action.

Quantity of zinc consumed in a primary battery per horse-power-hour

$$= \frac{1·995}{E} \text{ lbs.,}$$

where *E* is the electromotive force of the battery.

Quantity of any metal (used as the positive plate) consumed in a primary battery per horse-power-hour

$$= \frac{5921·8 \times a}{E} \text{ lbs.,}$$

where *a* is the value given in the foregoing table.

Weight for weight primary batteries contain a much greater storage of energy than *Accumulators*, but the energy being produced by the combustion of zinc and the decomposition of acids is more expensive to obtain.

**Accumulators.**

The largest size accumulators (Electric Power Storage Company) have a capacity of 660 ampère-hours, and weigh, when charged with acid, 265 lbs. The acid (acidulated water), weighs 73 lbs.; the approximate outside dimensions of the glass cells are,—length,  $18\frac{1}{2}$  inches; width,  $11\frac{1}{2}$  inches; height,  $13\frac{1}{2}$  inches; height over all,  $15\frac{1}{2}$  inches; each cell contains 31 plates. The cells are charged with a current of from 50 to 60 ampères, and discharged with a current not exceeding 60 ampères. The smaller cells are rather heavier in proportion.

Taking the plates alone, each 1 lb. weight of plates will store about 30,000 foot-pounds of energy.

The acidulated water contains 25 per cent. of sulphuric acid.

The cells should never be left standing uncharged, and should not be discharged to more than  $\frac{2}{3}$  of their capacity; they should not be discharged beyond the maximum rate for which they are designed, *i.e.*, a cell which is intended to discharge at a maximum rate of 60 ampères should not be worked at 70 ampères as this would tend to spoil the cells.

About 80 per cent. of the charge can be obtained by discharge if the cells are in good condition.

The electromotive force of accumulators averages 2 volts, though the force is slightly higher when the cells are freshly charged.

The charging electromotive force should not exceed the electromotive force of the accumulator by more than 5 per cent.

If  $E$  = the full electromotive force of the charging dynamo and  $C$  = the current passing, the *total* rate at which work is being expended on the charging is

$$EC \text{ Watts};$$

a portion of the work is wasted in heating the accumulator.

The actual rate at which work is being accumulated in the accumulator is

$$E' C$$

where  $E'$  is the electromotive force at the accumulator terminals *when the latter are disconnected*.

In the use of accumulators there is first a loss in charging, the loss being due to waste in the dynamo and waste in the accumulator; there is also waste in the accumulator in discharging partly due to heating and partly to local action.

It is more economical to charge accumulators with a weak



current continued for a lengthened period than with a strong current for a short period.

The resistance of an accumulator (when discharging) is

$$\frac{E_1 - E_2}{C}$$

where  $E_1$  is the electromotive force on open circuit, and  $E_2$  the electromotive force on closed circuit.

The accumulator cells should be kept in as dry (but not warm) a situation as possible.

For charging accumulators a *shunt* wound dynamo must be used.

### Current Induction.

If  $e$  = electromotive force set up in a rectilinear conductor of length  $l$  moving through a magnetic field of intensity  $H$ ,

$v$  = velocity of moving conductor,

$\alpha$  = angle the conductor makes with the lines of force,

$\phi$  = angle between the direction of motion and the direction of the force exerted between the magnetic field and the conductor; then,

$$e = H l v \sin \alpha \cos \phi.$$

If the conductor is at right angles to and moves so as to cut the lines of force at right angles (in which case  $\sin \alpha \cos \phi$  each equal 1), then 1 Gauss is the strength of field in which a length of one million centimetres of wire moving with unit velocity (1 centimetre per sec.), develops 1 volt of electromotive force = 100 times the strength of 1 C. G. S. field.

The strongest field of a dynamo magnet is about 100 Gaussses =  $100 \times 100 = 10,000$  C. G. S. units.

1 C. G. S. magnetic field has 1 line of force per square centimetre.

1 Kapp line = 6,000 C. G. S. lines.

1 " " per square inch = 930 C. G. S. lines per square centimetre.

A magnetic field whose strength is 100 Gaussses contains 10,000  
 $\frac{10,000}{930} = 10.75$  Kapp lines per square inch.

The Kapp line was proposed as a suitable factory unit because the revolutions of dynamo armatures are usually reckoned per minute instead of per second (60 secs. = 1 minute), and also by dividing by 100, the units expressing the number of magnetic lines are brought to numerical values easily dealt with and remembered.

## DYNAMOS.

## The Series Dynamo.

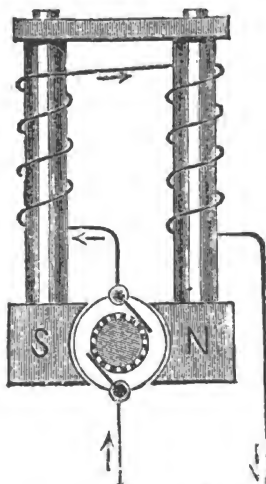


FIG. 86.—Series Wound.

If  $R$  = external resistance.

$r_a$  = resistance of armature.

$r_m$  = resistance of field-magnet coils.

$E$  = electromotive force of machine.

$e$  = potential difference between terminals of machine.

$c$  = current strength.

$$e = c R = E - (r_a + r_m) c$$

$$\left. \begin{array}{l} \text{Ratio of useful electric energy available} \\ \text{in external circuit to total electric} \\ \text{energy developed} \end{array} \right\} = \frac{R}{R + r_a + r_m}$$

$r_m$  may with advantage be made about two-thirds of  $r_a$ .

Series machines are used for running arc lamps direct.

## The Shunt Dynamo.

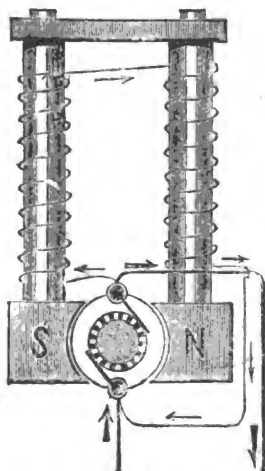


FIG. 87.--Shunt Wound.

If  $R$  = external resistance,

$r_a$  = resistance of armature,

$r_s$  = " " field-magnet coils,

$E$  = electromotive force of machine,

$e$  = potential difference between terminals of machine,

$c$  = current in external circuit,

$c_a$  = " " armature,

$c_s$  = " " field-magnet coils,

$$e = c R = c_s r_s = E - r_a (c + c_a)$$

$$E = \left( r_a + \frac{R r_s}{R + r_s} \right) c_a = e r_a \left( \frac{1}{R} + \frac{1}{r_a} + \frac{1}{r_s} \right)$$

$$\left. \begin{array}{l} \text{Ratio of useful electric energy} \\ \text{available in external circuit to} \\ \text{total energy developed} \end{array} \right\} = \frac{C^2 R}{C^2 R + c_s^2 r_s + c_a^2 r_a}$$

In order that a shunt dynamo may give in the external circuit as much as 90 per cent. of its total electric energy the resistance of the shunt must be at least 364 times as great as that of the armature.

Practically the armature resistance may be made  $\frac{1}{20}$ th of the external resistance, and the shunt resistance 20 times as great.

Shunt machines are used for charging accumulators and for electroplating.

### Separately Excited Dynamos.

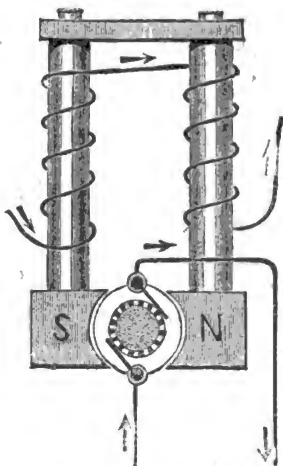


FIG. 88.—Separate Excitation.

If  $R$  = external resistance,

$r_m$  = resistance of field-magnet coils,

$E$  = electromotive force of machine,

$c$  = current in external circuit,

$c_m$  = „ „ field-magnets,

$$E = c R$$

$$\left. \begin{array}{l} \text{Ratio of useful electric energy available} \\ \text{in external circuit to total energy} \\ \text{developed} \end{array} \right\} = \frac{C^2 R}{c^2 R + c_m^2 r_m}$$

This gives the distribution of the energy as far as the machine itself is concerned, but there is also a loss of energy in the dynamo used for exciting the field magnets which must be taken into account. This exciting dynamo may be used to excite the field magnets of several dynamos.

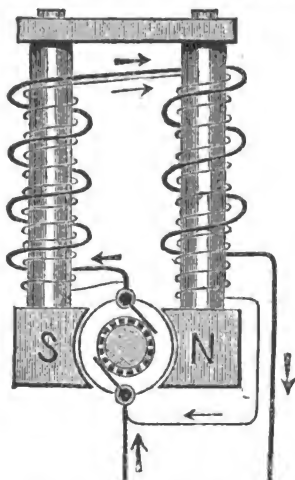
**Compound Wound Dynamos.**

FIG. 89.—Compound Wound.

If  $R$  = external resistance.

$r_a$  = resistance of armature.

$r_s$  = „ „ field-magnet shunt coils.

$r_m$  = „ „ „ „ series „

$c$  = current in external circuit.

$c_a$  = „ „ armature coils.

$c_s$  = „ „ shunt „

$c_m$  = „ „ series „

$$\left. \begin{array}{l} \text{Ratio of useful electric} \\ \text{energy available in ex-} \\ \text{ternal circuit to total} \\ \text{energy developed} \end{array} \right\} = \frac{c^2 R}{c^2 R + c_a^2 r_a + c_s^2 r_s + c_m^2 r_m}$$

$r_s$  should be from 1,000 to 1,500 times  $r_a$ , and  $r_m$  about two-thirds  $r_a$ .

Compound machines enable a constant potential to be kept at their terminals irrespective of the work to be done in the external circuit. This is required in the case of an installation of incandescent lamps.

**Alternating Current Dynamos.**

If  $E$  = electromotive force after time  $t$ .

$C$  = current

$T$  = half period of a "complete" alternation.

$t$  = time from the instant at which the electromotive was zero when changing from the direction reckoned as negative to that reckoned as positive.

$K$  = a constant.

$$C = \frac{K}{T} \sin \frac{\pi}{T} t$$

If  $C_m$  = mean current during the time  $T$ .

$$C_m = \frac{2}{\pi} \frac{K}{T}$$

When an alternating current passes through a wire,  $L$ , the resistance due to the self-induction in the wire whose ohmic resistance is  $R$  and self-induction  $L$  is

$$\frac{1}{T} \sqrt{R^2 T^2 + \pi^2 L^2}$$

If  $C'$  be the current indicated on an electro-dynamometer

$$C_m = \frac{9}{10} C'$$

Watts consumed in lamps  
worked with alternating  
currents  $\left\{ = \frac{r T \sqrt{A^2 V^2}}{\sqrt{l^2 \pi^2 + r^2 T^2}} \right.$

Where  $A$  = mean current measured on an electro-dynamometer.

$V$  = „ potential at terminal of lamps.

$r$  = ohmic resistance of lamp when hot.

$l$  = coefficient of self-induction.

$T$  = half period of a complete alternation.

**Efficiency of Dynamos.**

Commercial efficiency =  $\frac{\text{Electrical energy in external circuit.}}{\text{Mechanical energy applied at dynamo.}}$

Efficiency of conversion =  $\frac{\text{Total electrical energy.}}{\text{Mechanical energy applied at dynamo.}}$

Electrical efficiency =  $\frac{\text{Electrical energy in external circuit.}}{\text{Total electrical energy.}}$

The insulation of the various parts of a dynamo is a point of importance ; in particular, measurements should be made of the insulation resistance between the terminals of the machine and its metal bed-plate, and between the segments of the collector and the axle.

In order to determine the efficiency of a dynamo, measurements should be made of the horse-power expended at the pulley (which may be done by means of a Prony brake) and of the energy of the electric currents given out. A good dynamo should have a commercial efficiency of at least 50 per cent.

### Transformers or Converters.

Transformers are used for reducing the high potential from a dynamo to a low potential for working the lamps, the electric power being transmitted more economically at a high than a low potential, as conductors of small diameter can be used, whilst the danger of a high potential in the consumers houses is avoided.

The efficiency of a good transformer at full output is about 95 per cent. and at one-third output 90 per cent. The weight of a transformer varies from 15 to 50 lb. per horse-power according to the size and type.

The rate of alternation of the current in a transformer varies from about 50 to 130 complete alternations per second. Each type of transformer has its best rate of alternations to give the highest efficiency ; if this rate is exceeded or reduced an abnormal rise of temperature takes place.

Transformers are usually made to transform from a potential of 2,000 volts or 1,000 volts down to 100 or to 50 volts.

Great care must be taken in the construction of transformers to avoid any leakage from the primary to the secondary circuit.

The following gives dimensions, &c., of a Westinghouse transformer :—

Primary current, 1·5 ampères at 1,000 volts.

Secondary „ 37·5 „ „ 40 „

Outside dimensions, 20 × 6 × 4 inches.

Weight of primary wire, 5 lb. gauge, 35 mils.

„ „ secondary „ 5½ „ „ 120 „

The secondary wire is divided into 25 sections joined in parallel.

Weight of iron, 50 lbs.

Efficiency, 97·2 per cent. (?)

**ELECTRIC LAMPS.****Arc Lamps.**

If  $L$  = lighting power.

$C$  = current.

$$L \propto 100 \left\{ C + \left( \frac{C}{4} \right)^2 \right\} - 200.$$

Arc lamps for a given expenditure of energy give about 7 times the power of an incandescent lamp.

If  $l$  = length of arc in millimetres.

$E$  = electromotive force between the carbons.

$C$  = current flowing.

$R$  = resistance of arc.

$$R = \frac{39}{C} + 1.8 \frac{l}{C}$$

In an arc lamp the top or positive carbon burns about  $1\frac{1}{2}$  inches per hour, and twice as fast as the bottom or negative carbon.

A 1000 c.p. lamp requires carbons about  $\frac{9}{16}$ ths inch in diameter; it is usually run at a potential of 50 volts, and takes about 10 ampères; the power required is about 1 horse. Arc lamps are usually run in series.

**Incandescence Lamps.**

A 16 c.p. incandescent lamp is usually run at a potential of 100 volts, and takes .5 ampère, *i.e.*, requires a power of a little over 3 watts per candle.

1 indicated horse-power will run 8 incandescent lamps of 16 c.p.

Incandescence lamps are usually run in multiple arc.

**Rules and Regulations**

**of the Institution of Electrical Engineers for the Prevention of Fire Risks arising from Electric Lighting (1888).**

*Conductors.*

1. They must have a sectional area and conductivity so proportioned to the work they have to do that, if double the current proposed is sent through them, the temperature of such conductors shall not exceed  $150^{\circ}$  F.

2. The conductors, or their casings, should be placed in sight if possible; and they should always be as accessible as circumstances will permit.



3. Within buildings they should all be insulated ; and this rule applies equally to all conductors and parts of fittings which may have to be handled.

4. Whatever insulating material is employed, it should not soften until a temperature of 170° F. has been reached, and in all cases the material must be damp-proof.

5. When leads pass through roofs, floors, walls, or partitions, and where they cross or are liable to touch metallic substances, such as bell wires, iron girders, or pipes, they should be thoroughly protected by suitable additional covering ; and where they are liable to abrasion from any cause, or to the depredations of rats or mice, they should be encased in some suitable hard material.

6. In the case of portable fittings with which flexible leads are used, special precautions must be taken.

7. Conductors should be kept as far apart as circumstances will permit, the spacing between them being governed by their potential difference.

8. When conductors are carried in very inflammable structures, precautions should be taken to isolate them therefrom.

9. Conductors which are protected on the outside by lead, or metallic armour of any kind, require the greatest care in fixing, on account of the large conducting surface which would become connected to the core in the event of metallic contact between them.

10. In cases where conductors pass into a building, from one building to another, or from one room to another, precautions should be taken to prevent the possibility of fire or water passing along the course of the conductors.

11. All joints must be mechanically and electrically perfect, to prevent heat being generated at these points. When soldering fluids are used in making joints, the latter should be carefully washed and dried before insulation is applied.

12. Under all circumstances complete metallic circuits must be employed. Gas and water pipes must never form part of the circuit, as their joints are rarely electrically good and therefore become a source of danger.

13. Overhead conductors, whether passing over or attached to buildings, must be insulated at their points of support. Precautions must be taken to obviate all risk of short-circuiting where they are likely to touch a building or other overhead conductors and wires, either by their own falling or by being fallen upon by other conductors.

14. In the case of overhead wires, every main should have a lightning protector at each point where it enters or branches into a building.

15. Metal fastenings for fixing conductors should be avoided.

but, when unavoidable, some additional covering should protect the conductor from mechanical injury at such fixing points.

16. The insulation of a system of distribution should be such that the greatest leakage from any conductor to earth (and, in case of parallel working, from one conductor to the other, when all branches are switched on, but the lamps, motors, &c., removed), does not exceed one five-thousandth part of the total current intended for the supply of the said lamps, motors, &c.; the test being made at the usual working electromotive force.

17. It will often be found a great convenience and assistance in the prevention of accidents if the positive lead be coloured differently to the negative, or made otherwise distinguishable.

#### *Switches.*

18. Every switch or commutator should be of such construction as to comply with the following condition, namely:—That, when the handle is moved or turned to and from the positions of “on” and “off,” it is impossible for it to remain in any intermediate position, or to permit of a permanent arc, or heating.

19. The handles of every switch must be completely insulated from the circuit.

20. The main switches of a building should be placed as near as possible to the point of entrance of the conductors, or to the generators of the current if they are within the building itself. Switches should be provided on both leads.

21. Switch-boards should bear clear instructions for their use by the inexperienced.

#### *Electrical Fittings Generally.*

22. Switches, commutators, resistances, bare connections, lamps, &c., must be mounted on incombustible bases. Cut-outs mounted on bases of wood rendered unflammable are admissible. Vulcanite bases are undesirable in damp situations. The cracking of porcelain and earthenware fittings is a source of danger which can be avoided by precautions in fixing.

#### *Cut-outs.*

23. All circuits should be protected with cut-outs; and all leads from the mains, or small conductors from larger ones, must be fitted with cut-outs at their branching points.

24. Where fusible cut-outs are used, the section should be so situated within its frame that the fused metal cannot fall where it may cause a “short-circuit” or an ignition.

25. For all main conductors a cut-out should be provided for both the "flow" and "return," and the two fusible sections must not be in the same compartment.

26. The flexible leads of portable fittings must in all cases be protected by cut-outs at their fixed points of connection.

#### *Arc Lamps.*

27. Arc lamps must always be guarded by lanterns or netted globes, so as to prevent danger from ascending sparks and from falling glass and incandescent pieces of carbon.

28. All parts of the lamps and lanterns which are liable to be handled (except by the persons employed to trim them) should be insulated.

#### *The Dynamo.*

29. The armatures and field-magnet coils should be thoroughly insulated. Dynamos should always be fixed in dry places, and they must not be exposed to dust flyings or other industrial waste products carried in suspension in the air. They should not be permitted in the working-rooms of mills, where the liability to such dangers exists, or where any inflammable manufactures are carried on or inflammable materials are stored.

30. Motors should be subject to the same conditions; but when it is necessary to use them in positions such as those above referred to, they must be securely cased in, such cases having a non-combustible lining.

#### *Batteries.*

31. Both primary and secondary batteries should be placed and used under the same precautions as prescribed for dynamos; and the room in which they are placed should be well ventilated. The batteries themselves must be well insulated.

#### *Transformers.*

32. When these are used to transform either direct or alternating currents of high electro-motive force—that is, from or to an electro-motive force of, say, 200 volts—they, together with their switches and cut-outs, must be placed in a fire- and moisture-proof structure—preferably outside the building for which they are required. No part of such apparatus should be accessible except to the person in charge of their maintenance.

33. In all cases conductors conveying currents of high electro-motive force inside buildings must be specially

exceptionally insulated, cased in, and the casing made fire-proof.

34. The positive and negative terminals connected to such conductors should not be permitted to be nearer each other than 12 inches.

35. Transformers which, under normal conditions of load, heat above 150° F., should not be permitted to remain in use.

36. Transformers should be so constructed that under no circumstances whatever should a contact between the primary and secondary coils lead the high E.M.F. into the building.

### *Maintenance.*

37. The value of frequently testing and inspecting the apparatus and circuits cannot be too strongly urged as a precaution against fire. Records should be kept of all tests, so that any gradual deterioration of the system may be detected.

38. Cleanliness of all parts of the apparatus and fittings is essential to a good maintenance.

39. No repairs or alterations must be made when the current is "on."

### **Three-Wire System.**

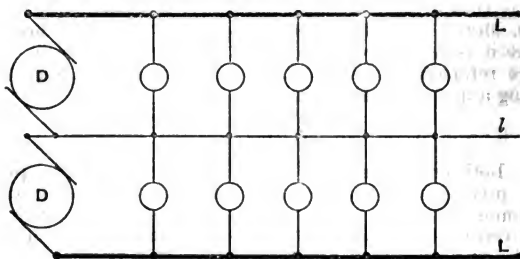


FIG. 90.

In this system of distribution, two equal dynamos, D, D, are joined in series. Three lead-wires are used, two, L, L, being of larger sectional area than the third, l, or centre lead. The advantage of the arrangement is that the main leads can be smaller than would be the case if a single dynamo were used and all the lamps were in parallel, whilst by the addition of the third or centre wire the breakage of one or more lamps does not cause the extinction of the other lamps with which they are in series, the continuity of the current being kept up by the centre wire.

**Electric Motors.**

Let  $E$  = electro-motive force of dynamo.

$e$  = back electro-motive force of motor.

$V$  = potential difference between terminals of dynamo.

$V$  = " " " " motor.

$r_1$  = Resistance of dynamo.

$r_2$  = " " motor.

$R$  = " " line.

$W_1$  = mechanical work put into dynamo.

$W_2$  = electrical " given out by "

$w_1$  = mechanical " taken out of motor.

$w_2$  = electrical " put into "

$w_3$  = " available in "

$$E = V + Cr_1$$

$$E = V + C(r_1 + R)$$

$$e = V - Cr_2$$

$$C = \frac{E - e}{r_1 + R + r_2}$$

$$w_2 = CV \text{ watts}$$

$$w_3 = Cr = C(V - Cr) \text{ watts}$$

$$W_2 = CE \text{ watts}$$

$$\text{Maximum possible electrical efficiency of system} = \frac{e}{E}$$

$$\text{Actual electrical efficiency} = \frac{w_1}{C(V + C(r_1 + R))}$$

$$\text{Actual mechanical efficiency} = \frac{w_1}{W}$$

In order to get the greatest possible efficiency the value of  $e$  should be as large as possible, *i.e.*, the motor should run at as high a speed as possible, and in order to get as much power as possible with high efficiency  $E$  should be as large as possible.

The greatest amount of work is got out of the motor when it runs at such a speed that  $e = \frac{E}{2}$ . But in this case the efficiency is only 50 per cent., *i.e.*, only half the power given out by the dynamo generator is utilised in the motor. If the motor runs at a higher speed, the work it does becomes less, but its efficiency increases. When the speed becomes such that  $e$  nearly equals  $E$ , the work done is small, but it is nearly all being utilised.

## Electric Light Cables.

TABLE 340.—ELECTRIC LIGHT CABLES: WEIGHTS, SIZES, AND RESISTANCES. (SILVERTOWN LIST.)

Number of Wires in Strand.	Legal Standard Gauge of each Wire.		Diameter. Of the Strand.		Equivalent to Solid Wires.			Weight of Conductor.		Resistance at 60° Fahr.	
	Inch.	m/in.	Inch.	m/in.	Inch.	m/in.	Sq. In.	Per Statute Mile.	Kilo-gramms.	Per Statute Mile.	Kilo-metre.
1	.028	.711	...	...	.028	.711	.0006	12	4	72.52	45.06
1	.032	.813	...	...	.032	.813	.0008	16	5	55.53	34.50
1	.036	.914	...	...	.036	.914	.0010	21	6	43.87	27.25
1	.040	1.02	...	...	.040	1.02	.0012	26	7	35.53	22.07
1	.048	1.22	...	...	.048	1.22	.0018	37	10	24.68	15.33
1	.056	1.42	...	...	.056	1.42	.0024	50	14	18.13	11.26
1	.064	1.62	...	...	.064	1.62	.0032	65	19	13.88	8.624
1	.072	1.83	...	...	.072	1.83	.0040	83	24	10.97	6.816
1	.080	2.03	...	...	.080	2.03	.0050	102	29	8.884	5.520
1	.092	2.34	...	...	.092	2.34	.0066	135	38	6.718	4.174
1	.104	2.64	...	...	.104	2.64	.0085	173	49	5.237	3.266
1	.116	2.94	...	...	.116	2.94	.0105	215	61	4.225	2.625
1	.128	3.25	...	...	.128	3.25	.0128	262	74	3.470	2.156
1	.144	3.65	...	...	.144	3.65	.0162	332	93	2.742	1.703
1	.160	4.06	...	...	.160	4.06	.0201	409	115	2.221	1.380
3	.020	.508	.042	1.07	.034	.863	.0009	19	6	46.79	29.07
3	.024	.609	.051	1.29	.042	1.06	.0014	28	8	32.50	20.19
3	.028	.711	.059	1.50	.049	1.24	.0019	38	11	23.87	14.83
3	.032	.813	.068	1.74	.053	1.35	.0022	45	13	20.01	12.43
3	.036	.914	.072	1.83	.064	1.62	.0032	65	19	13.89	8.630
3	.040	1.02	.084	2.13	.075	1.90	.0044	89	25	10.20	6.337
3	.048	1.22	.100	2.58	.090	2.30	.0050	102	29	8.893	5.525
3	.056	1.42	.116	2.95	.108	2.73	.0061	124	35	7.342	4.561

TABLE 340 (continued).

Number of Wires in Strand.	Diameter of each Single Wire.		Diameter of the Strand.		Equivalent to Solid Wire.		Weight of Conductor.		Resistance at 60 Fahr.	
	Inch.	m/m.	Inch.	m/m.	Inch.	m/m.	Sq. In.	Square m/m.	Per Statute Mile.	Per Statute metre.
20	.035	.914	.108	2.74	.006	2.43	.0072	4.65	6.175	3.835
19	.040	1.02	.120	3.04	.107	2.71	.0089	5.77	5.002	3.1079
18	.048	1.22	.144	3.66	.128	3.25	.0128	8.30	3.473	2.158
17	.055	1.42	.168	4.27	.149	3.78	.0174	11.28	2.552	1.585
16	.064	1.63	.192	4.88	.171	4.34	.0229	14.73	1.953	1.213
15	.072	1.83	.216	5.49	.192	4.87	.0289	18.66	1.543	.9589
14	.080	2.03	.240	6.10	.213	5.41	.0356	22.98	1.253	.7785
13	.086	.914	.180	4.57	.159	4.03	.0198	12.74	2.261	1.404
12	.094	1.02	.200	5.08	.176	4.47	.0243	15.72	1.831	1.137
11	.048	1.22	.240	6.10	.211	5.35	.0349	22.66	1.271	.7897
10	.055	1.42	.280	7.10	.247	6.27	.0479	30.91	1.079	.6704
9	.064	1.63	.320	8.12	.282	7.16	.0624	40.25	.7154	.4445
8	.072	1.83	.360	9.14	.317	8.05	.0789	50.96	.5652	.3512
7	.080	2.03	.400	10.1	.352	8.94	.0973	62.77	.4579	.2845
6	.086	2.34	.460	11.6	.404	10.7	.1282	83.20	.3462	.2151
5	.104	2.64	.520	13.2	.458	11.6	.1647	106.3	.2709	.1683
4	.120	3.04	.600	15.2	.534	13.6	.2119	136.6	.2061	.1277
3	.144	3.66	.720	18.3	.643	16.2	.2516	162.6	.1772	.1101
2	.168	4.27	.864	21.9	.778	19.8	.3117	200.7	.1407	.0861
1	.192	4.88	1.024	26.1	.883	22.6	.3519	226.4	.1072	.0666
									.0839	.0521

### Insulation of Wires.

For insulating wires india-rubber is preferable to gutta percha, as the latter gets soft when heated. Vulcanized rubber may be raised 200° without becoming deteriorated.

A good electrical and mechanical insulation is given by covering the conductors with pure india-rubber; then vulcanized india-rubber, then india-rubber-coated tape, the whole being vulcanized together, and finally covered with braided tarred flax, and a coating of preservative compound. It is false economy to use any but the very best insulation. For low tension currents (up to 100 volts) the coverings should be such as to give an insulation to the wires of not less than 1,000 megohms per statute mile; for high tension currents (above 100 volts), the insulation should be as high as 5,000 megohms per statute mile. It should be distinctly understood that should the cable whose insulation should normally be 5,000 megohms, test as low as 1,000 megohms, it would not do to use this for a low tension circuit, as the lowness of the insulation would not be due to the nature of the insulating material *but to a defect in it*, which defect would be almost certain to become worse in time. The cables should be tested in water at 75°, after immersion for at least 24 hours, a battery of about 400 to 500 volts being used. Tests as to insulation are perfectly useless unless carried out in a thorough manner.

According to the Board of Trade Regulations, the size of the conductor must be such that the maximum current which may have to pass does not exceed 2,000 ampères per square inch, the wire being of pure copper or its equivalent.

### Calculation of Size of Conductor.

To calculate the size of conductor required, let —

$p$  = greatest percentage of fall of E.M.F. along conductor which is to be allowed,

$E$  = E.M.F. at dynamo terminals,

$A$  = maximum number of ampères per square inch wire can safely carry,

$c$  = current wire is required to carry ;

then if length of circuit *exceeds*

$$\frac{pE \times 400}{A} \text{ yds.,}$$

to calculate the sectional area ( $a$ ) which the lead must have, use the formula

$$a = \frac{c}{pE \times 400} \text{ sq. ins.}$$

If the length of the circuit is *less than*

$$\frac{pE \times 400}{A} \text{ yds.,}$$

from the formula  $a = \frac{c}{A} \text{ sq. ins.}$



## TELEGRAPH AND TELEPHONE WIRE.

TABLE 341.—RELATIVE DIMENSIONS, LENGTHS, RESISTANCES (AT 60° F.), AND WEIGHTS OF  
PURE SOFT COPPER WIRE.

(Glover.)

B. W. G. No.	Diam. Mils.	Area. Sq. In.	Lbs. per Foot.	Lbs. per Mile.	Feet per Lb.	Miles per Lb.	Feet per Ohm.	Ohms per Foot.	Ohms per Mile.	Ohms per Lb.
0000	454	.1619	.6239	3294	1.603	.0003036	19966	.00005008	.2644	.00008027
000	425	.1419	.5468	2887	1.829	.0003464	17497	.00005715	.3018	.0001046
00	380	.1134	.4371	2308	2.288	.0004333	13988	.00007149	.3775	.0001636
0	340	.09079	.3499	1848	2.858	.0005412	11198	.00008930	.4715	.0002552
1	300	.07069	.2724	1438	3.671	.0006952	8718	.0001147	.6056	.0004210
2	284	.06335	.2442	1289	4.096	.0007757	7814	.0001280	.6758	.0005242
3	250	.05269	.2031	1072	4.925	.0009327	6498	.0001539	.8125	.0007579
4	238	.04449	.1715	905.3	5.832	.001105	5487	.0001822	.9623	.001063
5	220	.03801	.1465	773.6	6.826	.001293	4689	.0002133	1.126	.001456
6	203	.03237	.1247	658.6	8.017	.001518	3992	.0002506	1.323	.002008
7	180	.02545	.09808	517.8	10.20	.001931	3139	.0003186	1.682	.003249
8	165	.02138	.08241	435.1	12.13	.002298	2637	.0003792	2.002	.004601
9	148	.01720	.06631	350.1	15.08	.002856	2122	.0004713	2.488	.007108
10	134	.01410	.05435	287.0	18.40	.003485	1739	.0005749	3.036	.01058
11	120	.01131	.04359	230.2	22.94	.004345	1394	.0007169	3.785	.01645
12	109	.009331	.03596	189.9	27.81	.005266	1151	.0008689	4.588	.02416
13	95.0	.007082	.02732	144.2	36.60	.006933	874.3	.001144	6.039	.04187

TABLE 341.—RELATIVE DIMENSIONS, LENGTHS, RESISTANCES (AT 60° F.), AND WEIGHTS OF PURE SOFT COPPER WIRE—*continued*.

B.W.G. No.	Diam. Mils.	Area. Sq. In.	Lbs. per Foot.	Lbs. per Mile.	Feet per Lb.	Miles per Lb.	Feet per Ohm.	Ohms per Foot.	Ohms per Mile.	Ohms per Lb.
14	83.0	.005411	.02085	110.1	47.95	.009082	667.3	.001498	7.912	.07186
15	72.0	.004072	.01569	82.86	63.73	.01207	502.2	.001991	10.51	.1268
16	65.0	.003318	.01279	67.53	78.19	.01481	409.3	.002443	12.90	.1910
17	58.0	.002642	.01018	53.77	98.20	.01859	325.9	.003069	16.20	.3014
18	49.0	.001886	.007268	38.37	137.6	.02606	232.6	.004300	22.70	.5916
19	42.0	.001385	.005340	28.19	187.3	.03547	170.9	.005852	30.90	1.096
20	35.0	.0009621	.003708	19.58	269.7	.05108	149.4	.008427	44.49	2.273
21	32.0	.0008043	.003100	16.37	322.6	.06110	99.20	.01008	53.23	3.252
22	28.0	.0006158	.002373	12.53	421.4	.07981	75.95	.01317	69.52	5.548
23	25.0	.0004909	.001892	9.989	528.6	.1001	60.54	.01652	87.21	8.730
24	22.0	.0003801	.001465	7.736	682.6	.1293	46.89	.02133	112.6	14.56
25	20.0	.0003142	.001211	6.393	825.9	.1564	38.75	.02581	136.3	21.31
26	18.0	.0002545	.0009808	5.178	1020	.1931	31.39	.03186	168.3	32.49
27	16.0	.0002011	.0007749	4.092	1290	.2444	24.80	.04032	212.9	52.04
28	14.0	.0001539	.0005933	3.133	1685	.3192	18.99	.05267	278.1	88.77
29	13.0	.0001327	.0005116	2.701	1955	.3702	16.37	.06108	322.5	119.4
30	12.0	.0001131	.0004359	2.302	2294	.4345	13.95	.07169	378.5	164.5

TABLE 342.—HARD COPPER TELEGRAPH WIRE.

(Post Office Specification.)

Weight per Statute Mile.			Approximate Equivalent Diameter.			Minimum Breaking Weight.	Minimum Number of Twists in 3 Ins.	Maximum Resistance per Mile at 60° F.	Minimum Weight of each Coil of Wire.
Required Standard.	Minimum.	Maximum.	Standard.	Minimum.	Maximum.				
Lbs.	Lbs.	Lbs.	Mils.	Mils.	Mils.	Lbs.		Ohms.	Lbs.
100	97½	102½	79	78	80	330	30	9.1	50
150	146½	153½	97	95½	98	490	25	6.05	50
200	195	205	112	110½	113½	650	20	4.53	50

The wire must be capable of being wrapped, in six turns, round its own diameter, unwrapped, and again wrapped in six turns round its own diameter in the same direction as the first wrapping, without breaking.

When aerial copper wires are used for telegraphic purposes, resin should be employed as a flux in making joints, and too much heat should not be applied, as it softens the wire and weakens its tensile strength at that point.

Samples taken from coils of the 800-lbs. wire should bear bending round a bar 2½ inches diameter without any signs appearing of the zinc cracking or peeling off; the 600-lbs. wire should similarly bear bending round a bar 2¼ inches in diameter; the 450-lbs. and 400-lbs. wire round a bar 2 inches in diameter; the 200-lbs. wire round a bar 1½ inches in diameter.

### Iron Telegraph Wire

(page 640).

*Test of Galvanizing.*—Take samples from coils and plunge them into a solution of sulphate of copper saturated at 60°; allow them to remain in solution 1 minute, then withdraw and wipe clean. The galvanizing should permit of this process being 4 times performed with each sample without there being any sign of a reddish deposit of metallic copper on the wire, which would be the case if the coating of zinc were too thin.

See also page 643.

TABLE 343.—GALVANIZED IRON TELEGRAPH WIRE.

(Post Office Specification.)

Diameter.	Allowed.		Weight per Mile.		Tests for Strength and Ductility.						Weight of each piece of Coil of Wire.		Weight of each Bundle.	
	Required Standard.	Minimum.	Maximum.	Allowed.	Minimum Breaking Weight.	Minimum Number of Twists in 6 Inches.	For Breaking Weight not less than	Minimum Number of Twists in 6 Inches.	For Breaking Weight not less than	Minimum Number of Twists in 6 Inches.	Maximum Resistance per Mile of the Standard Size at 60° Fahr.	Constant, being Standard Weight $\times$ Resistance.	Minimum.	Maximum.
Mils.	Mils.	Mils.	Lbs.	Lbs.	Lbs.		Lbs.		Lbs.		Ohms.		Lbs.	Lbs.
242	237	247	800	767	2,480	15	2,550	14	2,620	13	6.75	5,400	90	120
209	204	214	600	571	1,860	17	1,910	16	1,960	15	9.00	5,400	90	120
181	176	186	450	424	1,390	19	1,425	18	1,460	17	12.00	5,400	90	120
171	166	176	400	377	1,240	21	1,270	20	1,300	19	13.50	5,400	90	120
121	118	125	200	290	620	30	638	28	655	26	27.00	5,400	40	65
													80	130

**Sags and Tensions for Suspending Wires.**

The tension when the temperature is lowest, *i.e.*, when the strain is greatest, should not exceed  $\frac{1}{4}$ th of the breaking strain.

The sag varies with the material, but not with the gauge; the tension varies directly with the weight per foot of the wire.

$$d = \frac{l^2 w}{8t}; \quad d = \sqrt{\frac{3l(1-l)}{8}}; \quad L = l + \frac{8d^2}{3l}; \quad t = \frac{l^2 w}{8d}.$$

where  $l$  = span;  
 $w$  = weight of unit length;  
 $d$  = sag (or dip);  
 $L$  = length of wire in span;  
 $t$  = tension;

also,

$w$  for 400 lbs. iron = .075758 lb. per foot.

„ 150 „ copper = .028409 „ „

„ 100 „ „ = .018939 „ „

and

Coefficient of expansion for iron = .00000683 per deg. F.

Coefficient of expansion for copper = .00000956 „ „

**TABLE 344.—SAGS AND TENSIONS TO BE OBSERVED IN ERECTING WIRES AT VARIOUS TEMPERATURES.**

400-lbs. Iron Wire (No. 7 $\frac{1}{2}$ ).

Span.	32° F. Low Winter Temperature.		40° F. Ordinary Winter Temperature.		58° F. Average Summer Temperature.		76° F. High Summer Temperature.	
	Sag.	Tension.	Sag.	Tension.	Sag.	Tension.	Sag.	Tension.
Yards.	Ft. In.	Lbs.	Ft. In.	Lbs.	Ft. In.	Lbs.	Ft. In.	Lbs.
100	3 1 $\frac{3}{4}$	270	3 9	227	4 3 $\frac{1}{4}$	200	4 8 $\frac{7}{8}$	180
90	2 6 $\frac{5}{8}$	270	3 1 $\frac{3}{4}$	219	3 2 $\frac{3}{4}$	190	4 0 $\frac{7}{8}$	169
80	2 0 $\frac{1}{4}$	270	2 7 $\frac{1}{8}$	210	3 0 $\frac{3}{4}$	178	3 5 $\frac{5}{8}$	157
70	1 6 $\frac{1}{2}$	270	2 1 $\frac{1}{4}$	198	2 6 $\frac{1}{2}$	164	2 10 $\frac{7}{8}$	143
60	1 1 $\frac{5}{8}$	270	1 8	184	2 0 $\frac{3}{4}$	148	2 4 $\frac{3}{4}$	128
50	0 9 $\frac{1}{2}$	270	1 3 $\frac{1}{2}$	165	1 7 $\frac{3}{4}$	130	1 11 $\frac{1}{4}$	110

T T

TABLE 344.—TABLE OF SAGS, ETC. (*continued*).  
150-lbs. Hard-drawn Copper Wire (No. 12½).

Yards.	Ft.	In.	Lbs.	Ft.	In.	Lbs.	Ft.	In.	Lbs.	Ft.	In.	Lbs.
100	2	8	120	3	7	89	4	3 $\frac{7}{8}$	74	4	11 $\frac{1}{2}$	64
90	2	2	120	3	1	84	3	9 $\frac{1}{2}$	69	4	4 $\frac{1}{8}$	60
80	1	8 $\frac{3}{8}$	120	2	6 $\frac{7}{8}$	80	3	2 $\frac{1}{2}$	64	3	8 $\frac{7}{8}$	54 $\frac{1}{2}$
70	1	3 $\frac{5}{8}$	120	2	1 $\frac{3}{4}$	73	2	8 $\frac{5}{8}$	57 $\frac{1}{2}$	3	2 $\frac{1}{2}$	49
60	0	11 $\frac{5}{8}$	120	1	9	66	2	3 $\frac{1}{8}$	51	2	8 $\frac{1}{4}$	43
50	0	8	120	1	4 $\frac{5}{8}$	58	1	10	44	2	2 $\frac{3}{8}$	36 $\frac{1}{2}$

100-lbs. Hard-drawn Copper Wire (No. 14).

Yards.	Ft.	In.	Lbs.	Ft.	In.	Lbs.	Ft.	In.	Lbs.	Ft.	In.	Lbs.
100	2	8	80	3	7	59	4	3 $\frac{7}{8}$	49	4	11 $\frac{1}{2}$	43
90	2	2	80	3	1	56	3	9 $\frac{1}{2}$	46	4	4 $\frac{1}{8}$	40
80	1	8 $\frac{3}{8}$	80	2	6 $\frac{7}{8}$	53	3	2 $\frac{1}{2}$	42 $\frac{1}{2}$	3	8 $\frac{7}{8}$	36
70	1	3 $\frac{5}{8}$	80	2	1 $\frac{3}{4}$	49	2	8 $\frac{5}{8}$	38	3	2 $\frac{1}{2}$	33
60	0	11 $\frac{5}{8}$	80	1	9	44	2	3 $\frac{1}{8}$	34	2	8 $\frac{1}{4}$	29
50	0	8	80	1	4 $\frac{5}{8}$	39	1	10	29	2	2 $\frac{3}{8}$	24

### Copper Wire.

#### Conductivity of Copper Wire.

$$\text{Percentage of conductivity} = \frac{l^2 \times 22.61}{w \times k \times r}.$$

$l$  = length of wire in feet.

$w$  = weight of wire in grains.

$r$  = resistance of wire in ohms.

$k$  = temperature coefficient (p. 604).

*Example.*—The resistance of a copper wire 35 feet ( $l$ ) long and weighing 297 grains ( $w$ ), was .932 ohm ( $r$ ), the temperature being 68° F.; what was the percentage of conductivity of the wire?

From Table, p. 604,  $k = 1.015$ , therefore

$$\text{Percentage of conductivity} = \frac{35 \times 35 \times 22.61}{297 \times 1.015 \times .932} = 98.6.$$

#### Resistance of Copper Wire.

Resistance per mile of pure soft copper wire at 60° F.,  $d$  mils. in diameter =  $\frac{54402}{d^2}$  ohms.

Resistance per mile of pure soft copper wire at 60° F., weighing  $w$  lbs. =  $\frac{872.2}{w}$  ohms.

Weight of pure soft copper wire 1 mile long having a resistance of 1 ohm at  $60^{\circ}$  = 872.2 lbs.

Length in yards of pure soft copper wire having a sectional area of  $a$  sq. ins. required to give a resistance of  $r$  ohms at  $60^{\circ}$  F. =  $ra \times 41,161$ . If

$l$  = length of a wire.

$a$  = sectional area.

$d$  = diameter.

$w$  = weight.

$r$  = resistance.

$$r = \frac{l}{a} \kappa = \frac{l}{d^2} \kappa' = \frac{l}{w} \kappa''.$$

Where  $\kappa$ ,  $\kappa'$ , and  $\kappa''$  are the resistances of a wire of unit dimensions. For pure soft copper at  $60^{\circ}$  F., if  $l$  is in feet,  $a$  in square inches,  $d$  in mils. ( $\frac{1}{1000}$ th in.) and  $w$  in grains (7000 grains = 1 lb.).

$$\kappa = .000008098, \kappa' = 10.311, \kappa'' = .2190.$$

The resistance of a copper wire increases about .21 per cent. per  $1^{\circ}$  F. If

$r$  = resistance at  $t^{\circ}$  F.

$R$  = " "  $T^{\circ}$  F.

$R = r(1 + .0021(T - t))$  approximately.

., =  $r(1.0020935)^{T-t}$  more exactly.

### Iron Wire.

Two qualities of iron wire are used by the Postal Telegraph Department for aerial line purposes, known as low resistance and high resistance wire. The low resistance wire may consist either of "special blend" iron, giving a mean resistance of 11.3 ohms per mile at  $60^{\circ}$  F. for the standard gauge of 171 mils. (No.  $7\frac{1}{2}$  B. W. G.) : or of "charcoal" iron, giving under the same conditions a resistance of 11.2 ohms per mile. The high resistance wire which is more generally used (see Specification, page 630) of the same gauge has a mean resistance of 12.7 ohms per mile, but is cheaper in price. The low resistance iron is used for circuits over about 200 miles in length, its breaking strain is rather less than that of the high resistance wire.

1 foot-grain of pure iron has a resistance of 1.097 ohms at  $0^{\circ}$  C. ( $32^{\circ}$  F.).

1 ohm-mile (a wire 1 mile long, having a resistance of 1 ohm) of pure iron, weighs 4368.94 lbs.

Ditto, low resistance blend-wire weighs 4520 lbs.

Ditto, " " charcoal " 4480 "

Ditto, high " " " 5080 "

To determine the resistance  $R$  at a temperature  $t^{\circ}$  F. ( $r$ ) at a temperature  $t^{\circ}$  being known

$$R = r(1.0027)^{t-t}.$$

**TELEGRAPHY.**

*Connections of Apparatus on the Morse System adopted by the Postal Telegraph Department.*

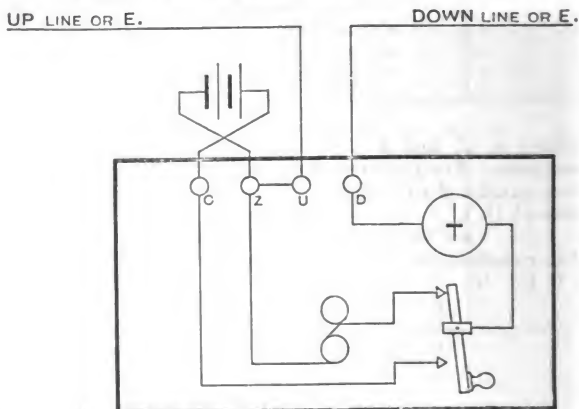
**SINGLE CURRENT SYSTEM.****DIRECT WRITER (Combination Instrument.)**

FIG. 91.

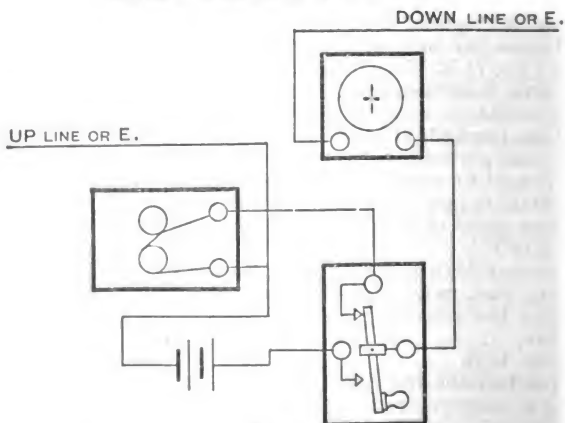
**DIRECT SOUNDER OR WRITER.**

FIG. 92.



DOWN LINE OR E.

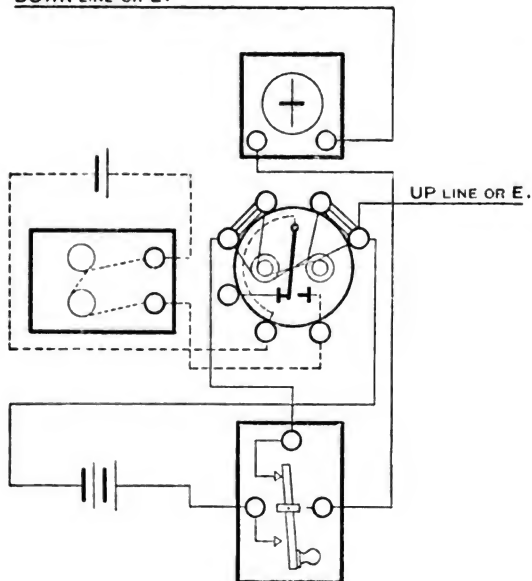


FIG. 93.

DIRECT WRITER. Duplex: with Switch.

UP LINE OR E.

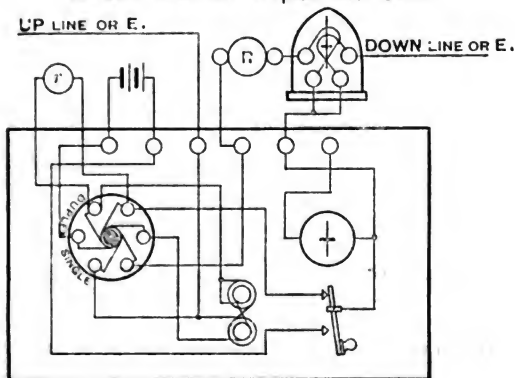


FIG. 94.

All the systems require from 15 to 20 milliampères of current.

The Direct Writer Duplex system is suitable for circuits up to about 25 miles in length. The switch is employed for the purpose of changing the connections to the arrangement for ordinary working, should the insulation of the line become such as to render a proper balance by means of the Rheostat R difficult or impossible, and duplex working consequently impossible also. R is a fixed resistance equal as nearly as possible to the resistance of the battery.

TABLE 345.—TELEGRAPH POLES.

SIZES OF LIGHT POLES.				SIZES OF STOUT POLES.			
Length in Feet.	Diameter at Top. Inches.		Minimum Diameter at 5 Feet from Butt End. Inches.	Length in Feet.	Diameter at Top. Inches.		Minimum Diameter at 5 Feet from Butt End. Inches.
	Mini- mum.	Maxi- mum.			Mini- mum.	Maxi- mum.	
18	5	5 $\frac{3}{4}$	6 $\frac{1}{2}$	18	5 $\frac{1}{2}$	6 $\frac{1}{2}$	7 $\frac{1}{4}$
20	5	5 $\frac{3}{4}$	6 $\frac{1}{2}$	20	5 $\frac{1}{2}$	6 $\frac{1}{2}$	7 $\frac{1}{2}$
22	5	5 $\frac{3}{4}$	6 $\frac{3}{4}$	22	5 $\frac{1}{2}$	6 $\frac{3}{4}$	7 $\frac{3}{4}$
24	5	5 $\frac{3}{4}$	7	24	5 $\frac{1}{2}$	6 $\frac{3}{4}$	8
26	5	6	7 $\frac{1}{4}$	26	5 $\frac{3}{4}$	7	8 $\frac{1}{4}$
28	5	6 $\frac{1}{4}$	7 $\frac{3}{4}$	28	6	7 $\frac{1}{4}$	8 $\frac{3}{4}$
30	5	6 $\frac{1}{4}$	8	30	6	7 $\frac{1}{4}$	9
32	5 $\frac{1}{4}$	6 $\frac{1}{2}$	8 $\frac{1}{4}$	32	6 $\frac{1}{4}$	7 $\frac{1}{2}$	9 $\frac{1}{4}$
34	5 $\frac{1}{4}$	6 $\frac{3}{4}$	8 $\frac{3}{4}$	34	6 $\frac{1}{4}$	7 $\frac{3}{4}$	9 $\frac{3}{4}$
36	5 $\frac{1}{2}$	7	9	36	6 $\frac{1}{2}$	7 $\frac{3}{4}$	10
38	5 $\frac{1}{2}$	7	9 $\frac{1}{4}$	38	6 $\frac{1}{2}$	7 $\frac{3}{4}$	10 $\frac{1}{4}$
40	5 $\frac{1}{2}$	7 $\frac{1}{4}$	9 $\frac{3}{4}$	40	6 $\frac{1}{2}$	8	10 $\frac{3}{4}$
45	5 $\frac{3}{4}$	7 $\frac{1}{2}$	10 $\frac{1}{2}$	45	6 $\frac{3}{4}$	8 $\frac{1}{2}$	11 $\frac{1}{2}$
50	6	7 $\frac{3}{4}$	11 $\frac{1}{4}$	50	7	8 $\frac{3}{4}$	12 $\frac{1}{4}$
55	6	8	12	55	7 $\frac{1}{4}$	9	13
60	6	8	12 $\frac{1}{2}$	60	7 $\frac{1}{2}$	9	13 $\frac{1}{2}$

### Telegraphic Solder.

Equal parts by weight of ingot tin and pig lead.

### Materials and Tools for constructing a 300 Mile Iron Pole Telegraph Line of 1 Wire.

#### Materials.

6,000 iron tubular and conical telegraph poles attached to

base pile for driving, the pole complete not weighing more than 100 lbs. ; length over all when jointed 18 ft. Length of cast iron base pile about 4 ft., and tube about 14 ft. 6 in., with slit-joint between base pile and tube.

6,000 soft iron rings for caulking into base plate.

6,000 lightning rods, 18 ins. long, to surmount poles.

6,150 insulators, Cordeaux pattern.

4 Hand rammers, for driving base piles.

14 tons No. 14 hand-drawn copper wire, 103 lbs. to the mile, 340 lbs. breaking strain ; resistance about 8 ohms per mile.

$\frac{1}{4}$  cwt. best tin solder ; 4 gals. soldering solution in gallon jars.

250 anchor plates, stay-rods, stay-wires, clips, &c., complete, for angle poles.

2 $\frac{1}{2}$  cwt. No. 18 soft copper wire for binding wire to insulator.

$\frac{1}{2}$  cwt. No. 20 tinned copper wire for jointing line wire.

1 wire dynamometer vice for copper wire.

### *Construction Tools.*

3 pairs small-draw vices and keys for No. 14 copper wire.

2 pairs devil's claws.

2 fire-pots.

6 8-in. cutting-pliers.

3 10-in. flat bastard files.

6 soldering-irons, large.

2 tool baskets.

12 lbs. lump sal-ammoniac.

3 large hammers.

2 sledge-hammers.

6 steel wedges.

1 2-ft. rule.

6 Picks, handled.

6 shovels.

6 spades.

3 jumpers.

2 iron punners, handled.

2 crow-bars, steel-pointed.

2 wire-drums and barrows, light and portable.

3 bill-hooks.

3 15-ft. wooden ladders.

3 American axes.

2 hand-saws.

2 saw-files.

2 screw-hammers.

### TELEPHONES.

The limiting distance over which *good* speaking is possible in the case of *cables* and *underground work* is reached when the "KR." is about 8000, KR being the product of the *Total Inductive Capacity* and the *Total Conductor Resistance* of the Line. If the value of KR exceeds 8,000, the speaking commences to become difficult.

Through underground Wire No. 18 Copper and No. 7½ Gutta-percha, the *good-speaking* limit is about 36 miles.

If the working is carried on through a looped wire *with no earth used*, the value KR (*i.e.*, the capacity of the whole length of wire multiplied by the total resistance of the whole length of wire) must be divided by 4, to give the working value of the loop.

In the case of an *overhead iron wire loop* the KR must not exceed 5,000; with a *copper aerial loop* the limit exceeds 30,000, the two wires of the loop in each case being on the same poles.

### LIGHTNING CONDUCTORS.

#### CODE OF RULES FOR THE ERECTION OF LIGHTNING CONDUCTORS (*Lightning Rod Conference*).

*Points.*—The point of the terminal should not be sharp, not sharper than a cone of which the height is equal to the radius of its base. But a foot lower down a copper ring should be screwed and soldered on to the upper terminal, in which ring should be fixed three or four sharp copper points, each about 6 in. long. It is desirable that these points be so platinized, gilded, or nickel-plated, as to resist oxidation.

*Upper Terminals.*—The number of conductors or points to be specified will depend upon the size of the building, the material of which it is constructed, and the comparative height of the several parts. No general rule can be given for this; but the architect must be guided by circumstances. He must, however, bear in mind that even ordinary chimney-stacks, when exposed, should be protected by short terminals connected to the nearest rod, inasmuch as accidents often occur owing to the good conducting power of the heated air and soot in a chimney.

*Insulators.*—The rod is not to be kept from the building by glass or other insulators, but attached to it by metal *connections*.

*Fixing.*—Rods should preferentially be taken down the side of the building which is most exposed to rain. They should be held firmly, but the holdfasts should not be driven in so tightly as to pinch the rod, or prevent the contraction and expansion produced by changes of temperature.

*Factory Chimneys.*—These should have a copper band round the top, and stout, sharp, copper points, each about 1 ft. long, at intervals of two or three feet throughout the circumference, and the rod should be connected with all bands and metallic masses in or near the chimney. Oxidation of the joints must be carefully guarded against.

*Ornamental Ironwork.*—All vanes, finials, ridge ironwork &c., shall be connected with the conductor, and it is not absolutely necessary to use any other point than that afforded by such ornamental ironwork, provided the connection be perfect and the mass of ironwork considerable. As, however, there is risk of derangement through repairs, it is safer to have an independent upper terminal.

*Material for Rod.*—Copper, weighing not less than 6 oz. per foot run, and the conducting of which is not less than 90 per cent. of that of pure copper, either in the form of tape or rope of stout wires, no individual wire being less than No. 12 B. W. G. Iron may be used, but should not weigh less than 2½ lbs. per foot run.

*Joints.*—Although electricity of high tension will jump across bad joints, they diminish the efficacy of the conductor, therefore every joint, besides being well cleaned, screwed, scarfed, or riveted, should be thoroughly soldered.

*Protection.*—Copper rods to the height of 10 feet above the ground should be protected from injury and theft, by being enclosed in an iron pipe reaching some distance into the ground.

*Painting.*—Iron rods, whether galvanised or not, should be painted; copper ones may be painted or not according to architectural requirements.

*Curvature.*—The rod should not be bent abruptly round sharp corners. In no case should the length of the rod between two joints be more than half as long again as the line joining them. When a stringcourse or other projecting stonework will admit of it, the rod may be carried straight through, instead of round the projection. In such a case the hole should be large enough to allow the conductor to pass freely, and allow for expansion, &c.

*Extensive Masses of Metal.*—As far as practicable it is desirable that the conductor be connected to extensive masses of metal, such as hot-water pipes, &c., both internal and external; but it should be kept away from all soft metal pipes, and from internal gas-pipes of every kind. Bells inside well-protected spires need not be connected.

*Earth Connection.*—It is essential that the lower extremity of the conductor be buried in permanently damp soil; hence proximity to rain-water pipes, and to drains, is desirable. It is a very good plan to make the conductor bifurcate close below the surface of the ground, and adopt two of the following methods for securing the escape of the lightning to earth. A strip of copper tape may be led from the bottom of the rod to the nearest gas or water *main*—not merely to a lead pipe—and be soldered to it; or a tape may be soldered to a sheet of copper 3 ft.  $\times$  3 ft. and  $\frac{1}{16}$ th in. thick, buried in permanently wet earth, and surrounded by cinders or coke; or many yards of the tape may be laid on a trench filled with coke, taking care that the surfaces of copper are, as in previous cases, not less than 18 square feet. Where iron is used for the rod, a galvanized iron plate of similar dimensions should be employed.

*Inspection.*—Before giving his final certificate, the architect should have the conductor satisfactorily examined and tested by a qualified person, as injury to it often occurs up to the latest period of the works from accidental causes, and often from the carelessness of workmen.

*Collieries.*—Undoubted evidence exists of the explosion of fire-damp in collieries through sparks from atmospheric electricity being led to the mine by the wire ropes of the shaft and the iron rails of the galleries. Hence the head-gear of all shafts should be protected by proper lightning conductors.

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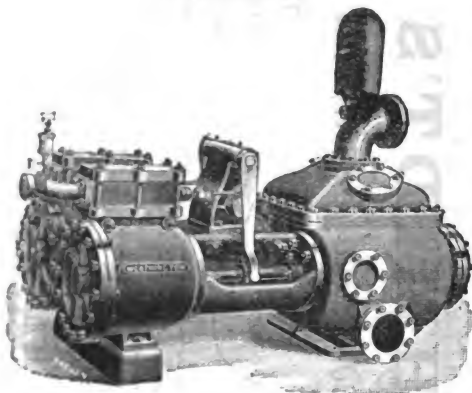
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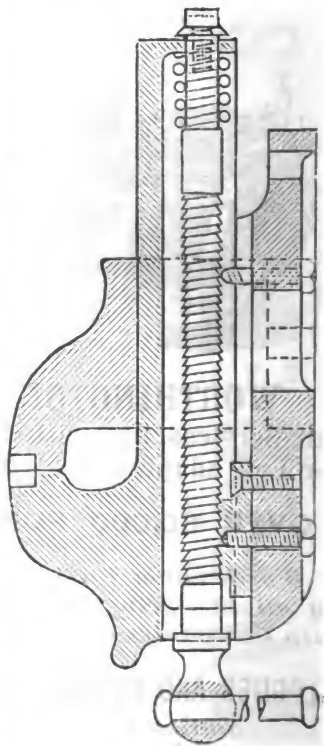
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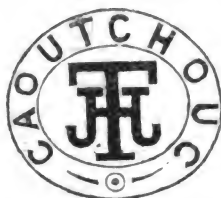
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